Atacama Cosmology Telescope: Modeling the gas thermodynamics in BOSS CMASS galaxies from kinematic and thermal Sunyaev-Zel’dovich measurements


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Compton scattering of the CMB photons with the hot gas creates shifts in the photon energy, known as the Sunyaev-Zel’dovich effects (SZ) [1,2]. The inverse Compton scattering of the CMB photons with the hot thermal gas causes a nonblackbody distortion in the CMB temperature, known as thermal SZ effect (tSZ), which is proportional to the pressure due to the electrons integrated along the line of sight. The scattering of the CMB photons by the free electrons having bulk motion relative to the CMB rest frame causes another shift in the CMB temperature, preserving the blackbody shape. It is known as kinematic SZ effect (kSZ), and it is proportional to the electron momentum integrated along the line of sight (see [3] for a recent review of the SZ effects). The analysis of these distortions offers a direct probe of the spatial distribution and abundance of baryons down to the outskirts of galaxies and clusters (see, e.g., [4]). These quantities are still poorly constrained, especially for group-sized structures. The kSZ effect is particularly well suited to probe low density and low temperature environments like the outskirts of galaxies and clusters, since it is linearly proportional to the electron density and independent of the temperature, and is therefore complementary to the tSZ and x-ray measurements that are more sensitive to the central regions. However, while the tSZ has been extensively measured in clusters (and for a wide range of halo masses), kSZ detections (3σ–5σ) are relatively new.

I. INTRODUCTION

Studying the physical processes and thermodynamic properties that govern the ionized baryons in galaxies and galaxy clusters is essential to our pursuit of understanding galaxy evolution and formation across cosmic time. The circumgalactic medium (CGM) and the intracluster medium (ICM), the baryonic reservoirs for galaxies and clusters, contain the vast majority of baryons in these systems. The thermodynamic properties of the CGM and ICM encode the effects of the assembly history and feedback processes that shape galaxy and cluster formation. Moreover, the impact of baryons and their effects on the underlying dark matter must be known to the percent level if we are to fully utilize the next generation of large-scale-structure cosmological datasets.

The interaction between the CGM or ICM and the photons of the cosmic microwave background (CMB) creates shifts in the photon energy, known as the “Sunyaev-Zel’dovich effects” (SZ) [1,2]. The inverse Compton scattering of the CMB photons with the hot gas...
from stacking analyses [5–10] or from studies of individual clusters [11–13]. Both the tSZ and kSZ signals contain information about the thermodynamic properties of the CGM and ICM. In a theoretical forecast, [14] showed that combining kSZ and tSZ profile measurements can place tight constraints on baryonic processes like feedback and nonthermal pressure support in the CGM and ICM. Additionally, joint tSZ and kSZ measurements provide constraints on the CGM that are complementary to more traditional probes of the CGM, like absorption line measurements (e.g., [15–17]).

The kSZ measurements [8,18] have traced the distribution of free electrons around galaxies using independent measurements of the peculiar velocity from the galaxy overdensity field. Combining CMB data from the Atacama Cosmology Telescope (ACT) with individual velocity estimates from the “constant stellar mass” (CMASS) catalog of the Baryon Oscillation Spectroscopic Survey (BOSS DR10) [19], they showed that the gas density profiles in groups deviate significantly from a “dark matter only” Navarro-Frenk-White profile (NFW) [20] expected in the absence of feedback. This is another manifestation of the well-known “missing baryon problem,” i.e., that in late-time galaxies and groups, only a small fraction of the cosmological abundance of baryons is found within the virial radius [21,22]. It is speculated that the baryons are pushed out beyond the virial radius by a number of feedback mechanisms, and reside in the outskirts of galaxies in a diffuse and warm state usually referred to as the warm-hot intergalactic medium [22]. Localizing the “missing baryons” by measuring the gas profile out to several times the virial radius is of primary importance for understanding galaxy formation, interpreting weak-lensing measurements, and characterizing the complex physical processes behind feedback. While a number of previous observations have made progress in characterizing the missing baryons (see, for example, [23–25]), SZ measurements are particularly well suited to study the outskirts of intermediate and low mass halos, and shed light on this important issue.

There are observational hints that baryonic effects could be responsible for discrepancies between weak-lensing galaxy cross-correlation measurements and analytic models that do not account for baryons [26]. On these small scales the baryon distribution no longer traces the dark matter distribution, and thus impacts the matter power spectrum (e.g., [27,28]). If these baryonic effects are not accounted for in theoretical modeling of the matter power spectrum, then the resulting cosmological parameter inferences will be biased (e.g., [29,30]). Understanding the systematic effects from baryons and disentangling them from cosmological information is one of the biggest challenges for the next decade of cosmological surveys, like the Dark Energy Survey (DES) [31], the Hyper Suprime-Cam Subaru Strategic Program (HSC-SSP) [32], the Vera Rubin Observatory [33], and the Nancy Grace Roman Space Telescope [34]. Theoretical models exist that are calibrated using observations of the baryon fraction [35] or simulations [36,37]. In this paper, we use kSZ measurements of the gas profile that probe the baryon distribution on smaller scales and we explore a simple empirical model of this relationship.

Large cosmological simulations provide a partially predictive model and are now able to reproduce many of the optical properties of galaxies (e.g., [28,38–41]). It is necessary for these simulations to include physically motivated subgrid modeling schemes for processes like star formation and various energetic feedback mechanisms, since they do not resolve the scales necessary to perform \textit{ab initio} calculations of these critical physical processes in galaxy evolution. With kSZ and tSZ cross-correlation measurements we can directly test and inform these subgrid feedback models [14,42,43], as these subgrid models are not precisely tuned to reproduce SZ observations of the CGM and ICM.

In this paper, we use the new stacked tSZ and kSZ measurements obtained in a companion paper [18] by cross-correlating the CMASS galaxy catalogs of BOSS DR10 [19] and temperature maps from combined ACT DR5 and Planck data from [44] in the f150 and f090 bands (centered at roughly 150 GHz and 98 GHz, respectively) to constrain the baryonic processes, such as feedback and nonthermal pressure support, and the thermodynamic profiles of the CGM/ICM. Our models include a correction for the contamination of the tSZ signal by the thermal emission of dust from galaxies in our sample, which we estimate from ACT DR5 (f1090, f150) and Herschel/H-ATLAS data [45] in the three bands centered at 500 μm (600 GHz), 350 μm (857 GHz), and 250 μm (1200 GHz). We compare our results to predictions from Illustris TNG cosmological simulations [28] and older simulations by [46]. Finally, we use the best-fit density profiles to estimate the effects of including baryons in the modeling of weak-lensing galaxy cross-correlation measurements by [26].

Two upcoming papers [47,48] present kSZ (5σ) and tSZ (∼10σ) measurements using the same ACT and Planck maps as those used here, but different galaxy samples from BOSS. They explore the luminosity dependence of the signals, as well as the shape of the velocity correlation function. These probes contain information about dark energy and modifications to general relativity [49], neutrino masses [50], and primordial non-Gaussianity [51]. Because the galaxy samples are different, with different host halo masses, the results from these two papers are not directly comparable to ours.

