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1       **Effect of flood hydrograph duration, magnitude, and shape on bed-load**  
2    **transport dynamics**

3  
4 **Authors** C. B. Phillips<sup>1</sup>, K. M. Hill<sup>2,4</sup>, C. Paola<sup>3,4</sup>, M. B. Singer<sup>5</sup>, and D. J. Jerolmack<sup>6</sup>

5  
6 <sup>1</sup>Civil and Environmental Engineering, Northwestern University, Evanston, IL.

7 <sup>2</sup>Civil, Environmental, and Geo-Engineering, University of Minnesota, Minneapolis, MN.

8 <sup>3</sup>Earth Sciences, University of Minnesota, Minneapolis, MN.

9 <sup>4</sup>St. Anthony Falls Laboratory, University of Minnesota, Minneapolis, MN.

10 <sup>5</sup>Earth and Ocean Sciences, Cardiff University, Cardiff, UK.

11 <sup>6</sup>Earth and Environmental Sciences, University of Pennsylvania, Philadelphia, PA.

12  
13 Corresponding author: Colin B. Phillips (colinbphillips@gmail.com)

14  
15 **Key Points**

16 (1) Laboratory experiments reveal that cumulative bed load flux for a flood is linearly related to  
17 the flow impulse (integrated potential transport capacity).

18 (2) For an equivalent flow impulse, transient and steady floods transport the same total bed-load  
19 sediment flux.

20 (3) Flood duration, magnitude and shape affect bed load flux in terms of their contribution to the  
21 flow impulse but are otherwise interchangeable for well sorted gravel.

22

23 **Abstract**

24 Bed load sediment transport is an inherently challenging process to measure within a river,  
25 which is further complicated by the typically transient nature of the hydrograph. Here we use  
26 laboratory experiments to explore how sediment flux under transient – unsteady and intermittent  
27 – flow differ from those under steady flow. For a narrow unimodal sediment distribution, we  
28 calculated fluid stress and measured sediment flux for a range of hydrograph durations,  
29 magnitudes, shapes, and sequences. Within a hydrograph, we find considerable variability in  
30 sediment flux for a given stress above the threshold for motion. However, cumulative bed-load  
31 flux resulting from a flood scales linearly with the integrated excess transport capacity (flow  
32 impulse). This scaling indicates that, to first order, flow magnitude, duration, shape, and  
33 sequence are only relevant to bedload flux in terms of their contribution to the total flow  
34 impulse, in agreement with prior field results. The flood impulse represents a quantitative  
35 parameter through which the effects of transient flow on coarse sediment transport may be  
36 parsed.

37

38 **Plain language summary**

39 Mountain river floods produced from snowmelt can last months but remain relatively shallow,  
40 while floods resulting from storms are often shorter in duration and deeper. These floods have, in  
41 a sense, different “shapes” and “sizes” determined by their environment and climate. We  
42 performed laboratory experiments to understand how these flood shapes and sizes affect the  
43 amount of sediment they can move, a key precursor to understanding how rivers and flooding  
44 impact the landscapes in which they reside. Our experiments show that if one accounts for the  
45 forcing of the flood in a physically based manner, there is no difference between floods of  
46 different shapes and sizes in terms of how much sediment they move. We suggest that these  
47 results may make floods easier to characterize when modeling landscapes.

48

49 **1. Introduction**

50 Under steady flow, the rate of bed-load transport in rivers is a stochastic process that varies both  
51 spatially and temporally due to turbulent fluid-stress fluctuations, bed topography, and granular  
52 structure. Field and laboratory observations demonstrate that variability within the grain size  
53 distribution (Wilcock and McArdell, 1997), the magnitude of upstream sediment supply (Singer,

54 2010; Recking, 2012), mobility (Wilcock, 1998), and structural arrangement (Church et al.,  
55 1998; Strom et al., 2004; Zimmermann et al., 2010; Marquis and Roy, 2012; Houssais et al.,  
56 2015) of river-bed sediments affect the flux resulting from an applied flow stress (Recking,  
57 2013). Stream hydrology is assumed to be a primary control on the magnitude and duration of  
58 the applied bed stress. In natural environments, river flows are rarely steady as gravel-bed rivers  
59 typically experience flows that exceed the threshold required for sediment motion only during  
60 floods. Strictly speaking, natural floods violate the assumptions of steady and uniform flow  
61 required for current sediment transport calculations. The transience of natural hydrographs  
62 presents a barrier to applying the mechanistic understanding of sediment transport dynamics  
63 developed under steady flows in laboratory experiments to natural rivers.

