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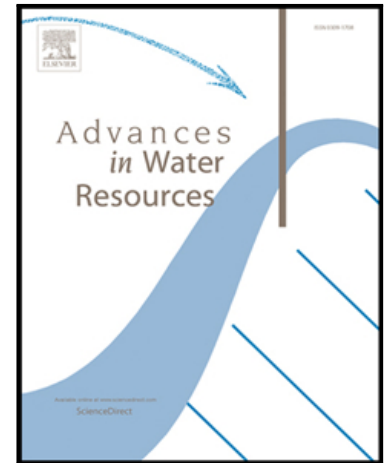


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Assessing sequential data assimilation techniques for integrating GRACE data into a hydrological model

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Highlights

- We use GRACE data to improve a hydrological model estimations
- Data assimilation is used to ingrate observation into a model
- We apply stochastic and deterministic ensemble-based Kalman filters (EnKF) and Particle filter
- Filters performances are compared to reach the best result
- Independent in-situ measurements are used to evaluate the results

ACCEPTED MANUSCRIPT

Assessing sequential data assimilation techniques for integrating GRACE data into a hydrological model

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Abstract

1 The time-variable terrestrial water storage (TWS) products from the Gravity Recovery And
 2 Climate Experiment (GRACE) have been increasingly used in recent years to improve the simu-
 3 lation of hydrological models by applying data assimilation techniques. In this study, for the first
 4 time, we assess the performance of the most popular data assimilation sequential techniques for
 5 integrating GRACE TWS into the World-Wide Water Resources Assessment (W3RA) model.
 6 We implement and test stochastic and deterministic ensemble-based Kalman filters (EnKF), as
 7 well as Particle filters (PF) using two different resampling approaches of Multinomial Resam-
 8 pling and Systematic Resampling. These choices provide various opportunities for weighting
 9 observations and model simulations during the assimilation and also accounting for error distri-
 10 butions. Particularly, the deterministic EnKF is tested to avoid perturbing observations before
 11 assimilation (that is the case in an ordinary EnKF). Gaussian-based random updates in the
 12 EnKF approaches likely do not fully represent the statistical properties of the model simula-
 13 tions and TWS observations. Therefore, the fully non-Gaussian PF is also applied to estimate
 14 more realistic updates. Monthly GRACE TWS are assimilated into W3RA covering the entire
 15 Australia. To evaluate the filters performances and analyze their impact on model simulations,
 16 their estimates are validated by independent in-situ measurements. Our results indicate that
 17 all implemented filters improve the estimation of water storage simulations of W3RA. The best
 18 results are obtained using two versions of deterministic EnKF, i.e. the Square Root Analy-

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19 sis (SQRA) scheme and the Ensemble Square Root Filter (EnSRF), respectively improving
20 the model groundwater estimations errors by 34% and 31% compared to a model run without
21 assimilation. Applying the PF along with Systematic Resampling successfully decreases the
22 model estimation error by 23%.

23

Keywords: Data assimilation, GRACE, Hydrological modelling, Kalman filtering, Particle filtering.

1. Introduction

24 Hydrological models offer important tools for simulating and predicting hydrological
25 processes at global (e.g., [Doll et al., 2003](#); [Hunt, 2006](#); [Coumou and Rahmstorf, 2012](#); [van Dijk](#)
26 [et al., 2013](#)) and regional (e.g., [Chiew et al., 1993](#); [Wooldridge and Kalma, 2001](#); [Christiansen](#)
27 [et al., 2007](#); [Huang et al., 2016](#)) scales. Models are still being developed to simulate all available
28 hydrological processes (e.g., groundwater recharge) and the inclusion of all interactions between
29 water cycle components (e.g., evapotranspiration, precipitation, and runoff). Currently, the
30 most important deficiencies in hydrological models are caused by a high level of uncertainties
31 in imperfect modelling of complex water cycle processes, data deficiencies on both temporal
32 and spatial resolutions (e.g., limited ground-based observations), uncertainties in input and
33 forcing data, and uncertainties of (unknown) empirical model parameters ([Vrugt et al., 2013](#);
34 [van Dijk et al., 2011, 2014](#)). Since making models more complex introduces ever increasing
35 model parameters that cannot be well interpreted and makes computations more expensive, a
36 logical step to address these limitations is the assimilation of observations into models (e.g.,
37 [McLaughlin, 2002](#); [Zaitchik et al., 2008](#); [van Dijk et al., 2014](#)). Data assimilation techniques
38 have found increasing interests with the availability of new data sources, such as those derived
39 from satellite remote sensing observations. For example, time-variable gravity fields from the
40 Gravity Recovery And Climate Experiment (GRACE) mission ([Tapley et al., 2004](#)) can be
41 converted to terrestrial water storage (TWS) fields, a fundamental parameter of the water
42 cycle that might be used to reduce uncertainties in hydrological models.

43 Data assimilation is a procedure that constrains the dynamic of a model with available
44 observations in order to improve its estimates ([Bertino et al., 2003](#)). The solution of the data
45 assimilation problem is based on the Bayes' rule ([Jazwinski, 1970](#); [van Leeuwen and Evensen,](#)

46 1996), which basically computes the Probability Density Function (PDF) of the state, i.e., the
47 model variable of the system that should be estimated, given the data. The updated distribution
48 is then propagated with the model to the time of the next available observation to obtain the
49 prior PDF. In the case of a nonlinear or non-Gaussian system (as it is the case for hydrological
50 models), it is not possible to analytically derive the posterior (analysis) PDF of the state (Hoteit
51 et al., 2008; Vrugt et al., 2013). The Bayesian estimation problem, therefore, needs to be solved
52 numerically, using either variational smoothing or sequential filtering methods (Subramanian
53 et al., 2012).

54 Variational methods look for the model trajectory that best fits the data by minimizing a
55 chosen cost function that measures the misfit between the model state and the observations
56 (Talagrand and Courtier, 1987). These methods require coding and executing an adjoint model,
57 which is very demanding in terms of human and computational resources (Hoteit et al., 2005).
58 Furthermore, variational methods do not provide an efficient framework for updating the esti-
59 mating statistics during the data assimilation process (Courtier et al., 1994; Kalnay, 2003). In
60 contrast, sequential techniques process the data as they become available following two steps
61 including a forecast step to propagate the distribution forward in time and an analysis step
62 to update the distribution with the newly available observation. Monte Carlo methods are
63 commonly used in the forecast step (based on ensembles or particles) and Kalman (Ensemble
64 Kalman filtering) or point-mass weight (Particle filtering) updates are applied in the analysis
65 step (Evensen, 2009; Hoteit et al., 2012). Sequential methods do not require an adjoint and are
66 becoming increasingly popular because of their reasonable computational requirements (Hoteit
67 et al., 2002; Bertino et al., 2003; Robert et al., 2006).

68 The Particle filter (PF) is based on a point-mass (particle) representation of the system
69 state's PDF. It forecasts the PDF by propagating the particles forward in time. At the analysis
70 time, the state PDF is updated by assigning new weights to the particles based on incoming
71 observations (Doucet et al., 2001; Pham, 2001; Hoteit et al., 2012). The fundamental problem
72 of this technique is the degeneracy phenomenon of its particles, with only very few particles
73 carrying most of the weights (Subramanian et al., 2012). Moreover, errors in the assimilated
74 observations may propagate to the estimated distribution because the method was not designed
75 to improve the structure of the model (Hoteit et al., 2008; Smith et al., 2008). This problem
76 is addressed by the Ensemble Kalman filters (EnKFs), which assume a Gaussian forecast PDF

77 at the analysis time, so a Kalman update-step is applied to the particles (Hoteit et al., 2015).
78 This allows an efficient implementation of the Bayesian filtering approach for data assimilation
79 into large systems using small ensembles (van Leeuwen and Evensen, 1996; Hoteit et al., 2008).

80 EnKFs can be classified into stochastic and deterministic filters, depending on whether
81 the observations are perturbed with noise before assimilation, or not (Tippett et al., 2003;
82 Hoteit et al., 2015). In the stochastic EnKF, each ensemble member is updated with perturbed
83 observations, readily providing an analysis ensemble for the next filtering cycle. In contrast,
84 a deterministic EnKF updates only the mean and the covariance of the ensembles exactly as
85 in the Kalman Filter, and thus require a resampling step to generate a new analysis ensemble.
86 The resampling step is not unique, and as such several deterministic EnKFs have been proposed
87 (Sun et al., 2009; Hoteit et al., 2015).

88 Sequential filtering methods have been extensively applied and compared in oceanic and
89 atmospheric applications (Garner et al., 1999; Elbern and Schmidt, 2001; Bennett, 2002; Kalnay,
90 2003; Schunk et al., 2004; Lahoz, 2007; Zhang et al., 2012; Altaf et al., 2014). In hydrological
91 studies, data assimilation has been used to estimate different water compartments, such as soil
92 moisture (e.g., Reichle et al., 2002; Brocca et al., 2010; Renzullo et al., 2014) and surface water
93 storage (e.g., Alsdorf et al., 2007; Neal et al., 2009; Giustarini et al., 2011). However, the
94 efficiency of various filtering methods in dealing with remotely sensed data in hydrology has
95 not been fully investigated (McLaughlin, 2002; Schumacher et al., 2016).

96 Global terrestrial water storage data derived from the GRACE satellite mission can be now
97 employed to improve the behaviour of hydrological models (e.g., Zaitchik et al., 2008; Tang-
98 damrongsub et al., 2015; Thomas et al., 2014; van Dijk et al., 2014; Eicker et al., 2014; Reager
99 et al., 2015), providing unprecedented temporal and spatial coverage. For instance, Zaitchik et
100 al. (2008) demonstrated the relevance of GRACE data in improving the estimation of ground-
101 water variability over the four major sub-basins of the Mississippi through data assimilation
102 into the Catchment Land Surface Model using an ensemble Kalman smoother. Houborg et al.
103 (2012) investigated drought conditions in North America through GRACE data assimilation.
104 The developed GRACE-based drought indicators in the USA led to an improved monitoring of
105 soil moisture and groundwater conditions of deep layers. The impact of GRACE error corre-
106 lation structure on the assimilation of GRACE data was very recently studied by Schumacher
107 et al. (2016). Yet, to the best of our knowledge, however, a comparison with the application

108 of different sequential filtering methods for assimilating GRACE TWS in models has not been
109 fully explored.