In this paper and [18], our main interest is instead in the radial dependence of the kSZ and tSZ signals, and particularly the baryon profiles. We focus on the CMASS galaxy sample, for which clustering and galaxy lensing measurements are available, in order to obtain a
complete picture of the gas thermodynamics. This allows us to constrain the properties of feedback in these halos, and shed new light on the low lensing tension [26]. Because these two pairs of papers focus on different information from the kSZ and tSZ signals, they use different estimators: the pairwise kSZ estimator in [47,48] is particularly suited to measure the velocity correlation function, whereas the stacking with reconstructed velocities of [18] and this work is convenient for measuring the baryon profiles. Overall, these two pairs of papers are complementary, and highlight the wealth of information in joint kSZ and tSZ measurements.

The paper is organized as follows: Section II describes our modeling of the tSZ and kSZ signals in terms of both a polytropic gas model, which includes energetic feedback and a nonthermal pressure component, and parametric (generalized NFW) models for the gas thermal pressure and density of the Universe at the halo redshift, \( \rho(z) \), at a radius of \( R_{200} \), and 6 arcmin, corresponding to approximately 1.3 (f150) arcmin (see Fig. 15 in [18]). The tSZ and kSZ signals are measured from microwave temperature maps by applying a compensated aperture photometry (CAP) filter at the position of each galaxy; we average the value of the pixels within a disk of radius \( \theta_d \) and subtract the average of the pixels in an adjacent, equal area ring with external radius \( \sqrt{2}\theta_d \). With the ACT CMB maps in temperature units relative to the CMB (\( \mu K \)), the output of the CAP filter is given by

\[
AP(\theta_d) = \int d^2\theta \delta T(\theta) W_{\theta_d}(\theta),
\]

with units of \( \mu K \cdot \text{arcmin}^2 \), where the angular CAP filter function \( W_{\theta_d}(\theta) \) is dimensionless, defined as

\[
W_{\theta_d}(\theta) = \begin{cases} 
1 & \text{for } \theta < \theta_d, \\
-1 & \text{for } \theta_d \leq \theta \leq \sqrt{2}\theta_d, \\
0 & \text{otherwise}.
\end{cases}
\]

The filter aperture \( \theta_d \) has been chosen to vary between 1 and 6 arcmin, corresponding to approximately 1–4 times the typical virial radius \( R_{200} \), in order to investigate the physical scales relevant for the effects of feedback. The tSZ and kSZ signals are measured with a signal-to-noise ratio of 11 and 8, respectively [18], from ACT + Planck coadded maps in two frequency bands, f090 and f150 [44]. In order to properly model this specific set of data, we convolve 2D-projected temperature profiles to the same beams with which the [44] ACT + Planck coadded maps are convolved. These beams have non-Gaussian, scale-dependent profiles, with full widths at half-maximum of 2.1 (f090) and 1.3 (f150) arcmin (see Fig. 15 in [18]). The tSZ and kSZ signals can be modeled in terms of temperature fluctuations as described below.

The tSZ temperature fluctuations are given by

\[
\frac{\Delta T_{\text{tSZ}}}{T_{\text{CMB}}} = f(\nu),
\]

where the frequency dependence, neglecting relativistic corrections (e.g., [58,59]), is given by \( f(\nu) = x \coth(x/2) - 4 \), with \( x = h\nu/k_BT_{\text{CMB}} \). \( T_{\text{CMB}} \) is the CMB...
temperature, \(k_B\) is the Boltzmann constant, and the Compton-\(y\) parameter measured within \(\theta\), at an angular diameter distance to redshift \(z\), \(d_A(z)\), is

\[
y(\theta) = \frac{\sigma_T}{m_e c^2} \int_{\text{los}} P_e \left( \sqrt{\ell^2 + d_A(z)^2 \theta^2} \right) d\ell.
\]  

(4)

Here \(\sigma_T\) is the Thomson cross section, \(m_e\) is the electron mass, \(c\) is the speed of light, \(P_e\) is the thermal electron pressure, and \(d\ell\) is the line-of-sight (los) physical distance.

The kSZ temperature fluctuations are given by

\[
\frac{\Delta T_{\text{kSZ}}}{T_{\text{CMB}}} = \frac{\sigma_T}{c} \int_{\text{los}} e^{-\tau} n_e v_p d\ell,
\]  

(5)

where \(n_e\) is the electron number density, \(v_p\) is the peculiar velocity, and \(\tau\) is the optical depth to Thomson scattering along the line of sight, defined as

\[
\tau(\theta) = \sigma_T \int_{\text{los}} n_e \left( \sqrt{\ell^2 + d_A(z)^2 \theta^2} \right) d\ell.
\]  

(6)

The mean optical depth in our redshift range (0.4 < \(z\) < 0.7) is below one percent (see, e.g., [60]); therefore, we approximate the \(e^{-\tau}\) factor in the integral as 1. Moreover, since [18] selectively extracts the kSZ signal correlated with the galaxy group of interest, we can further simplify Eq. (5) as

\[
\frac{\Delta T_{\text{kSZ}}}{T_{\text{CMB}}} = \tau_{\text{gal}} \left( \frac{v_p}{c} \right).
\]  

(7)

where \(\tau_{\text{gal}}\) refers to the optical depth of the galaxy group considered, and \(v_p = 1.06 \times 10^{-3} c\) is the rms of the peculiar velocities, projected along the line of sight, where the magnitude adopted is for the median redshift of the CMASS sample, \(z = 0.55\), in the linear approximation. We estimate the uncertainty on the velocity reconstruction being less than few percent [18] and given our current signal-to-noise ratio, we do not propagate it into the uncertainty on the kSZ profile. However, this will be crucial for upcoming measurements with higher kSZ signal-to-noise ratio [61].

The electron density and pressure can be converted into the gas density \(\rho_{\text{gas}}\) and thermal pressure \(P_{\text{th}}\). Assuming a fully ionized medium with primordial abundances

\[
n_e = \frac{(X_H + 1) \rho_{\text{gas}}}{2 m_{\text{amu}}}.
\]

\[
P_e = \left( \frac{2 + 2X_H}{3 + 5X_H} \right) P_{\text{th}},
\]  

(8)

where \(X_H = 0.76\) is the hydrogen mass fraction and \(m_{\text{amu}}\) is the atomic mass unit.

Therefore, the tSZ and kSZ temperature fluctuations are related to the gas thermal pressure \(P_{\text{th}}\) and to the gas density \(\rho_{\text{gas}}\), respectively.

In order to model the observed signal we apply the same aperture photometry filters used in the analysis of the observations by substituting the temperature models for the kSZ and tSZ [Eqs. (3)–(4) and (7)–(6), respectively] in Eq. (1).

To summarize, (i) we project the 3D gas profiles along the line of sight as in Eqs. (4) and (6), (ii) we convolve them with the beam profile measured at f090 and f150, (iii) for the pressure model we also multiply by the map response to the tSZ in each band [44], (iv) we then get the average temperature within disks of varying radii \(\theta_{\text{los}}\), and (v) for each aperture, we subtract the mean temperature in an adjacent ring of external radius \(\sqrt{2}\theta_{\text{los}}\) and equal area, so as to reproduce the same aperture photometry filtering applied to data.

These profiles from both OBB and GNFW are defined for a halo of given mass and redshift. We compute average profiles that account for the mass distribution of the CMASS sample. Using mass-weighted averages is particularly important for the tSZ modeling, as the tSZ signal is proportional to \(M^{1/3}\), while the kSZ is linearly dependent on mass. We do not average over the distribution of redshifts, which is peaked around the median (see Fig. 2 in [18]), and we use therefore the median redshift of our sample, \(z = 0.55\). Using test models, we have checked that computing mass and redshift-weighted average profiles does not significantly change the results, for both density and pressure. Our modeling of the CMASS sample does assume that all CMASS galaxies are central galaxies, which is reasonable given the CMASS selection and our current measurement errors. Additionally, we assume the direct mapping between stellar mass and halo mass used on the CMASS sample [57].