64  
65 At timescales of a single flood event (from the initiation of motion to the cessation of bed  
66 material transport) to timescales of multiple flood events, it remains an open question how steady  
67 and transient flows differ in terms of their effects on channel morphology and bed load sediment  
68 dynamics. Observations within the natural environment have led to the attribution of various  
69 phenomena to aspects of transient flow such as: the degree of vertical and spatial bed grain size  
70 segregation (armor) (Reid and Laronne, 1995), the amount of grain protrusion (Yager et al.,  
71 2012), channel bed complexity (Singer and Michaelides, 2014; Whiting and Stamm, 1995), and  
72 variability in the threshold of motion (Turowski, 2011). However, for flows in natural rivers it is  
73 exceedingly difficult to distinguish between phenomena that occur under steady flow and those  
74 that require a transient hydrograph. The majority of transient-flow laboratory experiments  
75 explore the role of magnitude and duration (Hassan et al., 2006; Bombar et al., 2011; Humphries  
76 et al., 2012; Mao, 2012), flow sequence (Humphries et al., 2012; Guney et al., 2013; Waters and  
77 Curran 2015), and to a lesser degree the time between floods (intermittency) (Ferrer-Boix and  
78 Hassan, 2015; Masteller and Finnegan, 2017) on the development of bed-surface texture in  
79 mixed unimodal or bimodal sediment beds. When compared with their accompanying steady  
80 flow counterparts, these experiments collectively paint a complex picture of the intermixing of  
81 gravel-bed morphology, adjustment timescales, and mixed grain-size mobility thresholds (e.g.  
82 Wilcock, 1998; Wilcock and Crowe, 2003; Parker et al. 2008) with changing flow rates at  
83 various durations. Using a well sorted gravel sediment with constant sediment feed and a  
84 sequence of identical hydrographs, Wong and Parker (2006) determined that downstream of a

85 short inlet boundary layer, the sediment flux adjusted to track the variations in the hydrograph.  
86 The use of sediment beds with broad, mixed, or bimodal grain-size distributions complicates  
87 these findings considerably (An et al., 2017). With more complex grain-size distributions the  
88 magnitude of the peak and duration of the rising and falling limbs have the potential to create  
89 bed states with a higher threshold of motion (Mao, 2012). These complex bed states induce a  
90 variety of hysteresis loops between flow and sediment flux (Mao, 2012; Humphries et al., 2012;  
91 Guney et al., 2013), making it difficult to predict the instantaneous flux using equations  
92 developed under steady flow conditions (Guney et al., 2013; Lee et al., 2004). However, despite  
93 the shortcomings of most transport equations to compute instantaneous transport, they can be  
94 modified to provide reasonable predictions of the total flux (Lee et al., 2004; Wong and Parker,  
95 2006; Humphries et al., 2012), suggesting that this complexity may not be intractable over  
96 complete flood hydrographs.

97  
98 Linking sediment transport dynamics to landscape evolution requires developing physically  
99 based metrics capable of bridging the gaps between discrete floods, sequences of hydrographs  
100 that define a regional climate, and the long-term approximation of hydrographs within landscape  
101 evolution models (Paola et al., 1992; Lague, 2014; Phillips and Jerolmack, 2016). Recent field  
102 results on the transport of marked tracer cobbles demonstrate that despite substantial hydrologic  
103 variability, average particle displacement scales linearly with the integrated excess shear  
104 velocity, or impulse (Phillips et al., 2013; Phillips and Jerolmack, 2014; Imhoff and Wilcox,  
105 2016), suggesting that to first order the effects of flow transience may be accounted for through  
106 the quantification of the flow impulse. However, substantial variability exists within these data  
107 as the cumulative impulse is scaled down to that of a single flood. Here we report results from  
108 laboratory flume experiments at St. Anthony Falls Laboratory (SAFL) at the University of  
109 Minnesota under transient flow to quantitatively compare the flow impulse to bed load flux for  
110 individual floods and sequences of floods (Phillips, 2018). These experiments explore a  
111 parameter space of magnitude and duration for four geometrically simplified flood shapes. We  
112 demonstrate that even with a well sorted unimodal sediment bed, there is considerable variability  
113 in instantaneous flux-stress relationships for different flood shapes. At the same time, we show  
114 that, when integrated over a flood hydrograph, flows of equivalent total impulse transport the

115 same total sediment flux. Finally, we show how the impulse concept can be used to normalize  
 116 floods to facilitate the comparison of both steady and unsteady floods.

