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23

ABSTRACT

24 Tides in fluvial estuaries are distorted by non-stationary river discharge, which makes
25 the analysis of estuarine water levels less accurate when using the conventional tidal
26 analysis method. As a powerful and widely-used method for non-stationary and
27 nonlinear time series, the application of Variational Mode Decomposition (VMD)
28 method to non-stationary tides is nonexistent. This paper aims to illustrate and verify
29 the suitability of the VMD method as a new tidal analysis tool for river tides. The
30 efficiency of VMD is validated by the measurements from the Columbia River Estuary.
31 VMD strictly divides different tidal species into different modes, and thus avoids mode
32 mixing. Compared to VMD, Ensemble Empirical Mode Decomposition (EEMD),
33 which is another commonly-used method, fails to completely solve the problem of
34 mode mixing. The observed water levels at Longview station are decomposed into 12
35 modes via VMD. Based on the mean periods and amplitudes of each VMD mode, the
36 12 VMD modes sequentially correspond to the tidal species from the sub-tides (D_0),
37 diurnal tides (D_1), semi-diurnal tides (D_2), and up to D_{11} tides. The non-stationary
38 characteristics of tides influenced by river discharge are accurately captured by VMD
39 without mode mixing. The results also show that the EEMD and VMD modes can
40 capture the subtidal signals better than the nonstationary tidal harmonic analysis tool
41 (NS_TIDE). As a general method, the VMD mode can also be used for other research
42 purposes related to non-stationary tides, such as detiding.

43 **Keywords:** VMD; EEMD; NS_TIDE; river tides; tide-river interplay

44 **1. Introduction**

45 Tides are the periodic rise and fall of sea levels induced by the combined effects
46 of the gravitational forces of the Moon and the Sun acting on the orbiting and rotating
47 Earth (Amin, 1982). Tidal fluctuations including vertical and horizontal tides are the
48 basic movements of sea water. They are very important to human activities in the deep
49 sea and coastal areas such as navigation, energy utilization, oceanographic engineering
50 and aquaculture (Pan et al., 2017). The most widely used approach in tidal data analysis
51 is the Classical Harmonic Analysis (CHA), which assumes water levels can be
52 represented by a linear combination of sinusoidal terms (Foreman and Henry, 1989;
53 Pan et al., 2018b). These sinusoidal terms called tidal constituents are perfectly
54 stationary in the CHA. Namely, the amplitudes and phases of tidal constituents are
55 assumed constant. In most tidal observations, this stationary assumption is reasonable.
56 Thus, CHA has an excellent performance in explaining observed water levels (usually
57 over 90 percent of the variance) (Hoitink and Jay, 2016).

58 Tidal phenomena, such as internal tides, tides in tidal rivers and ice-covered bay
59 are highly non-stationary. For these tidal processes, the stationary assumption of CHA
60 is unsuitable. In such conditions, CHA performs badly in hindcasting and forecasting
61 water levels and only provides time-averaged values of time-varying tidal properties
62 (Jay and Flinchem, 1997; Pan et al., 2018a). To obtain the time-dependent tidal
63 amplitudes and phases, CHA can be conducted by adding a time window (Jay and
64 Flinchem, 1997; Guo et al., 2015), which becomes the short-term harmonic analysis

65 (STHA). Although the STHA method can extract the time-dependent tidal properties,
66 it can only separate a limited number of the main tidal constituents. Moreover, STHA
67 may provide inaccurate results when the variation of river discharge is strong (Jalón-
68 Rojas et al., 2018).