110 In this study, we investigate the performance of the most common sequential filtering tech-
111 niques for data assimilation using the hydrological model of the World-Wide Water Resources
112 Assessment (W3RA; [van Dijk, 2010](#)) over Australia. The amount of rainfall in Australia, es-
113 pecially over its northern and eastern parts, is low in comparison to other inhabited continents
114 on Earth leading to prolonged drought in the interior regions ([Forootan et al., 2016](#)). Hence,
115 accurate estimation of water storages (e.g., using hydrological models) is necessary to manage
116 water resources in this region. Here, different filters are used to assimilate GRACE TWS into
117 W3RA to improve its estimates. Both stochastic and deterministic EnKFs are tested and their
118 performances are compared against two standard Particle filters. We applied the standard
119 EnKF and its deterministic variants, including, the Square Root Analysis (SQRA) scheme fol-
120 lowing [Evensen \(2004\)](#) and [Schumacher et al. \(2016\)](#), the Ensemble Transform Kalman Filter
121 (ETKF, [Bishop et al., 2001](#)), the Deterministic EnKF (DEnKF, [Sakov and Oke, 2008](#)), and
122 the Ensemble Square-Root Filter (EnSRF, [Whitaker and Hamill, 2002](#)). We also implement
123 the static-ensemble variant of the EnKF, the Ensemble Optimal Interpolation (EnOI, [Evensen,](#)
124 [2003](#)), in an attempt to reduce the computational burden. To mitigate the deficiency that may
125 arise from limited ensemble sizes and knowledge of model errors' statistics ([Anderson et al.,](#)
126 [2007](#); [Oke et al., 2007](#)), covariance inflation (e.g., [Anderson et al., 1999, 2007](#); [Ott et al., 2004](#))
127 and localization techniques (e.g., [Bergemann and Reich, 2010](#); [Hamill and Snyder, 2002](#)) are
128 applied. The performance of these ensemble filters is assessed against two nonlinear Particle
129 filters based on two different resampling strategies: (i) Multinomial Resampling and (ii) System-
130 atic Resampling techniques ([Arulampalam et al., 2002](#)). The summary of applied filters in this
131 study is presented in Table 1. The results of assimilations are evaluated by comparing their es-
132 timates against independent groundwater in-situ measurements over the Murray-Darling basin
133 and measurements from the moisture-monitoring network in the Murrumbidgee catchment in
134 New South Wales, Australia.

TABLE 1

135 2. Model and Datasets

136 2.1. W3RA

137 The World-Wide Water Resources Assessment (W3RA), based on the Australian
138 Water Resources Assessment system (AWRA) model (version 0.5) is used in this study
139 (<http://www.wenfo.org/wald/data-software/>). The model was first developed in 2008 by the
140 Commonwealth Scientific and Industrial Research Organisation (CSIRO) to monitor, represent
141 and forecast Australian terrestrial water cycles. The W3RA is a grid-distributed biophysical
142 model that simulates landscape water stores in the vegetation and soil systems ([van Dijk, 2010](#)).
143 The $1^\circ \times 1^\circ$ global daily fields of minimum and maximum temperature, downwelling short-wave
144 radiation, and precipitation from Princeton University (<http://hydrology.princeton.edu>) are
145 used for meteorological forcing data ([Sheffield et al., 2006](#)). This one-dimensional grid-based
146 water balance model represents the water balance of the soil, groundwater and surface water
147 stores in which each cell is modelled independently of its neighbours ([van Dijk, 2010](#); [Renzullo
148 et al., 2014](#)). The model state is composed of the $1^\circ \times 1^\circ$ W3RA model storages of the top,
149 shallow root and deep root soil layers, groundwater storage, and surface water storage in a one-
150 dimensional system (vertical variability). In this study, we use W3RA providing daily model
151 states for the period of February 2002 to December 2012. More detailed information on the
152 W3RA model can be found in [van Dijk \(2010\)](#).

153 2.2. GRACE-derived Terrestrial Water Storage

154 Here, we use monthly GRACE level 2 (L2) products along with their full error infor-
155 mation between February 2002 to December 2012 as provided by the ITSG-Grace2014 gravity
156 field model ([Mayer-Gurr et al., 2014](#)). The GRACE monthly Stokes' coefficients are truncated
157 at spherical harmonic degree and order 90, which resulting in approximately ~ 300 by 300 km
158 spatial resolution at the equator.

159 Following [Swenson et al. \(2008\)](#), degree 1 coefficients are replaced to account for movements
160 of the Earth's centre of mass (i.e., realized by a set of tracking stations on the surface of the
161 Earth). Degree 2 and order 0 (C20) coefficients from GRACE are not well determined (e.g.,
162 [Tapley et al., 2004](#); [Tregoning et al., 2012](#)) and are replaced by more reliable estimations of
163 the Satellite Laser Ranging solutions ([Cheng and Tapley, 2004](#)). Correlated noise exists in L2
164 products due to anisotropic spatial sampling, instrumental noise (K-band ranging system and

165 GPS), and temporal aliasing caused by the incomplete reduction of short-term mass variations
166 (Forootan et al., 2014). These errors are reduced by smoothing based on a Gaussian averaging
167 kernel with 300 km half radius and destriping following Swenson and Wahr (2006). However,
168 the smoothing may cause signal attenuation (Klees et al., 2008) and can result in considerable
169 spatial leakage, such as the apparent movement of masses from one region to another (Chen
170 et al., 2007) especially over coastlines (see examples within Australia in e.g., Brown and
171 Tregoning, 2010; Forootan et al., 2012). In order to address this issue, following Swenson and
172 Wahr (2002), we apply an isotropic kernel using a Lagrange multiplier filter to best balance
173 signal and leakage errors over the basin of interest.

174 An additional post-processing step is applied to convert the filtered L2 gravity fields (after
175 removing the mean field of study period) to gridded TWS fields ($1^\circ \times 1^\circ$) following Wahr et al.
176 (1998). The GRACE TWS data are gridded at the same spatial $1^\circ \times 1^\circ$ resolution of W3RA
177 resulting in 794 grid points for Australia that covers an area of 7.692 million km^2 located
178 between $10^\circ S$ and $46^\circ S$ latitude, and $110^\circ E$ and $160^\circ E$ longitude. GRACE data provide
179 changes in TWS while W3RA produces absolute TWS. Accordingly, the mean TWS for the
180 study period is taken from W3RA and is added to the GRACE TWS change time series in order
181 to obtain absolute values in accordance with the model (Zaitchik et al., 2008). In addition, the
182 monthly full error information of the Stokes' coefficients is used to construct an observation
183 error covariance matrix for the GRACE TWS fields (Eicker et al., 2014; Schumacher et al.,
184 2016).

185 2.3. In-situ data

186 For validating the assimilation results, we use in-situ groundwater level data that are
187 collected over the Murray-Darling Basin. The independent in-situ measurements from the model
188 and observations are provided by New South Wales Government (NSW) groundwater archive
189 (<http://waterinfo.nsw.gov.au/pinneena/gw.shtml>). Monthly well measurements are acquired
190 and time series of groundwater storage anomalies are generated. Measurements with data gaps
191 and those without showing seasonal variations are flagged (we assume these belong to confined
192 aquifers) and are thus excluded (Houborg et al., 2012; Tangdamrongsub et al., 2015). Selected
193 bore-water levels are then converted to variations in groundwater (GW) storage. To this end,
194 instead of using specific yield estimates (Rodell et al., 2007; Zaitchik et al., 2008) that is not
195 available in the region, TWS variation from GRACE and GLDAS soil moisture are used to

196 scale the observed head following [Tangdamrongsub et al. \(2015\)](#). [Tregoning et al. \(2012\)](#) show
 197 that this approach can be used to find a scaling factor over the Canning Basin and Murray
 198 Basin in Australia. The scaled in-situ groundwater level fluctuations are then used to assess
 199 the assimilation results.

200 In addition, in-situ measurements of the moisture-monitoring network
 201 (<http://www.oznet.org.au/>) in Murrumbidgee catchment ([Smith et al., 2012](#)) are used
 202 to evaluate the results. These data are known as the OzNet network, which provides long-term
 203 records of measuring volumetric soil moisture at various soil depths at 57 locations across
 204 the Murrumbidgee catchment area. Following [Renzullo et al. \(2014\)](#), we averaged the
 205 measurements into a daily scale and use 0–8 cm to evaluate the estimated model top-layer soil
 206 moisture and the 0–30 cm and 0–90 cm measurements for the evaluation of the model shallow
 207 root-zone soil moisture estimation. The distribution of the in-situ moisture network, as well as
 208 in-situ groundwater stations, are shown in Figure 1.

FIGURE 1

209 3. Filtering Methods and Implementation

210 The Bayesian filtering procedures are selected here for data assimilation ([Jazwinski,](#)
 211 [1970](#); [van Leeuwen and Evensen, 1996](#)). The analytical process conditions a prior PDF of the
 212 state with available observations to compute the posterior PDF based on Bayes' rule ([Koch,](#)
 213 [2007](#)) in two steps; (1) forecasting the state PDF using a dynamical model and (2) updating the
 214 forecast PDF by assimilating observations using Bayes' rule. In the case of a linear system with
 215 Gaussian noise, the popular KF provides the Bayesian filtering solution by computing the first
 216 two moments of the state PDF, which remains always Gaussian ([van Leeuwen and Evensen,](#)
 217 [1996](#)). This two-step process is repeated whenever new observations become available. The
 218 basic KF equations are given by [Kalman \(1960\)](#) starting from an analysis of the state, X_t^a , and
 219 the associated error covariance, P_t^a , at a given time t . These can be summarized as:

220 1) The forecast step consists of the evolution of the state estimate and its error covariance
 221 matrix with a linear dynamical model (M) to the assimilation step (the time of the next avail-
 222 able observation),

223

$$X_{t+\Delta t}^f = MX_t^a + \eta, \quad (1)$$

$$P_{t+\Delta t}^f = MP_t^a M^T + Q, \quad (2)$$

224 where $X_{t+\Delta t}^f$ refers to the forecast state (X^f) at time $t + \Delta t$, with Δt represents the model
 225 time step, and T is the transpose index. In Eq.1, η is the process noise, which is drawn from
 226 $N(0, Q)$ with covariance matrix Q , and $P_{t+\Delta t}^f$ (in Eq.2) denotes the forecast error covariance
 227 (P^f) at time $t + \Delta t$.

228 2) The analysis step updates the forecast state using new incoming observations Y that are
 229 related to the state vector by the linear observation operator (H) as,

230

$$Y = HX + \epsilon, \quad (3)$$

231 where ϵ is the measurement noise. The analysis state (X^a) is then computed using

232

$$X^a = X^f + K(Y - HX^f), \quad (4)$$

$$P^a = (I - KH)P^f, \quad (5)$$

$$K = P^f H^T (HP^f H^T + R)^{-1}, \quad (6)$$

233 where K refers to the Kalman gain, R is the observation error covariance matrix, and I denotes
 234 the identity matrix.