117

## 118 **2. Experiments**

### 119 **2.1 Experimental design**

120 Our experiments do not attempt to recreate a natural flood regime in the lab (Paola et al., 2009).

121 Rather they are designed to understand how transport in transient flows might differ from steady

122 flows and how the components of transient flows, unsteadiness and intermittence, potentially

123 contribute to different sediment dynamics. We explore these components of flow transience

124 through the use of sequences of geometrically simplified steady and unsteady floods where the

125 effects of flood peak magnitude, duration, and shape on sediment transport dynamics can be

126 independently investigated (Figure 1a-b). For clarity, in this Letter, we use the term ‘flood’ to

127 refer to a distinct transport event, from the period where particles start moving to when they stop.

128 We use ‘flood shape’ to describe the time dependence of the flow magnitude for a single flood,

129 and the phrase ‘flood sequence’ to refer to multiple sequential discrete floods. Flood sequences

130 of steady or unsteady floods represent the intermittent component of transient flows (Figure 1c).

131 To compare the effects of these components on particle transport, we normalize each flood by its

132 potential fluid-derived transport capacity, or impulse ( $T_*$ ):

$$133 T_* = \int_{t_s}^{t_f} (U_\tau^2 - U_{\tau c}^2)^{3/2} dt / gD^2 \quad (1)$$

134 where  $U_\tau$  is the shear velocity (m/s),  $U_{\tau c}$  is the threshold shear velocity for sediment motion

135 (m/s),  $g$  is the acceleration due to gravity ( $m/s^2$ ),  $D$  is a representative grain size (m) taken here

136 as the geometric mean, and  $t_f$  and  $t_s$  are the starting and ending times of the flood, respectively.

137 We note that equation (1) is valid only for flows able to transport sediment ( $U_\tau > U_{\tau c}$ ). We then

138 compare runs of equivalent  $T_*$  and varying magnitude, duration, and shape in terms of their

139 measured dimensionless cumulative sediment flux ( $Q_*$ ):

$$140 Q_* = \int_{t_s}^{t_f} (q_b) dt / D^2 \quad (2)$$

141 where  $q_b$  is the volumetric sediment flux per unit width ( $m^2/s$ ). Normalizing each flood by  $T_*$

142 accounts for the expected average behavior under steady flow, effectively representing all flows

143 as square waves, because  $T_*$  does not distinguish between flow magnitude, duration, or shape.

144

145 We performed two experiments to isolate the effects of transient flow at the flood scale. The first  
146 experiment is comprised of sequences of floods with constant peak hydrograph magnitudes,  
147 while sequences of floods in the second experiment had variable peak magnitudes (Figure 1c). In  
148 the first type of experiments, we ran sequences (12-20) of intermixed steady and unsteady floods  
149 with equal  $T^*$  and equivalent hydrograph peak magnitude. To explore a parameter space of peak  
150 magnitude and duration (Figure 1b) we ran additional sequences with increased or decreased  
151 flood magnitude and/or flood duration (see supporting information and Figure S2). The second  
152 set of experiments was designed to test the effects of sequences of floods (6-12) with variable  
153 magnitude and duration (Figure 1c lower panel). These experiments allow us to contrast sets of  
154 floods with high magnitude and short duration against those of low magnitude and longer  
155 duration, but with equivalent  $T^*$ . Throughout both experiments, the bed within the test section of  
156 the flume was not disturbed or altered; it was allowed to evolve.

157

## 158 **2.2 Experimental setup**

159 We conducted the experiments at SAFL in a 30 m by 0.5 m sediment and water feed flume  
160 (Figure S1). Water discharge ( $Q$ , m<sup>3</sup>/s) was controlled using a variable speed pump that  
161 discharged into a head tank before flowing over a weir and entering the 22.5 m long  
162 experimental section of the flume. The flume data acquisition system was set up to record  
163 measurements every second of water surface elevation and the mass of sediment accumulating at  
164 the end of the flume. A narrow unimodal mixture of sediment (with geometric mean diameter  
165  $D=7.2$  mm and standard deviation 1.2 mm) was fed 2.5 m downstream of the inlet weir via  
166 sediment feeder during all periods when bed shear stress exceeded the critical threshold for  
167 motion. We note that we used the same sediment and flume, though with a different setup, as  
168 used in Wong and Parker (2006), Wong et al. (2007), and Hill et al. (2010). For each run, water  
169 discharge was brought from baseflow up to the peak flow rate and then back to baseflow. In the  
170 case of unsteady runs, the rate of rise and fall depends on the shape of the hydrograph (Figure 2a  
171 & S2). This results in a temporally variable and often rapidly changing flow depth within the  
172 flume. We kept the slope of the sediment bed at steady state, no net aggradation or erosion, by  
173 feeding sediment for each flood such that  $Q_{*in} \approx Q_{*out}$ , resulting in a proportional feed system. To  
174 achieve this, we adjusted the sediment feed rate for each flood (Figure S3) such that sediment

175 was supplied only during periods where the flood was capable of transporting sediment (see  
 176 supporting information for additional details).