**B. OBB model**

In order to investigate the thermodynamic properties of the CGM and ICM, we implement a model proposed by [53] (see also [62,63]). The model assumes that the gas has an initial energy per unit mass equivalent to that of the dark matter halo. In our implementation, we assume that the dark matter follows a spherically symmetric NFW density profile [20], characterized by a density normalization \(\rho_0\) and a scale radius \(r_s\):

\[
\rho_{\text{DM}}(x) = \frac{\rho_0}{x(1 + x)^2},
\]  

(9)

where \(x = r/r_s\). The scale radius is related to the halo mass through the concentration parameter \(c_{\text{NFW}}\), \(r_s = R_{200}/c_{\text{NFW}}\). We use the concentration-mass power-law relation by [64] obtained from \(N\)-body simulations for halo masses in the range \(10^{11}–10^{15} h^{-1} M_{\odot}\) at \(0 < z < 2\):
\[ c_{\text{NFW}} = 5.71 \times (1 + z)^{-0.47} \times \left( \frac{M}{2 \times 10^{12} M_\odot} \right)^{-0.084}, \]  

(10)

with a scatter of 0.15 dex. The assumption of spherical symmetry for the sample should be accurate for both the gas and the dark matter since we are modeling stacked profiles (e.g., [65–67]). Assuming that the initial gas mass is a fraction of the total halo mass equal to the cosmic baryon fraction \((M_{\text{gas,i}} = \Omega_b/\Omega_m M_{\text{tot,i}})\), we can use the virial theorem to get the gas energy and surface pressure in terms of the dark matter halo parameters. As the system evolves, some fraction of the initial ICM gas will cool and turn into stellar mass, plus the energy \(\Delta E_p\) due to expansion or contraction of the halo boundaries:

\[ E_f = E_i + eM_* c^2 + \Delta E_p, \]  

(15)

with the condition that the total pressure at the halo boundary must match the initial surface pressure.

This model was found to be in good agreement with high-resolution hydrodynamic simulations and can reproduce the observed x-ray scaling relations. For massive clusters \((M_{\text{tot}} = 10^{14} h^{-1} M_\odot)\), [53] finds a good fit to simulations with a polytropic index \(\Gamma = 1.2\), a fraction of the baryonic mass condensed into stars that is transferred back to the remaining gas, estimating the feedback efficiency, of \(e = 3.9 \times 10^{-5}\), and 10% of the total pressure due to a nonthermal component. For clusters in a similar mass range, [62] gives a comparable amount of feedback, between 3 and \(5 \times 10^{-5}\), while [63] adopts a smaller value in their fiducial model, \(e = 10^{-6}\), and a redshift-dependent nonthermal pressure parameter in the range \(\alpha_{\text{Nth}} = [0 - 0.33]\). We implement this model to constrain the normalization of a nonthermal pressure profile, \(\alpha_{\text{Nth}}\), and the energy injected in the gas by feedback, \(e\).

### C. GNFW models

We parametrize the three-dimensional profiles of the gas density and the thermal pressure, respectively, using two generalized NFW models. For both models, we choose parameters and parameter ranges motivated by fits to cosmological simulations described below. In general, our SZ measurements constrain the shape of the pressure and density profiles at large radii, while they do not constrain that well the parameters which are sensitive to the profile properties at small radii. Thus, we fix the values of such parameters motivated by the simulations mentioned below when we fit the GNFW models.

For the density model, we refer to the following generalized NFW profile [54]:

\[ \rho_{\text{GNFW}}(x) = \rho_0 \left( \frac{x}{x_{c,k}} \right)^{\alpha_k} \left[ 1 + \left( \frac{x}{x_{c,k}} \right)^{\alpha_k} \right]^{-\beta_k - \gamma_k}, \]  

\[ \rho_{\text{gas}}(x) = \rho_{\text{GNFW}}(x) \rho_{\text{cr}}(z) f_b, \]  

(16)

where \(x \equiv r/R_{200}\), \(x_{c,k}\) is a core scale, \((\alpha_k, \beta_k, \gamma_k)\) are the slopes at \(x \sim 1\), \(x \gg 1\), and \(x \ll 1\), respectively, \(\rho_{\text{cr}}(z)\) is the critical density of the Universe at redshift \(z\), and \(f_b = \Omega_b/\Omega_m\) is the baryon fraction. Given the considerable
TABLE I. Marginalized constraints on the OBB parameters.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
<th>Prior</th>
<th>Constraints (1 σ)</th>
</tr>
</thead>
<tbody>
<tr>
<td>ξ</td>
<td>Polytropic index</td>
<td>[1.5/3]</td>
<td>1.2 ± 0.1</td>
</tr>
<tr>
<td>α_{\text{th}}</td>
<td>Nonthermal pressure norm.</td>
<td>[0.0, 0.8]</td>
<td>0.04 ± 0.03</td>
</tr>
<tr>
<td>ε</td>
<td>Feedback efficiency</td>
<td>[10^{-4.8}, 10^{-0.0}]</td>
<td>(40 ± 9) × 10^{-6}</td>
</tr>
<tr>
<td>A_{k_{2h}}</td>
<td>Two-halo density amplitude</td>
<td>[0, 5]</td>
<td>0.8 ± 0.5</td>
</tr>
<tr>
<td>A_{2h}</td>
<td>Two-halo pressure amplitude</td>
<td>[0, 5]</td>
<td>0.9 ± 0.3</td>
</tr>
</tbody>
</table>

TABLE II. Marginalized constraints on the GNFW parameters.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
<th>Prior</th>
<th>Constraints (1 σ)</th>
</tr>
</thead>
<tbody>
<tr>
<td>log_{10} ρ_{0}</td>
<td>Log amplitude</td>
<td>[1, 5]</td>
<td>2.8 ± 0.3</td>
</tr>
<tr>
<td>x_{c,t}</td>
<td>Core radius</td>
<td>[0.1, 1]</td>
<td>0.6 ± 0.3</td>
</tr>
<tr>
<td>β_{t}</td>
<td>Outer slope</td>
<td>[1, 5]</td>
<td>2.6 ± 0.6</td>
</tr>
<tr>
<td>A_{k_{2h}}</td>
<td>Two-halo term amplitude</td>
<td>[0, 5]</td>
<td>1.1 ± 0.7</td>
</tr>
<tr>
<td>P_{0}</td>
<td>Amplitude</td>
<td>[0.1, 30]</td>
<td>2.0 ± 0.8</td>
</tr>
<tr>
<td>α_{t}</td>
<td>Intermediate slope</td>
<td>[0.1, 2]</td>
<td>0.8 ± 0.3</td>
</tr>
<tr>
<td>β_{t}</td>
<td>Outer slope</td>
<td>[1, 10]</td>
<td>2.6 ± 1.0</td>
</tr>
<tr>
<td>A_{2h}</td>
<td>Two-halo term amplitude</td>
<td>[0, 5]</td>
<td>0.7 ± 0.8</td>
</tr>
</tbody>
</table>

For the thermal pressure model, we use a slightly modified GNFW profile following [55]:

\[ P_{\text{GNFW}}(x) = P_{0}(x/x_{c,t})^{\gamma_{t}}[1 + (x/x_{c,t})^{\alpha_{t}}]^{-\beta_{t}}, \]
\[ P_{\text{th}}(x) = P_{\text{GNFW}}(x)P_{200}. \]

where \( P_{200} = GM_{200}v_{200}^{2}/(2R_{200}) \), \( x_{c,t} \), and \( x \) are a core scale, and \( (\alpha_{t}, \beta_{t}, \gamma_{t}) \) are the slopes at \( x \sim 1, x \gg 1, \) and \( x \ll 1 \), respectively. These parameters define the pressure radial profile and are different from the parameters in Eq. (16). There is significant degeneracy among all the GNFW parameters, so we fix two parameters sensitive to the profile properties at small radii, \( \gamma_{t} = -0.2, \) and \( \alpha_{t} = 1 \), as in [77].