235 The KF algorithm is not suited for high-dimensional or non-linear systems (Pham, 2001).
 236 The ensemble Kalman filter provides an efficient alternative for the implementation of the KF
 237 with these systems by representing the first two-moments of the state using a sample of state
 238 vectors, called ensemble. The forecast state and covariance matrix in Eq.1 and Eq.2 are then
 239 estimated as the sample mean and covariance of the ensembles members $X^i, i = 1 \dots N$:

240

$$\bar{X}^f = \frac{1}{N} \sum_{i=1}^N X^{f,i}, \quad (7)$$

$$P^f = \frac{1}{N-1} \sum_{i=1}^N (X^{f,i} - \bar{X}^f)(X^{f,i} - \bar{X}^f)^T = \frac{1}{N-1} A^f A^{fT}. \quad (8)$$

241 \bar{X}^f is the forecast ensemble mean and A^f ($A^f = [A^{f,1} \dots A^{f,N}]$) is the forecast ensemble of
 242 anomalies (perturbations; $A^{f,i} = X^{f,i} - \bar{X}^f$). When a new observation is available, the forecast

243 ensemble is then updated with the data using Eq.4, as in the KF. Several ensemble Kalman
 244 filters have been proposed, all sharing the same forecast step in which an available analysis
 245 ensemble ($[X^{a,1} \dots X^{a,N}]$) is propagated forward with the model. The analysis step based on
 246 the KF, however, can be applied stochastically or deterministically.

247 3.1. Stochastic Ensemble Kalman Filter (EnKF)

248 The analysis step of the Stochastic EnKF updates each ensemble member with a per-
 249 turbed observation written as,

250

$$X^{a,i} = X^{f,i} + K(Y^i - HX^{f,i}), \quad i = 1 \dots N, \quad (9)$$

251 where $Y^i = Y + \varepsilon^i$, with ε^i a random error sampled from $N(0, R)$. The use of perturbed
 252 observations in the EnKF results in an analysis error covariance that matches that of the KF,
 253 in a statistical sense (Hoteit et al., 2012). The advantage of the stochastic update is that it
 254 readily provides a randomly sampled ensemble from the Gaussian-assumed state analysis PDF
 255 for the next forecast cycle (Hoteit et al., 2015). However, as illustrated by Whitaker and Hamill
 256 (2002), sampling error can be reflected in the EnKF background covariance matrix, especially
 257 for the small-size ensembles. This could be particularly pronounced when a large number of
 258 (independent) observations are assimilated (Nerger, 2004), as the observation covariance cannot
 259 be properly sampled with a small ensemble (Hoteit et al., 2015).

260 3.2. Deterministic Ensemble Kalman Filters

261 Instead of updating each forecast member separately, deterministic EnKFs (DEnKFs)
 262 update the forecast ensemble in two steps, first the ensemble-mean and then the ensemble
 263 perturbations (Tippett et al., 2003) are calculated so that the sample mean and covariance of
 264 the updated ensemble exactly match those of the Kalman filter in Eq.4 and Eq.5.

265 Various methods have been proposed in order to update the ensemble perturbations. SQRA
 266 resamples the new ensemble perturbations (A^a) from the forecast ensemble perturbations (A^f)
 267 as,

268

$$A^a = A^f V \sqrt{I - \Sigma^T \Sigma \Theta^T}, \quad (10)$$

269 where Σ is computed by applying the following singular value decomposition (SVD),

$$U\Sigma V^T = \text{SVD}(\Lambda^{-\frac{1}{2}} Z^T H A), \quad (11)$$

$$Z\Lambda Z^T = (HP^f(H)^T + R)^{-1}, \quad (12)$$

270 where Θ in Eq.10 being a random orthogonal matrix for redistribution of the variance among
 271 the ensemble members (see Evensen, 2004, 2007, for more details). This is very similar to the
 272 random rotation that has been introduced in the context of the Singular Evolutive Extended
 273 Kalman (SEEK) filter (Pham, 2001; Hoteit et al., 2002).

274 ETKF introduces a transformation matrix to directly compute the analysis ensemble per-
 275 turbations from their forecast counterparts,

$$A^a = A^f.T, \quad (13)$$

277 where $T = U(I+\Lambda)^{-1/2}$, with U and Λ , respectively being the orthogonal and diagonal matrices
 278 computed from an eigenvalue decomposition of $(HX^f)^T R^{-1}(HX^f)$.

279 DEnKF and EnSRF adopt a similar analysis step to the EnKF in the sense that they
 280 compute the analysis perturbations from the forecast perturbations by updating each ensemble
 281 perturbation with a Kalman-like update step. To match the KF covariance matrix by an ensemble
 282 of perturbations, DEnKF computes a first-order approximation of the Kalman gain (Sakov
 283 and Oke, 2008). This approximate gain \tilde{K} is then used to compute the analysis perturbations
 284 as,

$$A^a = A^f - \frac{1}{2}KHA^f. \quad (14)$$

286 EnSRF exploits the serial formulation of the KF analysis step in which the observations are
 287 assimilated each at a time to compute the analysis perturbations that exactly match the KF
 288 covariance using the modified gain (αK) with,

$$\alpha = \left(1 + \sqrt{\frac{R}{HP^f H^T + R}}\right)^{-1}. \quad (15)$$

290 This requires the observations to be uncorrelated, which can always be satisfied by scaling the
 291 observations with the square-root inverse of the observational error covariance matrix (Hoteit
 292 et al., 2015).

293 Another form of ensemble Kalman filtering is the so-called Ensemble Optimal Interpolation
 294 (EnOI) scheme, which is basically the EnKF, but without an update of the ensemble anomalies.
 295 More precisely, EnOI only updates the forecast state with a Kalman gain computed from a
 296 preselected static ensemble. The main advantage of not updating the ensemble is of course
 297 to reduce the computational load, but it can also be beneficial to retain the spread of the
 298 ensemble and to enforce climatological smoothness in the update step. EnOI can be stochastic
 299 or deterministic (Hoteit et al., 2002). Here we only test the more standard stochastic variant
 300 (Evensen, 2003).

301 3.3. Particle Filtering

302 Particle filtering is also a sequential Monte Carlo method that was originally proposed
 303 by Gordon et al. (1993) and has since been applied in numerous studies (Doucet, 1998; Aru-
 304 lampalam et al., 2002). The idea is to represent the state PDF by a set of weighted particles
 305 (Arulampalam et al., 2002), hence the name Particle Filter (Gordon et al., 1993; Doucet, 1998),
 306 which is similar to the ensemble members in the EnKF but with non-uniform weights. The
 307 state PDF is then decomposed as,

$$308 \quad P(X_t|Y_{1:t}) \approx \sum_{i=1}^N \omega_t^i \delta(X_t - X_t^i), \quad (16)$$

309 where $\{X_t^i; i = 1 \dots N\}$ are the particles at time t , observations between time 1 and t are
 310 denoted by $Y_{1:t}$, ω_t^i are the weights of the particles, and δ is the Dirac function. In the forecast
 311 step, the PF just integrates the particles forward with the model, exactly as the EnKF, and
 312 their weights remain the same. In the analysis step, only the weights, and not the particles, are
 313 updated with the incoming observation as,

$$314 \quad \omega_t^i = \frac{P(y_t|X_{t|t-1}^i)}{\sum_j P(y_t|X_{t|t-1}^j)}. \quad (17)$$

315 The PF suffers from the degeneracy problem in which the weights of all particles become
 316 negligible except only for a very few, requiring a prohibitive number of particles to prevent
 317 particles collapse (Arulampalam et al., 2002). Degeneracy can be mitigated using the so-called
 318 resampling technique (Doucet et al., 2005), which resamples a new set of particles with uniform
 319 weights after every update step based on the analysis PDF. In this study, we consider two of the
 320 most common resampling techniques: the Particle filter with Multinomial Resampling (PFMR)

321 and Particle filter with Systematic Resampling (PFSR), as proposed by Doucet et al. (2005).
 322 PFMR is the most straightforward resampling scheme, where N independent random numbers
 323 ($u \sim U(0, 1)$) are generated to select a particle from the old set. PFSR, which is also called
 324 universal sampling, draws only one random number $u_1 \sim U(0, 1/N)$ and the remaining $N - 1$
 325 numbers are then calculated from u_1 (Doucet et al., 2005) as,

$$U_i = u_1 + \frac{(i-1)}{N}, \quad i = 2 \dots N. \quad (18)$$

327 These are then used to select a new set of particles according to the multinomial distribution
 328 (Hol et al., 2006).

329 PF has been applied in few hydrological studies. Among them, Moradkhani et al. (2005)
 330 investigated the relevance of the PF for estimating the joint posterior distribution of the pa-
 331 rameters and state. In another effort, Moradkhani et al. (2012) proposed a modified version of
 332 the PF, focusing on enhancing the sampling of the posterior with Markov chain Monte Carlo
 333 (MCMC) moves. Plaza et al. (2012) used the Sequential Importance Sampling with Resam-
 334 pling (SISR) Particle filter for soil moisture assimilation and focused on the consequent effect
 335 on baseflow generation. Existing studies focused on the different implementations of PF using
 336 various resampling techniques. However, a comparison between PF's performances with diverse
 337 resampling techniques and EnKFs has not been investigated yet in hydrology. Figure 2 shows
 338 a summary of the steps and filters applied for data assimilation in this study.

FIGURE 2

339 3.4. Filter Implementation

340 An experimental framework is developed in order to assess the relevance and efficiency
 341 of the filtering techniques presented in the previous section for assimilating GRACE data into
 342 the W3RA model. All filters are implemented under identical conditions, using the same spatial
 343 scales ($1^\circ \times 1^\circ$) for both the W3RA and the GRACE TWS, and daily temporal scales for the
 344 W3RA and monthly for the GRACE data. W3RA is integrated to simulate water storages over
 345 Australia using monthly sequential assimilation cycles of GRACE data applied at the middle
 346 of each month.

347 Several steps need to be undertaken before assimilating GRACE-derived TWS into the

348 W3RA model. Initial ensemble members (particles) are first generated by perturbing the three
349 most important forcing variables including precipitation, temperature, and radiation using their
350 reported error characteristics (Sheffield et al., 2006). Monte Carlo sampling of multivariate
351 normal distributions with the errors representing the standard deviations of the forcing sets
352 are used to produce an ensemble (see details in Renzullo et al., 2014). Different ensemble
353 sizes (30-120) and their spread are tested which the ensemble with 72 members (72 to 120 are
354 suggested by Oke et al., 2008) shows promising performance and is used in this study. The
355 model is integrated forward for two years (January 2001 to January 2003) using perturbed
356 meteorological forcing datasets and provided a set of 72 different states at the beginning of
357 2003 (study period), considered as the initial ensemble (with 72 members). The same initial
358 ensemble is used for all the filters.