177  
 178 Cumulative time series of sediment mass leaving the flume were continuously recorded as the  
 179 sediment deposited in a submerged suspended basket attached to a load cell (Interface SMT2-  
 180 500 N load cell, Figure S1). Water surface elevation (1 Hz, 1 mm accuracy) was measured at  
 181 three locations within the flume using ultrasonic transducers (Massa mPulse M-5000, Figure S1).  
 182 To reduce experimental noise within the time series all data were smoothed using a Savitzky-  
 183 Golay filter (7 second window, 2<sup>nd</sup> order polynomial). Laser sheet scans of bed topography (1  
 184 mm vertical and horizontal accuracy) were taken between sets of floods after the flow was turned  
 185 off and the flume had been allowed to drain the surface layer. The sediment mass, bed  
 186 topography scans, and water surface elevation data were used to derive the remaining variables.  
 187 Sediment flux ( $q_s$ , kg/s) represents the derivative of the cumulative mass time series over an  
 188 eight-second moving window. Water surface slope ( $S$ ) was estimated from the first and third  
 189 sensors by linear regression (see supporting information for further explanation). Flow depth ( $h$ ,  
 190 m) was estimated by differencing the intermittent bed topography scans from the water surface  
 191 elevation time series. The sediment bed slope remained relatively constant ( $S_{mean}=9.3\times 10^{-3}$  and  
 192  $S_{SD}=7.4\times 10^{-4}$ ) throughout both series of experiments, and differences in bed elevation ( $\Delta Z$ , mm)  
 193 between scans for the location where  $h$  was calculated were small ( $\Delta Z_{mean}=-0.1$  mm and  
 194  $\Delta Z_{SD}=1.5$  mm). Flow velocity ( $U$ , m/s) was calculated as  $U=Q/(hb)$  where  $b$  is the flume width.  
 195 Shear stress ( $\tau$ , Pa) was approximated using the procedure outlined in Vanoni and Brooks (1975)  
 196 to account for sidewall effects using time series of:  $h$ ,  $S$ ,  $Q$ , and  $U$ . We calculated shear velocity  
 197 as  $U_\tau = \sqrt{\tau/\rho}$  and Shields stress as  $\tau_* = \tau/(\rho_s - \rho)gD$ , where  $\rho_s$  is sediment density (2650  
 198 kg/m<sup>3</sup>), and  $\rho$  is the water density. Additional methodological notes are available in the  
 199 supporting information.

200

### 201 **3. Results**

202 For each flood, measured time series of water surface elevation and sediment mass were used to  
 203 derive time series of flow discharge, velocity, depth, water surface slope, and sediment flux  
 204 (Figure 2). Time series data are available for 209 runs totaling 23.5 hours of experiments and  
 205 2,155 kg of transported sediment with: peak  $U_\tau=0.087-0.12$  ( $\tau_*=0.065-0.12$ ), ratios of peak



206  $U_{\tau}/U_{\tau_c}=1.08-1.5$  ( $\tau^*/\tau_{*c}=1.18-2.23$ ), total durations ranging from 2.5-30 min, durations above the  
 207 threshold of motion of 0.6-29.1 min (Figure 1c), and cumulative flux masses per flood ranging  
 208 from 1-32 kg. We examine the results from these experiments first within individual floods and  
 209 second at the scale of a complete flood and multiple flood sequences.

210

### 211 **3.1 Within a flood**

212 Within each flood there is considerable variability between sediment flux and stress; however we  
 213 find that to first order the stress flux data can be described by a bed-load transport equation of the  
 214 form  $q^*=K(\tau^*-\tau_{*c})^\alpha$  (Meyer-Peter and Müller, 1948; Wong and Parker, 2006) (Figure 2b), where  
 215  $q^*$  is the dimensionless volumetric sediment flux. Here we fix the exponent at  $\alpha=1.5$  (Wong and  
 216 Parker, 2006; Wong et al., 2007). Allowing  $\alpha$  to vary produces only minor improvements that do  
 217 not provide a strong justification for the additional free parameter. We note that similar  
 218 formulations of the flux law (see Table 1 in Lajeunesse et al., 2010) provide equally convincing  
 219 fits to the data. For any given run, we observe a small range of coefficients, average threshold  
 220 stresses, and in some cases thresholds of initiation and cessation of transport (Figure 2b & c) that  
 221 change between rising and falling hydrograph limbs. We observe counter-clockwise hysteresis in  
 222 sediment flux primarily when the flow changes rapidly. The hysteresis occurs over short  
 223 timescales and represents a small fraction of the sediment flux. Hysteresis in sediment flux and  
 224 hysteresis in the threshold of motion were not always coincident in the same flood.

