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ABSTRACT

The interaction of atomic and molecular hydrogen with actinide dioxide (AnO_2 , $\text{An} = \text{U, Np, Pu}$) (111) surfaces has been investigated by DFT+U, where noncollinear 3k antiferromagnetic behaviour and spin-orbit interactions are considered. The adsorption of atomic hydrogen forms a hydroxide group, coupled to the reduction of an actinide ion. The energy of atomic hydrogen adsorption on the UO_2 (0.82 eV), NpO_2 (-0.10 eV), and PuO_2 (-1.25 eV) surfaces has been calculated. The dissociation of molecular hydrogen is not observed, shown to be due to kinetic rather than thermodynamic factors. As a barrier to the formation of a second hydroxyl group, an unusual charge distribution has been shown. This could be a limitation of a (1·1) unit cell method or an artefact of the systems. The recombination of hydrogen ions on the AnO_2 (111) surfaces is favoured over hydroxide formation.

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I. INTRODUCTION

The corrosion of actinide materials concerns nuclear industries, where the radiolysis of organic compounds and other sources generate hydrogen.^{1–6} This is known to catalyse the corrosion of the actinide metals.^{7,8} Incidents involving corrosion have resulted in thermal excursions, expansion of solids, formation of incondensable gases, and containment failure.⁹ The interaction of hydrogen with nuclear materials must be understood (imperative to the design of long-term storage facilities),¹⁰ where the corrosion and oxidation of the actinide metals are often treated as equivalent topics.¹¹

The actinide metals are highly reactive elements. The corrosion chemistry is controlled by the initial actinide dioxide (AnO_2) layer, formed by the unavoidable oxidation of the metal surface.^{7,9,11–17} As an active template for the equilibration of the hydrogen-oxygen system, knowledge of the electronic structure of the AnO_2 is critical to the understanding of corrosion mechanisms.^{5,18–20} A

number of investigations have shown the AnO_2 (111) surface to be the most stable. The interpretation of the corrosion mechanism is highly complex, inferred from studies with hydrogen, oxygen, and water.^{5,9} These involve the complex interplay of thermodynamic, kinetic, and catalytic factors.¹¹ A diffusion-controlled mechanism for oxygen migration across the oxide layer to the metal-oxide interface fails to account for hydrogen-catalysed oxidation and pyrophoric behaviour.^{8,11,13,21,22} The influence of hydrogen on AnO_2 corrosion chemistry is unclear. Mechanisms for water-catalysed corrosion often incorporate the diffusion of hydrogen (H or H^+) or hydrogen-containing species (H_2O or OH) across the oxide surface layer to the metal-oxide interface.²³ In addition, the mechanism is thought to include the formation of hyperoxides (AnO_{2+x}) which increases the oxygen concentration gradient, thereby facilitating the migration of O^{2-} ions to the metal-oxide interface.

The interaction of hydrogen within the crystal structure and water adsorption has been investigated in earlier studies.^{18–20,23–29}

The interplay of binding and formation energies has been shown to impact the thermodynamic stability of oxy-hydroxyl defects, where hydrogen stabilises isolated Willis clusters and greatly impacts the stability of oxygen clusters to form irreversible traps.^{27,30} The occupation of octahedral interstitial sites (early AnO₂) or the formation of hydroxyl groups (late AnO₂) by hydrogen has been shown to be controlled by the actinide element.²⁴ The formation energies of light impurity atoms (H, He, Li, Be, B, C, N, O, F, and Ne) are influenced by AnO₂.²⁴ The relative stability of the hydride ion compared to the hydroxyl group in UO₂ has been shown, where the uranium 5f electrons can form chemical bonds. The hydroxyl group is relatively stable in PuO₂ by contrast, where the plutonium 5f electrons are more localised.²³ The formation of hydroxyl groups on isostructural cerium dioxide (CeO₂) has also been found; however, cerium is a lanthanide element characterised by more simplistic behaviour.³¹

The interaction of hydrogen with AnO₂ surfaces is experimentally difficult to study.¹² The rate of corrosion is influenced by the extent of radiation damage, environmental conditions, and surface energetics. A limited number of experimental AnO₂ surface investigations have been published.^{5,7-9,11-14,21,22,32} To compliment experimental investigations of AnO₂ surfaces, computational methods offer another method of study.²³⁻²⁹ Although theoretical investigations are nontrivial,^{15,16,33-35} the actinides are highly correlated f-electron systems for which conventional methods often fail. To calculate highly correlated systems, a number of methods have been developed. These include the self-interaction correction (SIC) method,³⁶ modified density functional theory (DFT+U),³⁷⁻⁴¹ hybrid density functionals,⁴²⁻⁴⁴ and dynamic mean field theory (DMFT).⁴⁵ Of these methods, DFT+U is widely employed and offers a tractable means of study.