69 To acquire insights into underlying dynamics of highly non-stationary tidal signals,
70 Kukulka and Jay (2003a) proposed a framework in describing the decay of tides along
71 the estuary with the consideration of upstream river discharge. They also derived a
72 theory in modelling the sub-tidal water levels in their following work (Kukulka and Jay
73 2003b). Accordingly, Matte et al. (2013, 2014) developed the non-stationary harmonic
74 analysis tool (NS_TIDE) by directly embedding the frameworks of Kukulka and Jay
75 (2003a, b) into the CHA basis functions. Subsequently, Pan et al. (2018b) developed a
76 new version of NS_TIDE in which the contribution from coastal upwelling and
77 downwelling can be considered. NS_TIDE has been widely used to study the river-tide
78 dynamics in the fluvial estuaries, such as the Columbia River estuary (Matte et al., 2013;
79 Pan et al., 2018a, b; Gan et al., 2021), Yangtze River estuary (Gan et al., 2019; Chen et
80 al., 2020), St. Lawrence River estuary (Matte et al., 2014, 2018, 2019), and Pearl River
81 Delta (Cai et al., 2018; Zhang et al., 2018). Although NS_TIDE performs much better
82 than CHA in tidal rivers, it also has some limitations. First, synchronous river discharge
83 observations relative to water levels are needed to perform non-stationary harmonic
84 analysis using NS_TIDE. Second, based on the theoretical tide-river interaction model,
85 NS_TIDE cannot be applied to non-stationary tidal processes with other dynamic

86 mechanisms, *i.e.*, internal tides (Pan et al., 2018a, b).

87 Signal analysis tools, such as the Continuous Wavelet Transform (CWT) and
88 Complex Demodulation methods, are good supplements to study the non-stationary
89 tidal signals. Jay and Flinchem (1999) compared the model performance of the CWT,
90 STHA, and the modified STHA (mSTHA) methods. Their results show that the CWT
91 model can provide better results than the STHA and mSTHA methods once the time
92 window's length is longer than a few days. A system introduction about the application
93 of the CWT method in river tides is given in the study of Flinchem and Jay (2000).
94 Relative to the CWT method, the Complex Demodulation is more suitable to determine
95 the time variations of tidal signals in a particular frequency band (Jay and Kukulka,
96 2003). For instance, Jalón-Rojas et al. (2018) applied the Complex Demodulation
97 method to extract the time-dependent amplitudes and phase of semi-diurnal (D2) and
98 quarter-diurnal (D4) tides of the Gironde Estuary.

99 As a powerful and widely-used method for non-stationary and nonlinear time
100 series, Empirical Mode Decomposition (EMD, Huang et al., 1998) is another signal
101 analysis tool that has been widely used to analyze non-stationary tides in recent years
102 (Cheng et al., 2017; Devlin et al., 2020). Pan et al. (2018a, b) first applied the EMD
103 method to analyze river tides. EMD obtained the non-stationary characteristics of
104 diurnal and semi-diurnal tides related to river discharge successfully. By comparing the
105 results of NS_TIDE and EMD, it is found that the error in NS_TIDE hindcast mainly
106 comes from the less accurate sub-tidal water levels inversed by NS_TIDE (Pan et al.,

107 2018b). Though powerful, the EMD method is disturbed by a serious “mode mixing”
108 problem, which is defined as either a single mode of the EMD method including widely
109 disparate signals, or a similar signal residing in different modes of the EMD model
110 (Zhang et al., 2010). In terms of tidal levels, the mode mixing can be reflected in that
111 the energy of the same tidal species (a group of tidal constituents with similar
112 frequencies (Hoitink and Jay, 2016)) exist in more than one EMD mode. Therefore, the
113 EMD modes may need to be combined within a window of frequency to connect the
114 EMD modes to the physical processes (Ezer, 2019).

115 To solve this mode mixing problem, Wu and Huang (2009) proposed a noise-
116 assisted EMD method, namely Ensemble EMD (EEMD). Devlin et al. (2020) used the
117 EEMD method to analyze multi-timescale tidal variability in the Indian Ocean.
118 However, the mode mixing phenomenon still exists in the results of EEMD when
119 dealing with river tides (details displayed in section 4). Variational Mode
120 Decomposition (VMD), recently proposed by Dragomiretskiy and Zosso (2014), is an
121 alternative method to EMD. VMD is a generalization of the classic Wiener filter into
122 multiple, adaptive bands (Dragomiretskiy and Zosso, 2014). The VMD method obtains
123 each mode from the frequency domain, which enables the VMD model to be less
124 sensitive to noises and has the advantage of avoiding mode mixing. Therefore, the
125 VMD method has been widely applied to analyze the neuromuscular signal, audio
126 signal, and climate data (Zosso, 2021).