359 We use two tuning techniques of ensemble inflation and localisation in order to enhance the
360 assimilation performance of all EnKFs. Ensemble inflation uses a small coefficient (i.e., 1.12
361 in our study; Anderson et al., 2001) to inflate prior ensemble deviation from the ensemble-
362 mean to increase their variations and alleviate the inbreeding problem (Anderson et al., 2007).
363 Another auxiliary technique that has been proved to be helpful when using limited ensemble
364 size is localisation, initially proposed by Houtekamer and Mitchell (2001). We choose to use a
365 Local Analysis (LA) scheme which works by restricting the impact of a given measurement in
366 the update step to the points located within a certain distance from the measurement location
367 (Evensen, 2003; Ott et al., 2004). Different localization lengths are applied to reach the best
368 case (i.e., 5°). In terms of computational cost, all implemented filters are required more or
369 less the same CPU (central processing unit) time (when implemented with the same number of
370 members/particles), with the forecast step of the ensemble being the most demanding.

371 4. Results

372 In this section, we review and analyze the performance of all the selected filtering
373 techniques based on various factors. The implemented filters include (stochastic) EnKF, ETKF,
374 SQRA, DEnKF, EnSRF, EnOI and PF with Multinomial (PFMR) and Systematic (PFSR)
375 resampling. In addition to improving the estimation of the system state and quantifying the
376 associated uncertainties, a suitable data assimilation technique is expected to keep the model
377 system stable during the assimilation process after incorporating GRACE data. These are

378 provided at coarse temporal and spatial scales in comparison to the W3RA model, leading
379 to only one assimilation step every 30 model time-steps and providing information at about
380 three times less than the model grid resolution. Our analysis is organized into two parts;
381 we first examine the filters performance by comparing their estimates (analysis and forecasts)
382 against the assimilated GRACE data over the whole study area as well as the independent in-
383 situ measurements over the Murray-Darling River Basin as well as Murrumbidgee catchment.
384 We also compare the filters estimates with the outputs of a model-free run (open-loop) that
385 is integrated with the filters initial condition without assimilation to evaluate the impact of
386 assimilating GRACE data on the model behavior. Next, the filters behaviors in terms of
387 ensemble spread and the impact of assimilation on the forecast and analysis error covariances
388 are investigated.

389 *4.1. Assessment with GRACE and in-situ data*

390 Spatial correlation maps with high correlations may suggest that the applied filtering
391 method efficiently incorporates GRACE data into the model (Figure 3). The correlation be-
392 tween the model TWS outputs without assimilation and the GRACE data range between 0.11
393 and 0.64, with the highest correlations in the northern region and the lowest in the southern
394 region. All filters significantly improve the estimates correlations to the data after assimilation
395 with some filters leading almost to the perfect correlation with the data (e.g., EnSRF). The
396 model is not able to maintain this high correlation during the forecast and the 30-day assimi-
397 lation window, with the correlations mainly decreasing in the center and southern regions. After
398 monitoring the impact of observations on the model states throughout the study period, it is
399 found that this effect is decreasing gradually (approximately 3-5 days to lose more than 10%)
400 by comparing the correlation of the model states with and without assimilation. This mostly
401 refers to the daily effects of the perturbed forcing sets on model estimations and may suggest
402 that using the denser observation (temporally) could preserve assimilated information during
403 the study. The level of improvement in correlations, however, is different for each filter. For
404 instance, ETKF, SQRA, and PFSR lead to higher correlations with GRACE-derived TWS,
405 suggesting that these methods better reflect the observations in the state estimates. Overall,
406 EnKFs seem to perform better than PFs except only for DEnKF which shown no remarkable
407 impact on the model behavior after assimilation of GRACE data.

FIGURE 3

408 Those methods with the highest correlations to GRACE data lead, as expected, also the
 409 least estimation errors (Figure 4). The largest errors are found in the northern and southern
 410 parts of the domain (Figure 4a), with some of the filters not able to improve remarkably the
 411 model behavior over these areas. TWS variations are generally higher in the northern part
 412 of the study area with larger amplitudes especially during monsoonal seasons (Awange et al.,
 413 2009; Seoane et al., 2013). The model seems unable to predict these amplitudes due to larger
 414 estimated errors even though it performs better in predicting their phases considering high
 415 correlations in this area. SQRA, EnSRF, and to some extent ETKF, significantly decrease the
 416 estimation error over the whole domain. This is very important because these filters are able
 417 to incorporate most of the GRACE signals into the model.

FIGURE 4

418 The Root-Mean-Squared Errors (RMSE) time series between the GRACE TWS and filters
 419 estimates are calculated (Figure 5). In all cases, the analysis step decreases the RMSE with
 420 respect to the forecast. Nevertheless, the RMSE resulting from DEnKF, EnOI, and PFMR are
 421 significantly larger, indicating that these methods are not able to improve the model behavior
 422 after incorporating GRACE data as the rest of the filters do. Estimates by all filters have the
 423 largest error in some periods (e.g., July and October), which may be caused by uncertainties in
 424 forcing sets. The RMSEs from SQRA and EnSRF are smaller in comparison to the rest of the
 425 filters. The smaller average errors during the study period prove the more stable performance
 426 of SQRA and EnSRF. Results in Figures 4 and 5 suggest that the deterministic SQRA, ETKF,
 427 EnSRF filters, and to less extent PFSR, are more efficient at assimilating GRACE data. This
 428 might be due to the fact that for the stochastic ensemble filters perturbations of the obser-
 429 vations have to be generated that introduce an additional uncertainty source to the analysis
 430 step and might result in larger discrepancies to the assimilated observations compared to the
 431 deterministic filters. A summary of the filters' performance, including the coefficient of deter-
 432 mination (R^2) and RMSE in comparison to the assimilated observations (shown in Table 2)
 433 indicates higher correlation (84% average) and smaller RMSEs (35% average improvement) in
 434 the analysis step for all the filters. The maximum improvements regarding the achieved RMSE

435 are achieved by EnSRF and SQRA as 58.88% and 55.17% respectively.

436 **FIGURE 5**

TABLE 2

437 We investigate the performances of the filtering methods through comparison with the
 438 independent groundwater in-situ data over the Murray-Darling basin (cf. Section 2.3). We
 439 use the 54 in-situ measurements over the Murray-Darling basin for a grid comparison with
 440 the estimated GW (Figure 6). The filters estimates are spatially interpolated to the nearest
 441 observation bore. For each filter, the average RMSEs (over all 54 in-situ data) of the forecast
 442 state (red) and analysis state (blue) are determined. As for the assimilated GRACE data (cf.
 443 Figure 5), all the filters decrease the RMSE with respect to the in-situ data, with the largest
 444 errors resulting from DEnKF, EnOI, and PFMR. Furthermore, the average RMSEs are smaller
 445 in SQRA and EnSRF. The similar behavior of the filters in the analysis steps can be found
 446 in Figure 6 as in Figure 5. For some months (e.g., March and July), the larger errors can
 447 be seen in Figure 6 which are not existed in Figure 5. This can be associated to either an
 448 incompatibility between groundwater in-situ measurements and GRACE data or the absent
 449 water compartment terms such as the surface water storage in the model and in-situ data for
 450 the second assessment (Figure 6).

FIGURE 6

451 The relationship between the estimated states and both GRACE data and in-situ measure-
 452 ments (Figure 7) demonstrates the filters capability to dynamically propagate the information
 453 extracted from GRACE data into system variables. In agreement with the previous results, the
 454 best performances are obtained using SQRA, EnSRF, and ETKF (Figures 6 and 7).

FIGURE 7

455 The R^2 coefficient and RMSE results are summarized in Table 3 as another measure of the
 456 filter performances. For each filter, 54 error time series are computed (i.e., for each individual
 457 well), and their averages are then used to calculate R^2 and RMSE. The results of all the filters

458 summarized in Table 3 show improvements (by 35% average) in the analysis steps in all cases,
 459 similar to the assessment against GRACE data (cf. Table 2). SQRA and EnSRF lead to the
 460 highest correlations to the in-situ measurements of R^2 , i.e., 0.75 and 0.72 respectively. These
 461 filters also provide the best estimates in terms of estimation error, while DEnKF and to a
 462 lesser degree EnOI have the highest RMSEs. The PFs, on the other hand, especially using
 463 the systematic resampling technique exhibit a reasonably good performance. In terms of the
 464 assessment results against GRACE data, deterministic filters provide the best performance
 465 (except for DEnKF), generally better than the stochastic EnKF. Overall, SQRA and EnSRF
 466 seem to be the most efficient for assimilating GRACE data into W3RA.

TABLE 3

467 The correlations between model estimations and OzNet data also indicate the superiority of
 468 the successful methods in previous assessments (Table 4). Note that considering the difference
 469 between W3RA estimations (i.e., column water storage measured in mm) and the OzNet mea-
 470 surements (i.e., volumetric soil moisture) and the fact that converting the model output into
 471 volumetric units may introduce bias (Renzullo et al., 2014), only correlation analysis is assumed
 472 here. After estimating correlations for each individual layer, we determine an average correla-
 473 tion for the total soil column (cf. Table 4). The higher correlations are found in analysis steps
 474 with the average of 74% in comparison to forecast steps (59%). The highest correlation to the
 475 OzNet soil moisture measurements belongs to EnSRF with R^2 0.84. SQRA also demonstrate a
 476 significant impact on model estimations with the 35% correlation improvement. The weakest
 477 performance with R^2 0.48 and 0.57 in forecast and analysis step respectively, is achieved from
 478 DEnKF. These results prove the capability of EnSRF and SQRA in improving non-assimilated
 479 model states through data assimilation.

TABLE 4

480 4.2. Error Analysis

481 Analyzing the filters sampled error covariance, particularly the ensemble spread is impor-
 482 tant to understand the filters behaviors and performances. The performance of ensemble-based
 483 filters relies on their ability to represent and propagate the error statistics, which of course

484 depends on how the ensemble members are sampled and updated at the analysis steps (Sun
 485 et al., 2009). We assess the evolution of the ensemble spread and the error covariance matrix
 486 during the study period. An efficient filtering method should be able to preserve the variation
 487 of its ensemble to properly span the error sub-space. Error covariance matrices are analyzed in
 488 terms of estimated errors and correlations.

489 One important aspect of a filter performance refers to its ability to sample representative
 490 ensembles (or particles) at the analysis steps. Figure 8 outlines how the different filtering
 491 techniques adjust the ensemble members during the assimilation procedure. The average TWS
 492 variations time series over Australia and their ensembles at the analysis steps are calculated for
 493 all filters (Figure 8).