A fluorite-type structural motif is adopted by the AnO₂ under normal environmental conditions. At low temperature, the AnO₂ (An = U, Np, and Pu) show noncollinear 3k antiferromagnetic (AFM) behaviour.⁴⁶⁻⁵¹ The transverse 3k AFM state of UO₂ and NpO₂ results in Pa $\bar{3}$ (No. 205) crystal symmetry,³⁵ whereas the longitudinal 3k AFM state of PuO₂ results in Fm $\bar{3}m$ (No. 225) crystal symmetry.^{34,52} In each instance, the external cubic symmetry is retained. In contrast with collinear 1k AFM states, a reduction of cubic crystal symmetry has been found.³⁴ The importance of spin-orbit interactions (SOI) in the actinide elements has been highlighted;⁵³ however, the impact of relativistic contributions is often ignored for computational simplicity.⁵⁴⁻⁵⁶ Noncollinear magnetic behaviour is also infrequently considered.^{34,52} The corrosion chemistry of the AnO₂ (111) surface is controlled by the electronic structure.²⁷ To mirror the corrosion chemistry of AnO₂, the electronic structure must be correctly calculated.³³

The importance of noncollinear magnetic behaviour and spin-orbit interactions (SOI) on the electronic structure has been highlighted by a number of investigations.^{6,33-35,52,53,55} In this paper, the interaction of hydrogen with the AnO₂ (An = U, Np, and Pu) (111) surface has been investigated by DFT+U. These calculations incorporate noncollinear 3k AFM behaviour and SOI influences. As the surface offers a nonuniform interface, inequivalent adsorption sites have been investigated. The electronic structure is compared against the clean surface, and this can be found in the [supplementary material](#).³³

II. COMPUTATIONAL METHODOLOGY

A. Calculation details

A noncollinear relativistic study has been completed with the Vienna *Ab initio* Simulation Package (VASP) code.^{36,45,57} A planewave basis set, relativistic effective core potentials (ECPs), and the frozen-core projector-augmented wave (PAW) method have been used.^{43,58} The cut-off energy of the planewave basis set is 500 eV. The hydrogen (1s¹), oxygen (2s², 2p⁴), uranium (6s², 7s², 6p⁶, 6d² 5f²), neptunium (6s², 7s², 6p⁶, 6d² 5f³), and plutonium (6s², 7s², 6p⁶, 6d² 5f⁴) valence electrons are implicitly considered. The integration over the Brillouin zone with the Gaussian method has been completed.⁵⁹ Noncollinear magnetic wave-vectors and SOI are considered. The on-site Coulomb repulsion of the An 5f electrons is treated by the Liechtenstein *et al.* formalism, in which the Coulomb (U) and exchange (J) modifiers are treated as independent variables.³⁷⁻⁴¹ The exchange-correlation energy is evaluated by the revised Perdew-Burke-Ernzerhof for solid (PBEsol) functional, the improved performance of which

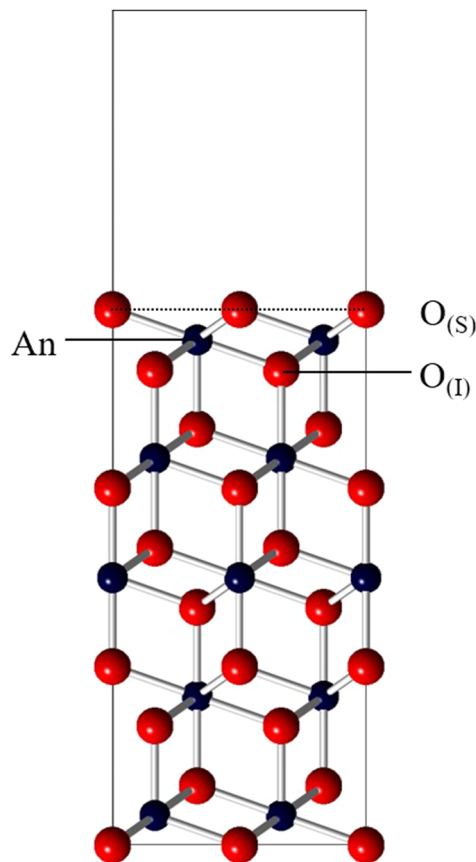


FIG. 1. The low-index AnO₂ (111) surface. The An⁴⁺ (blue) and O²⁻ (red) ions are indicated. The superior (primary layer, S) and inferior (tertiary layer, I) oxygen ions are labeled. The surface plane bisects the Os²⁻ ions as illustrated by the dashed black line. The surface model is comprised of 15 (5 O–An–O units) monolayers.

has been tested against other functionals.^{52,60} In this study, all ions are fully relaxed with the conjugate gradient algorithm as implemented by VASP. The iteration threshold for electronic and ionic convergence is 1×10^{-5} eV and 1×10^{-2} eV·Å⁻¹, respectively.

A transverse 3k AFM state for UO₂ ($U = 3.35$ eV, $J = 0.00$ eV) and NpO₂ ($U = 4.25$ eV, $J = 0.00$ eV) with Pa $\bar{3}$ (No. 205, 0.014–0.016 Å distortion) crystal symmetry is used,³⁵ whereas for PuO₂, a longitudinal 3k AFM ($U = 6.00$ eV, $J = 0.00$ eV) model with Fm $\bar{3}m$ (No. 225) crystal symmetry is used,³⁴ the implementation of which has already been documented. The surface is constructed from the ionically relaxed bulk structure with the METADISE code (Fig. 1).^{16,61} The surface is formed of 15 monolayers (5 O–An–O units) with a vacuum gap of 20 Å; this is sufficient to isolate the surface from its periodic image. The convergence of the Γ -centred k-point grid (5·5·1) (recommended for hexagonal constructs) has been checked.^{6,33,62}

B. Inequivalent positions

The adsorption of atomic H and molecular H₂ on the AnO₂ (111) surfaces is considered for multiple inequivalent lattice sites, where the influence of magnetic inequivalence is assumed to be negligible (Fig. 2). The inequivalent oxygen sites are differentiated by their position relative to the plane of the surface: superior (s) or inferior (i). The plane of the surface is defined as that which extends across the O_s²⁻ ions.