225

### 226 **3.2 Flood and sequence scale**

227 Examining the flux data at the sequence scale we find that all steady and transient floods follow  
 228 a similar trend (Figure 3a). There is considerable scatter in the flux data; however, the mean of  
 229 the data cloud is well described by a single transport law of the same power law form fit to data  
 230 from individual floods (Figure S4a), except those at the highest stresses, where data are sparse.  
 231 We fit the transport law to all data where  $q^* \geq 0$  and  $\tau^* \geq 0.045$  by least-squares regression,  
 232 yielding parameters for the coefficient ( $K=5.0$ ) and threshold of motion ( $\tau_{*c}=0.055$ ). These  
 233 cutoffs for  $\tau^*$  and  $q^*$  arise from the sensitivity of the load cell and noise associated with the  
 234 experimental set up of the sediment weighing basket. We also separated the bulk flux data into  
 235 steady and unsteady floods as well as by flood shape to assess if these subsets of the data  
 236 behaved differently. Inspection of the distributions of residuals determined from the transport

237 law (fit in Figure 3a) for each subset yield minimal discernable differences between them (Figure  
238 S4a-c).

239  
240 To compare flows of different shape, peak magnitude, and duration we computed  $T^*$  for each  
241 flood (eq. 1). Since the flux data can be represented with a single transport law (Figure 3a), we  
242 compute equations 1 and 2 for all runs using a single value for the threshold of motion ( $U_{\tau c}=0.08$   
243 m/s). Additionally, we use a single value for grain size ( $D=0.0072$  m) in both equations 1 and 2.  
244 After computing both integrated parameters we find that to first order the  $T^*$  parameter collapses  
245 the flux data onto a single linear trend (Figure 3b). All floods but one are within a factor of 1.5 of  
246 the mean trend. Within this data collapse, there is no systematic variation in the data with respect  
247 to flood magnitude, duration, or shape.

248

#### 249 **4. Discussion and Conclusions**

250 The degree of complexity present in the flux data for each run (Figure 2 a-c) is evident in the  
251 hysteresis present in both the calculated threshold of motion and magnitude of flux on the rising  
252 and falling limbs of unsteady flows. Hysteresis loops in these experiments occur for floods with  
253 rapidly changing hydraulic stresses and are typically absent in runs when the flow gradually  
254 increases or decreases. The short timescales over which the hysteresis is present for both rising  
255 and falling flows indicate a lag between the calculated instantaneous stress via the depth-slope  
256 product and the response of the bed, suggesting there may be a minimum time required to  
257 average the flow conditions in order to compute a representative stress via the depth-slope  
258 product. Hysteresis is common in transient flow experiments (Hassan et al., 2006; Mao, 2012),  
259 however the short run times and well-sorted gravel bed presented here preclude most of the  
260 commonly reported mechanisms. The narrow grain size distribution reduces grain scale sorting,  
261 armoring, and size selective transport, which even under steady flows can result in differentially  
262 mobile populations of bed sediments (Wilcock and McArdell, 1997). Additionally, the short  
263 duration of competent flow limits the effects of phenomena with longer timescales of adjustment  
264 such as bedforms and sediment texture (Ferrer-Boix and Hassan, 2014). In terms of total flux,  
265 though, the observed hysteresis represents a small fraction of the sediment transported in a flood.

266

267 Interestingly, and perhaps surprisingly, this intra-flood variability is not evident at the scale of a  
268 single flood, in which  $T^*$  collapses the  $Q^*$  data onto a single linear relation (Figure 3b). In terms  
269 of their cumulative sediment flux, the linear scaling between  $T^*$  and  $Q^*$  indicates that unsteady  
270 runs are equivalent to steady runs. The scatter in cumulative flux about the mean trend does not  
271 vary systematically with flood duration, peak magnitude, shape, or sequence, indicating its  
272 source is not associated with flood type or flow transience. Additionally, the data collapse  
273 indicates that for the parameter space explored here, flow magnitude and duration are relevant  
274 only in how they contribute to  $T^*$ . Under these conditions the sediment flux does not depend on  
275 the flow history, indicating that the sequence of runs did not exert substantial control on the total  
276 flux. This flow history independence indicates a memoryless system under the given conditions.  
277 In terms of flood intermittency, the linear scaling indicates that not only can a series of smaller  
278 events' impulses be summed to equal a run with a larger impulse, but that the sequence of the  
279 smaller impulses of various shapes does not matter (Figure 1 & 3).