FIGURE 8

494 Several important points can be made from the evolution of ensembles in the assimilation
 495 period (Figure 8). Firstly, most of the filters generate ensembles mean (red lines) close to
 496 the assimilated observations suggesting that the filters provide good estimates of the observed
 497 variables. However, one should also consider the distribution of the ensemble members. Those
 498 of EnKF, SQRA, ETKF, EnSRF, and PFSR are consistent over time, which suggests the ro-
 499 bustness of these techniques over time. The ensemble members, especially those of the EnSRF
 500 and SQRA, are evenly distributed around the mean, implying a good coverage of the error
 501 sub-space. The ensembles distribution for DEnKF and EnOI, on the other hand, are different
 502 and exhibit an excessively large spread. In most of the cases, the range of the ensemble con-
 503 centration in DEnKF and EnOI are either misplaced or overestimated. This would result in
 504 underestimating the forecast error and possibly inaccurate assimilation results. In the case of
 505 PF, the Systematic Resampling technique seems to be more robust; the PFMR ensembles and
 506 their variation (black dashed lines) span an unrealistically wide range space, even though the
 507 mean appears fairly close to the observations.

508 More information can be inferred about the filters ensemble distributions by evaluating the
 509 ensembles skewness and kurtosis. These indicate the departure of the ensembles distributions
 510 from a Gaussian distribution (with a skewness 0 and a kurtosis 3). Kurtosis quantifies the dis-
 511 tribution shape (i.e., heavy-tailed or light-tailed, in comparison to a normal distribution) and
 512 skewness measures the distribution asymmetry (Joanes and Gill, 1998). The average (forecast

513 and analysis) ensembles skewness and kurtosis of all filters (Figure 9) show skewness and kur-
 514 tosis are reduced after analysis steps for all filters, suggesting that the filters posterior become
 515 closer to Gaussian as assimilation proceeds. This is, however, more pronounced for skewness
 516 than for kurtosis, showing the filters higher impact on the ensembles distribution asymmetry.
 517 The stochastic EnKF ensemble is closer to a Gaussian distribution, which is related to the ap-
 518 plication of random noises to the observation (Hoteit et al., 2015). In contrast, the DEnKF and
 519 EnOI ensembles are not uniformly distributed, showing a remarkable departure from Gaussian
 520 distributions that is expected to introduce bias in the assimilation results.

FIGURE 9

521 As another evaluation of the filter performance, we further investigate how the model state
 522 error covariance changes over time for each filter. The forecast and analysis error covariance
 523 matrices at the analysis step indicate how errors change over time, especially after assimilation.
 524 We perform two analyses to investigate the influence of the filtering methods on the forecast
 525 and analysis error statistics. First, the reductions of error (diagonal elements) in the analysis
 526 covariance matrices in comparison to the forecast covariance matrices are calculated at each
 527 assimilation step. Next, their minimum, maximum, and average are calculated. The results
 528 show how different methods can decrease the errors using GRACE data (Table 5). All the
 529 filters reduce errors, where the best performance resulting from SQRA, EnSRF, and, to a less
 530 degree, PFSR. Again, DEnKF and EnOI show the weakest effects on error covariance.

TABLE 5

531 Further insights can be derived from the correlation between the estimated states on the
 532 grid points of the study area. For this, 794 grid-points over Australia are considered and the
 533 spatial correlation coefficients are computed between each of them and the rest of the points in
 534 the assimilation steps. In most of the cases (95%), data assimilation significantly decrease the
 535 correlation between grid points in the analysis error covariance matrices. As an example, an
 536 arbitrary point approximately in the middle of the study area (for a better visual representation)
 537 at the location 136.6854°E and 23.9015°S is chosen and its spatial correlation with the other grid
 538 points are plotted to show this effect. The average of spatial correlation map for all assimilation

539 steps and for each filter is presented in Figure 10. Similar results are achieved for the other
540 grid points.

FIGURE 10

541 One can see from Figure 10 that each filtering method affects the correlation between the
542 specific point and the others differently where some filters like PFs show higher ability to
543 decrease the correlations between errors. This can be related to the native of the algorithm
544 of PF, which produces random particles that are consistent with model nonlinear dynamics.
545 The results of the correlation analysis (cf. Figure 10) are consistent with the other results, with
546 DEnKF and EnOI showing the less ability to reduce errors, also having the least influence on the
547 correlations. These results, along with the outcomes of the ensemble distribution analysis (cf.
548 Figures 8 and 9), demonstrate the effect of successful ensemble generation on estimated errors.
549 The filters (e.g., EnKF, SQRA, and EnSRF) with the higher ability to sample representative
550 ensembles lead to the less estimation errors as well as correlations in contrast to the other filters,
551 especially DEnKF and EnOI.

552 Only a few filters show a good performance in both analyses. These filters, SQRA, and En-
553 SRF, not only improve the model state estimates compared to GRACE data and the (ground-
554 water level and soil moisture) in-situ measurements but also efficiently decrease the ensemble
555 spread and spatial correlation errors. The resulting estimates of groundwater storage further
556 exhibit less RMSE against independent groundwater level in-situ data.

557 5. Summary and Conclusions

558 There is evidence that different filter types are more suited to different applications
559 (Reichle et al., 2002). This study considered the implementation of different data assimilation
560 filtering techniques based on the two most commonly applied algorithms, ensemble Kalman,
561 and Particle Filter, to assess their performances for assimilating GRACE data into the hydro-
562 logical model of W3RA. GRACE-derived TWS over Australia was assimilated into the W3RA
563 hydrological model using the various filters. Among the ensemble Kalman filters, we tested the
564 stochastic and the deterministic schemes (EnSRF, ETKF, SQRA, DEnKF, and EnOI) along
565 with two different resampling approaches of Particle Filters (PFMR and PFSR). The effects

566 of the filtering methods on the ensembles spread and the estimation error covariance matrices
567 were investigated. The most promising results are obtained using SQRA, EnSRF, and EnKF,
568 both in terms of ensemble generation as well as in dealing with the estimation error covariance
569 matrices. The greatest error reduction with minimum error covariance is achieved by EnSRF
570 (47% average) and SQRA (44% average). These two filters (along with EnKF) also show a good
571 ability to sample representative ensembles with enough spread. The filters state estimates were
572 evaluated against GRACE data, in-situ groundwater measurements, and in-situ soil moisture
573 data. While improvements in the state estimations are observed for all implemented filters, the
574 best results are obtained with, respectively, SQRA (75% correlation to the groundwater level
575 in-situ measurements and 82% correlation to OzNet soil moisture network), EnSRF (42% error
576 reduction), PFSR (37% error reduction) and slightly less successful ETKF (33% error reduc-
577 tion). In contrast, DEnKF was the least successful in dealing with error covariance matrices
578 and suggested a larger error in the state estimates. SQRA and EnSRF, which efficiently dealt
579 with the error covariances, provided the least RMSEs (32.14 mm and 33.74 mm) and maxi-
580 mum correlations to both groundwater level and soil moisture in-situ measurements. These
581 two filters demonstrated a high capability in assimilating GRACE data. GRACE TWS fields
582 are unique in term of resolution, both spatially (almost 3 times rougher than the model) and
583 temporally (monthly). The weak spatial resolution also affects the observation error covariance
584 structure by increasing the correlation between neighboring grid points when working with a
585 fine (e.g., $1^\circ \times 1^\circ$) grid. Therefore assimilating such a dataset could be challenging requiring a
586 filter that is robust to the system error covariances and also powerful in term of resampling
587 representative ensembles after every assimilation step. However, a general conclusion on the
588 preference of ensemble filters might not be possible from this study due to model-specific and
589 application-specific characteristics. Thus, further research might be undertaken to investigate
590 various aspects of filters in different hydrological applications and to explore other filters like
591 new designed PFs that were not considered here.

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593 **References**

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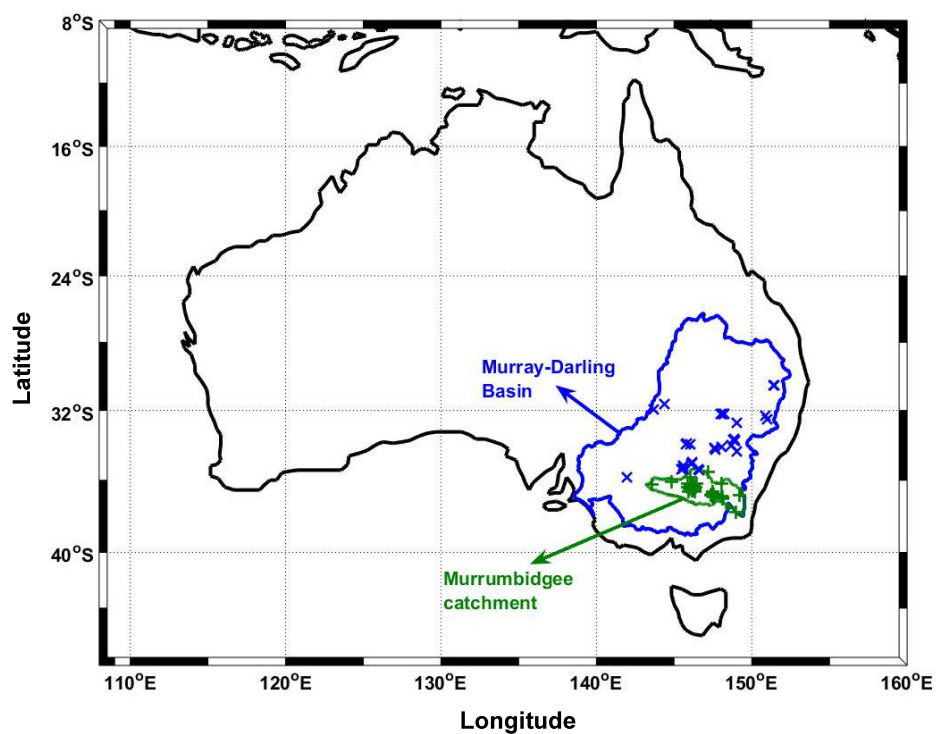


Figure 1: The study area is represented by black solid line. The figure also contains the boundary of the Murray-Darling basin and the locations of the groundwater bore stations (blue), and the outline of the Murrumbidgee catchment with the OzNet soil moisture network (green), which are used for results assessment.