For molecular H₂, the orientation of the molecule is considered. In this study, molecular H₂ is either placed orthogonal (v) to the plane of the surface or parallel (n) along the direction of a bond. In each configuration, hydrogen is situated at a minimum of 1 Å above the plane of the surface. The implementation of a dipolar correction is not needed in our treatment; hydrogen is adsorbed on both

sides of the model with inverse crystal symmetry. The seven inequivalent sites of the AnO₂ (111) surface include; three atomic [An, O_(s), O_(i)] positions, three [An–O_(s), An–O_(i), O_(s)–O_(i)] bridging sites, and one interstitial (I) site. The ionic coordinates, magnetic vectors, and dimensions of the unit cell can be found in the [supplementary material](#).^{6,33}

C. Hydrogen adsorption

The hydrogen adsorption energy (E_{ads}) is calculated from the fully ionically relaxed cells. The total energy of the slab with the adsorbate ($E_{\text{slab+adsorbate}}$), the energy of the adsorbate ($E_{\text{adsorbate}}$), and the clean (adsorbate-free) slab energy (E_{slab}) are indicated

$$E_{\text{ads}} = 0.5(E_{\text{slab+adsorbate}} - (E_{\text{slab}} + E_{\text{adsorbate}})). \quad (1)$$

The energy of the adsorbate ($E_{\text{adsorbate}}$) is derived from the isolated H₂ molecule in a 10 Å³ cubic cell. Integration of the Brillouin zone is completed with a 1·1·1 Γ -centred k-point mesh. The PBEsol calculations result in a H–H bond length ($r_{\text{H-H}}$) of 0.758 Å, in good agreement with the experimental value of 0.740 Å.⁶³ In terms of the adsorption energy, E_{ads} , negative values correspond to an energetically favourable exothermic process, while positive values correspond to an endothermic one. The adsorption energy (E_{ads}) is calculated from the full ionic relaxation. The dissociation energy of molecular H₂ ($E_{\text{ds}} = 4.478$ eV) has been measured by fluorescence-excitation spectroscopy.^{64,65} A difference of 0.152 eV is introduced by PBEsol ($E_{\text{ds}} = 4.630$ eV), which can impact the calculation of adsorption energetics. To measure physisorption energies for H (~0.010–0.200 eV), the PBEsol error is considerable; however, to measure chemisorption energies for H (~1–2 eV), the PBEsol error is relatively insignificant. All models consider SOI.

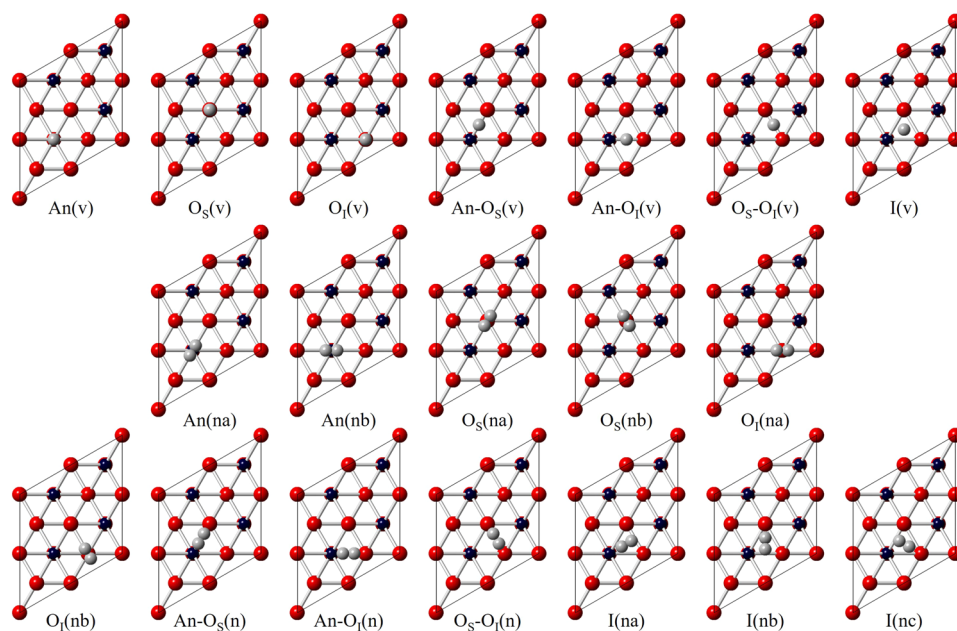


FIG. 2. The initial inequivalent configurations for the adsorption of atomic and molecular hydrogen on the AnO₂ (111) surface. The An⁴⁺ (blue) and O²⁻ (red) ions are indicated. The individual hydrogen positions are shown in grey. The minimum distance of the hydrogen atoms above the plane of the surface is 1 Å. The hydrogen molecule is considered with either orthogonal (v) or parallel (n) orientations relative to the surface plane.

III. RESULTS AND DISCUSSION

A. Uranium dioxide

Two interaction sites for atomic H- UO_2 (111) adsorption have been identified, both of which are endothermic in nature (Fig. 3). In hydrogenation and oxidation corrosion mechanisms, endothermic adsorption has been shown to be an important component.⁶⁶ The energetic ordering can be inferred from the position of the H s-band in the density of states (DoS), where lower energy states indicate a more stable configuration. In the high-energy $\text{aH}_{(111)}$ configuration, atomic H is located above an U ion and remains relatively isolated. The electronic structure is relatively unaffected, and no obvious hybrid OH sp-states are formed. The diagnosis is confirmed by the minimum U-H (2.001 Å) and O-H (2.589 Å) bond distance, which indicates that only weak interactions can occur. A weak hydride (H^-) ion from the Bader charge (-0.35 eV) has been indicated. In the low-energy $\text{bH}_{(111)}$ configuration, the interaction results in an unusual endothermic chemisorption mechanism. The formation of an OH ion is confirmed by the O-H bond distance (0.975 Å), hybrid OH sp-states (-9 eV to -8 eV), and Bader charge analysis ($\text{H} = 0.61$ eV). The corresponding reduction of an U ion is confirmed by the Bader charge reduction of the U (d) ion (2.55 eV to 2.19 eV) and the formation of the U f-defect in the bandgap. As the U (a-c) ions are closer in proximity to the H ion, the reduction of the outermost U (d) ion is unusual in terms of electrostatics.

