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1	An analytical model for chemical diffusion in layered
2	contaminated sediment systems with bioreactive caps
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13	

Abstract

15 An analytical model for contaminant transport in multi-layered capped 16 contaminated sediments including the degradation of organic contaminant is presented. The effect of benthic boundary layer was treated as a Robin-type 17boundary condition. The results of the proposed analytical model agree well with 18 19 experimental data. The biodegradation of contaminant in bioturbation layer 20 shows a significant influence on the flux at the surface of system. The maximum 21 flux for the case with $t_{1/2,bio} = 0.07$ year can be 4.5 times less than that of the case 22 without considering the effect of biodegradation. The thickness of bioturbation 23 layer has a significant effect on the performance of the capped contaminated 24 sediment. The maximum flux for the case with l_{bio} =15cm can be 17 times larger 25 than that of the case without bioturbation layer. This may be due to the fact that 26 the effective diffusion coefficient of sand cap can be 28 times lower than D_{bio} . 27 The mass transfer coefficient should be considered for the design of the capping 28 system as the contaminant concentration at the top of system for the case with k_{bl} =2.5×10⁻⁵ cm/s can be 13 times greater than that of the case with k_{bl} =10⁻⁴ cm/s. 29 30 The proposed analytical model can be used for verification of complicated 31 numerical methods, evaluation of experimental data and design of the capping 32 contaminated sediment systems with reactive cap layers.

33 Keywords: Analytical model; chemical diffusion; degradation; capped

34 contaminated sediment; mass transfer coefficient; bioturbation layer

35

36 **1. Introduction**

37 Sediments contaminated with organic compounds are always found in many waterways, harbors and estuaries^{1,2}. The transfer of these chemicals from the 38 39 sediments into overlying waters will affect the marine food web and the human using 40 these waters for recreation and supply of sea food. In order to reduce risk associated with contaminant in the sediments, different remediation strategies have been 41 42 developed. The general characteristics of the three basic sediment management options are natural recovery, capping or in situ treatment, and dredging². In order to 43 isolate the contaminants from organisms in the water and surficial sediments, in-situ 44 capping is used as a cover for placement over contaminated sediment³. The cap can be 45 constructed with multiple layered clean sediments such as sand and gravel ^{1,2,4,5}. The 46 47 application of sand and sediment caps as a remediation technology for contaminated sediments was subsequently investigated. Wang et al.⁴ and Thoma et al.⁶ found that a 48 layer of clean sand sediment successfully reduced the concentrations of the HOC 49 50 2,4,6-trichlorophenol in the laboratory.

The traditional sand caps are less effective at sites where groundwater seepage or mobile contaminants are present⁷. The active caps incorporating reactive or sorptive constituents are designed to reduce contaminant flux⁸⁻¹⁰. For instance, the coke and other "active" materials (e.g., activated carbon and kraft lignin) are used as capping to enhance sorption in order to reduce the availability of the contaminant and improve the effectiveness of in situ capping^{5,11-15}. The isolation times provided by the sorbent layers increased with the increase of sorption strength and capacity (activated carbon>> coke≈soil>> sand)⁵. Eek et al. ¹developed the laboratory microcosm test to
measure the diffusion of PAHs and PCBs from sediment with different capping layers.
They found that caps with passive material can significantly reduce the diffusive
contaminant flux through the cap.

62 It has been shown that diffusive transport is often the dominant mode of 63 contaminant transport through subaqueous caps for contaminated sediments since the water flow in fine-grained sediments is very slow^{4, 16, 17}. Diffusion of contaminant 64 65 through layered porous media is often modeled by numerical methods. For instance, Rowe et al.¹⁸ have developed the finite layer methods for contaminants transport 66 though multi-layered barrier systems. Leo and Booker¹⁹ developed the boundary 67 68 element method for contaminant diffusion in non-homogeneous porous media. Praveen Kumar and Dodagoudar²⁰ provide an accurate methodology for numerical 69 70 simulation of the two-dimensional contaminant transport through the saturated 71 homogeneous porous media and landfill liners using element-free Galerkin method 72 (EFGM). The finite element method based numerical model COMPASS has also been used for the analysis of contaminant diffusion in the layered porous media ²¹⁻²⁴. Zhang 73 et al.25 investigated contaminant transport in the two-layered system consisting of 74 75 compacted clay liner and the aquifer using the numerical method including the 76 finite-difference method and the numerical inversion of Laplace transform. However, the use of the numerical models is restricted to experienced users and for sites where 77 78 field data are known in great detail.

79	Analytical solutions play an important role in understanding many scientific
80	phenomena ²⁶⁻²⁸ , although some simplifications need to be made in the process of
81	deriving them. In particular, analytical solutions can also play a unique role in
82	validating many new numerical methods ²⁹⁻³¹ . For these reasons, analytical solutions
83	have been derived in recent years for many scientific and engineering problems ³²⁻³⁴ .
84	This means that by using analytical solutions in this particular study, a better
85	understanding of the mechanism of contaminant diffusion can be explored, the
86	movement of contaminant plumes can be predicted, and the results of numerical
87	modeling can be verified ³⁵ . They are also more computationally efficient and can be
88	used to address the Robin-type boundary condition that is often not available in the
89	numerical programs ^{37,38} . Some works have been done on solving the diffusion or
90	advection-dispersion equation of solute transport in two- or multi-layered porous
91	media using the Laplace transform method ³⁸ , the integral transform method ³⁹ , and an
92	approach combining the Laplace transformation method and binomial theorem ⁴⁰ . An
93	analytical solution for contaminant diffusion through multi-layered system was
94	presented by Chen et al. ⁴¹ . Li and Cleall ³⁷ presented analytical solutions for various
95	combinations of fixed solute concentration and zero-flux boundary conditions applied
96	at each end of a finite one-dimensional domain considering arbitrary initial solute
97	concentration distribution throughout the media. Deng et al. ⁴² proposed the integral
98	transform solution for solute transport in multi-layered porous media with the implicit
99	treatment of the interface conditions and arbitrary boundary conditions. Zhao and his
100	coworkers have conducted extensive studies to derive analytical solutions for both

101 chemical dissolution front instability problems⁴³⁻⁴⁸ and physical dissolution front 102 instability problems ⁴⁹ in fluid-saturated porous media. However, the effect of 103 degradation on the transport of contaminant was not considered in the literature 104 analytical models.