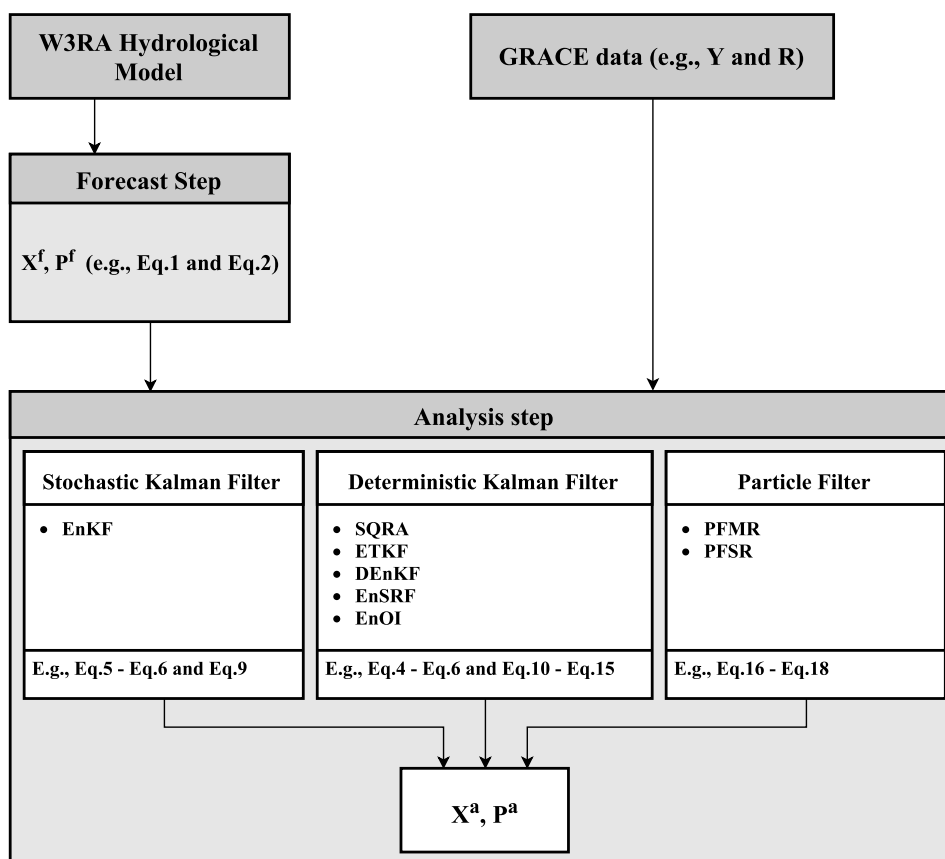


Figure 2: A schematic illustration of the steps and filters applied for data assimilation in this study.

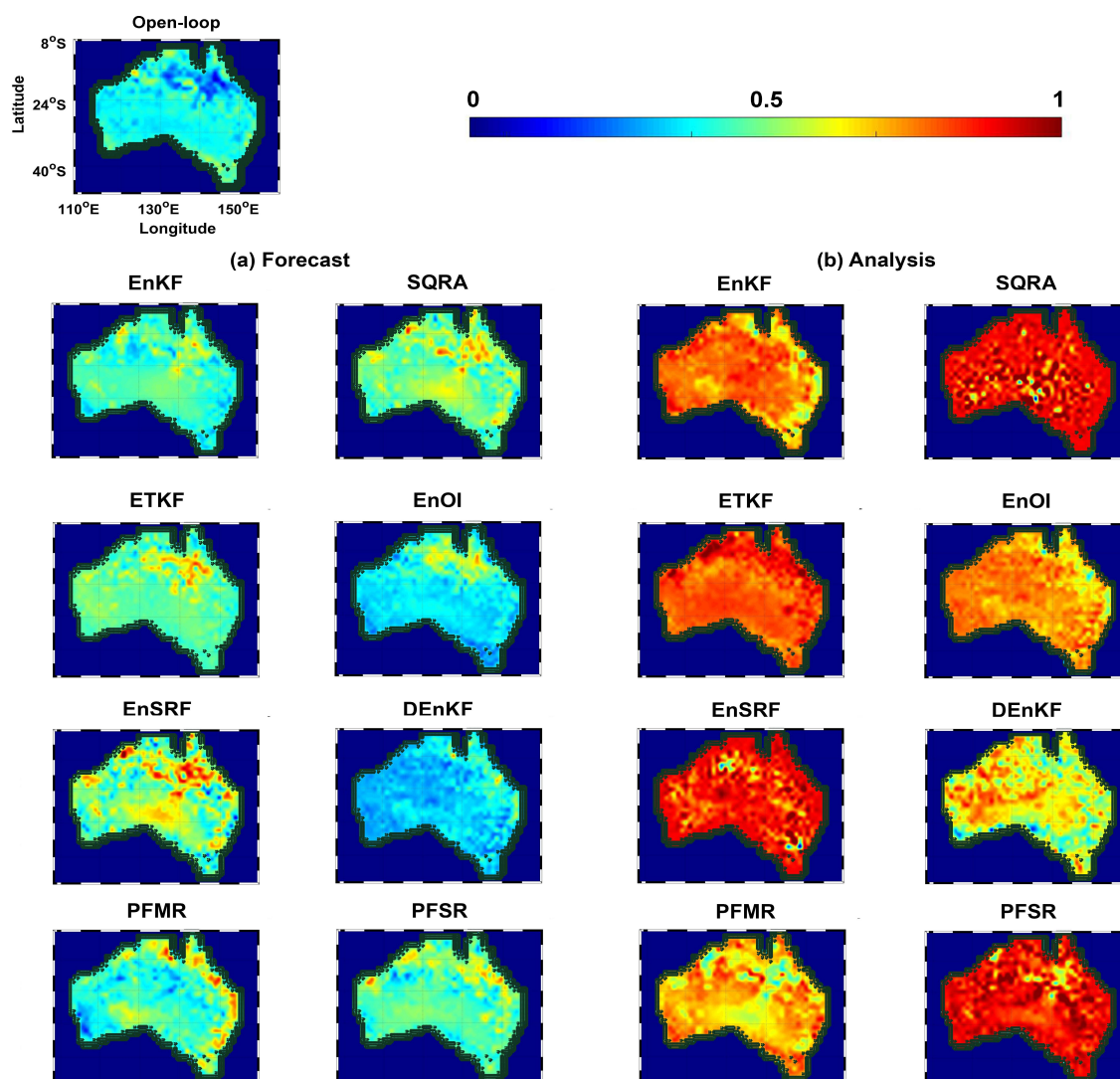


Figure 3: Time average correlations between the assimilated GRACE TWS and different filters estimations at the (a) forecast and (b) analysis steps. Spatial correlation maps are generated at every assimilation step over the study period and their averages are presented.

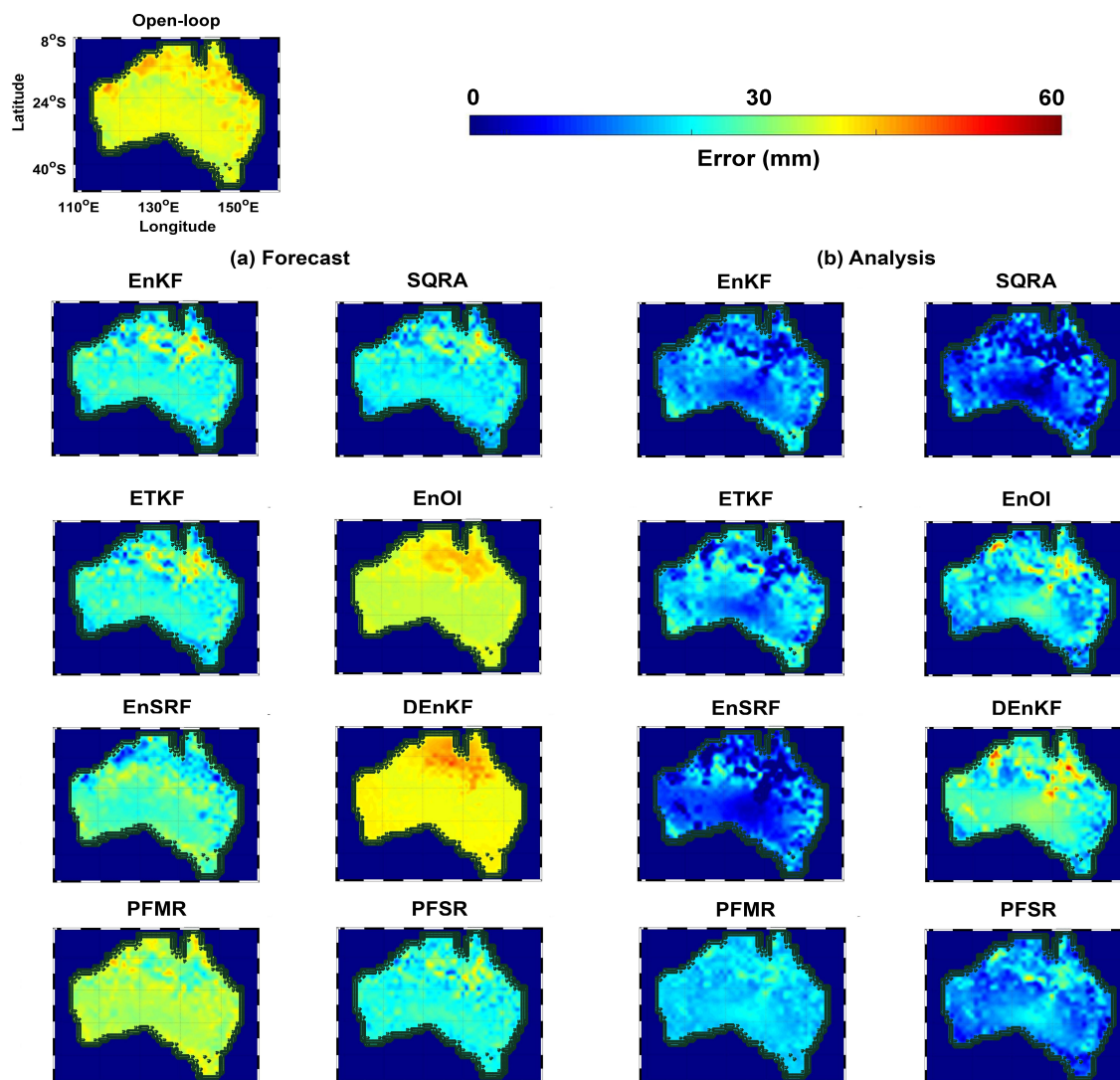


Figure 4: Time average errors between the assimilated GRACE TWS and different filters estimations at the (a) forecast and (b) analysis steps (units are mm). The spatial distribution of the misfits between the filters solution and GRACE data is shown, which plots the time-averaged errors calculated at the forecast steps and the analysis steps.