For the thermal pressure model, we use a slightly modified GNFW profile following [55]:

\[ P_{\text{GNFW}}(x) = P_{0}(x/x_{c,t})^{\gamma_{t}}[1 + (x/x_{c,t})^{\alpha_{t}}]^{-\beta_{t}}, \]
\[ P_{\text{th}}(x) = P_{\text{GNFW}}(x)P_{200}. \]

where \( P_{200} = GM_{200}v_{200}^{2}/(2R_{200}) \), \( x_{c,t} \) is a core scale, and \( (\alpha_{t}, \beta_{t}, \gamma_{t}) \) are the slopes at \( x \sim 1, x \gg 1, \) and \( x \ll 1 \), respectively. These parameters define the pressure radial profile and are different from the parameters in Eq. (16). There is significant degeneracy among all the GNFW parameters, so we fix two parameters sensitive to the profile properties at small radii, at the values suggested by previous cosmological simulations [55,76]: \( \gamma_{t} = -0.3 \) and \( \alpha_{t} = 1 \).

D. Two-halo term

For both profiles we include a two-halo term. The total density and pressure profiles are modeled as \( \rho(r) = \rho_{\text{one-halo}}(r) + A_{k_{2h}}\rho_{\text{two-halo}}(r) \) and \( P(r) = P_{\text{one-halo}}(r) + A_{k_{2h}}P_{\text{two-halo}}(r) \), respectively, where the one-halo terms are computed according to the models above. In Appendix A we show how the fiducial profiles for the two-halo terms are calculated and we include free parameters \( A_{2h} \) in front of those terms for both density and pressure that scale the amplitude and include them in our fits.

III. RESULTS

Reference [18] presents the results for the individual integrated aperture quantities (the optical depth to Thomson scattering and the Compton y), which is a standard practice for SZ cross-correlation measurements. Here we study instead how these SZ cross-correlations (the thermodynamic profiles) change as a function of the distance from the galaxy center. Given the good signal-to-noise ratio (S/N) of the [18] measurements in each radial aperture, we are able to move beyond single aperture analyses and use the information from all the scales we can access in these measurements. We can thus improve our ability to constrain models or simulations of the CGM, while this constraining power would be reduced if we compressed the SZ measurements into a single aperture.

In this section, we present constraints on feedback and nonthermal pressure from combined kSZ and tSZ profile data (Sec. III A) and constraints on our parametric models of the gas density (Sec. III B) and thermal pressure profile (Sec. III C). We begin each subsection by describing the free parameters in the fit and motivating the use of priors, then we show the results of fitting in Tables I and II and Figs. 1–4.
For our fits, we use the data ($\vec{d}$) and covariance matrices ($C$) estimated by [18] using the bootstrap method. We use all the data points between 1 and 6 arcmin when we fit the kSZ profile, while we exclude the smallest aperture when we fit the tSZ profile since the dust contamination is a large fraction of the signal there.

We assume the likelihood ($L$) to be Gaussian, written as

$$\ln L = \frac{1}{2} [\vec{d} - \vec{m}(\vec{\theta})]^T C^{-1} [\vec{d} - \vec{m}(\vec{\theta})],$$

where $\vec{m}(\vec{\theta})$ is the model evaluated at the parameter $\vec{\theta}$. The posterior on the model parameters ($P$) is then expressed as

$$\ln P(\vec{\theta}|\vec{d}) = \ln [L(\vec{d}|\vec{m}(\vec{\theta})) P(\vec{\theta})],$$

where $P(\vec{\theta})$ are the priors on $\vec{\theta}$. We use Markov chain Monte Carlo calculations (MCMC) [78,79] to estimate the posterior probability functions, with the affine-invariant ensemble sampler algorithm implemented in EMCEE [80]. We run multiple EMCEE ensembles, adding independent sets of chains until the Gelman-Rubin convergence parameter, $\hat{R}$, reaches values smaller than 1.1 [81].

### A. OBB model

We probe the efficiency of energetic feedback and nonthermal pressure in the CMASS sample by fitting the OBB model, described in Sec. II B, to kSZ and tSZ data simultaneously. The tSZ likelihood includes the dust correction described in Appendix B. We assume a uniform prior for the polytropic index in the range $1 < \Gamma < 5/3$.

The lower limit guarantees the existence of the polytropic

FIG. 1. Constraints on the polytropic index, $\Gamma$, the amplitude of the nonthermal pressure profile, $\alpha_{\text{Nth}}$, the feedback efficiency parameter, $\epsilon$, and the amplitudes of the two-halo terms of the density and pressure profiles, $A_{k2h}$ and $A_{t2h}$, obtained by fitting the OBB model to combined kSZ and tSZ measurements by [18]. The radial data have large correlations (see Fig. 7 in [18]) that are accounted for in the analysis. The triangle plot shows one and two dimensional projections of the posterior probability distributions of the free parameters. We assume uniform priors within the following: $1 < \Gamma < 5/3$, $0 < \alpha_{\text{Nth}} < 0.8$, $-4.8 < \log_{10} \epsilon < -4.0$, $0 < A_{k2h} < 5$, $0 < A_{t2h} < 5$. The top right panels show the observed kSZ and tSZ profiles (points) with the best-fit and the $2\sigma$ range (2nd–98th percentiles) of the distribution of the models obtained from the MCMC chains.
function [Eq. (12)],

\[ T_{\text{vir}} = 1.7 \times 10^7 \text{ K} \]

is the mean electron temperature at the virial temperature. This is a lower limit to the energy injected as we have not included radiative losses from cooling. Also we have not propagated any uncertainties on the stellar or total masses of the CMASS sample. The ratio of energy injected to the binding energy that we estimate is consistent with the 25% value that can be calculated from the results in [46].