105 Many types of organic contaminant (e.g., aliphatic and aromatic compounds) can be significantly degraded in soils ⁵⁰⁻⁵³. For the sediment capping systems, Lampert and 106 107 Reible⁵⁴ reported that degradation of sediment contaminant in the biologically active 108 capping may be of primary importance for the control of the contaminant release from the sediments. Himmelheber et al. ¹⁰ demonstrated that in situ bioreactive capping can 109 be a feasible remedial approach for the contaminated sediments. Thoma et al.⁶ also 110 111 found that degradation of contaminant in sediment has a great influence on 112 contaminant flux discharged. For example, the maximum flux released for the case 113 with half-life of 100 years in the sediment can be 67 times lower than the case without 114 considering degradation. Therefore, it is of great importance to consider the 115degradation process to impede contaminant release from the sediment. In addition, the 116 boundary condition at the cap-water interface is quite complex, as it essentially 117requires the effluent boundary condition from a porous medium; therefore, the surface boundary condition for the capping sediment systems is often modeled with a mass 118 transfer coefficient². Thibodeaux⁵⁵ and Boudreau and Jørgensen⁵⁶ presented empirical 119 120 correlations for mass transfer coefficient based on mixing conditions in the overlying water. The value of mass transfer coefficient should be conservatively estimated, as 121 its value directly affects the surficial sediment concentrations⁵⁴. However, few 122

analytical models have considered the effect of mass transfer coefficient on
contaminant transport through the contaminated sediment and the capping layer.

125 The objective of this paper is to develop an analytical model for contaminant 126 transport in multi-layered capped sediment system considering the effect of 127 contaminant degradation, diffusion, and adsorption. The effects of bioturbation layer 128 on contaminant transport in capped contaminated sediment system will be analyzed 129 by using the mass transfer coefficient at the cap-water interface. The analytical 130 solutions are compared with an observed contaminant flux. Based on the analytical 131 solutions, the effect of degradation of organic contaminant and mass transfer 132 coefficient on contaminant transport in capped contaminated sediment system will be 133analyzed.

134 **2. Mathematical model**

135 The analytical model for contaminant diffusion in the multi-layered capped

136 contaminated sediment system was developed based on the following assumptions:

137 1. Contaminant diffusion is one-dimensional and follows Fick's second law.

138 2. The porous medium is isotropic, homogeneous and saturated.

- 139 3. Adsorption is a linear and equilibrium process.
- 140 4. Biodegradation model of organic contaminant in the medium is based on first-order
- 141 kinetics. Due to its mathematical simplicity, its easy implementation into transport
- 142 models, and the necessity of determining only a single parameter, the biodegradation
- 143 model most frequently used is first-order kinetics 57 .

144 Based on the above assumptions, one dimensional model for organic

145 contaminant in a finite composite media of *M* layers is developed (see Fig. 1). The

146 thickness of m layer is l_m . The system consists of the contaminated sediment, the

147 capping layers and the benthic boundary layer. The governing equations of

148 contaminant transport in the soils can be expressed as 18 :

149
$$R_{dm}\frac{\partial C_m}{\partial t} = D_m^*\frac{\partial^2 C_m}{\partial z^2} - \lambda_m C_m \qquad (m=1, 2, 3, ..., M)$$
(1)

150 where $C_m(z,t)$ is the concentration of contaminant in soil layer m; D_m^* is the

151 effective diffusion coefficient in the soil layer m; R_{dm} is retardation factor of the soil

152 layer m; z is the coordinate with downward positive; t is time; and λ_m is the

153 biodegradation rate ¹⁸:

154
$$\lambda_m = \ln 2/t_{1/2}$$
 (m=1, 2, 3,..., M) (2)

155 where $t_{1/2}$ is the half-life of contaminant in the soil layer *m*.

156 At the interface between soil layer m and m+1, the concentration and flux of the

158
$$C_m(L_m,t) = C_{m+1}(L_{m+1},t)$$
 (*m*=1, 2, 3,..., *M-1*) (3)

159
$$n_m D_m^* \frac{\partial C_m(L_m, t)}{\partial z} = n_{m+1} D_{m+1}^* \frac{\partial C_{m+1}(L_{m+1}, t)}{\partial z} \qquad (m=1, \ 2, \ 3, \dots, \ M-1)$$
(4)

where
$$n_m$$
 is the porosity of soil layer m ; L_m is the distance of layer m , $L_m=l_1+l_2+...+l_m$
For the top surface boundary, a Robin-type boundary condition is applied. The bottom
condition is a type of Neumann boundary condition. The boundary conditions for the
problem can then be expressed as follows^{6,60}:

164
$$\frac{\partial C_1(0,t)}{\partial z} = 0 \tag{5}$$

165
$$D_{M}^{*} \frac{\partial C_{M}(L_{M},t)}{\partial z} = k_{bl}C_{M}(L_{M},t)$$
(6)

where k_{bl} is the mass transfer coefficient in the benthic boundary layer. Eq.5 is 166 167 mathematically known as a second-type or Neumann boundary condition and 168 represents an impermeable base stratum. This bottom boundary may be assumed to not allow any transmission of contaminant⁵⁸. Eq.6 is known as the Robin-type 169 170boundary condition which is taken as a flux-matching relationship between the top of the sediment cap and the benthic boundary layer⁵⁴. When k_{bl} tends to be infinite, the 171172top boundary condition tends to be a zero concentration boundary condition. However, 173when k_{bl} tends to be 0, the top boundary condition would tend to be a zero flux 174boundary condition. This indicated that the mass transfer coefficient has a great 175influence on contaminant transport in the capped sediment system. It is also indicated 176 that the analytical solution of this paper can be applied to the situation of zero 177concentration boundary condition and zero flux boundary condition (i.e., Eq. 5).

178 The following equation can be used to estimate k_{bl} ⁵⁴:

 $k_{bl} = D_w / \delta \tag{7}$

180 where D_w is the molecular diffusion coefficient of the compound in water with typical 181 values ranging from 10⁻⁵ cm²/s to 10⁻⁶ cm²/s; and δ is thickness of the diffusive 182 boundary layer, in most natural conditions $\delta \ll 1$ cm. δ in the microcosm test was 183 measured to be 1.7 ± 0.2 mm by the alabaster method¹. The corresponding minimum 184 of k_{bl} is 5.9×10^{-6} cm/s. Furthermore, the mass transfer coefficient reported by the field 185 studies ranged from 2.8×10^{-5} cm/s to 4.6×10^{-4} cm/s^{61,62}. The mass transfer coefficients 186 obtained in the laboratory experiments ranges from 1.5×10^{-6} cm/s to 5.1×10^{-5} cm/s, 187 which are much lower than those obtained by the field studies due to overestimation 188 of pore water concentrations or artificially high fluxes^{63,64}. In this study, 2.5×10^{-5} , 189 5×10^{-5} and 10^{-4} cm/s will be used in the following analysis.

190 The initial conditions are assumed to be

191
$$C_m(z,0) = C_{m,int}(z)$$
 $(m=1, 2, 3,..., M)$ (8)

192 where $C_{m,int}$ is the initial concentration in soil layer *m*.