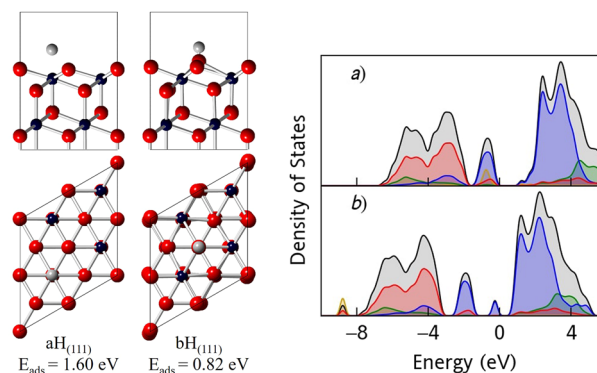


FIG. 3. The adsorption sites of atomic H on the UO_2 (111) surface. The U^{4+} (blue), O^{2-} (red), and H (grey) ions are indicated. The energy of adsorption (E_{ads}) is also shown. The density of states of the a- $\text{bH}_{(111)}$ configurations for the UO_2 (111) surface has been calculated. The total density of states (black), U f- (blue), U d- (green), O p- (red), and H s- (yellow) bands are coloured. Note: the hydrogen s-band has been magnified by a factor of 40 for clarity.

In earlier investigations with stoichiometric UO_2 models, hydride (H^-) ions are formed within interstitial sites.²⁶ The formation of the OH group was 0.27 eV higher in energy. It was also found that the compensating cation was distinct from the octahedral cage. The result indicates that reduction of the outermost cation is an

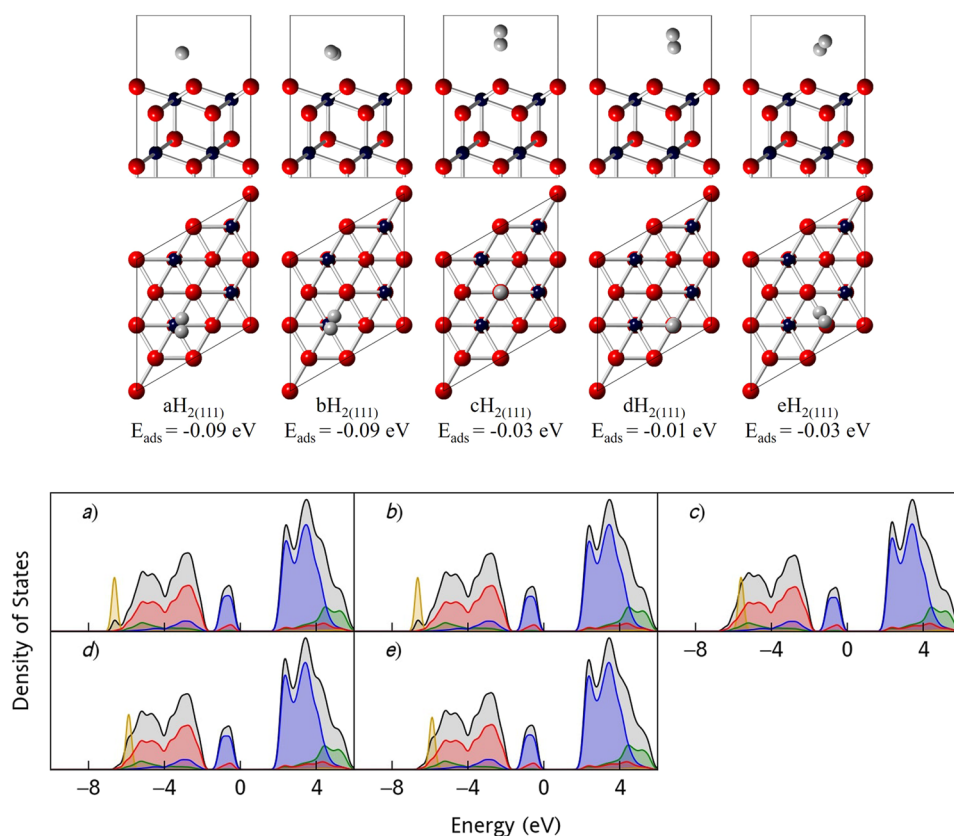


FIG. 4. The adsorption sites of molecular H_2 on the UO_2 (111) surface. The U^{4+} (blue), O^{2-} (red), and H (grey) ions are indicated. The energy of adsorption (E_{ads}) is also shown. The density of states of the a- $\text{eH}_{2(111)}$ configurations for the UO_2 (111) surface has been calculated. The total density of states (black), U f- (blue), U d- (green), O p- (red), and H s- (yellow) bands are coloured. Note that the hydrogen s-band has been magnified by a factor of 10 for clarity.