Reference [83] uses x-ray measurements of gas density and mass in galaxy groups and clusters to calibrate a model similar to the model used in this work. They find a feedback efficiency factor of \( \epsilon = (4^{+3}_{-5}) \times 10^{-6} \) (95% confidence level) that is smaller, at \( \sim 4\sigma \), than our result. However, we note that their x-ray sample is on average more massive than ours and the parameter space explored is also different. We obtain profiles of the gas density and thermal pressure from Eqs. (11)–(14), and estimate the electron temperature profile as

\[ T_e = P_e/(n_e k_B) \]

where we calculate \( P_e \) and \( n_e \) from Eq. (8). Figure 2 shows the median (black line) and the \( 2\sigma \) range (blue band) of the models obtained from the MCMC chains. We constrain the temperature profile at more than \( 4\sigma \) in the first two radial bins, i.e., within approximately the virial radius, at better than \( 2\sigma \) within \( \sim 2R_{\text{vir}} \) and less than \( 2\sigma \) at larger radii. We find a decreasing temperature profile from \( (1.3 \pm 0.2) \times 10^7 \) K (1.1 \pm 0.1 keV) to \( (1.8 \pm 2.4) \times 10^6 \) K (0.2 \pm 0.2 keV) in our radial range. These values are overall consistent with the mean electron temperature estimated by [18] as the ratio of tSZ and kSZ measurements for each aperture photometry radius. For reference, we compute the expected virial temperature as

\[ T_{\text{vir}} = \mu m_p G M_{200}/2 k_B R_{200} \]

assuming a singular isothermal sphere of gas of the mass equal to the mean mass of our CMASS sample \( (M_{200} = 3.3 \times 10^{13} M_\odot) \), where \( \mu = 1.14 \) is the mean molecular weight for a fully ionized medium with primordial abundances. We get \( T_{\text{vir}} = 1.7 \times 10^7 \) K, which is of the same order of magnitude of our measured profile. In a recent paper, [85] compares gas profiles and temperatures obtained from Planck SZ cross-correlation measurements of halos in the Sloan Digital Sky Survey (SDSS) [86] at \( z \sim 0 \), with different cosmological simulations. We note that our temperature measurements are higher, although not directly comparable because the samples are different and the scales involved in the analysis are different, mostly dictated by the different resolution of Planck and ACT.

![FIG. 2. Average, inferred electron temperature profile of CMASS galaxies halos weighted by density obtained from the joint kSZ + tSZ fit to the OBB model using the MCMC chains.](image)
Our GNFW density profile is defined by Eq. (16). For the density amplitude \( \rho_0 \), the core radius \( x_{c,k} \), the power-law index \( \beta_k \) for the asymptotic falloff of the profile, and the amplitude of the two-halo term \( A_{k2h} \). Given the considerable degeneracy of the parameters we fix two parameters that are sensitive to the profile properties at small radii, \( \gamma_k = -0.2 \), and \( \alpha_k = 1 \), as in [77]. We define the likelihood combining the two density models for f090 and f150, accounting for the different beams and the correlated noise, in order to jointly fit the kSZ measured in the two bands. We assume uniform priors on the parameters within: 

\( 1 < \log_{10} \rho_0 < 5 \), 
\( 0.1 < x_{c,k} < 1 \), 
\( 1 < \beta_k < 5 \), 
\( 0 < A_{k2h} < 5 \).

The top right panel shows the measured kSZ profile at f090 and f150 (circles) with the median (50th percentile, dashed curves) and the 2\( \sigma \) (2nd–98th percentiles, bands) range of the models obtained from the MCMC chains. The solid lines indicate the best-fit model with \( \chi^2 = 20.2 \) and PTE = 0.32.

### B. GNFW density

Our GNFW density profile is defined by Eq. (16). We fit for the density amplitude \( \rho_0 \), the core radius \( x_{c,k} \), the power-law index \( \beta_k \) for the asymptotic falloff of the profile, and the amplitude of the two-halo term \( A_{k2h} \). Given the considerable degeneracy of the parameters we fix two parameters that are sensitive to the profile properties at small radii, \( \gamma_k = -0.2 \), and \( \alpha_k = 1 \), as in [77]. We define the likelihood combining the two density models for f090 and f150, accounting for the different beams and the correlated noise, in order to jointly fit the kSZ measured in the two bands. We assume uniform priors on all the free parameters in the following ranges: 

\( 1 < \log_{10} \rho_0 < 5 \), 
\( 0.1 < x_{c,k} < 1 \), 
\( 1 < \beta_k < 5 \), 
\( 0 < A_{k2h} < 5 \).

Table II reports the marginalized constraints with 1\( \sigma \) error bars. Figure 3 shows the posterior contours of the GNFW density parameters. The top right panel shows the best-fit model (solid lines) and the \( \pm 2\sigma \) range of the models obtained from the MCMC over the kSZ data. The \( \chi^2 \) of the best-fit model (i.e., the minimum \( \chi^2 \)) is 20.2, and the PTE is 0.32, indicating a good fit of the data. We next assess the significance of the detection of a two-halo term by our kSZ measurements. We find a best-fit amplitude of \( A_{k2h} = 1.1^{+0.8}_{-0.7} \), indicating a 1.6\( \sigma \) evidence, consistent with the values obtained with the OBB fit.

The \( \chi^2 \) does not change if we reduce the number of free parameters by fixing the core radius to our best-fit value, \( x_{c,k} = 0.6 \). In this case we get \( \chi^2 = 20.1 \), with three free parameters (PTE = 0.33) and the same 2\( \sigma \) range of the models obtained from the MCMC chains. The constraint on the log-amplitude improves from 13% to 7% (log\( \rho_0 = 2.9 \pm 0.2 \)), while the constraints on \( \beta_k \) and \( A_{k2h} \) do not substantially change.

We check the consistency between the kSZ radial profiles obtained with the GNFW and the OBB models.
using \( \chi^2 \) statistics. We find that they match within \( 1\sigma \), with \( \chi^2 = 15.8 \) for 16 data points (PTE = 0.47).

C. GNFW pressure

Our GNFW pressure profile is defined by Eq. (17). We fit for the amplitude \( P_0 \), the core radius \( x_c \), the power-law index \( \beta \), and the amplitude of the two-halo term, \( A_{2 h} \), obtained by fitting the GNFW pressure model to tSZ measurements by [18]. The radial data have large correlations (see Figs. 7 and 8 in [18]) that are accounted for in the analysis. The blue contours and lines show the fit of the GNFW thermal pressure + dust model to ACT and Herschel temperature measurements (see Fig. 11 for the simultaneous constraints on the dust model), while in red is the fit of the GNFW thermal pressure model to Compton-\( \gamma \) measurements obtained with CIB-deprojected maps. The corner plot shows one and two dimensional projections of the posterior probability distributions of the free parameters. We assume uniform priors within the following: \( 0.1 < P_0 < 30, 0.1 < \alpha_t < 2, 1 < \beta_t < 10, 0 < A_{2h} < 5 \). The top right panel shows best-fit (solid lines), the median (50th percentile, dashed lines), and the \( 2\sigma \) (2nd–98th percentiles, bands) of the distribution of the models obtained from the MCMC chains.
Fig. 11. The top right panel shows the median \((\pm 2\sigma)\) range of the models obtained from the MCMC runs over the tSZ (+dust) data, and the best fit corresponding to a minimum \(\chi^2\) of 43.5 with \(\text{PTE} = 0.45\) (solid lines). In order to validate our model, and check that the constraints on the GNFW parameters are not determined by the dust fit, we also use measurements of the tSZ alone \([18]\) obtained with the internal linear combination component-separated maps from \([87]\), of the Compton \(y\) with deprojected cosmic infrared background (CIB) from Planck + ACT DR4. The result of fitting the CIB-deprojected Compton-\(y\) maps is shown by the red contours in Fig. 4. The best fit to the Compton-\(y\) profile has a \(\chi^2\) of 10.5 (PTE = 0.31) and matches within 1\(\sigma\) the tSZ + dust fit.

A notable feature is the degeneracy between \(\beta_t\) and \(P_0\). This is a well-known degeneracy and has been seen before in tSZ profile measurements \([88]\). We clearly observe this degeneracy in the fits to Compton-\(y\), CIB-deprojected measurements, and to a much lesser extent in the fits to tSZ + dust measurements. We attribute this difference to the fact that the measurement errors for the Compton-\(y\), CIB-deprojected case are larger, as a result of a slightly smaller area overlap with the CMASS sample. Moreover, the component-separated maps are not minimum variance, due to the nulling of the CIB, and they include ACT data up to 2015 only (DR4), as opposed to 2018 for our fiducial temperature maps (DR5).

