MNRAS 452, 2794-2803 (2015)

doi:10.1093/mnras/stv1427

Comparing simulations of ionization triggered star formation and observations in RCW 120

S. Walch, 1 * A. P. Whitworth, 2 T. G. Bisbas, 3 D. A. Hubber 4,5 and R. Wünsch⁶

Accepted 2015 June 24. Received 2015 June 24; in original form 2015 March 12

ABSTRACT

Massive clumps within the swept-up shells of bubbles, like that surrounding the galactic H II region RCW 120, have been interpreted in terms of the collect and collapse (C&C) mechanism for triggered star formation. The cold, dusty clumps surrounding RCW 120 are arranged in an almost spherical shell and harbour many young stellar objects. By performing high-resolution, three-dimensional smoothed particle hydrodynamics simulations of H II regions expanding into fractal molecular clouds, we investigate whether the formation of massive clumps in dense, swept-up shells necessarily requires the C&C mechanism. In a second step, we use RADMC-3D to compute the synthetic dust continuum emission from our simulations, in order to compare them with observations of RCW 120 made with APEX-LABOCA (The Large APEX BOlometer CAmera) at 870 µm. We show that a distribution of clumps similar to the one seen in RCW 120 can readily be explained by a non-uniform initial molecular cloud structure. Hence, a shell-like configuration of massive clumps does not imply that the C&C mechanism is at work. Rather, we find a hybrid form of triggering, which combines elements of C&C and radiation driven implosion (RDI). In addition, we investigate the reliability of deriving clump masses from their 870 µm emission. We find that for clumps with more than 100 M_☉ the observational estimates are accurate to within a factor of 2, while the agreement between simulated and observed masses is much worse for smaller clumps. We also find that even at 870 µm it is important to account for the radiative heating from triggered, embedded protostars.

Key words: hydrodynamics – stars: formation – ISM: bubbles – H II regions – galaxies: ISM.

1 INTRODUCTION

The possibility of star formation triggered by ionizing feedback from young, massive stars has been explored for several decades. From a theoretical point of view, two main triggering mechanisms have been suggested: collect and collapse (C&C) and radiation driven implosion (RDI).

The C&C mechanism was first analysed by Elmegreen & Lada (1977). In this mechanism, an expanding H II region sweeps up a layer of cold gas and dust beyond the ionization front (e.g. Dale, Bonnell & Whitworth 2007), and this shell eventually becomes gravitationally unstable due to the growth of perturbations along its surface (Elmegreen 1994; Whitworth et al. 1994b; Dale et al. 2009; Wünsch et al. 2010). One argument in favour of the C&C mecha-

nism is that it is predicted to spawn massive fragments (Whitworth et al. 1994a), and hence it affords the possibility of forming massive stars sequentially. The study by Thompson et al. (2012) of massive, young stellar objects (YSOs) associated with bubbles suggests that triggering could be responsible for the formation of between 14 and 30 per cent of all massive stars.

In contrast, RDI (Sandford, Whitaker & Klein 1982; Kessel-Deynet & Burkert 2003; Bisbas et al. 2011; Haworth & Harries 2012) triggers star formation by compressing pre-existing cold, but otherwise gravitationally stable, molecular cloud cores. Elmegreen, Kimura & Tosa (1995) were the first to show that bright rims are caused by ionization erosion around *pre-existing* turbulent clumps. Observational and theoretical studies (e.g. Gritschneder et al. 2009, 2010) suggest that RDI leads to star formation in the tips of pillarlike structures, for example as seen in the Eagle nebula (White et al. 1999). Tremblin et al. (2012) have conducted a similar study but focus on the formation of cometary globules, which form if the

¹University of Cologne, Zülpicher Str. 77, D-50937 Cologne, Germany

²School of Physics and Astronomy, Cardiff University, 5 The Parade, Cardiff CF24 3AA, UK

³Department of Physics and Astronomy, University College London, Gower Place, London WC1E 6BT, UK

⁴Excellence Cluster Universe, Technical University Munich, Boltzmannstr. 2, D-85748 Garching, Germany

⁵University Observatory Munich, Department of Physics, Ludwig-Maximilians-University Munich, Scheinerstr. 1, D-81679 Munich, Germany

⁶Astronomical Institute, Academy of Sciences of the Czech Republic, Bocni II 1401, CZ-141 31 Prague, Czech Republic

^{*} E-mail: walch@ph1.uni-koeln.de

turbulent pressure is high. Bisbas et al. (2011) have published a detailed numerical study of RDI in initially stable Bonnor–Ebert spheres.

The nearby H II region RCW 120 is one of the best studied H II regions in the Galactic plane. As observed with Spitzer at 8 μm (Churchwell et al. 2006), it appears to be an almost perfectly round bubble with a well-defined ionization front. Zavagno et al. (2007) and Deharveng et al. (2009) have combined Spitzer and 2MASS data with observations at 870 µm and 1.2 mm to analyse the star formation associated with RCW 120. They conclude that star formation in the shell of RCW 120 has probably been triggered by a combination of triggering mechanisms. Zavagno et al. (2010) study the YSO properties with Herschel PACS and SPIRE. They confirm the existence of a YSO with mass $M_{\star} = 8$ to $10 \,\mathrm{M}_{\odot}$ in one of the condensations, and identify a number of lower mass (0.8-4 M_☉) Class 0 sources within the shell. Massive clumps have also been found within the swept-up shells of other bubbles, e.g. Sh 104 (Deharveng et al. 2003) and RCW 79 (Zavagno et al. 2006), and it has been suggested that the C&C mechanism, which invokes the formation of massive clumps via shell fragmentation, could be at work. For all of these bubbles, the mass of the swept-up shell is in agreement with the expected swept-up mass (Anderson et al. 2012), as estimated using a simple model of an H II region expanding into a uniform-density ambient medium (e.g. Spitzer 1978; Whitworth et al. 1994a).

Walch et al. (2012b, 2013) show that clumpy, shell-like structures like that seen in RCW 120 are probably attributable to pre-existing density structures in the natal molecular cloud. During the expansion of the H II region and the collection of the dense shell, the pre-existing density structures are enhanced and lead to a clumpy distribution within the shell. The masses and locations of the sweptup clumps depend on the fractal density structure of the molecular cloud, through the parameters n and ρ_0 (see Section 2 and Walch et al. 2012b, 2013). Subsequently, the clumps grow in mass, and at the same time they are overrun and compressed by the H II region, until they become gravitationally unstable and collapse to form new stars. Due to the formation of massive clumps, it is possible that there is a second generation of massive star formation. This is a hybrid triggering scenario, which combines elements of both the C&C and RDI mechanisms. In this paper, we show that the distribution of massive clumps formed around an H II region, which expands into a structured molecular cloud, is in good agreement with observations of massive clumps around e.g. the Galactic H II region RCW 120.