193 It should be pointed out that compared with the one-dimensional partial-differential equation considered in this study, much more complicated 194 195 two-dimensional partial-differential equations have been considered in the process of 196 deriving analytical solutions for both chemical and physical dissolution front instability problems in fluid-saturated porous media⁴³⁻⁴⁹. Therefore, the factors 197 including solute dispersion, mineral dissolution ratio^{65,66}, medium permeability 198 anisotropy⁶⁷, temperature effect^{68,69}, non-linear adsorption⁷⁰, complex degradation 199 processes⁷¹, consolidation-induced advection⁷² were neglected in this study. 200

201 Analytical solution

202 The following dimensionless parameters are defined to derive the analytical solution

203 of the proposed mathematical model:

$$\omega = \frac{z}{l_{I}} \tag{9}$$

205
$$C^* = \frac{C}{C_0}$$
 (10)

206
$$\tau = \frac{D_1^* t}{R_{d_1} l_1^2}$$
(11)

207
$$D_{am} = \frac{\lambda_m l_m^2}{D_m^*} \qquad (m=1, 2, 3, ..., M) \qquad (12)$$

$$Sh = \frac{k_{bl}l_M}{D_M^*}$$
(13)

where ω , C^* and τ are dimensionless depth, dimensionless concentration and time factor, respectively. The Damköhler number (D_{am}) and Sherwood number (*Sh*) represent the ratio of reaction rate to the transport phenomena rate occurring in a system and the ratio of the total rate of mass transfer to the rate of diffusion, respectively⁵⁴.

The governing equation (1) can be rewritten in terms of the dimensionless parametersintroduced above:

216
$$a_m \frac{\partial C^*_m}{\partial \tau} = \frac{\partial^2 C^*_m}{\partial \omega^2} - \frac{D_{am} C^*_m}{c_m^2} \qquad (m=1, 2, 3, ..., M)$$
(14)

217 where

218
$$a_m = \frac{R_{dm} D_1^*}{R_{d1} D_m^*} \qquad (m=1, 2, 3, ..., M) \qquad (15)$$

219
$$c_m = \frac{l_m}{l_1}$$
 $(m=1, 2, 3, ..., M)$ (16)

220 The dimensionless boundary conditions are as follows:

221
$$C_m^* = C_{m+1}^*$$
 (*m*=1, 2, 3,..., *M*-1) (17)

222
$$n_m D_m^* \frac{\partial C_m^*}{\partial \omega} = n_{m+1} D_{m+1}^* \frac{\partial C_{m+1}^*}{\partial \omega} \qquad (m=1, 2, 3, ..., M-1)$$
(18)

223
$$\frac{\partial C_M^*}{\partial \omega}\Big|_{\omega=0} = 0$$
(19)

224
$$\frac{\partial C_1^*}{\partial \omega}\Big|_{\omega=\frac{L_M}{l_1}} = ShC_1^*\Big|_{\omega=\frac{L_M}{l_1}}$$
(20)

225 The initial condition is changed into

226
$$C_m^*(z,0) = \frac{C_{m,\text{int}}(z)}{C_0} \qquad (m=1, 2, 3, ..., M) \quad (21)$$

Eq. (14) can be solved by the method of the classic integral transform technique (CITT) ⁷³. Following the systematized procedure of the CITT, an auxiliary homogeneous problem for the space variable function $\psi_m(\omega)$ in the same layers of the original problem needs to be defined. An auxiliary problem can be obtained by applying separation of variables to Eqs. (14)-(21):

232
$$-a_{m}\xi_{i}^{2}\psi_{m} = \frac{\partial^{2}\psi_{m}}{\partial\omega^{2}} - \frac{D_{am}\psi_{m}}{c_{m}^{2}} = H_{m}\psi_{m} \qquad (m=1, 2, 3, ..., M)$$
(22)

233 The operator H_m is defined as

234
$$H_m = \frac{\partial^2}{\partial \omega^2} - \frac{D_{am}}{c_m^2} \qquad (m=1, 2, 3, ..., M)$$
(23)

235 And the boundary conditions are as follows:

236
$$\frac{\partial \psi_1}{\partial \omega} = 0$$
 (24a)

237
$$\Psi_m = \Psi_{m+1}$$
 (*m*=1, 2, 3,..., *M*-1) (24b)

238
$$n_m D_m^* \frac{d\psi_m}{d\omega} = n_{m+1} D_{m+1}^* \frac{d\psi_{m+1}}{d\omega} \qquad (m=1, 2, 3, ..., M-1) \quad (24c)$$

239
$$\frac{\partial \psi_M}{\partial \omega} = Sh\psi_M \tag{24d}$$

240 The above system is an eigenvalue problem and has nontrivial solutions for a discrete

spectrum of the eigenvalues
$$\xi_i$$
 (*i*=1, 2, 3,..., ∞). The general symbolic solution of Eq.

242 (22) can be written in terms of two linearly independent solutions
$$\phi_{m,i}(\omega)$$
 and $\theta_{m,i}(\omega)$:

243
$$\Psi_{m,i}(\omega) = A_{m,i}\phi_{m,i}(\omega) + B_{m,i}\theta_{m,i}(\omega)$$
 (*m*=1, 2, 3,..., *M*) (25)

244 where $A_{m,i}$ and $B_{m,i}$ are the parameters to be determined.

According to Eqs. (24a) and (25), the coefficients for the first layer can be obtained as

246 follows:

247
$$B_{1,i} = -\frac{\phi_{1,i}(0)}{\theta_{1,i}(0)} A_{1,i} \qquad (m=1, 2, 3, ..., M)$$
(26)

248 Substituting Eq.(25) into Eqs.(24) results in the following expressions for the

249 coefficients
$$A_{m,i}$$
 and $B_{m,i}$:

$$A_{m,i} = \left(\frac{A_{m-1,i}}{k_m}\right) \frac{k_m \phi_{m-1,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*) - k_{m-1} \theta_{m,i}(z_{m-1}^*) \phi'_{m-1,i}(z_{m-1}^*)}{\phi_{m,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*) - \theta_{m,i}(z_{m-1}^*) \phi'_{m,i}(z_{m-1}^*)} + \left(\frac{B_{m-1,i}}{k_m}\right) \frac{k_m \theta_{m-1,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*) - k_{m-1} \theta_{m,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*)}{\phi_{m,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*) - \theta_{m,i}(z_{m-1}^*) \phi'_{m,i}(z_{m-1}^*)} + \left(\frac{B_{m-1,i}}{k_m}\right) \frac{k_m \theta_{m-1,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*) - k_{m-1} \theta_{m,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*)}{\phi'_{m,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*) - \theta_{m,i}(z_{m-1}^*) \phi'_{m,i}(z_{m-1}^*)} + \left(\frac{B_{m-1,i}}{k_m}\right) \frac{k_m \theta_{m-1,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*) - k_{m-1} \theta_{m,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*)}{\phi'_{m,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*) - \theta'_{m,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*)} + \left(\frac{B_{m-1,i}}{k_m}\right) \frac{k_m \theta_{m-1,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*) - k_{m-1} \theta_{m,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*)}{\theta'_{m,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*) - \theta'_{m,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*)} + \left(\frac{B_{m-1,i}}{k_m}\right) \frac{k_m \theta_{m-1,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*) - k_{m-1} \theta_{m,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*)}{\theta'_{m,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*) - \theta'_{m,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*)} + \left(\frac{B_{m-1,i}}{k_m}\right) \frac{k_m \theta_{m-1,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*) - k_{m-1} \theta_{m,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*)}{\theta'_{m,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*)} + \left(\frac{B_{m-1,i}}{k_m}\right) \frac{k_m \theta_{m-1,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*) - \theta'_{m,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*)}{\theta'_{m,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*)} + \left(\frac{B_{m-1,i}}{k_m}\right) \frac{k_m \theta_{m-1,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*) - \theta'_{m,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*)}{\theta'_{m,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*)} + \left(\frac{B_{m-1,i}}{k_m}\right) \frac{k_m \theta_{m-1,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*)}{\theta'_{m,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*)} + \left(\frac{B_{m-1,i}}{k_m}\right) \frac{k_m \theta_{m-1,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1}^*)}{\theta'_{m,i}(z_{m-1}^*) \theta'_{m,i}(z_{m-1$$