127 The main objective of this research is to apply the VMD method to the river tides

128 of the Columbia River Estuary where the river-tide interaction plays a dominant
129 influence on the water levels of tidal reaches. As the influence of seasonal wind on the
130 water levels of the Columbia River Estuary is insignificant (Jay et al., 2014), it is
131 ignored in this study. River tides are selected because they are the simplest non-
132 stationary tidal phenomenon and the only one for which both abundant observations
133 and detailed theoretical models exist (Jay and Flinchem, 1997, 1999). The results of the
134 VMD modes are further compared with the results of the NS_TIDE and EEMD models
135 to fully compare their advantages and disadvantages. Moreover, the application of the
136 VMD model in other physical processes related to river tides is also investigated.

137 This paper is structured as follows. The NS_TIDE, EEMD and VMD methods are
138 described in section 2. The study area and data are shown in section 3. The results of
139 NS_TIDE, EEMD and VMD are displayed and discussed in section 4 and section 5,
140 respectively. Conclusions are presented in section 6.

141

142 **2. Methodology**

143 **2.1 Non-stationary Harmonic Analysis Model (NS_TIDE)**

144 In the CHA model, observed water levels can be expressed as (Pawlowicz et al.,
145 2002):

$$H(t) = Z + \sum_{i=1}^N (a_i \cos \sigma_i + b_i \sin \sigma_i) \quad (1)$$

146 where $H(t)$ is the observed estuarine water level at time t ; Z is the mean water level

147 (MWL); i is the index of tidal constituents and N is the total number of tidal
 148 constituents to be resolved; σ_i is the frequency of the i^{th} tidal constituent.

149 In the NS_TIDE model, time-invariant Z , a_i and b_i in **Eq. (1)** are replaced by
 150 the nonlinear functions of time-changing river discharge Q and greater diurnal tidal
 151 range R in the semi-diurnal tidal regime of a reference station near the estuary mouth:

$$H(t) = Z(Q, R) + \sum_{i=1}^N (a_i(Q, R)\cos\sigma_i + b_i(Q, R)\sin\sigma_i) \quad (2)$$

$$Z(Q, R) = c_0 + c_1 Q^{p_z} + c_2 \frac{R^{q_z}}{Q^{r_z}} \quad (3)$$

$$a_i(Q, R) = d_0 + d_1 Q^{p_f} + d_2 \frac{R^{q_f}}{Q^{r_f}} \quad (4)$$

$$b_i(Q, R) = e_0 + e_1 Q^{p_f} + e_2 \frac{R^{q_f}}{Q^{r_f}} \quad (5)$$

152 where (p_z, q_z, r_z) and (p_f, q_f, r_f) are the unknown exponents to be iteratively
 153 determined; c_h , d_h , and e_h ($h = [0, 2]$) are the unknown coefficients to be solved.

154 The first and second terms on the right-hand sided of **Eq. (2)** are respectively the “stage”
 155 and the “tidal-fluvial” models in NS_TIDE, which are adapted from the works of
 156 Kukulka and Jay (2003a, b). The stage model describes the sub-tidal water levels
 157 (oscillations with periods obviously greater than 1 day), while the “tidal-fluvial” model
 158 explains the diurnal, semi-diurnal and higher frequency tidal constituents.

159 $d_1 Q^{p_f} (e_1 Q^{p_f})$ is the river discharge term representing the nonlinear decay effect of
 160 river discharge on tides. The coefficient $d_1 (e_1)$ is often negative, indicating tidal
 161 amplitudes decrease when the river discharge increases. $\frac{R^{q_f}}{Q^{r_f}}$ is the tidal range term
 162 which represents the nonlinear tidal-river interplay induced by neap-spring variability.