The plan of the paper is the following. In Section 2, we describe the algorithm used to generate initial fractal molecular clouds, and the numerical method used to evolve them, including the treatment of ionizing radiation. In Section 3, we describe the resulting H $\scriptstyle\rm II$ regions and the modelled synthetic 870 μ m observations. We discuss the shell and clump masses inferred from the synthetic observations in Section 4, and compare them with the true masses. Our main conclusions are summarized in Section 5.

2 INITIAL CONDITIONS AND NUMERICAL METHOD

2.1 The generation of a fractal molecular cloud

The initial three-dimensional fractal density structure is constructed using an algorithm based on Fourier transformation. The algorithm has three main input parameters, (i) the 3D power spectral index n, where $P(k) \propto k^{-n}$, (ii) the random seed \mathcal{R} used to generate a particular cloud realization, and (iii) the density scaling constant ρ_0

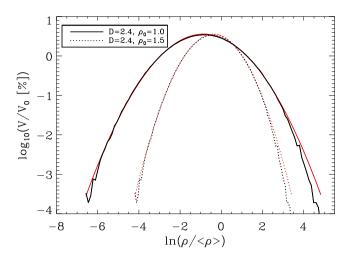


Figure 1. Volume-weighted density PDFs for fractal clouds having the same fractal dimension $\mathcal{D}=2.4$ and random seed \mathcal{R} , but different density scaling parameters: $\rho_0=1.5$ (dotted black line; Run 1) and $\rho_0=1.0$ (full black line; Run 2). Both distributions have been fitted with a lognormal (red lines).

(see below). We populate the integer modes k = 1–128 along each Cartesian axis (x, y, z), where k = 1 corresponds to the linear size of the cubic computational domain in one dimension. According to Stutzki et al. (1998), the box-coverage dimension, \mathcal{D} , of a fractal structure embedded in three-dimensional space is related to the power spectrum by

$$\mathcal{D} = 3 - \frac{(n-2)}{2} \tag{1}$$

(see also Federrath, Klessen & Schmidt 2009). Thus, defining \mathcal{D} is equivalent to defining the power spectral index n. Here, we choose setups with $\mathcal{D}=2.4$, in agreement with observations of molecular clouds in the Milky Way (Falgarone, Phillips & Walker 1991; Vogelaar & Wakker 1994; Stutzki et al. 1998; Lee 2004; Sánchez, Alfaro & Pérez 2005). This corresponds to n=3.2.

After constructing the density fluctuations in Fourier space, and applying a fast Fourier transform to generate $\rho_{\text{FFT}}(x, y, z)$ on a 128^3 grid, the resulting density field is scaled exponentially, using a scaling constant ρ_0 :

$$\rho(x, y, z) = \exp\left(\frac{\rho_{\text{FFT}}}{\rho_0}\right). \tag{2}$$

 $\rho(x,y,z)$ has a lognormal density probability density function (PDF) and a clump mass distribution in agreement with observations (as described in Shadmehri & Elmegreen 2011). In particular, for a given spectrum of density fluctuations, changing ρ_0 allows us to adjust the width of the density PDF, i.e. the variance σ of the lognormal distribution, whilst leaving the underlying topology of the density field unchanged. In Fig. 1, we show the resulting density PDFs for the two setups we discuss in this paper. Both clouds have equal mass (see Section 2.2), the same fractal dimension $\mathcal{D}=2.4$, and the same random seed \mathcal{R} , but two different values of ρ_0 .

Before populating the computational box with smoothed particle hydrodynamics (SPH) particles, we shift the point of maximum density to the centre of the computational domain, and position the ionizing star there. Then we partition the computational box with a 128^3 grid, compute the mass in each cell of the grid, and apportion each cell the corresponding number of SPH particles, distributed randomly within the cell. Finally, we cut out a sphere with radius $R_{\rm MC}$, centred on the ionizing star. The caveat of the fractal density

setup is that the particles all have no initial velocities. This assumption neglects possible flows towards/away from the source of ionizing radiation, which might change the detailed structure of the H $\scriptstyle\rm II$ region. However, since the recombination time in the ionized gas is $\lesssim 10^{-5}$ Myr, whereas the dynamical time-scale for the cloud is $\sim\!1$ Myr, radiative equilibrium should be a very good assumption, and the overall statistics of the structures that develop should not be significantly affected by such flows.

2.2 Initial conditions

We choose a cloud with total mass of $M_{\rm MC}=10^4\,{\rm M}_{\odot}$, and radius of $R_{\rm MC}=5.0\,{\rm pc}$. This results in a mean density of $\bar{\rho}=5.42\times10^{-21}\,{\rm g\,cm}^{-3}$, or equivalently $\bar{n}=1380\,{\rm cm}^{-3}$ for molecular gas having mean molecular weight $\mu=2.35$. The gas is initially isothermal at $T_{\rm MIN}=30\,{\rm K}$. In this paper, we discuss two simulations, both of which result in a shell-like structure very similar to the one observed in RCW 120. Apart from the scaling parameter ρ_0 , the initial clouds are identical, i.e. their density fields have the same topological structure. The simulation with $\rho_0=1.5$ (narrower density PDF in Fig. 1) is called *Run 1*, and the simulation with $\rho_0=1.0$ (broader PDF in Fig. 1) is called *Run 2*. By fitting their density PDFs using a χ -squared minimization method, we can estimate the standard deviation of the logarithmic density, viz. $\sigma_1=0.88$ (*Run 1*), and $\sigma_2=1.31$ (*Run 2*).

We can relate σ to the conditions produced in turbulent gas by introducing the scaling relation between σ and the turbulent Mach number derived by Padoan, Jones & Nordlund (1997), Padoan & Nordlund (2002) and Federrath, Klessen & Schmidt (2008),

$$\sigma^2 = \ln\left(1 + b^2 M^2\right),\tag{3}$$

with $b\simeq 0.5$. According to this relation, the density field in *Run 1* corresponds to a molecular cloud with Mach 2.2 turbulence; and *Run 2* corresponds to Mach 4.3 turbulence.

In both *Run 1* and *Run 2*, a star emitting hydrogen-ionizing photons at rate $\dot{N}_{\rm LyC}=10^{49}~{\rm s}^{-1}$ is placed at the centre of the cloud. This corresponds approximately to an O7.5 zero-age main-sequence (ZAMS) star with a mass of $\sim\!25\,{\rm M}_{\odot}$ and a surface temperature of $\sim\!40\,000\,{\rm K}$ (Osterbrock & Ferland 2006, their table 2.3). Thus, the ionizing source is more powerful than the central star within RCW 120, which is estimated to be an O8.5 to O9 star emitting $\dot{N}_{\rm LyC}=10^{48.04\pm0.1}~{\rm s}^{-1}$ (Zavagno et al. 2007).