251 (m=1, 2, 3, ..., M) (27)

252
$$B_{m,i} = \left(\frac{A_{m-1,i}}{k_m}\right) \frac{k_{m-1}\phi_{m,i}(z_{m-1}^*)\phi_{m-1,i}'(z_{m-1}^*) - k_m\phi_{m-1,i}(z_{m-1}^*)\phi_{m,i}'(z_{m-1}^*)}{\phi_{m,i}(z_{m-1}^*)\theta_{m,i}'(z_{m-1}^*) - \theta_{m,i}(z_{m-1}^*)\phi_{m,i}'(z_{m-1}^*)} + \left(\frac{B_{m-1,i}}{k_m}\right) \frac{k_{m-1}\phi_{m-1,i}(z_{m-1}^*)\theta_{m-1,i}'(z_{m-1}^*) - k_m\theta_{m-1,i}(z_{m-1}^*)\phi_{m,i}'(z_{m-1}^*)}{\phi_{m,i}(z_{m-1}^*)\theta_{m,i}'(z_{m-1}^*) - \theta_{m,i}(z_{m-1}^*)\phi_{m,i}'(z_{m-1}^*)} + \left(\frac{B_{m-1,i}}{k_m}\right) \frac{k_{m-1}\phi_{m-1,i}(z_{m-1}^*)\theta_{m-1,i}'(z_{m-1}^*) - k_m\theta_{m-1,i}(z_{m-1}^*)\phi_{m,i}'(z_{m-1}^*)}{\phi_{m,i}(z_{m-1}^*)\theta_{m,i}'(z_{m-1}^*) - \theta_{m,i}(z_{m-1}^*)\phi_{m,i}'(z_{m-1}^*)} + \left(\frac{B_{m-1,i}}{k_m}\right) \frac{k_{m-1}\phi_{m-1,i}(z_{m-1}^*)\theta_{m-1,i}'(z_{m-1}^*) - k_m\theta_{m-1,i}(z_{m-1}^*)}{\phi_{m,i}(z_{m-1}^*) - \theta_{m,i}'(z_{m-1}^*)} + \left(\frac{B_{m-1,i}}{k_m}\right) \frac{k_{m-1}\phi_{m-1,i}(z_{m-1}^*)}{\phi_{m,i}(z_{m-1}^*) - \theta_{m,i}'(z_{m-1}^*)} + \left(\frac{B_{m-1,i}}{k_m}\right) \frac{k_{m-1}\phi_{m-1,i}'(z_{m-1}^*)}{\phi_{m,i}'(z_{m-1}^*) - \theta_{m,i}'(z_{m-1}^*)} + \left(\frac{B_{m-1,i}'(z_{m-1}^*)}{\phi_{m,i}'(z_{m-1}^*)} + \frac{B_{m-1,i}'(z_{m-1}^*)}{\phi_{m-1,i}'(z_{m-1}^*)} + \frac{B_{m-1,i}'(z_{m-1}^*)}{\phi_{m-1,i}'(z_{m-1}^*)}$$

(*m*=1, 2, 3,..., *M*)

253

where
$$k_m = n_m D_m^*$$
. The value of $A_{1,i}$ is arbitrary and is set to $A_{1,i} = 1$.

Eqs. (24d) and (25) are used to find a symbolic general transcendental equation.

256
$$A_{M,i}\phi'_{M,i}(z_{M}^{*}) + B_{M,i}\theta'_{M,i}(z_{M}^{*}) = 0$$
(29)

257 The general solution of the eigenvalue problem (Eq. 22) can be expressed as

258 $follows^{73}$:

259
$$\phi_{m,i}(\omega) = \sin(\beta_{m,i}\omega)$$
 (m=1, 2, 3,..., M) (30)

260
$$\theta_{m,i}(\omega) = \cos(\beta_{m,i}\omega)$$
 (m=1, 2, 3,..., M) (31)

261 where $\beta_{m,i}$ are the layer eigenvalues, which are related to the eigenvalues ξ_i by

262
$$\beta_{m,i} = \frac{(4\xi_i^2 a_m - 4D_{am}/c_m^2)^{1/2}}{2} \qquad (m=1, 2, 3, ..., M) \qquad (32)$$

(28)

According to Eqs. (26) and (30)-(32), the coefficients for the first layer can be

264 obtained as follows:

265
$$B_{1,i} = 0$$

266

267 For the others layers, the following recursive formulas are obtained:

268
$$A_{m,i} = [A_{m-1,i}\cos(\beta_{m-1,i}z_{m-1}^*) - B_{m-1,i}\sin(\beta_{m-1,i}z_{m-1}^*)]\frac{k_{m-1}\beta_{m-1,i}}{k_m\beta_{m,i}} + \sin(\beta_{m,i}z_{m-1}^*)[A_{m-1,i}\sin(\beta_{m-1,i}z_{m-1}^*) + B_{m-1,i}\cos(\beta_{m-1,i}z_{m-1}^*)]$$

269
$$(m=2, 3, ..., M)$$
 (34)

270
$$B_{m,i} = \cos(\beta_{m,i} z_{m-1}^{*}) [A_{m-1,i} \sin(\beta_{m-1,i} z_{m-1}^{*}) + B_{m-1,i} \cos(\beta_{m-1,i} z_{m-1}^{*})] - \sin(\beta_{m,i} z_{m-1}^{*}) [A_{m-1,i} \cos(\beta_{m-1,i} z_{m-1}^{*}) - B_{m-1,i} \sin(\beta_{m-1,i} z_{m-1}^{*})] \frac{k_{m-1} \beta_{m-1,i}}{k_{m} \beta_{m,i}}$$

271
$$(m=2, 3, ..., M)$$
 (35)