artefact of the system, where further experimental and computational investigation is needed. In contrast with hydrogen-surface interactions, the formation of an OH (0.975 Å) group is (0.78 eV) lower in energy; here, the surface offers an oxygen-rich region which can bind local high concentrations of hydrogen.²⁷

The adsorption of molecular H₂ on the UO₂ (111) surface is non-dissociative, where five distinct [a-eH₂₍₁₁₁₎] configurations have been found (Fig. 4). In each instance, molecular H₂ is adsorbed in the -0.01 eV to -0.10 eV energy range. In the low-energy a-bH₂₍₁₁₁₎ configurations, molecular H₂ is located proximal to the U ion. In the aH₂₍₁₁₁₎ configuration, the H ions occupy chemically equivalent positions and are slightly off-centre from the U ion, whereas in the bH₂₍₁₁₁₎ configuration, the H ions are directed towards a nearby O_(S) ion. The nearby electrostatic attraction to an O_(S) ion is evident in each instance. If dissociation of the molecular H₂ were to occur, two mechanisms are possible: (1) the H ions separate uniformly along adjacent U-O(s) bonds forming chemically equivalent OH ions, (2) the H-H bond is elongated along a single U-O(s) bond forming an UH and OH pair. Although climbing nudged elastic band (cNEB) calculations are computationally unfeasible (due to the expense of noncollinear relativistic investigations), future investigations should consider these pathways.

In the cH₂₍₁₁₁₎ configuration, molecular H₂ is located directly above an O_(S) ion, offering another possibility for molecular H₂ dissociation, whereby one H ion initially forms an OH group. The dissociative mechanism could then proceed to the formation of a second OH group involving the remaining H ion. In the high-energy dH₂₍₁₁₁₎ configuration, molecular H₂ is located above an O_(T) ion orthogonal to the plane of the surface. Given the relatively high energetics of this configuration, it is unlikely to play any role in the dissociation of the H₂ molecule. In the eH₂₍₁₁₁₎ configuration, molecular H₂ is proximal to the O_(T) ion and directed towards the neighbouring O_(S) ion, which is suggestive of the electrostatic attraction of hydrogen to the O_(S) ion as a prelude to dissociation. The electronic structure for molecular H₂ adsorption on the UO₂ (111) surface, as indicated by the DoS, has been calculated for the a-eH₂₍₁₁₁₎ configurations (Fig. 4). The absence of defect states or hybrid H s- and O p-states, in the a-eH₍₁₁₁₎ configurations, indicates that molecular H₂ is physisorbed. The magnitude of the electrostatic interaction is indicated by the position of the H s-band.

The dissociation of molecular H₂ is not observed on the UO₂ (111) surface, although there is clear evidence of atomic H chemisorption. The adsorption energies, DoS, and optimized geometries indicate that molecular H₂ is physisorbed onto the (111) surface, which is likely to be due to a large energetic barrier for the dissociation pathways relative to the energetically favourable (-0.10 eV to -0.01 eV) physisorption based on van der Waals interactions. A series of cNEB calculation could confirm this diagnosis. As of the unusual charge distribution in the atomic aH₍₁₁₁₎ configuration, the absence of dissociation may be a limitation of a (1·1) unit cell model. The charge distribution is unusual in terms of electrostatics, where the outermost surface An ion is reduced. In contrast, a (2·2) unit cell would offer the option of distributing the charge imparted by the adsorption of a H ion over a larger surface area. One notes that the distribution of charge and the separation of hydrogen ions over a greater surface would introduce a significant energetic barrier for dissociation.

As a limitation of noncollinear relativistic models, a full systematic study of a (2·2) unit cell is computationally unfeasible at this time.

B. Neptunium dioxide

An exothermic adsorption energy of -0.10 eV is calculated for the aH₍₁₁₁₎ configuration, formed by the interaction of atomic H on the NpO₂ (111) surface (Fig. 5). This differs from the endothermic adsorption energy of 0.82 eV for the UO₂ bH₍₁₁₁₎ configuration, although the configurations are structurally nearly identical. Atomic H is adsorbed directly above an O_(S) ion, and the OH group is characterised by a bond length of 0.975 Å. In conjunction with the formation of an OH group, the Bader charge distribution confirms a H protonic state (Table A2). In contrast to atomic H adsorption on UO₂ (111) and PuO₂ (111) surfaces, no other stable configurations have been identified.

The formation of an OH group is confirmed by the hybridisation of the H s- and O p-states at -8 eV. The bandgap Np f-defect and the Bader charge analysis show the reduction of the Np (d) ion. The defect state reduces the bandgap of NpO₂ to 0.16 eV, and Mott-Hubbard characteristics are identified. In comparison with experimental data, the bandgap (0.40-3.10 eV) of NpO₂ differs considerably.⁶⁷⁻⁶⁹ As hydrogen is notoriously difficult to remove from experimental studies, its impact on X-ray adsorption and epitaxial thin-film measurements is shown.⁶⁷⁻⁶⁹

The interaction of molecular H₂ on the NpO₂ (111) surface generates five distinct a-eH₂₍₁₁₁₎ configurations (Fig. 6). The dissociation of molecular H₂ on the NpO₂ (111) surface (as with UO₂ and PuO₂) is not observed. The electronic structure indicates that molecular H₂ is physisorbed in each instance. In the low-energy aH₂₍₁₁₁₎ configuration, molecular H₂ ($E_{\text{ads}} = -0.10$ eV) is located