2.3 Numerical method

We use the SPH code SEREN (Hubber et al. 2011), which is extensively tested and has already been applied to many problems in star formation (e.g. Bisbas et al. 2011; Stamatellos, Whitworth & Hubber 2011; Walch, Whitworth & Girichidis 2012a). The ionizing radiation is treated with a HEALPIX-based adaptive ray-splitting algorithm, which allows for optimal resolution of the ionization front in high-resolution simulations (see Bisbas et al. 2009). The implementation is based on the on-the-spot approximation (Zanstra 1951; Osterbrock 1974; Spitzer 1978), which is valid if the hydrogen number density is sufficiently high; this is usually the case, in particular in the vicinity of the ionization front. The ionization front is located along each ray by assuming radiative equilibrium. We employ the standard SPH algorithm (Monaghan 1992). The SPH equations of motion are solved with a second-order Leapfrog integrator, in conjunction with a block time-stepping scheme. Gravitational forces are calculated using an octal spatial decomposition tree (Barnes & Hut 1986), with monopole and quadrupole terms and a GADGET-style opening-angle criterion (Springel, Yoshida & White 2001). We use the standard artificial viscosity prescription (Monaghan & Gingold 1983), moderated with a Balsara switch (Balsara 1995). In both simulations we use 2.5×10^6 SPH particles. Thus, each particle has a mass $m_{\rm SPH} = 4.0 \times 10^{-3} \, {\rm M}_{\odot}$ and the minimum resolvable mass is $\sim 0.4 \, {\rm M}_{\odot}$ (Bate & Burkert 1997).

The temperature of ionized gas particles well *inside* the ionization front is set to 10 000 K. The temperature of neutral gas particles well *outside* the ionization front is given by a barotropic equation of state that mimics the gross thermal behaviour of protostellar gas (Masunaga, Miyama & Inutsuka 1998, their fig. 4),

$$T(\rho) = T_{\text{MIN}} \left\{ 1 + \left(\frac{\rho}{\rho_{\text{CRIT}}} \right)^{(\gamma - 1)} \right\}, \tag{4}$$

with $T_{\rm MIN}=30~{\rm K}$, $\rho_{\rm CRIT}=10^{-13}~{\rm g}~{\rm cm}^{-3}$ and $\gamma=5/3$. Thus, for densities below $\rho_{\rm CRIT}$, the gas is approximately isothermal at 30 K, and for densities above $\rho_{\rm CRIT}$, the gas is approximately adiabatic with adiabatic index $\gamma=5/3$ (γ has the monatomic value, because, although the gas is primarily molecular hydrogen, it is too cold for the internal degrees of freedom of the hydrogen molecules, even the rotational ones, to be excited). The choice of $T_{\rm MIN}=30~{\rm K}$ is somewhat arbitrary, and was initially chosen simply because it agrees with the estimate in Deharveng et al. (2009). However, it agrees well with the mean *dust*-temperature calculated a posteriori using RADMC-3D (see Section 4.3). The temperatures of SPH particles within one local SPH smoothing length of the ionization front are forced to vary smoothly between the temperature of the ionized gas on one side and the temperature of the neutral gas on the other; this is required to avoid a numerical instability.

We use a new sink particle algorithm to capture forming protostars (Hubber, Walch & Whitworth 2013). Sinks are introduced at density peaks above $\rho_{\text{SINK}} = 10^{-11} \, \text{g cm}^{-3}$, provided that the density peak in question is at the bottom of its local gravitational potential well. Since $\rho_{\text{SINK}} \gg \rho_{\text{CRIT}}$, a peak that is converted into a sink is always well into its Kelvin-Helmholtz contraction phase. Once created, a sink has a radius of twice the SPH smoothing length at ρ_{SINK} , i.e. $R_{\text{SINK}} = 20$ au. A sink then accretes mass smoothly from the surrounding SPH particles within R_{SINK} , over many dynamical time-scales, but transfers their angular momentum to SPH particles just outside R_{SINK} (see Hubber et al. 2013, for more details). This procedure ensures that the masses and locations of sink particles are essentially independent of the arbitrary parameters of sink creation and evolution, ρ_{SINK} and R_{SINK} . Sinks are identified as protostars, and their luminosity can be included in the radiative transfer models produced with RADMC-3D in the post-processing step (Section 3.3).

3 RESULTS

3.1 SPH simulations

In this subsection we discuss the results of the SPH simulations. In Fig. 2, we show the initial and final column density distributions for the simulations. Note that $Run\ 2$ has the broader density PDF, and hence the more pronounced density contrasts in the initial conditions. Both setups develop an H II region with a diameter of \sim 5 pc. We compare the two simulations at the time when a total mass of \sim 500 M $_{\odot}$ has been converted into stars, which is $t_{\rm END}=0.98$ Myr for $Run\ 1$ and $t_{\rm END}=0.68$ Myr for $Run\ 2$. The black dots in the

¹ Both runs could be followed further, but become extremely time-consuming and slow once the dense shell is collapsing in many places.



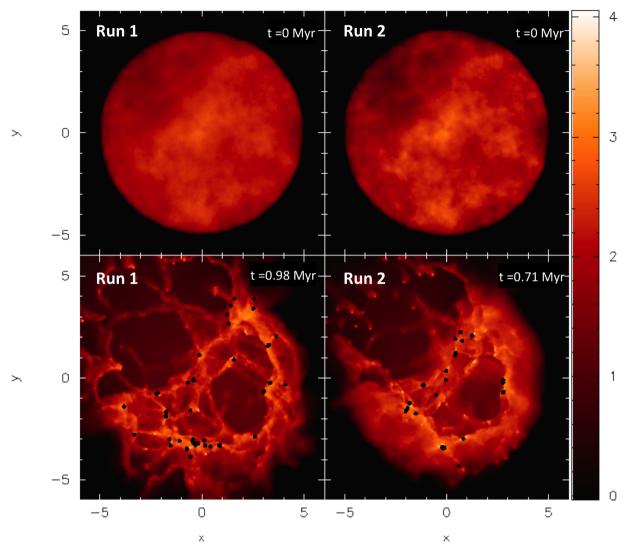


Figure 2. Upper panels: initial column-density distributions in M_{\odot} pc⁻² for the two runs. In both cases the initial conditions have been generated with the same fractal dimension, $\mathcal{D}=2.4$, and the same random seed, \mathcal{R} , but different scaling densities: $\rho_0=1.5$ (Run 1; left-hand column) and $\rho_0=1.0$ (Run 2; right-hand column). Lower panels: the column density distributions at $t_{\rm END}$, after $\sim 500\,{\rm M}_{\odot}$ of the cloud (~ 5 per cent) has been converted into stars. The black dots mark sink particles, which represent forming protostars. Each frame is $12\,{\rm pc}\times 12\,{\rm pc}$.

evolved H $\scriptstyle\rm II$ regions mark sink particles, which represent forming protostars. At $t_{\scriptstyle\rm END}$ there are 79 sinks in Run~1 and 38 sinks in Run~2. We stress that the simulations are highly dynamical. New sinks are constantly formed and existing sinks continue to accrete at different rates.