The same GNFW form was previously used in (e.g., \([89]\)) to model the tSZ-CMB lensing cross-correlation. There, the degeneracy was broken by keeping \(\beta_t\) fixed, and the amplitude \(P_0\) was that of the mean pressure profile of all halos in the Universe, weighted by their tSZ signal times their CMB lensing signal, instead of that of a specific galaxy sample like here.

The best-fit value \(A_{2\text{h}} = 0.7^{+0.3}_{-0.5}\) indicates a preference for a nonzero two-halo term at 1.8\(\sigma\) from tSZ measurements, which is consistent with the values obtained with the OBB fit. The measurement of the two-halo term alone is not new and previous studies have used stacked tSZ measurements to probe the distribution of hot gas in galaxy clusters and groups and to separate the one- and two-halo regimes. References \([90,91]\) measured the two-halo term by analyzing the cross-correlation function between SDSS galaxy groups at a lower redshift \((z < 0.2)\) and Planck \(y\) maps. They found evidence of both components in the most massive halos, \(M \geq 10^{13.5} h^{-1} M_{\odot}\), with a predominance of the two-halo term at \(\gtrsim 2\) Mpc, and evidence of two-halo term alone for lower mass systems. Also using Planck \(y\) maps, the two-halo regime has now been constrained through the measurement of \((bP_\gamma)\), the halo bias-weighted mean electron pressure, with galaxy samples from the Dark Energy Survey \([92]\), a compilation of the 2mass photometric redshift survey, WISE, and SuperCOSMOS \([93]\), and the DR14 SDSS release \([94,95]\). Unlike previous work based on Planck, the ACT data used here has a smaller beam, enabling us to study the pressure profiles in small group-sized halos, including both the one-halo and two-halo terms, at \(z \sim 0.6\).

The goodness of the fit does not substantially change if we reduce the number of free parameters by fixing the intermediate slope to our best-fit value \(\alpha_t = 0.8\). We get in this case \(\chi^2 = 40.1\) (PTE = 0.60) and the same 2\(\sigma\) distribution of the models obtained from the MCMC chains. The constraints on the amplitude get remarkably tighter, from 70\% to 20\% \((P_0 = 1.3^{+0.3}_{-0.3})\), and those on the outer slope improve from 33\% to 10\% \((\beta_t = 2.0 \pm 0.2)\), while the constraints on \(A_{2\text{h}}\) and on the parameters of the dust model remain essentially the same.

The tSZ radial profile that we obtain from fitting the GNFW model is consistent within 2\(\sigma\) with the tSZ profile obtained for the OBB model. We get \(\chi^2 = 27.9\) for 16 data points (PTE = 0.03). This is a reasonable match considering that these are fits of different parametric models, each one having some degenerate parameters, and also taking into account our measurement errors. By neglecting the outermost measurements which have the largest error bars, we find a better match within 1.6\(\sigma\), with \(\chi^2 = 20.4\) for 14 data points (PTE = 0.12).

IV. IMPLICATIONS FOR OPTICAL WEAK-LENSING OBSERVATIONS

The parametric GNFW model for the electron density profile we obtained from kSZ measurements serves as a first-order, empirical model for how baryons impact theoretical halo occupation distribution (HOD) models for optical weak-lensing measurements from the CMASS sample. Reference \([26]\) showed that their HOD model for the galaxy-galaxy lensing signal from CMASS overestimated this signal compared to their measurements, concluding that “lensing is low.” The details of their fiducial halo model (MDR1) are described in \([96]\) and the parameters of their model are calibrated to provide the best fit to CMASS galaxy clustering measurements.

Here, we do not attempt to disentangle the HOD from the individual profiles. Our best-fit GNFW profile describes the “HOD-convolved” density profile. In other words our parametric GNFW model contains within it the underlying properties of the CMASS sample, like what fraction of the CMASS sample is central or satellite galaxies. Thus, it is indeed the relevant quantity for predicting the impact of baryons on galaxy weak lensing, since the weak-lensing signal is also convolved with the same exact HOD.

With our HOD-convolved best fit we can straightforwardly estimate the impact of baryons on the MDR1 model \([96]\) by simply incorporating our parametric GNFW model for the electron density into it. The MDR1 model assumes that baryons trace the dark matter on all scales. We will use the MDR1 HOD model for the dark matter contribution to the galaxy-galaxy lensing measurement which uses a
standard weak-lensing shear estimator, \( \Delta \Sigma \). The projected mass density \( \Sigma \) is related to \( \Delta \Sigma \) through

\[
\Delta \Sigma(R) = \bar{\Sigma}(< R) - \Sigma(R),
\]

where \( \bar{\Sigma}(< R) \) is the mean projected mass density within projected radius \( R \) and \( \Sigma(R) \) is the surface mass density at \( R \). We can split the total \( \Delta \Sigma \) into a dark matter component (\( \Delta \Sigma_{\text{DM}} \) from MDR1) and baryon component (\( \Delta \Sigma_b \), obtained from our parametric GNFW model) such that \( \Delta \Sigma_{\text{tot}} = \Delta \Sigma_{\text{DM}} + \Delta \Sigma_b \). The \( \Delta \Sigma_{\text{DM}} \) is calculated by scaling the full \( \Delta \Sigma \) from MDR1 by the dark matter fraction, \((\Omega_M - \Omega_b)/\Omega_M\). The \( \Delta \Sigma_b \) is calculated by projecting our best-fit GNFW model for the electron density profile,

\[
\Sigma_b(R) \propto 2 \int_0^\infty \rho_{\text{gas}}(\sqrt{R^2 + l^2})dl.
\]

Here \( l \) is the line-of-sight direction on which we project, and the profile we fit is spherically symmetric so there is no preferred axis. The \( \Delta \Sigma_b(R) \) profile is calculated using Eq. (20) once \( \Sigma(R) \) is calculated. We normalize \( \Delta \Sigma_b(R) \) such that the baryon contribution to \( \Delta \Sigma_{\text{tot}} \) equals \( f_b \Delta \Sigma_{\text{DM}} \) at \( R_{\text{max}} \):

\[
\Delta \Sigma_b(R) \rightarrow \Delta \Sigma_b(R) \times \frac{f_b \Delta \Sigma_{\text{DM}}(R_{\text{max}})}{\Delta \Sigma_b(R_{\text{max}})}.
\]

Here \( R_{\text{max}} \) is the maximum angular radial bin for which we have a kSZ measurement. To summarize, we assumed that all the baryons are present within the maximum radius that we measured and beyond this radius the baryons trace the dark matter. We note that this model does not include the effect of the dark matter profile rearranging itself in response to the new baryon profile, often referred to as a “backreaction” to the baryons (e.g., [27,28]). We expect this to be a second-order correction to the model (supported by simulations, e.g., [28]), smaller than the baryonic effect we included.