272 The eigenfunctions $\psi_{m,i}(\omega)$ can be expressed as follows:

273
$$\Psi_{m,i}(\omega) = A_{m,i} \sin(\beta_{m,i}\omega) + B_{m,i} \cos(\beta_{m,i}\omega) \qquad (m=1, 2, 3, ..., M)$$
 (36)

Finally, using Eqs.(29)-(32) the following transcendental equation can be obtained:

275
$$A_{M,i}\sin(\beta_{M,i}z_{M}^{*}) + B_{M,i}\cos(\beta_{M,i}z_{M}^{*}) = 0$$
(37)

276 In the classification system given by Mikhailow and Ozisik⁷⁴ for self adjoint problems

277 of heat and mass diffusion, an eigenvalue problem is defined as:

278
$$\frac{d}{dz}\left[\frac{d\psi_m}{dz}\right] + \left[\xi^2 w_m(\omega) - q_m(\omega)\right]\psi_m = 0 \qquad (m=1, 2, 3, ..., M) \quad (38)$$

where

280
$$q_m(\omega) = \frac{D_m}{c_m^2}$$
 (m=1, 2, 3,..., M) (39)

281
$$w_m(\omega) = a_m$$
 $(m=1, 2, 3, ..., M)$ (40)

(33)

282 The orthogonality property for the set of linearly independent eigenfunctions, $\psi_{m,i}(\omega)$,

associated with Eq. (38) is given by:

284
$$\sum_{m=1}^{M} \int_{z_{m-1}^{*}}^{z_{m}^{*}} w_{m}(\omega) \psi_{m,i}(\omega) \psi_{m,j}(\omega) dx = \delta_{ij} N_{i} \qquad (m=1, 2, 3, ..., M) \quad (41)$$

285 where N_i is the norm. The closed-form expression for the norm is as follows:

286
$$N_i = \sum_{m=1}^{M} \overline{N}_{m,i} \qquad (m=1, 2, 3, ..., M) \quad (42)$$

where

288
$$\overline{N}_{m,i} = \frac{a_m}{4\beta_{m,i}} \{ 2\beta_{m,i} (A_{m,i}^2 + B_{m,i}^2) (z_m^* - z_{m-1}^*) + 2A_{m,i} B_{m,i} [\cos(2\beta_{m,i} z_{m-1}^* - \cos(2\beta_{m,i} z_m^*)] + (A_{m,i}^2 - B_{m,i}^2) [\sin(2\beta_{m,i} z_{m-1}^*) - \sin(2\beta_{m,i} z_m^*)] \}$$

 $(m=1, 2, 3, \dots, M)$

(43)

290 Representing the unknown function $C_m(\omega, \tau)$ as a series expansion in terms of the 291 eigenfunctions $\psi_{m,i}(\omega)$ and using the orthogonality property (Eq. 42) results in the

292 following integral transform pair:

293
$$C_m(\omega,\tau) = \sum_{i=1}^{\infty} \frac{\psi_{m,i}(\omega)}{N_i} \overline{C}_i(\tau) \qquad (m=1, 2, 3, \dots, M)$$
(44)

And its corresponding inverse transform is

295
$$\overline{C}_{i}(\tau) = \sum_{m=1}^{M} \int_{z_{m-1}^{*}}^{z_{m}^{*}} w_{m}(\omega) \psi_{m,i}(\omega) C(\omega,\tau) d\omega \qquad (m=1, 2, 3, ..., M)$$
(45)

Applying the inverse formula (Eq. 34) to Eq. (14) and recalling the eigenvalue

297 problem (Eq. 22) results in

298
$$a_m \frac{\partial}{\partial \tau} \sum_{j=1}^{\infty} \frac{\psi_{m,i}(\omega)}{N_j} \overline{C}_j(\tau) = -\sum_{j=1}^{\infty} \frac{a_m \xi_j^2 \psi_{m,j}(\omega)}{N_j} \overline{C}_j(\tau) \qquad (m=1, \ 2, \ 3, ..., \ M)$$
(46)

299 Applying $\sum_{m=1}^{M} \int_{z_{m-1}^{*}}^{z_{m}^{*}} \psi_{m,i}(\omega) d\omega$ to both sides of Eq. (46) results in

$$\frac{\partial}{\partial \tau} \sum_{j=1}^{\infty} \frac{C_{j}(\tau)}{N_{j}} \sum_{m=1}^{M} \int_{z_{m-1}^{*}}^{z_{m}^{*}} a_{m} \psi_{m,i}(\omega) \psi_{m,j}(\omega) d\omega$$

$$= -\sum_{j=1}^{\infty} \frac{\overline{C}_{j}(\tau)}{N_{j}} \xi_{j}^{2} \sum_{m=1}^{M} \int_{z_{m-1}^{*}}^{z_{m}^{*}} a_{m} \psi_{m,i}(\omega) \psi_{m,j}(\omega) d\omega$$
(m=1, 2, 3,..., M) (47)

301 By using the orthogonality property (Eq. 42), the following equation can be obtained:

302
$$\frac{d\overline{C}_{i}(\tau)}{d\tau} = -\xi_{i}^{2}\overline{C}_{i}(\tau)$$
(48)

303

The initial condition (Eq. 22) can also be transformed to yield

304
$$\overline{C}_i(0) = \sum_{m=1}^{M} \overline{f}_{m,i}$$
 (*m*=1, 2, 3,..., *M*) (49)

305

where

306
$$\overline{f}_{m,i} = \int_{z_{m-1}^{*}}^{z_m^{*}} w_m(\omega) \psi_{m,i}(\omega) C(\omega,0) d\omega \qquad (m=1, 2, 3, ..., M)$$
(50)

307 Solving Eq.(48) with initial condition Eq.(49) gives the transformed field:

308
$$\overline{C}_i(\tau) = \overline{C}_i(0) \exp(-\xi_i^2 \tau)$$
(51)

³⁰⁹ Finally, invoking the inverse formula Eq.(42) and the relationship in Eq.(51) the

³¹⁰ closed-form analytical solution is obtained as follows:

311
$$C_m(\omega,\tau) = \sum_{i=1}^{\infty} \frac{\psi_{m,i}(\omega)}{N_i} \overline{C}_i(0) \exp(-\xi_i^2 \tau) \qquad (m=1, 2, 3, ..., M)$$
(52)

The flux of at the surface of the cap can be obtained as

$$J(L_{M},\tau) = -n_{M}D_{M}^{*}\frac{\partial C_{1}(L_{M},\tau)}{\partial \omega}$$
(53)

314 Substituting Eq. (52) into Eq. (53) results in

315

$$J(L_{M},\tau) = -n_{M} D_{M}^{*} \sum_{i=1}^{\infty} \frac{A_{1,i} \cos(\beta_{1,i}\omega) + B_{1,i} \sin(\beta_{1,i}\omega)}{N_{i}} \overline{C}_{i}(0) \exp(-\xi_{i}^{2}\tau) \beta_{1,i}$$
(54)

316 The cap effectiveness factor, which can be used as the assessment of the cap

317 performance, can be expressed as follows:

$$CE = \frac{J_{uc} - J_c}{J_{uc} + J_c}$$
(55)

where J_{uc} and J_c are the (hypothetical) uncapped fluxes and capped fluxes at the top of the cap system, respectively.