In Fig. 3, we plot the mass accretion rate on to each sink particle as a function of its mass. The masses range from $\sim M_{\odot}$ to $\sim 40 \, \rm M_{\odot}$. The accretion rates of sink particles that have essentially stopped accreting are arbitrarily set to $\dot{M}_{\rm MIN} = 10^{-10} \, \rm M_{\odot} \, yr^{-1}$; most of these are from Run~1. For all other sinks there is no clear correlation between sink mass and mass accretion rate, and the mean accretion rate is $\sim 10^{-5} \, \rm M_{\odot} \, yr^{-1}$ in both Runs.~Run~2 forms more massive stars than Run~1, and has a clutch of eight massive and rapidly accreting sink particles at $t_{\rm END}$.

3.2 Overall bubble structure

As with RCW 120, we find that the shells formed in our simulations are not perfectly spherical, but elongated and perforated. For example, in the simulations illustrated in Fig. 2 the initial cloud has a region of reduced column density in the north-west corner, where the ionized gas breaks through and streams out, thereby relieving the pressure of the H $\scriptstyle\rm II$ inside the bubble.

The SPH mass distribution does show some small pillars and evaporating gaseous globules close to the north-west hole, but in general pillars are not a prominent feature of H $\scriptstyle\rm II$ regions expanding into clouds with fractal dimension $\mathcal{D}=2.4$, because – for this fractal dimension – large-scale density fluctuations dominate the cloud structure (Walch et al. 2012b).

3.3 Synthetic observations

In a post-processing step, we map the SPH density distributions at $t_{\rm END}$ on to a three-dimensional grid of $128^3~(0.12~{\rm pc})^3$ cells, using kernel-weighted interpolation. Hence the spatial resolution of the grid at the distance of RCW120, $D=1.34~{\rm kpc}$, corresponds to the angular resolution of 19.2 arcsec achieved when observing RCW 120 with APEX-LABOCA (The Large APEX BOlometer CAmera)

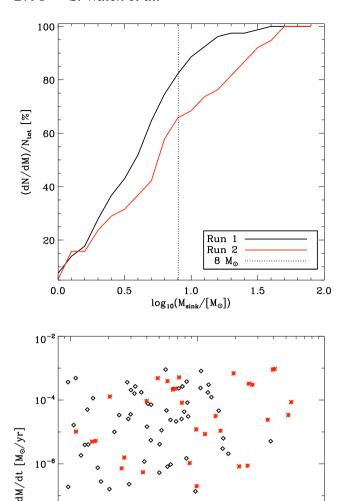


Figure 3. Upper panel: cumulative sink mass functions at $t_{\rm END}$, for Run 1 (black line) and Run 2 (red line), showing that Run 2 forms a higher proportion of massive stars than Run 1. The vertical dotted line marks $8~{\rm M}_{\odot}$, which is usually taken as the lower limit for a massive star, so at this stage $\sim 17~{\rm per}$ cent of the stars in Run 1 are massive, and $\sim 34~{\rm per}$ cent of the stars in Run 2 are massive. Lower panel: mass accretion rate, \dot{M} , plotted against current mass, M, at $t_{\rm END}$, for the sink particles formed in Run 1 (black open diamonds) and Run 2 (red stars). For sinks that have essentially stopped accreting, we set $\dot{M} = 10^{-10}~{\rm M}_{\odot}~{\rm yr}^{-1}$, so they appear in a line along the bottom of the plot; these stars are predominantly formed in Run 1. For the remaining sink particles, there is no strong correlation between \dot{M} and M, and no obvious difference between the stars formed in Run 1 and Run 2, apart from a clutch of eight massive, rapidly accreting stars in Run 2.

10

 $M_{sink} [M_{\odot}]$

Run 1 ♦

100

Run 2

at 870 μ m (Deharveng et al. 2009). All the main clumps and condensations are well resolved with $\gtrsim 10^4$ SPH particles. Assuming the standard, uniform gas-to-dust ratio of 100, the distribution of SPH particles translates directly into the distribution of dust. The only modification to this rule is that we assume dust to be destroyed at gas temperatures $T > T_{\rm cut} = 1200$ K, and therefore the dust den-

sity is set to a small offset value in cells above this temperature, which are exclusively those in the H $\scriptstyle\rm II$ region; the offset value is 10^{-3} times the minimum dust density in the rest of the computational domain. We only take into account silicate dust grains, on the assumption that these dominate the opacity at 870 μ m. We use the standard opacity table for this species given by Draine & Lee (1984).

Using the gridded density distribution, we model the transport of continuum radiation against dust opacity using RADMC-3D² (version 0.25, written by C. Dullemond; see also Peters et al. 2010). In the first step RADMC-3D performs a thermal Monte Carlo (MC) radiative transfer simulation to determine the equilibrium dust-temperature distribution. The MC implementation is based on the method of Bjorkman & Wood (2001), but includes various improvements, for instance the continuous absorption method of Lucy (1999). The total luminosity of all sources within the computational domain is distributed amongst $N_{\rm PHOT}=10\times10^6$ photon packages, where half of them, i.e. $N_{\rm SCAT}=5\times10^6$ photon packages, are used to compute scattering events. In one set of radiative transfer calculations we only invoke radiation from the central ionizing star; henceforth we refer to these calculations as ionizing source only. In addition, we perform radiative transfer calculations in which radiation from the newly-formed protostars is also included; henceforth we refer to these calculations as secondary sources included, and distinguish quantities derived from these calculations with a superscript *. For these calculations, we assume that each sink particle represents a single protostar. The luminosities of the protostars are estimated on the assumption that they are ZAMS main-sequence stars. This probably results in a significant underestimate of their time-averaged luminosities, but since the luminosities of young protostars are expected to be highly variable, due to infrequent episodic accretion bursts, this seems the safest way to proceed.