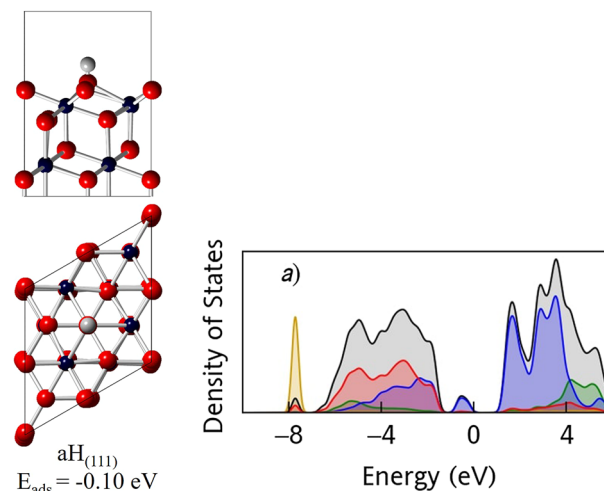


FIG. 5. The adsorption sites of atomic H on the NpO₂ (111) surface. The Np⁴⁺ (blue), O²⁻ (red), and H (grey) ions are indicated. The energy of adsorption (E_{ads}) is also shown. The density of states of the aH₍₁₁₁₎ configuration for the NpO₂ (111) surface has been calculated. The total density of states (black), Np f- (blue), Np d- (green), O p- (red), and H s- (yellow) bands are coloured. Note that the hydrogen s-band has been magnified by a factor of 40 for clarity.

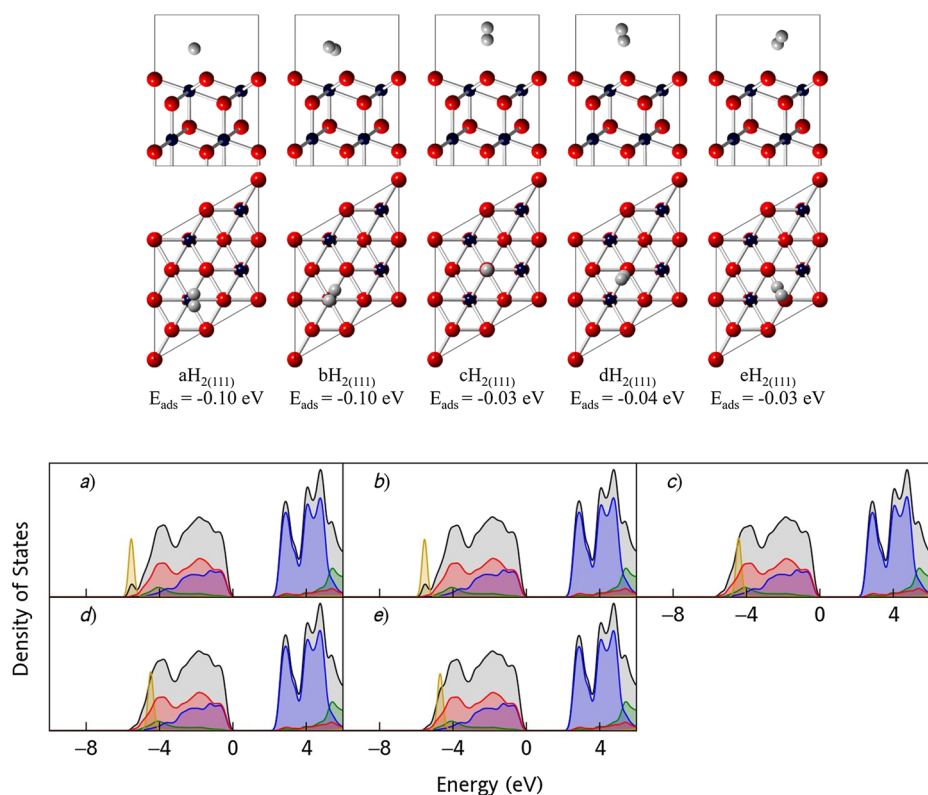


FIG. 6. The adsorption sites of molecular H_2 on the NpO_2 (111) surface. The Np^{4+} (blue), O^{2-} (red), and H (grey) ions are indicated. The energy of adsorption (E_{ads}) is also shown. The density of states of the a- $H_{2(111)}$ configurations for the NpO_2 (111) surface has been calculated. The total density of states (black), Np f- (blue), Np d- (green), O p- (red), and H s- (yellow) bands are coloured. Note that the hydrogen s-band has been magnified by a factor of 10 for clarity.

above the Np ion. As the adsorption energetics of atomic H and molecular H_2 are comparable, the dissociation of molecular H_2 is less favoured on the NpO_2 (111) surface.

By analysis of the Bader charge distribution of the atomic a $H_{(111)}$ state, a limitation of the (1·1) unit cell model employed is the inability to partition the electron density over a larger surface area. In addition, a large energetic barrier, introduced from the need to spread the negative charge over a greater distance, possibly hinders the formation of two OH groups. As such, even if molecular H_2 dissociates, recombination is highly probable. Given the surface areas involved in the distribution of charges, kinetic factors likely control the dissociation of molecular H_2 on the NpO_2 (111) surface. The dissociation mechanism may proceed by elongation of the H–H bond as each H ion moves towards an $O_{(S)}$ ion, or by the formation of a NpH and OH pair, with these mechanisms being analogues with those proposed for UO_2 .