163 When river discharge is large, the changes of tidal properties induced by the tidal range
164 term become less important. With Q , R and $H(t)$ known, **Eq. (2)** can be solved
165 using a least squares fitting method. In the NS_TIDE model, the iteratively reweighted
166 least squares (IRLS) is used to improve the overall fitting (Leffler and Jay, 2009).

167

168 **2.2 Ensemble Empirical Mode Decomposition (EEMD)**

169 The EMD method is developed by Huang et al. (1998). As an adaptive and
170 recursive signal decomposition algorithm designed for nonlinear and non-stationary
171 signals, EMD is widely used to analyze numerous kinds of geophysical data, such as
172 sea levels (Ezer, 2013; Cheng et al., 2016; Ezer et al., 2016), sea surface temperature
173 (Wu et al., 2008) and land surface air temperature (Ji et al., 2014). Via the EMD method,
174 a complicated non-stationary time series can be decomposed into a finite number of
175 components, which are usually called intrinsic mode functions (IMFs). Those IMFs are
176 not restricted to a narrow band signal, and their amplitudes, phases and frequencies are
177 all time-variant. A time series of water level observations can be decomposed using the
178 EMD method in the following form:

$$H(t) = \sum_{m=1}^M c_m(t) + r(t) \quad (6)$$

179 where m is the index of IMFs; M is the total number of IMFs which contain periodic
180 signals; $c_m(t)$ is the m^{th} IMF; $r(t)$ is the last IMF representing the trend term of
181 the observations. In total, there are $M + 1$ IMFs, which are related to the factors such

182 as the variation of the observations, the length of the record, as well as the stoppage
183 criteria of the sifting process (Pan et al., 2018a). The trend term $r(t)$ obtained by the
184 EMD method is often monotonic. Therefore, it does not contain any oscillation of a
185 fixed period.

186 The main processes of the EEMD method are described as follows (Wu et al.,
187 2008):

188 Step 1: Generate a white noise series and add it to the targeted signal. Decompose the
189 noise-added signal into a specified number of IMFs via the EMD method.

190 Step 2: Repeat step 1 a specified number of times. Note that the added white noise series
191 are distinct each time.

192 Step 3: Average the corresponding IMFs as the final results of EEMD.

193 The effects of the EEMD decomposition are that the added white noise time series
194 cancel each other once they are summed up. The mean IMFs of EEMD preserve the
195 good properties of the EMD method, while the strength of mode mixing in EEMD
196 obviously decreases relative to the EMD model (Wu et al., 2008).

197

198 **2.3 Variational Mode Decomposition (VMD)**

199 The VMD method generally treats the problem of mode decomposition as an
200 optimization problem by decomposing 1-dimensional input signal into a specified
201 number of modes. The signal gets fully reproduced by summing up the K number of
202 decomposition modes

$$H(t) = \sum_{k=1}^K u_k(t) \quad (7)$$

203 where k is the index of modes; K is the total number of modes; $u_k(t)$ is the k^{th}
 204 mode and it is an amplitude-modulated-frequency-modulated signal, which can be
 205 expressed as:

$$u_k(t) = A_k(t)\cos(\varphi_k(t)) \quad (8)$$

206 where $A_k(t)$ and $\varphi_k(t)$ are the time-dependent envelope and the phase of the k^{th}
 207 mode, respectively. The related instantaneous frequency $\omega_k(t)$ of the k^{th} mode is
 208 assumed to vary slowly relative to the phase and is nonnegative. It can be calculated as:

$$\omega_k(t) = \frac{\partial \varphi_k(t)}{\partial t} \quad (9)$$

209 The decomposition process of the time series by the VMD method can be
 210 expressed as a constrained variational problem (Dragomiretskiy and Zosso, 2014)
 211 whose objective function is:

$$\begin{aligned} \min_{\{u_k\}, \{\bar{\omega}_k\}} & \left\{ \sum_{k=1}^K \left\| \partial_t \left[\left(\delta(t) + \frac{j}{\pi t} \right) * u_k(t) \right] e^{-j\bar{\omega}_k t} \right\|_2^2 \right\} \\ \text{s.t.} & \sum_{k=1}^K u_k(t) = H(t) \end{aligned} \quad (10)$$

212 where $\{u_k\} = \{u_1, \dots, u_K\}$ and $\{\bar{\omega}_k\} = \{\bar{\omega}_1, \dots, \bar{\omega}_K\}$ are the sets of all modes and
 213 their related center frequencies; $\delta(t)$ is the Dirac function; $*$ represents the
 214 convolution; $j = \sqrt{-1}$.