In the second step, RADMC-3D computes isophotal maps at 870 μ m, using ray tracing. Fig. 4 shows the resulting isophotal maps of our simulations, as seen in their (x, y)-projection. The outer white contour marks the 0.1 Jy beam⁻¹ cut-off value, which we use to define the total mass of the shell. The inner white contour marks the 0.5 Jy beam⁻¹ value, which we use to define the masses of the clumps. With radiation from the ionizing source only (top row of Fig. 4), the total flux an observer at 1.34 kpc would receive at 870 μ m is $F_{870}^{\text{tot}} = 312 \,\text{Jy}$ for $Run\ 1$ and $F_{870}^{\text{tot}} = 535 \,\text{Jy}$ for $Run\ 2$. If radiation from the secondary sources is included (bottom row of Fig. 4), the resulting total fluxes are significantly higher: $F_{870}^{\text{tot}} = 500 \,\text{Jy}$ for $Run\ 1$ and $F_{870}^{\text{tot}} = 760 \,\text{Jy}$ for $Run\ 2$. The fluxes are higher in the second case, because most of the newly-formed protostars are located in the shell, and in or near the clumps.

Qualitatively, the synthetic isophotal maps of our simulations are very similar to the $870\,\mu m$ observations of RCW 120. In the following, we compare synthetic and observed images in greater detail, in order to assess the SPH simulation, but also to evaluate the uncertainty of the mass estimates for clumps in the shell of RCW 120

We use the 0.5 Jy beam⁻¹ contour to define clumps within the shell. In particular, we identify the three most massive clumps, which we label C1, C2, C3, and focus our analysis on their properties. The total mass and number of sinks located within each clump are listed in Table 1. The mass in gas and dust in the shells and in the individual clumps are listed in Table 2, which we describe more thoroughly in the next section.

10⁻⁸

² http://www.ita.uni-heidelberg.de/~dullemond/software/radmc-3d

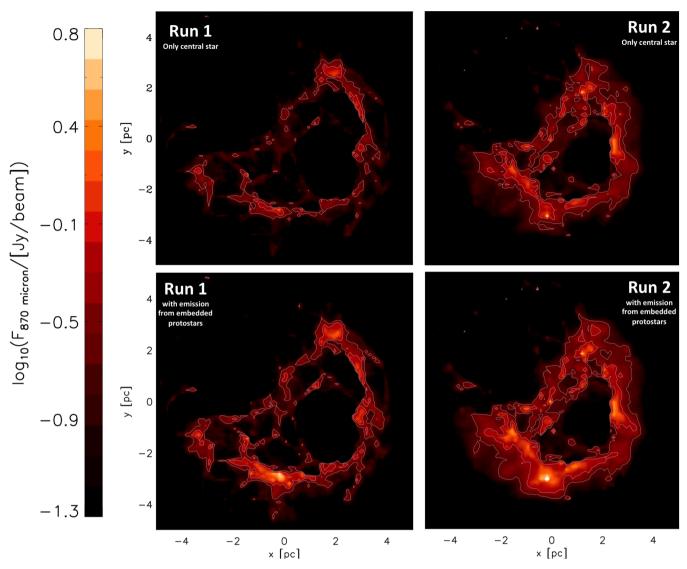


Figure 4. 870 μ m emission calculated using RADMC-3D. The frames on the left refer to Run 1, and those on the right to Run 2; the frames on the top row have been calculated with radiation from the ionizing source only, and those on the bottom row with radiation from secondary sources included. The left-hand column shows the images for Run 1, and the right-hand column for Run 2. The white contours are set to fluxes of 0.1 and 0.5 Jy beam⁻¹ in all images. Each frame is $12 \text{ pc} \times 12 \text{ pc}$.

Table 1. Properties of the sink particles embedded in the shell, and in the main clumps. For $Run\ 1\ (Run\ 2)$, Column 1 (4) gives the ID of the shell or clump, Column 2 (5) the number of sink particles it contains, and Column 3 (6) the total mass of the sinks it contains, at $t_{\rm END}$. Note that the sink masses do not add up to the total mass in sink particles at $t_{\rm END}$, because some sinks are located outside the main clumps.

| Run 1 | | | Run 2 | | |
|-------|--|---------------|-------|---|---------------|
| С | $\frac{M_{\mathrm{SINK,tot}}}{(\mathrm{M}_{\odot})}$ | $N_{ m SINK}$ | С | $\frac{M_{\rm SINK,tot}}{({ m M}_{\odot})}$ | $N_{ m SINK}$ |
| Shell | 400.0 | 31 | Shell | 483.0 | 36 |
| C1 | 0.0 | 0 | C1 | 34.6 | 3 |
| C2 | 0.0 | 0 | C2 | 54.2 | 6 |
| C3 | 140.0 | 11 | C3 | 171.0 | 9 |

4 DISCUSSION

4.1 Clump masses

In order to compare the simulations with observations of RCW 120, we adopt the same procedure as in Deharveng et al. (2009) to calculate the masses of the shells, and of the individual clumps, from the synthetic emission maps,

$$M_{870} = 100 \frac{F_{870} D^2}{\kappa_{870} B_{870} (T_{\text{DUST}})}.$$
 (5)

Here D is the distance of the source ($D=1.34\,\mathrm{kpc}$ for RCW 120), $\kappa_{870}=1.8\,\mathrm{cm^2\,g^{-1}}$ (Ossenkopf & Henning 1994) is the opacity per unit mass of dust at 870 $\mu\mathrm{m}$, and $B_{870}(T_\mathrm{DUST})$ is the Planck function at 870 $\mu\mathrm{m}$ for dust temperature T_DUST . We adopt $T_\mathrm{DUST}=30\,\mathrm{K}$, since we do not allow the gas to cool below this temperature in the simulations; Deharveng et al. (2009) also invoke this temperature

Table 2. Column 1 identifies the different structures analysed. Columns 2 and 3 give mass estimates derived by applying equation (5) to the synthetic 870 μ m images which were calculated with radiation from the ionizing source only, M_{870} , and with radiation from secondary sources included, M_{870}^{\star} (see Fig. 5). Columns 4 and 5 give the true masses, obtained by integrating the SPH column density over the area inside the 0.1 Jy beam⁻¹ contour for shells, and the 0.5 Jy beam⁻¹ contour for the clumps. M_{TRUE} is the mass within these contour levels calculated with radiation from the ionizing star only, whereas M_{TRUE}^{\star} is the mass within these contour levels calculated with radiation from the secondary sources included. Both, M_{TRUE} and M_{TRUE}^{\star} account only for the mass of gas and dust and do not include embedded protostars (here, each sink particle is treated as a single protostar); the total mass of embedded sink particles is listed in Table 1.

| ID | $(\overline{	ext{M}_{\odot}})$ | $(\overline{\mathrm{M}_{\odot}^{\star}})$ | $rac{M_{ m TRUE}}{({ m M}_{\odot})}$ | $\frac{M_{\mathrm{TRUE}}^{\star}}{(\mathrm{M}_{\odot})}$ |
|-------|--------------------------------|---|---------------------------------------|--|
| | | Run 1 | | |
| Shell | 1818 | 2928 | 3031 | 4450 |
| C1 | 33 | 91 | 5.0 | 23.0 |
| C2 | 75 | 146 | 114 | 262 |
| C3 | 61 | 493 | 32.0 | 336 |
| | | Run 2 | | |
| Shell | 3013 | 4420 | 6291 | 6853 |
| C1 | 193 | 302 | 129 | 228 |
| C2 | 74 | 184 | 114 | 270 |
| C3 | 160 | 783 | 89 | 655 |

to analyse their results. A constant gas-to-dust mass ratio of 100 has been assumed.