280

281 The linear scaling between  $T^*$  and  $Q^*$  and its implications are contingent on the validity of the  
282 non-linear flux law relating  $U_\tau$  or  $\tau^*$  to  $q^*$  that forms the basis of the impulse (Equation 1).  
283 However, these experiments demonstrate that this relation need be valid only at an integral scale  
284 to recover a reasonable collapse of the data (Figure 3b), though this integral scale remains to be  
285 determined in natural systems. To place these results into a broader context, we summarize two  
286 important limitations of these experiments: (1) limited flow durations and (2) limited range of  
287 shear velocity. The limited flow durations simulated here preclude the observation of  
288 morphologic structures with longer time scales of formation or adjustment, if they are not  
289 already precluded by the narrow grain size distribution. The range in peak stress magnitudes is  
290 comparable to previous similar experiments (Hassan et al., 2006; Mao, 2012; Humphries et al.,  
291 2012) and represents approximately half the reach average transport capacity ( $U_\tau/U_{\tau c}$ ) observed  
292 within natural bed load rivers (Phillips and Jerolmack, 2016). In practice, this limited range of  
293 peak stresses may be less restricting as bed-load flux laws are more robust for  $U_\tau \gg U_{\tau c}$  (Capart  
294 and Fraccarollo, 2011; Recking et al., 2012). Meaningful deviations from the flux law are more  
295 likely for floods with low stress magnitudes near the threshold of motion, where sufficiently  
296 longer averaging timescales are required (Recking et al., 2012; Houssais et al., 2015). In such  
297 cases, dynamic interactions between the bed and the flow may be capable of altering  $U_{\tau c}$ . This

298 includes processes such as bed dilation due to high stresses or compaction from constant forcing  
299 above and below the threshold of motion (Charru et al. 2004; Marquis and Roy, 2012; Houssais  
300 et al., 2015; Masteller and Finnegan, 2017). However, such dynamic interactions were not  
301 observed within the data.

302  
303 The largest unknown is the role of the grain size distribution, as the narrow one used here greatly  
304 reduced the textural, morphological, and granular adjustments that could have occurred (see  
305 Ferrer-Boix and Hassan, 2014) within the flume (by design). Introducing a wider grain-size  
306 distribution with particle size dependent mobility (common for broad or bimodal grain size  
307 distributions) would likely require the impulse in equation (1) to be modified to reflect a  
308 fractional transport equation (Wilcock and Crowe, 2003). The narrow grain size distribution was  
309 chosen to isolate the influence of the hydrograph; however, one of the implications of our  
310 experiments is that the grain-size distribution potentially represents the largest source of  
311 variability (Hassan et al., 2006). It remains an open question which grain-size distribution  
312 (bimodal, broad, or mixed transport), when paired with transient flow, has the greatest potential  
313 to add memory to the system.

314  
315 Despite the limitations, our results may be more general than they initially seem. These  
316 experiments support the surprising conclusion that the total sediment mass transported is  
317 insensitive to the details of the transient hydraulic forcing, as has also been observed for bed load  
318 tracers in natural rivers (Phillips et al., 2013; Imhoff and Wilcox, 2016). Additionally, these  
319 results are (in spirit) the same treatment of the hydrograph embodied in the simplest physically  
320 based models of landscape evolution (see Paola et al., 1992), where the full complexity of a  
321 hydrograph is replaced by the bankfull flood (average, see Phillips and Jerolmack, 2016)  
322 multiplied by an intermittency factor. This similarity is by no means a complete test of such  
323 treatments, due to our simplified size distribution, other missing processes, and scale differences,  
324 yet it does reinforce the notion present in both landscape evolution models and field tracer  
325 studies that substantial complexity need not preclude a simple treatment.