215 Dragomiretskiy and Zosso (2014) used a quadratic penalty term and Lagrangian
 216 multiplier to transform **Eq. (10)** to an unconstrained optimization problem:

$$L(\{u_k\}, \{\bar{\omega}_k\}, \lambda) = \alpha \sum_{k=1}^K \left\| \partial_t \left[\left(\delta(t) + \frac{j}{\pi t} \right) * u_k(t) \right] e^{-j\bar{\omega}_k t} \right\|_2^2 + \left\| H(t) - \sum_{k=1}^K u_k(t) \right\|_2^2 + \left\langle \lambda(t), H(t) - \sum_{k=1}^K u_k(t) \right\rangle \quad (11)$$

217 where α is the regularization parameter representing the variance of the white noise;
 218 $\lambda(t)$ is the Lagrangian multiplier.

219 The solution of **Eq. (11)** is by using the alternate direction method of multipliers
 220 (ADMM) method. Only the final expressions of the ADMM method are summarized in
 221 this study. For more details, the reader can refer to Dragomiretskiy and Zosso (2014).
 222 The solution of each mode in the frequency domain can be expressed as:

$$\hat{u}_k^{n+1}(\omega) = \frac{\hat{H}(\omega) - \sum_{i < k} \hat{u}_i^{n+1}(\omega) + \sum_{i > k} \hat{u}_i^n(\omega) + \frac{\hat{\lambda}^n(\omega)}{2}}{1 - 2\alpha(\omega - \bar{\omega}_k)} \quad (12)$$

223 where $\hat{u}_k(\omega)$, $\hat{H}_k(\omega)$, and $\hat{\lambda}_k(\omega)$ denote the spectrum of $u_k(t)$, $H(t)$, and $\lambda(t)$,
 224 respectively; The superscript $n + 1$ and n denote the results of the current and
 225 previous steps of the iteration process, respectively.

226 During each update of $\hat{u}_k^{n+1}(\omega)$, the corresponding center frequency $\bar{\omega}_k^{n+1}$ is
 227 subsequently updated as the center-of-gravity of the power spectrum of each mode:

$$\bar{\omega}_k^{n+1} = \frac{\int_0^{\infty} \omega |\hat{u}_k^{n+1}(\omega)|^2 d\omega}{\int_0^{\infty} |\hat{u}_k^{n+1}(\omega)|^2 d\omega} \quad (13)$$

228 Once all the $\hat{u}_k^{n+1}(\omega)$ and $\bar{\omega}_k^{n+1}$ are obtained, the $\hat{\lambda}_k^{n+1}(\omega)$ is updated as:

$$\hat{\lambda}_k^{n+1}(\omega) = \hat{\lambda}_k^n(\omega) + \tau \left(\hat{H}(\omega) - \sum_{k=1}^K \hat{u}_k^{n+1}(\omega) \right) \quad (14)$$

229 where τ is user-defined coefficient for dual ascent to enforce the exact signal
 230 reconstruction (Ni et al., 2018).

231 The convergence state of the model iteration process is defined as:

$$\sum_{k=1}^K \frac{\|\hat{u}_k^{n+1}(\omega) - \hat{u}_k^n(\omega)\|_2^2}{\|\hat{u}_k^n(\omega)\|_2^2} < \varepsilon \quad (15)$$

232 where ε is the user-defined coefficient for the judgement of model convergence. When
 233 the VMD modes in the frequency domain reach the convergence state, their results in
 234 the time domain can be obtained by the inverse of Fourier transform:

$$u_k(t) = R\{ift(\hat{u}_k(\omega))\} \quad (16)$$

235 where $R\{\}$ represents the real part; ift represents the inverse of Fourier transform.