C. Plutonium dioxide

The interaction of hydrogen with the PuO_2 (111) surface results in a-b $H_{(111)}$ configurations (Fig. 7). The a $H_{(111)}$ configuration is characterised by an endothermic adsorption energy of 2.18 eV, whereas the b $H_{(111)}$ configuration is characterised by an exothermic adsorption energy of –1.25 eV. In the a $H_{(111)}$ configuration, the atomic H is positioned directly above a Pu ion. After a full ionic relaxation of hydrogen and the surface ions, the minimum Pu–H (2.403 Å) and O–H (2.754 Å) distances have been calculated. The configuration shares structural similarities with the UO_2

a $H_{(111)}$ configuration, although the endothermic energy of adsorption is considerably greater. In reference to the UO_2 b $H_{(111)}$ site and the NpO_2 a $H_{(111)}$ configurations, the PuO_2 b $H_{(111)}$ configuration is almost identical in terms of structural configuration. The energy of adsorption decreases from 0.82 eV to –1.25 eV along the AnO_2

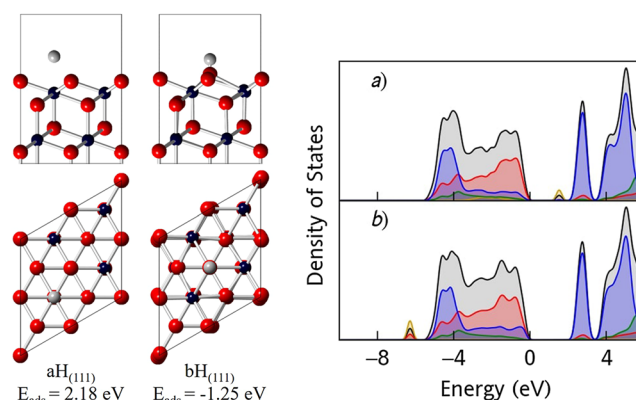


FIG. 7. The adsorption sites of atomic H on the PuO_2 (111) surface. The Pu^{4+} (blue), O^{2-} (red), and H (grey) ions are indicated. The energy of adsorption (E_{ads}) is also shown. The density of states of the a-b $H_{(111)}$ configurations for the PuO_2 (111) surface has been calculated. The total density of states (black), Pu f- (blue), Pu d- (green), O p- (red), and H s- (yellow) bands are coloured. Note that the hydrogen s-band has been magnified by a factor of 40 for clarity.

(An = U, Np, and Pu) series, which offers an indication of the increasing reactivity of the AnO₂ (111) surfaces. In the bH₍₁₁₁₎ site, the H atom is bonded to an O_(S) atom to form an OH group, where the O–H bond distance of 0.976 Å is consistent with that of an OH group. The adsorption energy of –1.25 eV indicates an exothermic chemisorption mechanism. At the O_(S) site, the neighbouring oxygen ions are drawn inwards, which results in a slight structural deformation. The formation of the OH group is confirmed by the H ion Bader charge of 0.58 eV (Table A3). This indicates a protonic state. In addition, the Pu (d) ion is reduced, whereas the O ions are only partially oxidised. In each instance, the electronic structure of the PuO₂ (111) surface is relatively unaffected and indicates molecular H₂ physisorption. As there is clear evidence of atomic H chemisorption on the PuO₂ (111) surface, it is perhaps surprising that the dissociation of molecular H₂ is not observed. As the charge cannot be distributed over a larger surface area, the aH₍₁₁₁₎ result implies a limitation of a (1·1) unit cell model. A large energetic barrier is thought to inhibit a dissociative adsorption mechanism, although cNEB calculations would markedly confirm the idea.

The instability of the aH₍₁₁₁₎ configuration is highlighted by the H s-defect state located within the bandgap. In the bH₍₁₁₁₎

configuration, the number of Pu f-states in the valence band has increased, whereas the number of Pu f-states in the conduction band has decreased. These changes indicate that high-energy Pu f-states (due to the interaction of hydrogen) are shifted to lower energy levels. The reduction of the formal Pu⁴⁺ (2.47 eV) ion to Pu³⁺ (2.08 eV) ion by hydrogen is confirmed by the Bader charge. Additionally, the hybridisation of the H s- and O p-states at 6 eV is indicative of the formation of an OH group.

In comparison, the interaction of molecular H₂ on the PuO₂ (111) surface results in four distinct a-dH₂₍₁₁₁₎ configurations (Fig. 8). As with the UO₂ (111) and NpO₂ (111) surfaces, the dissociation of the molecular H₂ on the PuO₂ (111) surface is not observed. In each instance, the physisorption of molecular H₂ is in an energy range of –0.01 eV to –0.09 eV. The aH₂₍₁₁₁₎ site, relative to the bH₂₍₁₁₁₎ site, is marginally higher in energy by 0.01 eV. In both instances, molecular H₂ is positioned proximal to a Pu ion. In the cH₂₍₁₁₁₎ site, molecular H₂ is located above an O_(S) ion with an adsorption energy of –0.03 eV. The configuration potentially acts as an intermediate position for the dissociation of H₂ and the formation of an OH group. This is seen in the atomic aH₍₁₁₁₎ site; however, as stated, this has not been observed in these calculations. In addition, the dH₂₍₁₁₁₎ site is reminiscent of the cH₂₍₁₁₁₎