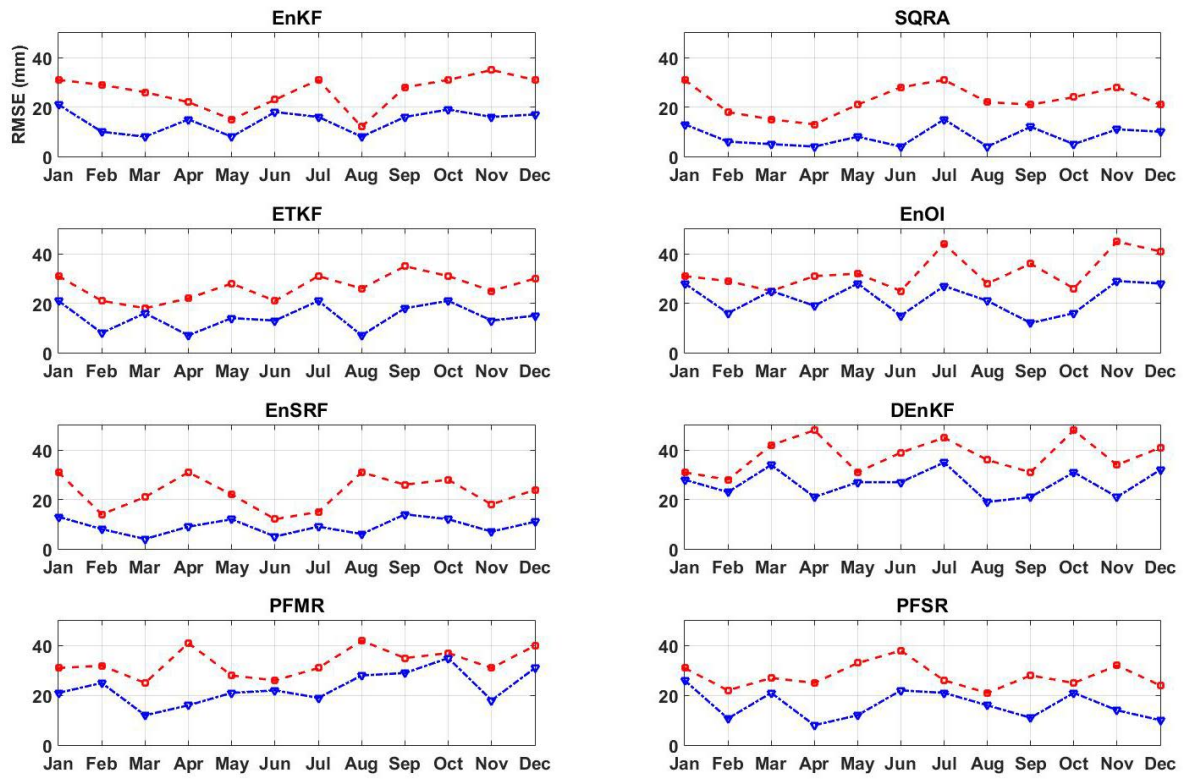


Figure 5: RMSE time series between the assimilated GRACE TWS and the filters' forecasts and analyses which are calculated over all grid points at the forecast (red) and analysis (blue) steps and their averages at each month (during the study period) are shown here.

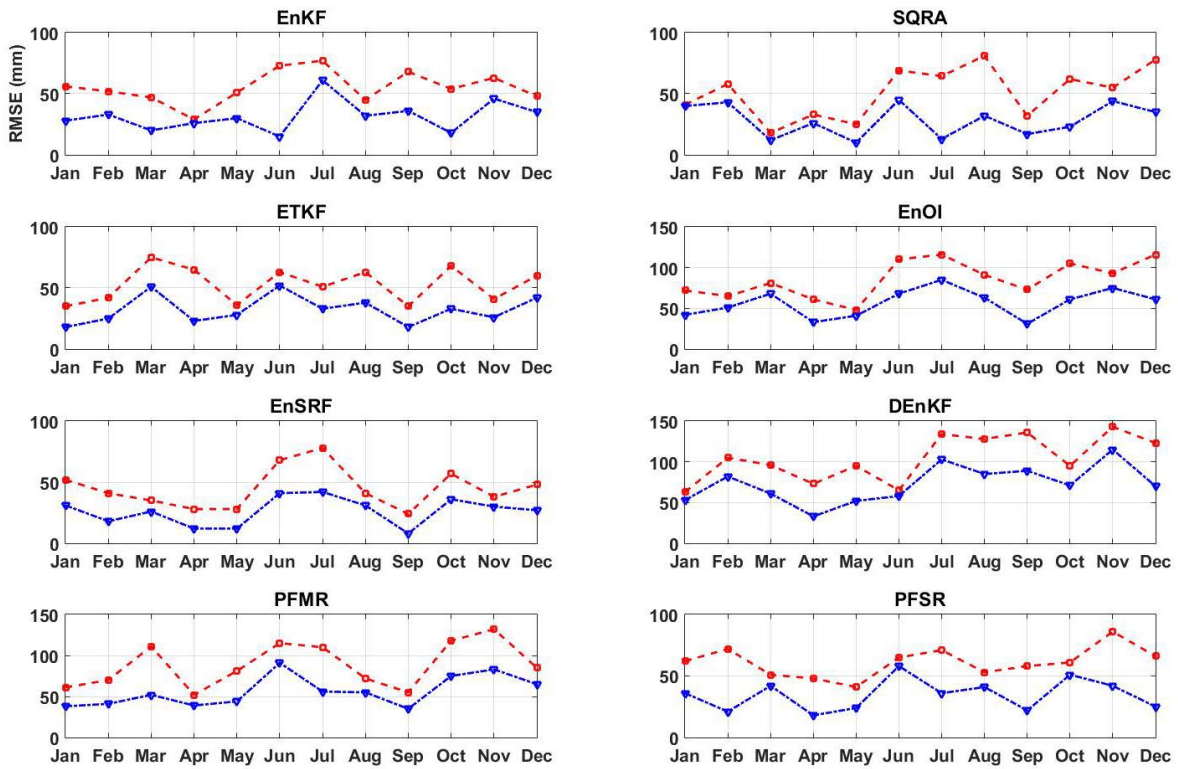


Figure 6: Same as Figure 5, but for the in-situ groundwater measurements and the filters estimates.

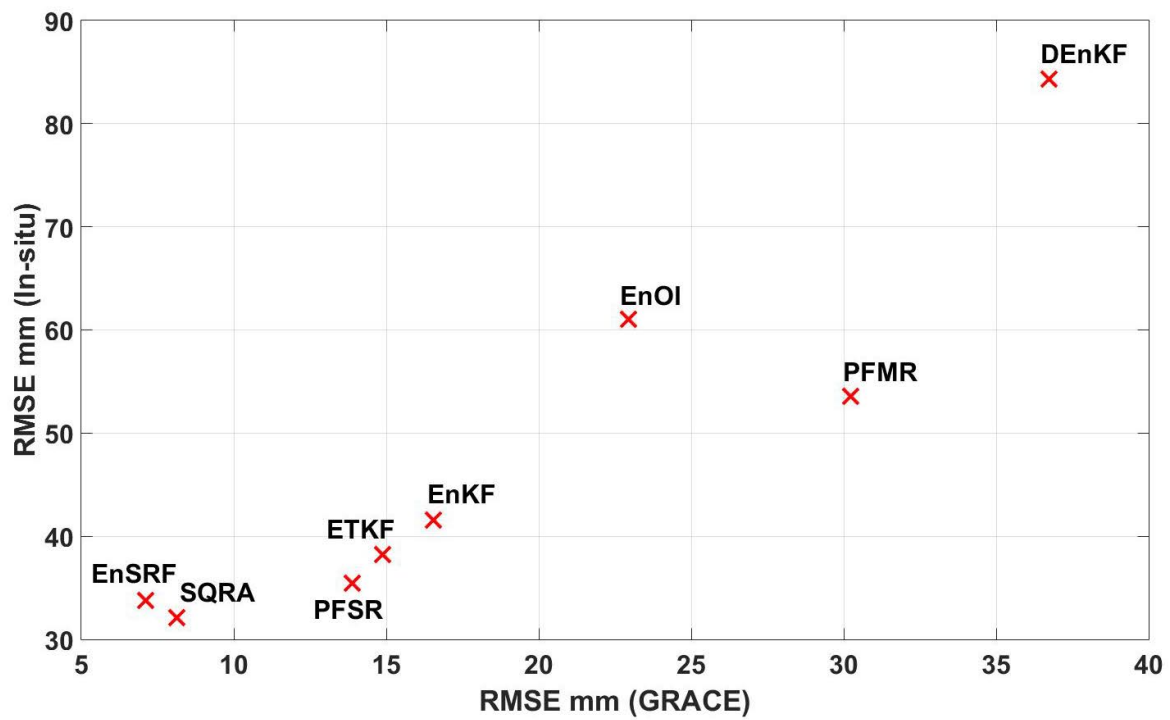


Figure 7: Comparison between the computed average RMSEs of assimilation results from each applied filter using GRACE and the groundwater in-situ datasets. This figure presents the average of the best performances of the filters at the analysis steps from both assessments against GRACE and groundwater in-situ.

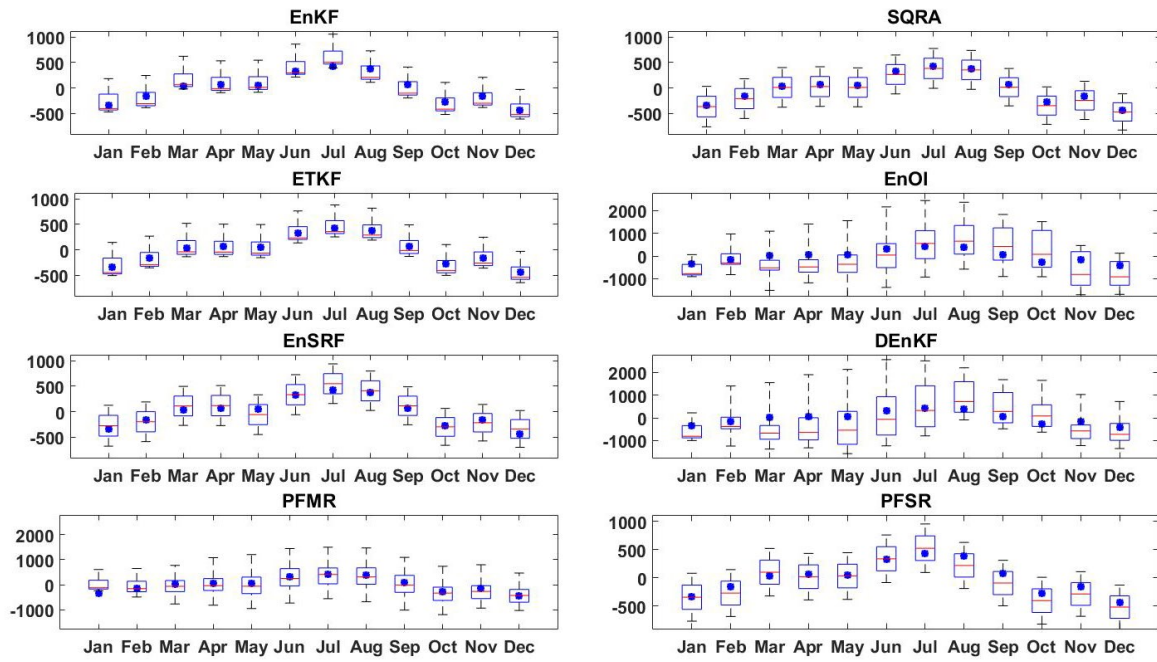


Figure 8: The average TWS variation of ensembles during at the assimilation steps represent by black dashed lines for each filtering method (units are mm). The blue boxes are the ensemble concentrations and horizontal red lines show the median values of the ensembles at each analysis step.