321 **4. Results and discussions**

322 *4.1. Good experimental set-up to verify the model.*

323 Fig. 2a and 2b presents the comparison of the results of the proposed analytical 324 models with experimental data obtained from laboratory-scale simulations of capped contaminated sediment⁴.In the experiments, the contaminated sediment layer in the 325 326 two cases was obtained from the lake bottom located at the Louisiana State University 327 campus in Baton Rouge. In the two cases, the cap materials are Balsam sand cap and 328 Tao River sand cap, respectively. The balsam sand is a proposed cap material from a 329 quarry near New Bedford and The Tao River sample was obtained from the bed of the 330 Yellow River in China. The retardation factors for the Balsam sand and Tao River sand cap are 4.94 and 8.3, respectively. The effective diffusion coefficients of the 331 Balsam sand and Tao River cap are 7×10^{-10} and 8.3×10^{-10} m²/s, respectively⁶. In the 332 333 experiments, 1.5-cm-thick sediment was contaminated by trichloropropane (TCP) and 334 covered by a 0.7-cm-thick capping layer to impede the TCP from diffusing into the 335 surface water. The transport properties for these two layers are summarized in Table 1. 336 The initial concentration of TCP in the sediment and the capping layer is 150 mg/L 337 and 0, respectively. A zero-flux boundary condition is imposed at the bottom of the 338 sediment layer. The concentration remains zero at the top of the capping layer to

model the flushing effect of the surface water. The half-life of TCP is 30-60 years reported by Thoma et al. ⁶. The half-life of TCP in capping and sediment are assumed to be 100 years in this case. The solid line is the predicted flux by the proposed analytical model and the dot is the experimental data from laboratory-scale simulations (see Fig.2). It can be seen that the predicted flux is in good agreement with the experimental data for both of the capped systems. This indicates that the proposed analytical solutions are rational and can yield correct results.

346 *4.2 Dimensionless analysis of contaminant diffusion in capped contaminated*

347 sediments

The soil and transport properties considered for these four layers are summarized in Table 2. A zero-flux boundary condition is assumed at the bottom of the sediment layer, and the Robin-type boundary condition and zero concentration boundary

351 condition are assumed at the top of the capping layer.

Fig. 3 shows the dimensionless concentration profiles for different Damköhler 352 numbers at time factor $\tau = \frac{D_1^* t}{R_{al} l_1^2} = 0.01$. $D_{a4} = \frac{\lambda_4 l_4^2}{D_4^*}$ is Damkohler number in the 353 bioturbation layer. The experimental data from Gilevska et al.75 showed that 354 biodegradation rate of contaminant in bioturbation layer ranges from 0.4 year⁻¹ to 84 355 year⁻¹. Damkohler number in the bioturbation layer (D_{a4}) here is assumed to be 1, 5, 356 357 10 and 30, respectively. The relative concentration in the capping layer is significantly reduced with the increase of D_{a4} . For example, the relative concentration at the 358 surface of sand layer for the case with $D_{a4}=1$ can be 2.8 times greater than that of the 359 case with $D_{a4}=30$. The above analysis indicated that considering the effect of 360

361 contaminant biodegradation in bioturbation layer can improve the efficiency of the
 362 capping systems.

363	Fig. 4 shows the effect of $a_2 = \frac{R_{d2}D_1^*}{R_{d1}D_2^*}$ and $D_{a4} = \frac{\lambda_4 l_4^2}{D_4^*}$ on cap effectiveness
364	factor. Five cases including case 1 (a_2 =2.26, Da_4 =1), case 2 (a_2 =2.26, Da_4 =5), case 3
365	$(a_2=2.26, Da_4=10)$, case 4 $(a_2=11.3, Da_4=1)$ and case 5 $(a_2=22.6, Da_4=1)$ were
366	selected to analyze the effects of different combinations a_2 and Da_4 on cap
367	effectiveness factor. The parameter a_2 has a less significant effect on the cap
368	effectiveness factor than that of D_{a4} . For instance, the time required for CE to reach
369	0.5 for case 1 can be 1.8 and 50 times less than that of case 2 and case 5, respectively.
370	This is due to the fact that the sorbent layer is relatively thin and the diffusion barrier
371	effect is also weak. It can be seen that the cap effectiveness factor significantly
372	increases with the increment of Da_4 . For example, the time factor required for CE to
373	reach 0.5 for case 1, case 2 and case 3 is 0.02, 1.05 and 2.12, respectively. When $\tau=1$,
374	the effectiveness factor for the case 2 and case 3 is 0.5 and 0.8, respectively. It
375	indicates that biodegradation of contaminant in bioturbation layer can effectively
376	decrease flux released from capped contaminated sediment.

Fig.5a and 5b show the effect of sorbent layer on relative concentration over time at surface of sand layer for different a_2 and c_2 . The effective remediation time was designed to be the time for the concentration at the top of the sand layer to reach 10% of initial contaminant concentration². It can be seen that both of the dimensionless retardation factor a_2 and dimensionless thickness c_2 have a great influence on contaminant transport in the capping system. The effective remediation 383 time for the case with $a_2=100$ can be 22.7 times larger than that with $a_2=10$ (Fig.5a). 384 The time required to reach the maximum relative concentration for the case with 385 $a_2=20$ can be 11.2 times larger than the case with $a_2=1$. Furthermore, the maximum 386 relative concentration for the case with $a_2=20$ can be around 1.9 times less than the case with $a_2=1$. As for c_2 , the effective remediation time and the time required to 387 reach the maximum relative concentration for the case with $c_2=0.01$ can be around 10 388 389 times larger than $c_2=0.05$, respectively (Fig.5b). If the capping system is designed to 390 be effective for a 200-year period which equals to $\tau=0.02$, the reasonable value of a_2 391 should be larger than 50 under $c_2=0.03$ for the in-situ capping system (Fig.5a). 392 Similarly, the reasonable value of c_2 should be larger than 0.05 under $a_2=20$ (Fig.5b). 393 The above analysis indicates that the proposed dimensionless analytical model can be 394 used to design a final capping system. The results also indicate that capping will be an 395 attractive alternative for remediation when the adsorption factor and the thickness of 396 sorbent layer are well designed⁷.