In Fig. 5, we show the mass distribution derived from the isophotal maps using equation (5). For reference we overplot the 0.1 and 0.5 Jy beam contours from Fig. 4, which define – respectively – the shell and the most massive clumps. For *Run 1* we calculate a total shell mass of $1818\,\mathrm{M}_\odot$ with radiation from the ionizing source only, and $2928\,\mathrm{M}_\odot$ with radiation from secondary sources included. Both of these estimates are similar to the shell mass of $1100\,\mathrm{M}_\odot$ found in RCW 120 with $T_\mathrm{DUST}=30\,\mathrm{K}$. For *Run 2* the corresponding shell masses are 3013 and $4420\,\mathrm{M}_\odot$.

4.2 Massive clumps without C&C

We divide the shells up into clumps using the $0.5 \, \mathrm{Jy} \, \mathrm{beam}^{-1}$ contour on the synthetic isophotal maps. These clumps typically have masses between a few and a few hundred M_{\odot} . In Fig. 5, we identify the three main clumps formed in each Run , and their properties are listed in Table 2. All these clumps are sufficiently massive that they may spawn massive sink particles, leading to sequential propagation of massive star formation (see Koenig et al. 2012, for observational evidence of sequential triggering).

The individual clumps are well aligned with the overall structure of the ionization front and the swept-up dense shell. However, our simulations clearly show that the formation of separate clumps in these simulations is not really due to C&C – in the sense that at no time do we observe the formation of a coherent shell, which grows to subsequently become gravitationally unstable and undergo fragmentation. The seeds for the clumps are already present in the initial fractal density structure of the cloud, and as the H II region expands

it sweeps additional low-density material into the clumps, and the clumps themselves are pushed outwards and collect additional material that way. At the same time, the ionizing radiation penetrates low-density regions much more easily than high-density regions, and as a result the hot, high-pressure ionized gas tends to envelop the dense clumps and compress them, as in RDI. It is the combination of collecting additional mass *and* being enveloped by the H II region that renders the clumps unstable and drives them into collapse. This is therefore a hybrid process, combining elements of both C&C and RDI. Based on 2D radiation-hydrodynamic simulations, Elmegreen et al. (1995) discuss a similar scenario for massive core formation by shock focusing of turbulent clumps inside a moving post-shock layer.

We are unable to comment on whether individual protostars are regularly spaced within individual clumps (as noted by Deharveng et al. (2009) in the unsharp-masked $24 \,\mu m$ *Spitzer* image of their Condensation 1) because properly modelling the $24 \,\mu m$ emission is beyond the scope of this paper (see for example, Koepferl et al. 2015). However, we note that regularly spaced protostars could also arise in the scenario we have described above; they are not necessarily a product of C&C.

The masses estimated for the three main clumps are strongly dependent on whether the radiative transfer modelling includes the radiation from secondary sources or not (see Table 2 and Section 4.3). The variations can be as high as a factor of 8, as is the case for clump C3 in $Run\ I$, for which the estimated mass increases from 61 to 493 M_{\odot} when the radiation from secondary sources is included. This is because the extra heating from newly-formed protostars makes the dust in their vicinity hotter, and therefore more material falls within the 0.5 Jy beam $^{-1}$ threshold.

In a companion paper (Walch et al. 2013) we show that the mass distribution of the swept-up clumps depends on the initial fractal dimension of the cloud. Low fractal dimensions lead to a density distribution that is dominated by large-scale density fluctuations. Hence the average resulting clump mass is higher than in the case of high fractal dimension, where the density distribution is dominated by small-scale fluctuations, which leads to a smaller average clump mass. For the case of $\mathcal{D}=2.4$, which is in good agreement with observations, we expect an intermediate result.

4.3 How reliable is the mass distribution obtained from $870 \mu m$ fluxes?

In this section we compare how well the actual mass distribution in the simulations is recovered by applying equation (5) to the synthetic isophotal maps at $870\,\mu m$. This comparison can provide useful insights into the reliability of clump mass estimates from observational data.

We define four masses, and list their values in Table 2. M_{870} is the mass obtained using equation (5) on synthetic isophotal maps calculated with radiation from the ionizing source only, and M_{870}^{\star} is the mass obtained in the same way, but with secondary sources included. Likewise, M_{TRUE} is the actual mass falling within a shell or clump on synthetic 870 μ m isophotal maps calculated with radiation from the ionizing source only, whilst M_{TRUE}^{\star} is the corresponding quantity obtained when radiation from secondary sources is included in the radiation transfer modelling. M_{TRUE} and M_{TRUE}^{\star} are obtained by integrating the surface density of SPH particles over the area covered by the shell or clump (i.e. the area inside the 0.1 or 0.5 Jy beam⁻¹ contours, respectively).

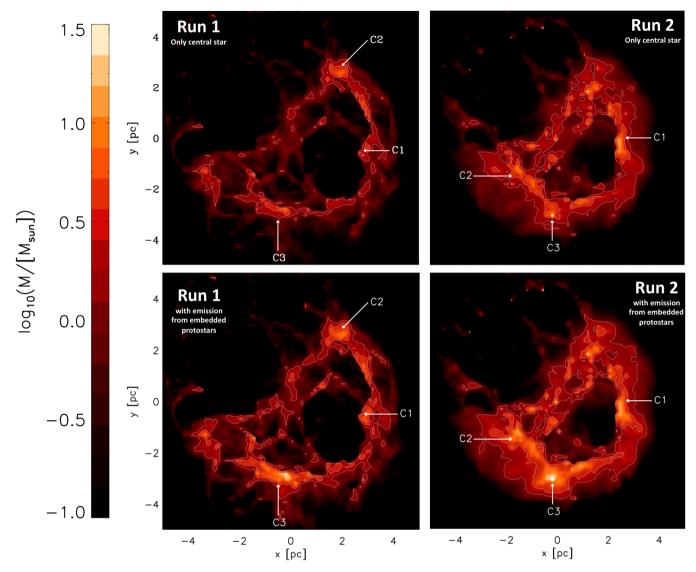


Figure 5. Mass distribution derived from the thermal dust emission at 870 μ m shown in Fig. 4. For comparison we overlay contours marking 0.1 and 0.5 Jy beam⁻¹ from Fig. 4. As in Fig. 4, the frames on the left refer to Run 1, and those on the right to Run 2; the frames on the top row have been calculated with radiation from the ionizing source only, and those on the bottom row with radiation from secondary sources included. The three largest clumps, which are discussed in the text, are marked with C1, C2 and C3. Each frame is 12 pc \times 12 pc.