Figure 5 shows the original galaxy-galaxy lensing measurement from [26] with green points and error bars, along with the original MDR1 HOD model from [96] shown as a red line. Our new estimate for the MDR1 halo model with a baryon correction coming from our kSZ profile measurements is shown in blue and the corresponding blue band illustrates the 2\( \sigma \) uncertainty obtained by sampling the best-fit GNFW MCMC chains. The dashed red line illustrates what the [96] HOD model would predict if one were to remove all the baryons. This “no-baryons” curve sets a lower limit to the MDR1 HOD model of the galaxy-galaxy lensing signal, in the absence of a modification to the dark matter profile. The yellow band shows the 2\( \sigma \) upper limit from the stellar component of \( \Delta \Sigma_{\text{tot}} \) following the calculations from [97] and the vertical grey lines show the radial range of kSZ measurements from [18]. Our estimates for the inner radii beyond the grey boundary are extrapolations of the model. At these radii the uncertainty from the stellar component is dominant.

Our empirical model for the baryon correction to the MDR1 halo model does reduce the difference between the galaxy-galaxy lensing measurement of the CMASS sample [26] and the predicted signal from the [96] MDR1 HOD model, which is calibrated to the clustering of the CMASS sample. At its largest, our baryon correction accounts for half the difference (50%). However, the lensing measurements still fall below our model on all scales. Even assuming an extreme baryon correction model where all the baryons are removed from the MDR1 HOD model, without altering the dark matter profile, the measured lensing signal is still below the model on scales of 500 kpc/\( h \) and less. The impact of baryons is one of many effects considered in [26], the others being measurement systematics, sample selection, assembly bias, and extensions to our concordance cosmological model. It is likely that a combination of these effects is responsible for the low lensing signal (e.g., [98]), since baryonic effects cannot explain the entire difference.
V. COMPARISON TO SIMULATIONS

Our measured kSZ and tSZ profiles from ACT + CMASS [18] offer a new opportunity to test current cosmological simulations [14,42,43] and the subgrid physics models they include to capture physical processes like feedback from stellar sources and AGN. Since these measurements are new, current simulations are not calibrated to match them, and thus the simulations permit a genuine prediction for these tSZ and kSZ CGM profiles.

We use predicted density and pressure profiles from Illustris TNG [28] and the [46] simulations, and a NFW density profile [20], shown in the top panel of Fig. 6. For the TNG simulations, we use the simulation snapshot data for each halo within a red galaxy at each redshift that matches the observed sample from Illustris TNG, and we weight each halo to match the observed sample’s stellar (TNG S) and halo mass (TNG H) distributions, respectively. These two halo selections are meant to capture the uncertainty in the stellar mass to halo mass relation used for the CMASS sample and they are a decent metric for the uncertainty in the modeling of the CMASS sample with TNG. Red galaxies within Illustris TNG were selected to have colors ranging from 0.12 to 0.14. For the pressure profile the [46] simulations have the lowest χ total$^2$ of 12.7 (PTE = 0.03), while the χ$^2$ for the TNG S and TNG H predictions are 20.2 (PTE = 0.00) and 23.1 (PTE = 0.00). Unfortunately, unlike the smaller radii, this radial range is completely unexplored. The simulations are underpredicting the gas density and temperature at these radii. This suggests that the subgrid stellar and AGN feedback models these simulations use to stop overcooking in the center and remove low entropy gas does not sufficiently heat the gas in the outer regions of the CGM.

There are numerous reasons why simulations could under predict the amount of CGM pressure and to a lesser extent CGM density at these larger radii. For example, the numerical methods chosen to inject energy and how that energy is allowed to propagate through the CGM will impact the thermodynamic properties of the CGM on all scales. Previous comparisons between simulations and tSZ profiles have been mostly limited to higher masses, like galaxy clusters (e.g., [88,100–102]), where the simulations matched the observations across a large range in radii. This implies that the current subgrid models for energy injection and numerical method for propagation are sufficient at describing the ICM but do not sufficiently heat the CGM at radii beyond the virial radius.

Predicting the gas profiles on these large scales in 10$^{13}$ M$_\odot$ galaxies is challenging as they have smaller potential wells than galaxy clusters and their CGM is more susceptible to small changes in the feedback modeling. A challenge going forward for cosmological simulations will be to sufficiently heat the CGM at radii beyond the virial radius without completely unbinding the CGM from halos at this mass scale. We look forward to investigating additional data from other current cosmological simulations and potentially enabling further refinement of the current subgrid feedback models.
VI. SUMMARY AND CONCLUSIONS

We present constraints on the gas thermodynamics of CMASS galaxies using kSZ and tSZ cross-correlation measurements from [18]. Combining kSZ and tSZ measurements we constrain the efficiency of feedback, in terms of thermal energy injected into the gas from AGN and supernovae, \( \epsilon = (40 \pm 9) \times 10^{-6} \) (1\( \sigma \)), which we robustly estimate with a 23\% relative
electron pressure within our observations. This includes convolving our models to both measurement and modeling systematics. The main higher signal-to-noise measurements require attention to this galaxy-galaxy lensing measurement. Using our best-fit density profile from the kSZ measurements to estimate the baryon correction to the HOD model of the CMASS galaxy-galaxy lensing signal, which is calibrated to match the CMASS clustering measurements. We find that including our baryon correction reduces but does not fully reconcile the difference with this galaxy-galaxy lensing measurement.

Using our best-fit density profile from the kSZ measurements we estimate the baryon correction to the HOD model of the CMASS galaxy-galaxy lensing signal, which is calibrated to match the CMASS clustering measurements. We find that including our baryon correction reduces but does not fully reconcile the difference with this galaxy-galaxy lensing measurement.

With upcoming higher signal-to-noise data, precisely modeling the HOD and the selection of the galaxy sample will be crucial to meaningfully compare measurements and hydrodynamical simulations.

This work demonstrates the power of joint tSZ and kSZ cross-correlation measurements in studying the distribution of baryons in the CGM of CMASS galaxy groups, especially in low-density environments and out to the outskirts, where they can reveal information about assembly history and the feedback processes. Future CMB observations such as the Simons Observatory [103], CCAT-Prime [104], CMB-S4 [105], and spectroscopic surveys of the large-scale structure like the Dark Energy Spectroscopic Instrument [106], the Subaru Prime Focus Spectrograph [107], and Euclid [108], will improve the precision in this radial range even more, with higher sensitivity, larger sky, and frequency coverage, and larger galaxy samples, enabling more detailed studies across multiple subsamples of mass, redshift, and galaxy properties.

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APPENDIX A: TWO-HALO TERM

We investigate the contribution to the halo gas profiles from neighboring halos, known as the “two-halo term.” We are interested in the two-halo kSZ signal observed from our cross-correlation analyses. In order to estimate this contribution, we construct an analytical model of the signal following the halo model of [90] (based on the formalism of [109]). The total halo-density correlation function describes the average excess density around halos with respect to random locations in the Universe, as a function of the comoving distance from the halo center \( r \). This has both a one-halo and a two-halo contribution:

\[
\xi_{h\rho}(r|M) = \xi_{h\rho}^\text{one-halo}(r|M) + \xi_{h\rho}^\text{two-halo}(r|M),
\]

where \( \xi_{h\rho}^\text{one-halo}(r|M) = \rho_{\text{gas}}(r|M) \) is the gas density profile of the halo itself [or equivalently the halo pressure profile \( P_{\text{th}}(r|M) \)], while \( \xi_{h\rho}^\text{two-halo}(r|M) \) is the contribution from correlated neighboring halos.