397 *4.3 Effect of sorbent layer and bioturbation layer on flux at surface of system*

Fig. 6 shows the effect of sorbent layer on the flux at surface of the system ($z=L_M$). Five cases including case 1 (without sorbent layer), case 2 ($l_{sorbent}=5$ mm, and $R_{d2}=260$), case 3 ($l_{sorbent}=10$ mm and $R_{d2}=130$), case 4 ($l_{sorbent}=10$ mm, $R_{d2}=260$) and case 5 ($l_{sorbent}=20$ mm, $R_{d2}=130$) are selected to analyze the effects of retardation factor and thickness of sorbent layer on surface flux. For each case, there is a period of time before any contaminant has transported through the cap system (isolation time), followed by a period of increasing flux through the cap and into the bioactive zone 405 until a maximum is reached, and then a decrease in flux over time until the underlying sediment layer is depleted⁵. The isolation time is defined as the time when the flux of 406 407 contaminant at the top of the cap system reaches 10% of the maximum flux simulated 408 in that case. The isolation time for case 1, case 2, case 3, case 4 and case 5 is 3.1 years, 409 5.2 years, 6.4 years, 9 years and 17 years, respectively. The maximum flux for case 1 410 can be 1.8 times larger than that of case 4. However, the time required to reach the 411 maximum flux for case 1 can be 7.5 times less than that of the case 4. The above 412 results show that increasing the adsorption properties and thickness of sorbent layer 413 would result in an effective improvement of the cap system. The isolation time for 414 case 5 can be 2.7 and 1.9 times longer than that of case 3 and case 4, respectively. 415 Furthermore, the maximum flux for case 2 can also be 1.1 times larger than that of 416 case 3. The above analysis indicates that increasing the thickness of sorbent layer might be more effective than that of the improvement of adsorption factor in sorbent 417 418 layer.

419 Fig. 7a and 7b show the effect of bioturbation layer on the flux at the surface of 420 system under different half-lives of contaminant and thicknesses of bioturbation layer. 421 Bioturbation is the normal life cycle activity of benthic organisms that lead to mixing 422 of sediment and porewater in the near surface layer of sediments. These activities 423 have a great influence on the fate and behavior of contaminants. They are often the dominant mixing process in stable sediment environments⁷⁶. Thoms et al.⁷⁷ 424 425 summarizes the literature reported values of the depth of bioturbation at more than 426 200 sites via a variety of different organisms. It is indicated that the bioturbation depth

427 for freshwater and estuarine systems are approximately 3.1cm and 14.8cm, respectively. The biodiffusion coefficients are around 1×10^{-5} cm²/s and 5×10^{-4} cm²/s 428 for freshwater and estuarine systems, respectively⁷. In order to assure that the 429 430 designed cap can meet the requirement of the quantitative goals, it is important to 431 analyze how the height of bioturbation layer and biodegradation of contaminant can 432 affect the performance of a cap. The range of biodegradation rate in bioturbation layer is assumed to be from 0.4 year⁻¹ to 84 year⁻¹. The corresponding half-life in the 433 bioturbation layer $t_{1/2,bio}$ ranges from 0.008 to 1.73 years⁷⁵. The flux at surface of 434 435 system is significantly reduced with a decrease of half-life of contaminant. For example, the maximum flux for the case with $t_{1/2,bio} = 0.07$ year can be 4.5 times less 436 437 than that of the case without considering the effect of biodegradation (Fig.7a). 438 However, the biodegradation of contaminant shows a less important influence on the isolation time. For instance, the isolation time for the case with $t_{1/2,bio} = 0.07$ year and 439 case with $t_{1/2,bio} = 0.7$ year is 12.7 years and 11.2 years, respectively. The thickness of 440 441 bioturbation layer also has a great influence on flux at surface of system. For example, 442 the maximum flux for the case with $l_{bio}=15$ cm can be 1.5 times greater than that of the case with l_{bio} =5cm. Increasing the thickness of bioturbation layer would result in a 443 444 decrease of the maximum contaminant flux dispersing into water. This is due to the 445 fact that the effective contaminant transport pathway increases with the increment of 446 bioturbation layer. In addition, degradation of contaminant can play a more significant 447 role when bioturbation layer has a larger thickness. However, the maximum flux for 448 the case with l_{bio} =15cm can be 17 times larger than that of the case without bioturbation layer. This may be due to the fact that the effective diffusion coefficient of sand cap is 28 times lower than D_{bio} . The result from the model was in accordance with the experimental studies⁷⁸. Granberg et.al.⁷⁹ also showed that bioturbation can stimulate an augmented release flux of PCBs.

Fig.8a and Fig.8b show the flux at the surface of system under different 453 454 combinations of properties of sorbent layer and bioturbation layer. The case with $t_{1/2,bio} = 0.7$ year and $R_{dsorbent} = 260$ is selected as a reference case to investigate the 455 456 relative importance of biodegradation rate in bioturbation layer and retardation factor 457 in sorbent layer (Fig.8a). It can be seen that the maximum flux for the reference case can be 3.6 and 1.9 times larger than the cases with $t_{1/2,bio} = 0.07$ year, $R_{dsorbent} = 260$ and 458 459 $t_{1/2,bio} = 0.7$ year, $R_{dsorbent} = 2600$, respectively. The isolation time for the case with $t_{1/2,bio}$ 460 =0.7 year and $R_{dsorbent}$ =2600 can be 4.3 times larger than the case with $t_{1/2,bio}$ =0.7 year and $R_{dsorbent}$ =260. The above results indicate that increasing half-life of contaminant in 461 462 bioturbation layer can significantly reduce the contaminant flux at the surface of system. However, the increase of half-life of contaminant in bioturbation layer has a 463 464 negligible effect on isolation time. On the contrary, increasing retardation factor in 465 sorbent layer can effectively extend the isolation time although retardation factor has a less influence on surface flux. The case with $l_{bio}=10$ cm and $l_{sorbent}=1$ mm is selected 466 467 as a reference case to investigate the relatively importance of thickness of bioturbation 468 layer and sorbent layer (Fig.8b). The maximum flux for the reference case can be 1.7 469 and 1.3 times larger than the case with $l_{bio}=20$ cm, $l_{sorbent}=1$ mm and $l_{bio}=10$ cm, 470 $l_{sorbent}$ =2mm, respectively. The isolation time for the case with l_{bio} =10cm, $l_{sorbent}$ =2mm

is 25 years. The isolation time for the reference case and the case with $l_{bio}=20$ cm, 471 *l*_{sorbent}=1mm are 13 years and 15 years, respectively. The above results indicate that 472 473 surface flux is sensitive to biodegradation rate and thickness of bioturbation layer 474 although the properties of bioturbation layer have a weak effect on the isolation time. However, the properties of sorbent layer include retardation factor and thickness have 475 476 a significant influence on both surface flux and isolation time. The above analysis also 477 indicates that increasing the adsorption properties and thickness of sorbent layer 478 would result in an effective improvement of the cap system.