The resulting fractional errors,

$$\epsilon = \frac{\left| M_{870} - M_{\text{TRUE}} \right|}{M_{\text{TRUE}}} \,, \tag{6}$$

and

$$\epsilon^{\star} = \frac{\left| M_{870}^{\star} - M_{\text{TRUE}}^{\star} \right|}{M_{\text{TRUF}}^{\star}}, \tag{7}$$

are plotted against the true masses (M_{TRUE} , M_{TRUE}^*) in Fig. 6. The shell masses obtained using equation (5) on synthetic 870 μ m isophotal maps are always lower than the true masses, typically by a factor $\lesssim 2$, irrespective of whether the radiation from secondary sources is included or not. In contrast, the masses of individual *clumps* obtained using equation (5) on synthetic 870 μ m isophotal maps are sometimes higher and sometimes lower than the true masses; for massive clumps (>100 μ) the fractional error is always less than two, but for lower mass clumps it can be very large, and such masses should probably not be trusted.

In general, masses obtained using equation (5) on synthetic 870 µm maps calculated including radiation from secondary sources are more accurate than those obtained with radiation from the ionizing source only, as they should be. In order to quantify the effect of including secondary sources, we have generated the mass-weighted distribution of temperature, both with and without secondary sources; in addition, we have generated the corresponding distributions for radiation transport calculations without the gas-temperature cut-off at $T_{\rm cut} = 1200 \, \rm K$, so that emission from dust within the H II region is included. The resulting distributions for Run 1 are shown in Fig. 7; similar results are obtained for Run 2. We note two features of this plot. First, when there is no cut-off, the mean dust-temperature is lower. This is because the dust in the H II region absorbs much of the short wavelength radiation from the ionizing source and the newly-formed protostars, and then radiates it at long wavelengths, with the result that it escapes without heating the neutral gas further out. Secondly, when the secondary sources are included, the mean dust-temperature is almost exactly 30 K,

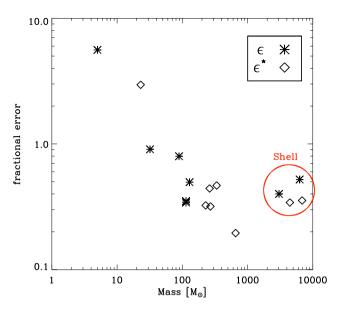


Figure 6. Fractional errors in the masses of shells and clumps, which were obtained using equation (5) on the synthetic isophotal maps, plotted against their true masses. Here, $\epsilon = \frac{|M_{870} - M_{TRUE}|}{M_{TRUE}}$ (see equation 6; star symbols) is the fractional error without radiation from newly-formed protostars and ϵ^{\star} is the fractional error including the radiation from newly-formed protostars (see equation 7; open diamonds). A value of 0 is a perfect match, while a value of 1 corresponds to a difference of 100 per cent, respectively a factor of 2. Values pertaining to the shell are contained within the red ring; all the other values represent clumps. The two outliers with a fractional error greater than 1 correspond to C1 in Run 1, for which M_{870} is much larger than M_{TRUE} .

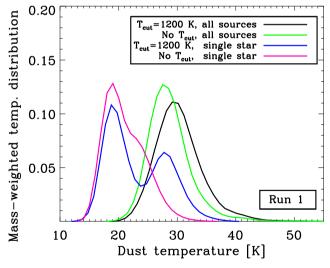


Figure 7. Mass-weighted dust-temperature distribution for different RADMC-3D models of Run 1. All dust-temperature distributions were derived using 10^7 photon packages. The black line shows the fiducial case, where we include the emission from triggered protostars and cut the dust abundance at gas temperatures above $T_{\rm cut}=1200$ K, while the green line ('No $T_{\rm cut}$ ') shows the case where also dust within the H II region is included. Most of the mass is found at $T_{\rm dust}=30$ K. In the latter case the distribution shifts to a slightly colder mean temperature since less photons are available to heat the dust within the shell due to the increased absorption within the H II region. The blue and pink lines show the resulting dust-temperature distribution in the case that only the emission from the central O-star is taken into account.

as we have assumed following the observational interpretation of RCW 120.

5 CONCLUSIONS

We have performed high-resolution SPH simulations of H II regions expanding into fractal molecular clouds, and compared synthetic 870 μm isophotal maps of these simulations (obtained using RADMC-3D) to 870 μm observations of the well-studied, galactic H II region RCW 120. Our model reproduces a swept-up shell with a mass between 3000 and 7000 M_{\odot} . The shell contains several star-forming clumps, with masses between 30 and 700 M_{\odot} . These cores are not formed by shell fragmentation.

We suggest that finding massive clumps and sites of high mass star formation within an expanding shell around an H II region need not, and probably should not, be taken as evidence for the C&C mechanism at work. The clumpiness of the dense shell can be attributed to density structures in the fractal, turbulent, molecular cloud into which the H II region expands. Two processes combine to render the larger clumps gravitationally unstable. First the expanding H II region sweeps lower density gas into the clumps, and pushes the clumps outwards so they also sweep up lower density gas further out. Secondly, the H II region advances more rapidly through the lower density gas around a clump, thereby enveloping and squeezing it. In other words, a hybrid mechanism is at work, which combines elements of C&C and RDI; it is not standard C&C because at no stage does a coherent shell form and then become gravitationally unstable and fragment, but it relates to C&C because the clumps do collect additional material, due to the expansion of the H II region. A detailed study of the growth of clumps in the shells of expanding H II regions is presented in Walch et al. (2013).

Overall, we find good agreement (to within a factor of 2) between the actual mass distribution and the mass distribution inferred from thermal dust emission, for shells and clumps having masses greater than $\sim\!100\,M_{\odot}$. In particular, masses estimated from synthetic 870 μm isophotal maps always underpredict the mass of the large-scale <code>shell</code> structure, whereas for individual <code>clumps</code> both overand underestimates are possible, and usually the result is accurate to within a factor of 2. To obtain a realistic estimate of the shell and clump masses from synthetic 870 μm isophotal maps, it is important to take into account the heating from embedded protostars.