236

237 2.4 Flowchart

238 A flowchart is given in **Fig. 1** for a better illustration of the roadmap of this
 239 research. The water level measurements at Longview station are analyzed by NS_TIDE,
 240 EEMD and VMD models, respectively. The NS_TIDE model is used to extract the
 241 time-dependent amplitudes and phases of tidal constituents to describe the influence of
 242 external force (river discharge) on tidal constituents. Moreover, the sub-tidal water
 243 levels (D0 tidal frequency band) modelled by the NS_TIDE model are compared with
 244 the sub-tidal water levels extracted from the EEMD and the VMD models. In
 245 comparison with the NS_TIDE model, the attention of the EEMD and VMD model
 246 results is on tidal species rather than specific tidal constituents. When the tidal signals

247 in different tidal frequency bands, such as D1 and D2 tides, are filtered by the EEMD
248 and VMD models, Fourier analysis is conducted on these tidal signals within different
249 frequency band to compare whether there exists mode mixing in the results of the VMD
250 model.

251 **3. Study area and data**

252 The Columbia River (**Fig. 2**) has a watershed of $\sim 660500 \text{ km}^2$ and an annual
253 average flow of $\sim 7500 \text{ m}^3/\text{s}$ (Jay and Flinchem, 1997). The Willamette River, which is
254 the largest tributary of the Columbia River, enters the river main stem at Portland, ~ 160
255 river kilometer (rkm) from the ocean, with an annual average flow of $\sim 950 \text{ m}^3/\text{s}$ (Matte
256 et al., 2013; Pan and Lv, 2019). As the third largest river in the United States, the
257 Columbia River is important and essential for local fisheries industry, hydropower,
258 ocean transport and other economic sectors. The tides in the Columbia River estuary
259 (CRE) are diurnal (D_1) and semi-diurnal (D_2) mixed with a D_2/D_1 ratio of ~ 1.8 at the
260 CRE mouth (Jay et al., 2011; Moftakhari et al., 2016; Pan et al., 2018a, b). The diurnal
261 tidal range at Astoria (**Fig. 2**, rkm 29) varies from ~ 1.59 to 3.83 m . As tides propagate
262 landward, tidal range gradually decreases and becomes nearly zero at Bonneville dam
263 at rkm 234 (Jay et al., 2011; Jay et al., 2014). Hourly water level records (**Fig. 3a**) for
264 a year period (January 2003 - December 2003) from Astoria (rkm 29) and Longview
265 (rkm 107) stations (**Fig. 2**) provided by the National Oceanic and Atmospheric
266 Administration (NOAA) are analyzed in this research. Additional river discharge data
267 (**Fig. 3b**) for the Willamette River and the main stem of the Columbia River (at

268 Bonneville Dam) are provided by the U.S. Geological Survey (USGS).

269 The skewness coefficient referred to the work of Nidziko (2011) is used to
270 evaluate the tide characteristics of the CRE. The skewness coefficient of the time
271 derivative of the tide levels at Astoria (29 rkm) is close to zero, indicating the symmetric
272 tide. This means the tides at Astoria are nearly stationary and are only under an
273 ignorable influence of upstream river discharge (**Fig. 3a**). At Astoria, the hindcast of
274 CHA (Pawlowicz et al., 2002) explains 97.5% of the observed signal variance, with a
275 root-mean-square error (RMSE) of 0.13 m and a maximum absolute error (MAE) of
276 0.61 m for tidal heights. The largest tidal constituent is M_2 tide, followed by K_1 tide
277 with amplitudes of 0.94 and 0.44 m, respectively. The amplitudes of overtide and
278 compound constituents (less than 0.04 m) are much smaller than those of major diurnal
279 and semi-diurnal constituents.