326

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337

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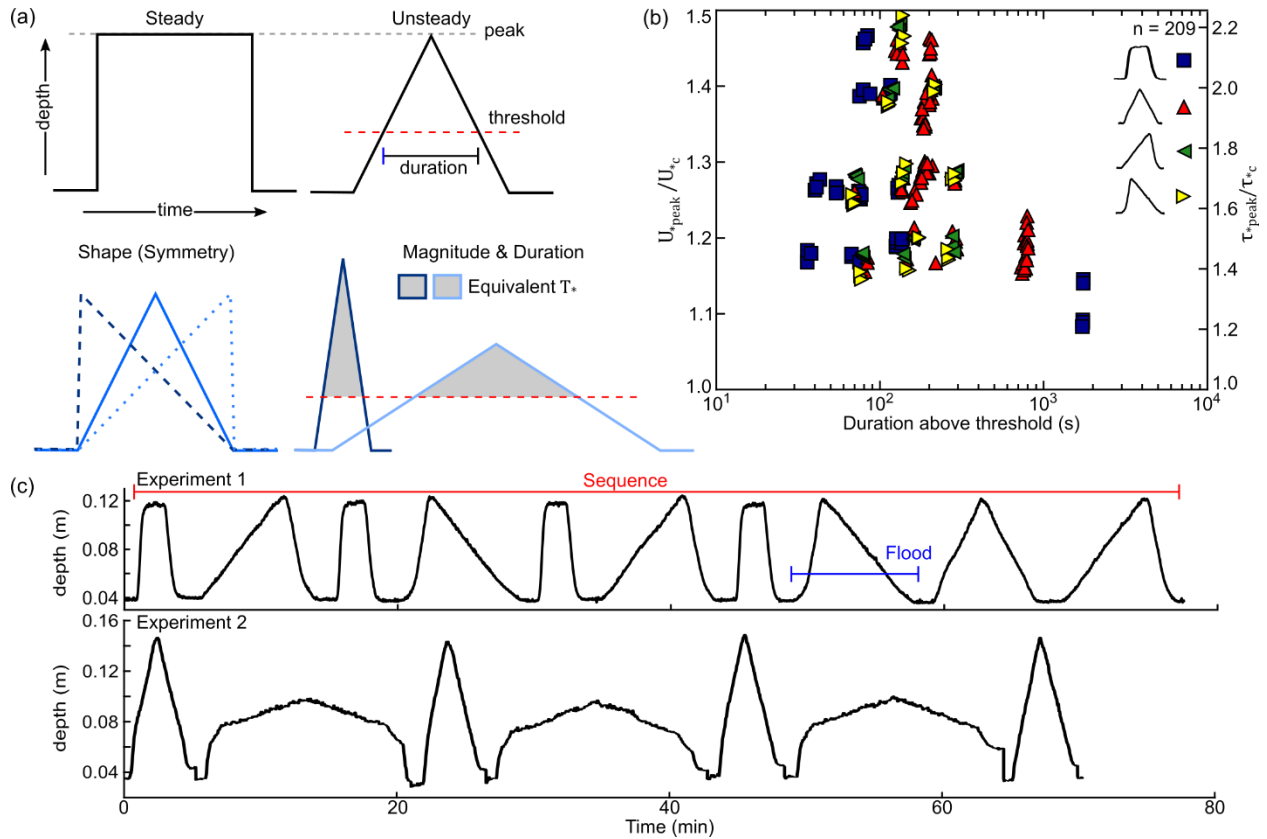
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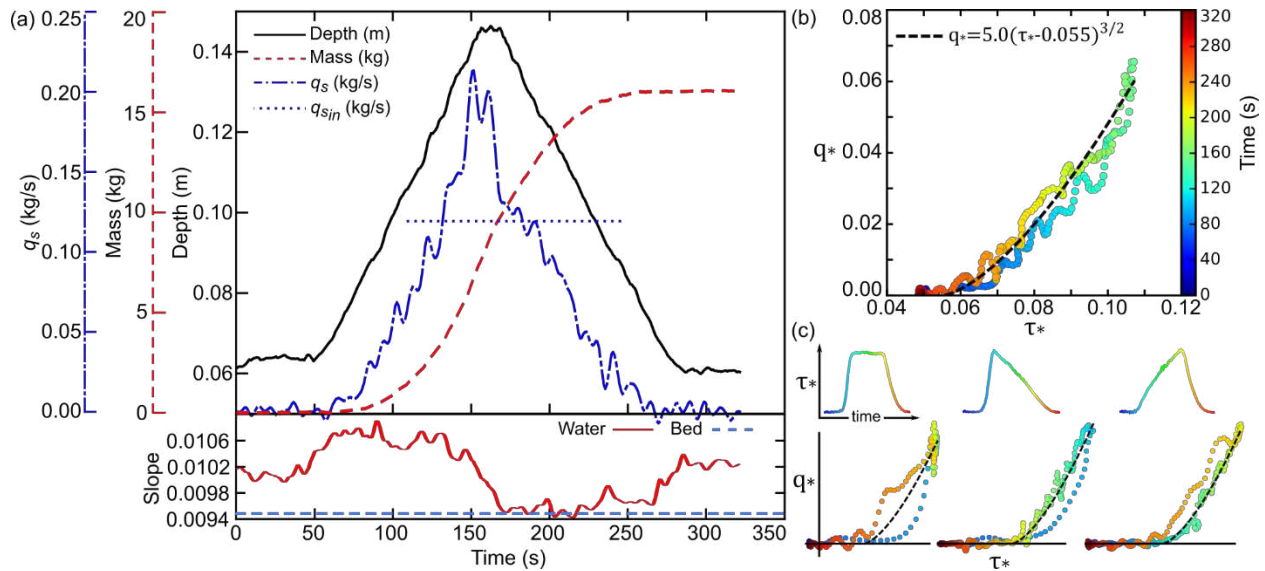
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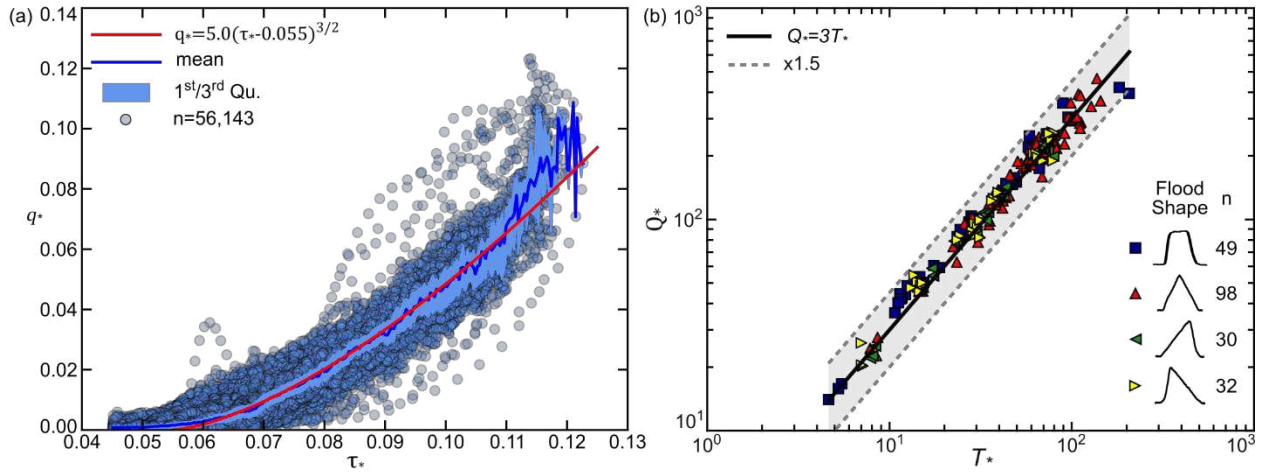