ACKNOWLEDGEMENTS

We thank the anonymous referee for her/his very useful comments, which helped us to improve the paper. SW and AW acknowledge the support of the Marie Curie RTN CONSTELLATION. SW further thanks the DFG for their support in the framework of the ISM priority programme 1573 and through SFB 956 on 'The conditions and impact of star formation'. The work of TGB was funded by STFC grant ST/J001511/1. RW acknowledges support by the Czech Science Foundation grant 209/12/1795 and by the project RVO: 67985815; the Academy of Sciences of the Czech Republic. The column density plots were made using the SPLASH visualization code (Price 2007). This paper is a revised and resubmitted version of arXiv1109.3478 (http://arxiv.org/abs/1109.3478).

REFERENCES

Anderson L. D. et al., 2012, A&A, 542, A10 Balsara D. S., 1995, J. Comput. Phys., 121, 357 Barnes J., Hut P., 1986, Nature, 324, 446 Bate M. R., Burkert A., 1997, MNRAS, 288, 1060

Bisbas T. G., Wünsch R., Whitworth A. P., Hubber D. A., 2009, A&A, 497, 649

Bisbas T. G., Wünsch R., Whitworth A. P., Hubber D. A., Walch S., 2011, ApJ, 736, 142

Bjorkman J. E., Wood K., 2001, ApJ, 554, 615

Churchwell E. et al., 2006, ApJ, 649, 759

Dale J. E., Bonnell I. A., Whitworth A. P., 2007, MNRAS, 375, 1291

Dale J. E., Wünsch R., Whitworth A., Palouš J., 2009, MNRAS, 398, 1537Deharveng L., Lefloch B., Zavagno A., Caplan J., Whitworth A. P., Nadeau D., Martín S., 2003, A&A, 408, L25

Deharveng L., Zavagno A., Schuller F., Caplan J., Pomarès M., De Breuck C., 2009, A&A, 496, 177

Draine B. T., Lee H. M., 1984, ApJ, 285, 89

Elmegreen B. G., 1994, ApJ, 427, 384

Elmegreen B. G., Lada C. J., 1977, ApJ, 214, 725

Elmegreen B. G., Kimura T., Tosa M., 1995, ApJ, 451, 675

Falgarone E., Phillips T. G., Walker C. K., 1991, ApJ, 378, 186

Federrath C., Klessen R. S., Schmidt W., 2008, ApJ, 688, L79

Federrath C., Klessen R. S., Schmidt W., 2009, ApJ, 692, 364

Gritschneder M., Naab T., Walch S., Burkert A., Heitsch F., 2009, ApJ, 694, L26

Gritschneder M., Burkert A., Naab T., Walch S., 2010, ApJ, 723, 971

Haworth T. J., Harries T. J., 2012, MNRAS, 420, 562

Hubber D. A., Batty C. P., McLeod A., Whitworth A. P., 2011, A&A, 529, A27

Hubber D. A., Walch S., Whitworth A. P., 2013, MNRAS, 430, 3261

Kessel-Deynet O., Burkert A., 2003, MNRAS, 338, 545

Koenig X. P., Leisawitz D. T., Benford D. J., Rebull L. M., Padgett D. L., Assef R. J., 2012, ApJ, 744, 130

Koepferl C. M., Robitaille T. P., Morales E. F. E., Johnston K. G., 2015, ApJ, 799, 53

Lee Y., 2004, J. Korean Astron. Soc., 37, 137

Lucy L. B., 1999, A&A, 344, 282

Masunaga H., Miyama S. M., Inutsuka S.-i., 1998, ApJ, 495, 346

Monaghan J. J., 1992, ARA&A, 30, 543

Monaghan J. J., Gingold R. A., 1983, J. Comput. Phys., 52, 374

Ossenkopf V., Henning T., 1994, A&A, 291, 943

Osterbrock D. E., 1974, Astrophysics of Gaseous Nebulae. Freeman & Co., San Francisco

Osterbrock D. E., Ferland G. J., 2006, Astrophysics of Gaseous Nebulae and Active Galactic Nuclei. University Science Books, Sausalito, CA

Padoan P., Nordlund Å., 2002, ApJ, 576, 870

Padoan P., Jones B. J. T., Nordlund A. P., 1997, ApJ, 474, 730

Peters T., Mac Low M.-M., Banerjee R., Klessen R. S., Dullemond C. P., 2010, ApJ, 719, 831

Price D. J., 2007, PASA, 24, 159

Sánchez N., Alfaro E. J., Pérez E., 2005, ApJ, 625, 849

Sandford M. T., II, Whitaker R. W., Klein R. I., 1982, ApJ, 260, 183

Shadmehri M., Elmegreen B. G., 2011, MNRAS, 410, 788

Spitzer L., 1978, Physical Processes in the Interstellar Medium. Wiley-Interscience, New York

Springel V., Yoshida N., White S. D. M., 2001, New Astron., 6, 79

Stamatellos D., Whitworth A. P., Hubber D. A., 2011, ApJ, 730, 32

Stutzki J., Bensch F., Heithausen A., Ossenkopf V., Zielinsky M., 1998, A&A, 336, 697

Thompson M. A., Urquhart J. S., Moore T. J. T., Morgan L. K., 2012, MNRAS, 421, 408

Tremblin P., Audit E., Minier V., Schmidt W., Schneider N., 2012, A&A, 546, A33

Vogelaar M. G. R., Wakker B. P., 1994, A&A, 291, 557

Walch S., Whitworth A. P., Girichidis P., 2012a, MNRAS, 419, 760

Walch S. K., Whitworth A. P., Bisbas T., Wünsch R., Hubber D., 2012b, MNRAS, 427, 625

Walch S., Whitworth A. P., Bisbas T. G., Wünsch R., Hubber D. A., 2013, MNRAS, 435, 917

White G. J. et al., 1999, A&A, 342, 233

Whitworth A. P., Bhattal A. S., Chapman S. J., Disney M. J., Turner J. A., 1994a, MNRAS, 268, 291

Whitworth A. P., Bhattal A. S., Chapman S. J., Disney M. J., Turner J. A., 1994b, A&A, 290, 421

Wünsch R., Dale J. E., Palouš J., Whitworth A. P., 2010, MNRAS, 407, 1963

Zanstra H., 1951, Bull. Astron. Inst. Neth., 11, 359

Zavagno A., Deharveng L., Comerón F., Brand J., Massi F., Caplan J., Russeil D., 2006, A&A, 446, 171

Zavagno A., Pomarès M., Deharveng L., Hosokawa T., Russeil D., Caplan J., 2007, A&A, 472, 835

Zavagno A. et al., 2010, A&A, 518, L81

This paper has been typeset from a TEX/LATEX file prepared by the author.