280 The skewness coefficient of the time derivative of the tide levels at Longview
281 station significantly increases to 0.83, indicating an asymmetric tide (Nidziko, 2011).
282 More specifically, the rising tide duration is shorter than the falling tide duration at
283 Longview station. In comparison with Astoria, the tides at Longview station are
284 significantly distorted and damped by river discharge (**Fig. 3a**). The CHA hindcast only
285 explains 80.0% of the signal variance and has an RMSE of 0.24 m and an MAE of 1.80
286 m. This unsatisfactory result indicates that CHA is unable to describe the nonlinear
287 process of tidal-fluvial interplay. The amplitudes of M_2 and K_1 tides at Longview
288 decrease to 0.43 and 0.20 m, respectively. The amplitudes of shallow water constituents

289 obtained from the CHA method have an obvious increase especially the M_{sf} and M₄
290 tides (**Table 1**) due to the nonlinear interaction between tides and river discharge. Other
291 high-frequency constituents such as the M₆ and M₈ tides are still very weak though their
292 amplitudes have increased.

293 **4. Results**

294 **4.1 The results of NS_TIDE**

295 Astoria is selected as the reference station in the NS_TIDE model for providing
296 the ocean tidal range forcing. The parameter η for the modified Rayleigh criterion
297 (Matte et al., 2013) in NS_TIDE is set to 0.20 (see **Table 2**, 26 tidal constituents are
298 resolved). It should be noted that the long-period tidal constituents, such as M_f (13.66
299 days), M_{sf} (14.77 days), M_m (27.55 days), S_{sa} (182.59 days), and S_a (365.18 days)
300 tides are indirectly contained in the variations of the sub-tidal water levels (**Eq. (3)**) and
301 do not be extracted separately to avoid overfitting. The hindcast of the NS_TIDE model
302 is performed with tidal constituents whose time-averaged signal-to-noise ratios (SNRs)
303 larger than two.

304 Results obtained by NS_TIDE are obviously improved compared to CHA at
305 Longview: the NS_TIDE hindcast explains 94.48% of the signal variance and has an
306 RMSE of 0.13 m and an MAE of 0.81 m. The hindcast obtained by NS_TIDE shows a
307 high consistency with the water level observations at most periods. The correlation
308 coefficient between the model results and the measurements is 0.97. However, the
309 difference between the model results and the measurements is more significant during

310 high-flow events (**Fig. 4b**). As shown in **Fig. 3b**, there is a sudden rise in river discharge
311 in early February 2003 which is caused by flow regulation. This transient high-flow
312 event sharply increases the water levels and depresses the tides at Longview (**Fig. 4a**).
313 The offset between NS_TIDE hindcast and observations (blue dashed box in **Fig. 4a**
314 and **Fig. 4b**) indicates that NS_TIDE successfully reproduces the tidal variations but
315 fails to accurately reconstruct sub-tidal variations during high-flow events.

316 **Fig. 5** displays the time-dependent K_1 and M_2 tidal heights extracted by NS_TIDE.
317 Both K_1 and M_2 tides oscillate following the non-stationary external forcing. The mean
318 amplitudes of the time-dependent K_1 and M_2 tidal constituents at Longview from the
319 NS_TIDE model are 0.19 and 0.45 m, respectively. The amplitudes of the K_1 and M_2
320 tidal constituents are significantly reduced during the high-flow event in early February
321 2003 (blue box in **Fig. 5b**). Furthermore, both K_1 and M_2 tides have clear neap-spring
322 oscillations related to semimonthly changing bottom friction.