In order to calculate the two-halo term, the first step is to compute the Fourier transform of the density profile around a neighboring halo:

\[
\rho_{\text{th}}(k,M) = \int_0^\infty dr 4\pi r^2 \frac{\sin(kr)}{kr} \rho_{\text{gas}}(r|M),
\]

assuming a spherically symmetric density profile. We then compute the two-halo contribution to the halo-density power spectrum:

\[
P_{\text{h\rho}}(k) = b(M)P_{\text{lin}}(k) \int_0^\infty dM' \frac{dn}{dM'} b(M')u_\rho(k,M').
\]

APPENDIX B: DUST EMISSION

A contaminant of the tSZ signal is the light emitted from star-forming CMASS galaxies in the optical/UV that is absorbed by dust grains and reemitted in the thermal spectrum to get the two-halo term of the correlation function:

\[
\xi_{\text{two-halo}}^t(r|M) = \frac{\sin(kr)}{kr^2} W(k)P_{\text{h\rho}}(k).
\]

We consider that for the kSZ signal, the two-halo contribution comes from halos within the correlation length of the linear velocity field, \( r_{\text{corr}} \), which is approximately 50 Mpc. Therefore, we apply a window function \( W(k) = 1 \) for \( k > 1/r_{\text{corr}}, 0 \) elsewhere.

Figure 7 shows the fiducial two-halo term profiles that we calculate for the gas density and thermal pressure of an average CMASS halo. For our fits, we include a free parameter in front of those terms that scales the amplitude, so that our final models of density and pressure profiles are

\[
\rho(r) = \rho_{\text{one-halo}}(r) + A_{2h}\rho_{\text{two-halo}}(r),
\]

\[
P(r) = P_{\text{one-halo}}(r) + A_{2h}P_{\text{two-halo}}(r),
\]

where \( A_{2h} \) and \( A_{1h} \) are the free amplitude parameters for the density and pressure two-halo terms, respectively.
infrared/sub-mm. This contribution must be accounted for in the tSZ signal modeling. On the other hand, since the dust emission does not correlate with the velocities, it does not affect the kSZ measurements. We model both the frequency and spatial distribution of the dust emission as

\[ I(\nu, R) = A_{\text{dust}} \left( \frac{\nu (1 + z)}{\nu_0} \right)^{\beta_{\text{dust}} + 3} \left( \frac{e^{(h\nu_0/k_B T_{\text{dust}})} - 1}{e^{(h\nu_1/k_B T_{\text{dust}})} - 1} \right) \times (c_0 + c_1 R + c_2 R^2), \]  

where \( \nu_0 \) is the rest-frame frequency at which we normalize the dust emission, \( R \) is the radius of the aperture photometry filter, \( z \) is the redshift of the dust emitters, \( A_{\text{dust}} \) is the amplitude of the dust emission in [kJy/sr], \( \beta_{\text{dust}} \) is the dust spectral index, \( T_{\text{dust}} \) is the dust temperature in K, and \( c_0, c_1, \)

FIG. 8. Survey footprints, in equatorial coordinates, for the ACT + CMASS (blue) and overlapping Herschel (magenta) regions: three H-ATLAS/GAMA fields (circles), HerS (triangle), and HeLMS (star). We use the H-ATLAS/GAMA data only to estimate the dust emission (see text).

FIG. 9. CMASS stacked profiles from H-ATLAS/GAMA. For each of the three SPIRE frequency bands, we show the profiles in intensity units [kJy/sr] (left) and cumulative temperature [\( \mu \)K · arcmin] to match the units of the stacked SZ profiles. The small number density, 0.02 sources/arcmin\(^2\) may explain the small covariance among the apertures. We have also tested that the covariance effectively increases at even larger apertures.
$c_2$ are the polynomial coefficients parametrizing the radial profile. In order to model the dust in the ACT f090 and f150 bands, we include in our analysis data at larger frequencies where dust emission is dominant over the tSZ. We use Herschel data from one large extragalactic survey that overlaps with ACT and the Herschel Astrophysical TeraHertz Large Area Survey (H-ATLAS [45]) in the three fields GAMA-9, GAMA-12, and GAMA-15 (see Fig. 8). The H-ATLAS/GAMA survey mapped over 161 deg$^2$ of the sky in five photometric bands: 100 and 160 μm using the PACS instrument, and 250, 350, and 500 μm using the SPIRE instrument. In this area lie 8871 halos of the ACT + CMASS catalog. We use the maps released by the H-ATLAS team in the three SPIRE bands. We use the raw maps instead of the filtered, background-subtracted maps that are also released because in the latter the signal on scales larger than 3 arcmin has been removed to avoid the contribution from the Milky Way or other large-scale extragalactic emissions, while we are interested in scales up to 6 arcmin that are relevant for feedback effects. We apply the same aperture photometry and stacking technique used for measuring the tSZ and we obtain the profiles shown in Fig. 9. The results of the null test shown in Fig. 10 ensure that the measured signal is not a feature of the stacking technique, since stacking on random positions returns a profile consistent with zero on average. The probability to exceed the $\chi^2$ computed accounting for the covariance in each band is consistent with an average zero signal.
FIG. 11. Top: Constraints on the dust model (B1). Results obtained with the simultaneous fit to the GNFW pressure model using ACT and Herschel temperature measurements are shown in blue. Results from the fit of the dust model to Herschel data only are shown in orange. All parameters match within $1\sigma$. Middle: Profiles measured in the three Herschel/SPIRE frequency bands (black) in intensity units [kJy/sr]. The blue and orange curves show the best-fit models to Herschel + ACT and Hershel only data, respectively, and the corresponding bands show the $2\sigma$ (2nd–98th percentiles) of the distribution of the models obtained from the MCMC chains. Bottom: Profiles measured in the two ACT frequency bands (black) in cumulative temperature units of [$\mu K \cdot \text{arcmin}^2$]. The blue curves and $2\sigma$ bands show results obtained with the simultaneous fit of the dust and the GNFW pressure models using Herschel + ACT data. We separate the dust contribution (dot-dashed curves) from the thermal pressure (dashed curves). The best-fit model is the sum of the two contributions.
the CAP contributions on the photometric errors, HerS sources do not add significant signal and do not help increasing the S/N, when added to GAMA sources.

Figure 11 shows the fit results of the dust model [Eq. (B1)] to the Herschel data in orange, and the results of the simultaneous fit of the GNFW pressure model using ACT and Herschel data, in blue. The top panel shows the constraints on the parameters of the dust model obtained in the two cases; all match within 1σ. We assume flat priors for the dust amplitude and temperature parameters in the ranges: 0.05 < A_dust [KJy/σr] < 5, 10 < T_dust [K] < 40. For the emissivity index we assume a truncated Gaussian prior distribution centered on 1.2 and with standard deviation of 0.1, in the range 1 < β_dust < 2.5. These values are consistent with the model used by [87] to produce CIB-deprojected y maps and with the sky-average CIB spectral energy distribution obtained by Planck measurements of the CIB power spectra [114]. We also assume flat priors for the polynomial coefficients in the ranges: 0.1 < c_0 < 10, −10 < c_1 < 10, −10 < c_2 < 10.

The middle and bottom panels show the best-fit model over the data in our ACT and Herschel bands, and the 2σ bounds of the distribution of the models obtained from the MCMC chains. This analysis is justified by the need to correct our pressure model for dust contamination, which is relevant at 150 GHz (more than at 90 GHz) as shown in the bottom panel of Fig. 11. The dust model and the parameters inferred from it are entirely to marginalize over and mitigate the dust contamination in the tSZ signal. These parameters are degenerate with each other and we find consistent values for them throughout our analyses. We make no attempt to infer anything about the dust properties of the CMASS galaxies.
[52] https://github.com/samodeo/Mop-c-GT