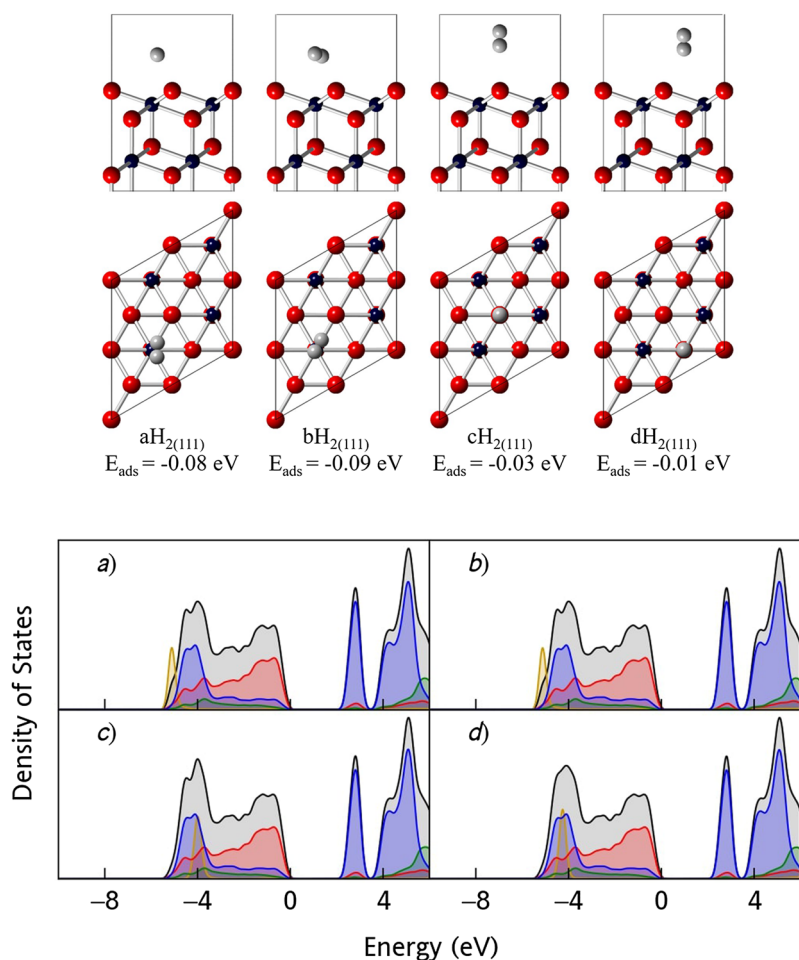


FIG. 8. The adsorption sites of molecular H₂ on the PuO₂ (111) surface. The Pu⁴⁺ (blue), O²⁻ (red), and H (grey) ions are indicated. The energy of adsorption (E_{ads}) is also shown. The density of states of the a-dH₂₍₁₁₁₎ configurations for the PuO₂ (111) surface has been calculated. The total density of states (black), Pu f- (blue), Pu d- (green), O p- (red), and H s- (yellow) bands are coloured. Note that the hydrogen s-band has been magnified by a factor of 10 for clarity.

site, although molecular H_2 is now located above the $O_{(1)}$ ion. The lowest-energy $bH_{2(111)}$ site is characterised by an adsorption energy of -0.09 eV. A physisorption mechanism is confirmed by the Bader charge distribution (Table A3). The disruption to the surface is negligible, and the hydrogen ions remain effectively charge neutral.

In each instance, the electronic structure of the PuO_2 (111) surface is relatively unaffected, which indicates molecular H_2 physisorption. As there is clear evidence of atomic H chemisorption on the PuO_2 (111) surface, it is perhaps surprising that the dissociation of molecular H_2 is not observed. A large energetic barrier is thought to influence the adsorption mechanism, which in future could be confirmed by cNEB calculations and the use of a (2·2) unit cell. This offers the option of distributing the charge imparted by the adsorption of a H ion over a larger surface area.

IV. CONCLUSIONS

The interactions of atomic H and molecular H_2 on the AnO_2 ($An = U, Np, Pu$) (111) surfaces has been investigated by DFT+U. The study considers SOI and noncollinear 3k AFM behaviour. The reactivity of the AnO_2 (111) surfaces increase along the U-Pu series. Multiple adsorption configurations were identified on the UO_2 and PuO_2 surfaces, while only one was found on NpO_2 . In the interaction of atomic H with the AnO_2 (111) surfaces, an OH group is formed coupled with the reduction of an An ion. The energy of atomic H adsorption for UO_2 (0.82 eV), NpO_2 (-0.10 eV), and PuO_2 (-1.25 eV) is shown and is caused by increasing surface instability along the actinide series.⁶ A clear shift from an endothermic to an exothermic mechanism is identified. The formation of the OH group is confirmed by the DoS and the Bader charge distribution. The structure of the low-energy UO_2 $bH_{(111)}$, NpO_2 $aH_{(111)}$, and PuO_2 $bH_{(111)}$ configurations is effectively identical.

The dissociation of molecular H_2 on the AnO_2 (111) surface is not observed; instead, molecular H_2 is weakly physisorbed. As the formation of the OH group is thermodynamically feasible, the dissociation of molecular H_2 is possibly hindered by kinetic factors. These observations can be explained in terms of the charge distribution, where the furthest actinide ion from the adsorption site is reduced. The inability to distribute charge is a key limitation of a (1·1) unit cell model, which is thought to hinder the formation of a second OH group. To incorporate the reduction of another An ion furthest away from the OH group, a second unit cell must be included within the model. Although a fully relativistic cNEB investigation is computationally intractable at this time, future investigations should consider the reaction pathways proposed in this study. The diffusion of hydrogen through the AnO_2 can be investigated by molecular dynamics. Investigation of hydrogen interactions with AnO_2 (011) and (001) surfaces for comparison are also planned.⁶

SUPPLEMENTARY MATERIAL

See [supplementary material](#) for the following information: Clean surface—fixed unit cell dimensions, ionic positions, magnetic structure, k-point convergence, and electronic density of states, and hydrogen interactions—ionic positions, magnetic structure, and Bader charges.

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