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Figure 1. Experimental design. (a) Schematic hydrographs of steady (upper left) and unsteady (upper right) symmetric flows, and three unsteady flow shapes (lower left) explored in these experiments. (lower right) Schematic hydrographs showing two flows of equal impulse with different peak magnitude and duration. (b) Experimental parameter space of flow durations above the threshold of motion and dimensionless peak magnitude in shear velocity and shields stress normalized by the threshold of motion. Legend denotes experimental flood shape next to symbol. (c) Examples of experimental sequences. (top panel) Hydrograph sequence of steady and unsteady flows with equal peak magnitude and impulse for each run. (lower panel) Hydrograph of unsteady runs with alternating peak magnitude and duration.



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 486 Figure 2. Experimental data. (a) Primary data are flow depth (black line), cumulative sediment  
 487 mass (red dashed line), sediment feed rate (blue dotted line), and sediment flux (blue dash dot  
 488 line). The subplot shows the water surface slope throughout the flood (red line) and the post  
 489 flood bed surface slope (dashed line). (b) Dimensionless bed load flux and Shields stress for the  
 490 run shown in (a), where color represents the experimental run time. The dashed black line  
 491 represents a fitted bed load transport law. (c) Examples of flux stress relations for the other three  
 492 flood shapes. The top row shows the flow hydrograph in time and stress with the color of the line  
 493 corresponding to the approximate time location of the flux data in the bottom row. The bottom  
 494 row shows sediment flux and Shields stress and the dashed black line represents the flux law in  
 495 (b). For these schematic examples flux and stress are on the same scale for all three, while time is  
 496 compressed by a factor  $\sim 1.3$  for the asymmetric flood shapes.  
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 499 Figure 3. (a) Dimensionless sediment transport rate and Shields stress for all experimental runs  
 500 for  $q_* \geq 0$  and  $\tau_* \geq 0.045$ . The blue line represents the average, shaded regions are the first and third  
 501 quartiles, and the red line is the fitted sediment transport flux law. (b) Dimensionless impulse  
 502 ( $T_*$ ) versus dimensionless cumulative sediment flux ( $Q_*$ ) for all runs. Example hydrographs for  
 503 each run are depicted next to the symbols alongside the number of runs for that flood shape. The  
 504 black line is a linear trend line fit through the origin, and the grey dashed lines represent a factor of  
 505 1.5 times the linear trend.