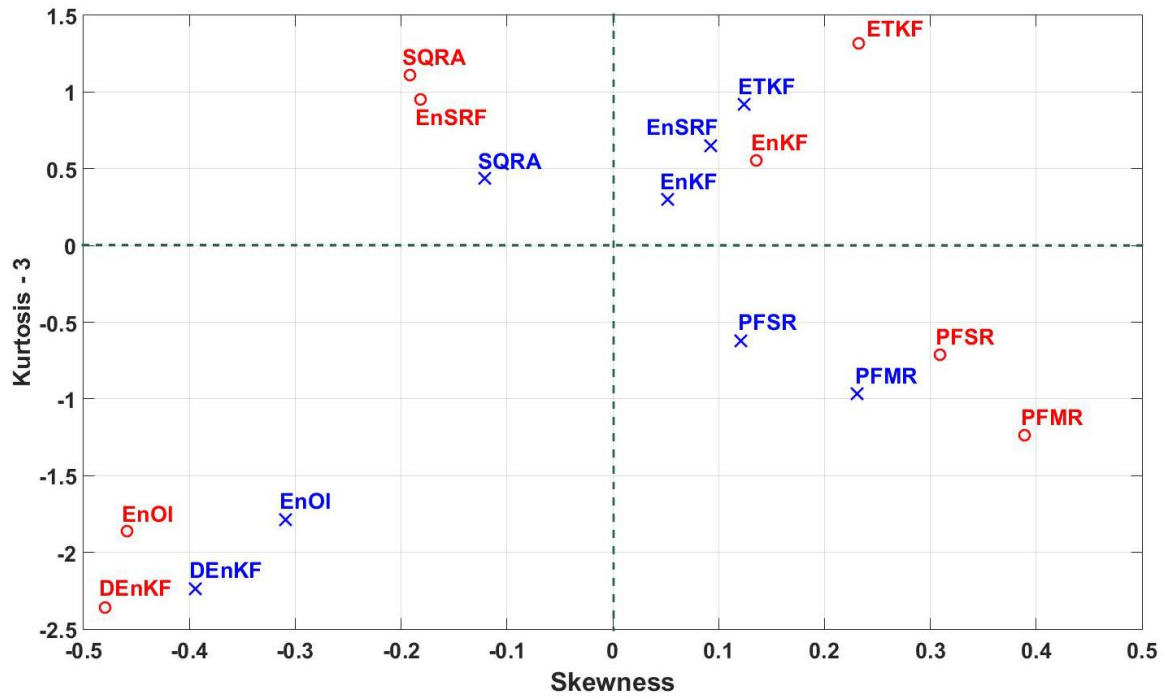


Figure 9: Comparison between the average skewness and kurtosis of each filter for forecast (red circles) and analysis (blue crosses). Note that a normal distribution has a kurtosis of 3 and uses as a reference so the excess kurtosis is usually presented by kurtosis-3.

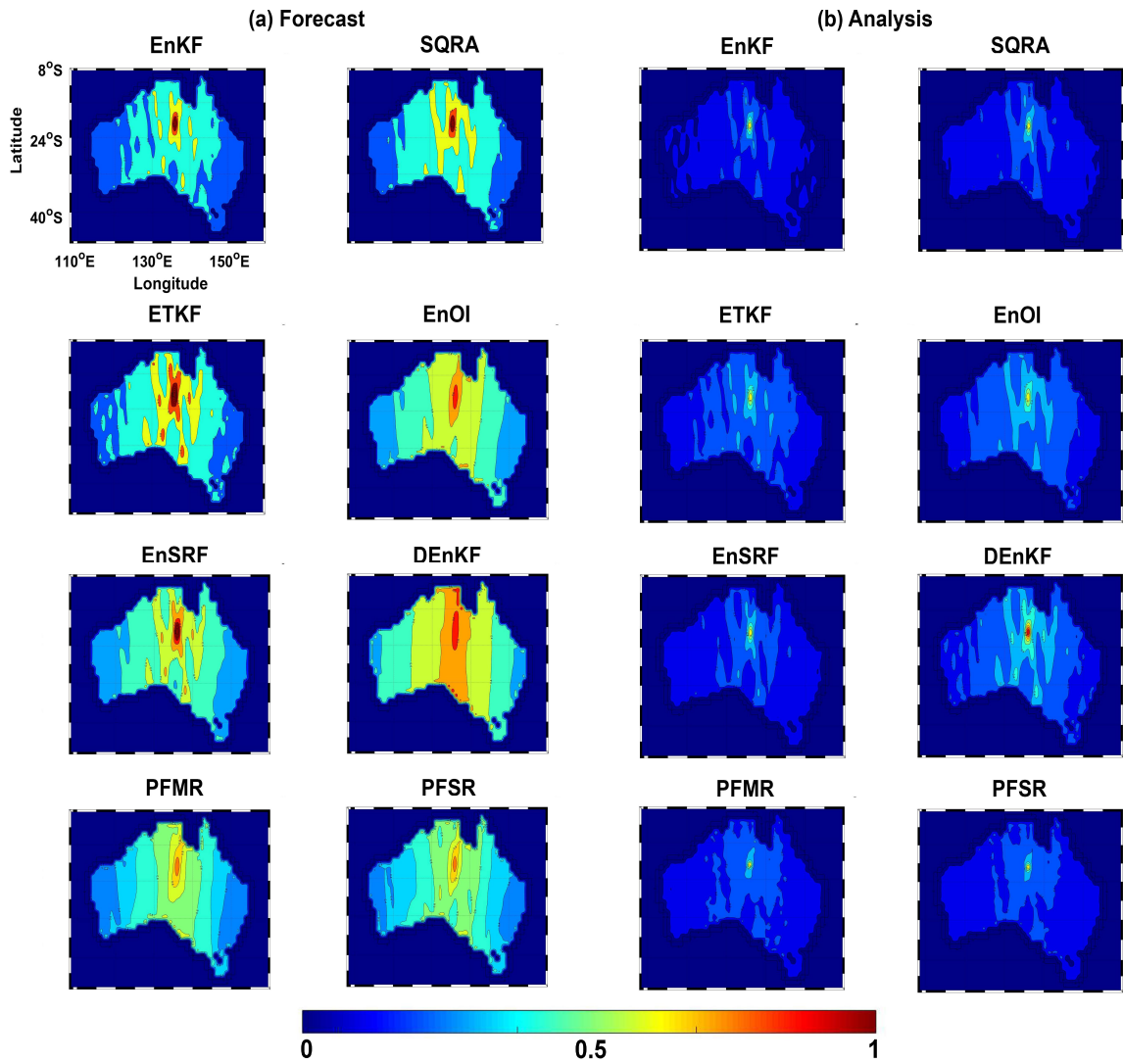


Figure 10: 2-D representation of correlation coefficients of TWS estimated between the arbitrary point (136.6854°E and 23.9015°S) and the rest of the grid points from the covariance matrices. The temporal average of the computed correlation coefficients in forecast and analysis steps are presented.

Table 1: A summary of the applied filters for data assimilation.

Filter	Acronym	Type	Reference
Ensemble Kalman Filter	EnKF	Stochastic ensemble Kalman filter	Evensen (1994)
Square Root Analysis	SQRA	Deterministic ensemble Kalman filter	Evensen (2004)
Ensemble Transform Kalman Filter	ETKF	Deterministic ensemble Kalman filter	Bishop et al. (2001)
Ensemble Square-Root Filter	EnSRF	Deterministic ensemble Kalman filter	Whitaker and Hamill (2002)
Ensemble Optimal Interpolation	EnOI	Deterministic ensemble Kalman filter	Evensen (2003)
Deterministic Ensemble Kalman Filter	DEnKF	Deterministic ensemble Kalman filter	Sakov and Oke (2008)
Particle Filter, Multinomial Resampling	PFMR	Particle filter	Arulampalam et al. (2002)
Particle Filter, Systematic Resampling	PFSR	Particle filter	Arulampalam et al. (2002)

Table 2: A summary of the statistics derived from the implemented methods using the assimilated GRACE data. The improvements in the analysis state RMSE estimates are calculated using the GRACE data in comparison to the model-free run.

Method	Forecast		Analysis		Improvement (%)
	RMSE (<i>mm</i>)	R^2	RMSE (<i>mm</i>)	R^2	
EnKF	26.5165	0.4354	16.5484	0.9084	39.59
SQRA	18.1156	0.4845	8.1208	0.9335	55.17
ETKF	21.8431	0.4456	14.8704	0.9123	41.92
EnOI	35.2105	0.3951	22.9304	0.7165	34.87
EnSRF	17.2950	0.4912	7.1105	0.9518	58.88
DEnKF	41.6417	0.3610	36.7408	0.6324	15.77
PFMR	37.6009	0.3851	30.2198	0.8137	19.63
PFSR	20.0344	0.4722	13.8711	0.9045	41.74

Table 3: A summary of the statistics derived from implemented methods using the groundwater in-situ measurements. The improvements in the analysis state RMSE estimates are calculated using the in-situ measurements in comparison to the model-free run.

Method	Forecast		Analysis		Improvement (%)
	RMSE (<i>mm</i>)	R^2	RMSE (<i>mm</i>)	R^2	
EnKF	62.6521	0.2254	41.5469	0.6456	31.68
SQRA	56.3493	0.2834	32.1387	0.7546	42.96
ETKF	60.7741	0.2574	38.2156	0.6718	33.12
EnOI	89.5411	0.1756	61.0514	0.4675	23.82
EnSRF	58.5271	0.2378	33.7420	0.7225	42.35
DEnKF	112.9712	0.1454	84.3153	0.3385	10.36
PFMR	75.3744	0.1914	53.5445	0.5546	14.96
PFSR	61.0124	0.2246	35.4581	0.6840	37.88

Table 4: A summary of the average correlations between state estimates derived from implemented methods and the soil moisture in-situ measurements. The improvements in the analysis state estimates are calculated using the in-situ measurements in comparison to the model-free run.

Method	Forecast	Analysis	Improvement (%)
EnKF	0.6248	0.7824	25.22
SQRA	0.6524	0.8216	35.93
ETKF	0.6412	0.8003	28.81
EnOI	0.5706	0.6940	21.63
EnSRF	0.6331	0.8431	38.17
DEnKF	0.4867	0.5754	18.22
PFMR	0.5574	0.6835	22.62
PFSR	0.6128	0.7568	32.50

Table 5: Effects of filtering methods on the model state covariance matrix as a percentage improvement.

		Method							
		EnKF	SQRA	ETKF	EnOI	EnSRF	DEnKF	PFMR	PFSR
Error reduction (%)	Minimum	29	35	22	15	34	6	18	28
	Maximum	47	52	44	38	55	20	35	48
	Average	35	44	33	21	47	8	27	38