479 *4.4 Effect of mass transfer coefficient*

480 Fig. 9a and 9b show the effect of the mass transfer coefficient on contaminant 481 concentration and flux at the surface of system. The mass transfer coefficient is in 482 inverse proportion to the thickness of the effective diffusive boundary layer (DBL). This DBL is the thin layer of water adjacent to the sediment surface through which 483 molecular diffusion is the dominant transport mechanism for dissolved material⁸⁰. k_{bl} 484 =2.5×10⁻⁵ cm/s, 5×10⁻⁵ cm/s and 10⁻⁴ cm/s are used in the following analysis 485 486 (according to Eq.7). The effect of mass transfer coefficient on the contaminant 487 concentration over time at the surface of system was shown in Fig. 9a. At the top of the bioturbation layer, the maximum contaminant concentration for the case with k_{bl} 488 = 2.5×10^{-5} cm/s can reach 0.26 mg/L, which is 13 times larger than that of the case 489 with $k_{bl} = 10^{-4}$ cm/s. The surface contaminant concentration decreases with the increase 490 491 of the mass transfer coefficient since the thickness of the DBL also decreases with the 492 increase of the mass transfer coefficient. It indicates that considering the effect of k_{bl}

493 $(<10^{-4} \text{ cm/s})$ may reduce the performance of the cap. Fig. 9b shows the effect of the 494 mass transfer coefficient on contaminant flux over time at the surface of the 495 bioturbation layer. The contaminant flux at the top of bioturbation layer increases with 496 the increase of k_{bl} . For example, the maximum contaminant flux for the case with k_{bl} =10⁻⁴ cm/s can be 1.3 and 1.1 times greater than that of the case with k_{bl} =2.5×10⁻⁵ 497 cm/s and 5×10^{-5} cm/s, respectively. The result from the model agrees with the 498 499 experimental studies which showed that larger mass transfer coefficient results in a greater flux⁸¹. This is due to the fact that the increment in the concentration gradient 500 induced by the increase of mass transfer coefficient augments the contaminant flux at 501 502 the surface of system.

503 **5. Summary and conclusions**

504 An analytical model for contaminant transport in multi-layered capped contaminated sediment considering the degradation of organic contaminant was 505 506 presented. The results obtained by the proposed analytical model agree well with 507 those obtained from the laboratory tests. Based on the analytical model, the effects of 508 half-life of contaminant in bioturbation, thickness of bioturbation layer, retardation 509 factor of sorbent layer, thickness of sorbent layer and mass transfer coefficient on 510 contaminant transport in capped contaminated sediment system were analyzed. The conclusions are as follows: 511

512 (1) The properties of bioturbation layer have a significant effect on the performance 513 of the capped contaminated sediment system. The maximum flux for the case with 514 $t_{1/2,bio}$ =0.07 year can be 4.5 times less than that of the case without considering the effect of biodegradation. The effectiveness factor for the case with D_{a4} =10 can be 1.6 times than that with D_{a4} =5. This indicated that the effect of contaminant biodegradation in bioturbation layer should be considered for the design of the capping system.

519 (2) Increasing the thickness of sorbent layer might be more effective on improving 520 isolation time than that of the increment of adsorption factor in sorbent layer. The 521 isolation time for the case with $l_{sorbent}=10$ mm, $R_{dsorbent}=130$ can be 1.4 and 2.7 times less than that of case lsorbent=10mm and Rdsorbent=260 and lsorbent=20mm, 522 R_{d2} =130, respectively. Increasing the biodegradation rates of contaminant in 523 524 bioturbation layer is more effective on the decrease of surface flux than that of the 525 increment of adsorption factor in sorbent layer. The surface maximum flux for the 526 case with $t_{1/2,bio} = 0.7$ year, $R_{dsorbent} = 260$ can be 3.4 and 1.9 times larger than the cases with $t_{1/2,bio} = 0.07$ year, $R_{dsorbent} = 260$ and $t_{1/2,bio} = 0.7$ year, $R_{dsorbent} = 2600$, 527 528 respectively.

(3) The mass transfer coefficient should be considered for the design of the capping system. At the top of the bioturbation layer, the maximum contaminant concentration at the surface of system for the case with $k_{bl}=2.5\times10^{-5}$ cm/s can be 13 times larger than that of the case with $k_{bl}=10^{-4}$ cm/s.

(4) It should be noted that this study has certain limitations. For example, some
important factors, such as solute dispersion⁶¹, mineral dissolution ratio⁶², medium
permeability anisotropy⁶³, temperature effect^{64,65}, non-linear adsorption⁶⁶,
complex degradation processes⁶⁷, advection and consolidation-induced

advection⁶⁸ were neglected in this study. To further improve the analytical
solutions derived from this study, these factors need to be considered in the future
study.

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546 Notations

- 547 $C_m(z,t)$ Concentration of contaminant
- 548 D_m^* Effective diffusion coefficient
- 549 D_{am} Damköhler number
- 550 $F_m(x)$ Concentration distribution of the contaminant in soils
- 551 $J_m(z,t)$ Mass flux
- 552 k_{bl} Mass transfer coefficient in the benthic boundary layer
- 553 l_m Thickness of the soil layer m
- 554 R_{dm} Retardation factor
- 555 Sh Sherwood number
- 556 *t* Time
- 557 $t_{1/2}$ Half-life of contaminant in soil
- 558 $U_c(t)$ Average degree of diffusion

559	Ζ	Space coordinate
560	$\lambda_{_i}$	Biodegradation rate
561	ω	Dimensionless depth
562	τ	Time factor
563	$\psi_{\scriptscriptstyle m}$	Eigenfunction
564	ξ_i	Eigenvalues
565	$eta_{\scriptscriptstyle m}$	The layer eigenvalues

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	comparison with experimental data			
	Balsam sand cap	Tao river cap		
Cap properties				
$D_w(\mathrm{m}^2/\mathrm{s})$	7×10 ⁻¹⁰	8.3×10 ⁻¹⁰		
n_1	0.38	0.5		
R_{dI}	4.95	8.7		
$L_{l}(\mathbf{m})$	0.7	0.7		
$t_{1/2,\text{capping}}$ (year)	100	100		
Sediment properties				
n_2	0.45	0.45		
R_{d2}	50.5	55		
$L_2(\mathbf{m})$	1.5	1.5		
$t_{1/2,\text{sediment}}$ (year)	100	100		
Initial TCP concentration	150	150		
(mg/L)				

Tab.1. Transport properties for capping layer and contaminated sediment for

comparison with experimental data

Parameters	$L_i(\mathbf{m})$	$D^*(m^2/s)$	R_d	$t_{1/2}(\text{year})$
Bioturbation layer	0.1 ^a	2.8×10 ^{-9 c}	10 °	1 ^d
Cap layer	0.05 ^a	1.0×10^{-10} b	8.7 ^c	70
Sorbent layer	0.01 ^a	1.0×10^{-10} b	260 °	70
Contaminated sediment	0.5 ^a	1.02×10^{-10} b	115 °	70 ^b

Tab. 2. Parameters used in a layered sediment cap system simulations

813 a: Murphy et al.⁵; b: Bortone et al.¹⁵; c: Go et al.⁷; d: Gilevska et al.⁷¹

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817	capped contaminated sediment
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