323 4.2 The results of EEMD

324 Water level records at Longview are decomposed into 13 IMFs via EEMD (**Fig.**
325 **6**). **Table 3** shows that the mean periods of the most EEMD modes nearly double those
326 of their previous one, indicating that EEMD is a dyadic filter (Wu and Huang, 2004;
327 Flandrin et al., 2004). The mean period and mean amplitude of IMF1 are 4.20 h and
328 0.04 m, respectively, which indicates that IMF1 mainly consists of high-frequency
329 shallow water constituents. The mean period and mean amplitude of IMF2 are 12.44 h
330 and 0.43 m, respectively, which are nearly the same as the period and amplitude of M_2

331 tidal constituent (12.42 h and 0.43 m). This indicates that IMF2 is dominated by M₂
332 tide. The mean period and mean amplitude of IMF3 are 23.57 h and 0.18 m, respectively,
333 very close to the period and amplitude of K₁ tide (23.93 h and 0.20 m), which indicates
334 that IMF3 may be dominated by K₁ tide. For the rest EEMD modes, their mean periods
335 are significantly larger than 1 day. Therefore, they represent sub-tidal oscillations with
336 different time scales. IMF6 (mean period 9.87 days) may correspond to Mt tide (9.12
337 days) and Mst tide (9.56 days). IMF10 may correspond to the solar annual tide Sa since
338 its mean period is very close to one year. Note that the mean amplitudes IMF11 and
339 IMF12 are nearly zero, while IMF13 is monotonous and does not have any peaks. The
340 sum of IMFs 11-13 may represent the long-term trends that are not resolved in this
341 study because of the length of the data. The sum of IMFs except for the first three can
342 be regarded as sub-tidal water levels (green line in **Fig. 7**). It is obvious that the sub-
343 tidal water levels obtained by EEMD are more accurate than those obtained by
344 NS_TIDE, especially during high-flow events (**Fig. 7**).

345 To show the mode mixing phenomenon in the EEMD method, spectral analysis is
346 conducted on the IMFs of the EEMD model. It can be seen from **Table 3** that the IMFs
347 from the 4th to the 13th contain the tidal signals with frequency smaller than diurnal tides
348 (D₁), which means those IMFs are from the same tidal species (*i.e.*, subtidal tides, D₀)
349 but with different periods. Therefore, spectral analysis is only applied to the IMF1,
350 IMF2, and IMF3 of the EEMD model to compare their energy distribution with
351 different frequency bands. It can be seen from **Fig. 8a** that Quarter-diurnal (D₄) tides

352 are the strongest in IMF1, but the amplitudes of semi-diurnal (D_2) tides, terdiurnal (D_3),
353 and penta-diurnal (D_5) tides are also noticeable. The IMF2 (**Fig. 8b**) is dominated by
354 D_2 tides, while the amplitudes of D_1 , D_3 and D_4 tides are relatively smaller. The IMF 3
355 (**Fig. 8c**) is dominated by D_1 tides but includes a small part of the energy of D_2 tides.
356 **Fig. 8** indicates that D_2 tides are split into three modes (IMF1, IMF2 and IMF3), while
357 D_1 tides are split into two modes (IMF2 and IMF3). D_3 and D_4 tides are divided into
358 two modes (IMF1 and IMF2). Since these EEMD modes still contain oscillations of
359 dramatically distinct time scales, the problem of mode mixing is not completely solved.

360 Similarly, spectral analysis is performed on the IMF1 and IMF2 obtained by EMD
361 as they contain the tidal signal with frequencies equal to or higher than diurnal tides. It
362 is clear from **Fig. 9** that IMF1 and IMF2 are dominated by D_2 and D_1 tides, respectively.
363 As displayed in **Fig. 9a**, EMD fails to separate D_3 , D_4 and D_5 tides from D_2 tides.
364 Compared to EMD, EEMD (**Fig. 8a** and **Fig. 8b**) partly separates D_3 , D_4 and D_5 tides
365 from D_2 tides. However, this separation is not perfect and complete, and thus the
366 problem of mode mixing still exists.

367

368 4.3 The results of VMD

369 The VMD model coefficients of α , τ and ε are specified as 2000, 0, and 10^{-7}
370 which are referred to Dragomiretskiy and Zosso (2014). Water levels at Longview are
371 decomposed into 12 modes through VMD (**Fig. 10**). **Table 4** lists the mean periods and
372 amplitudes of VMD modes. The VMD mode 1 represents the sub-tidal oscillations

373 (mean period 4.74 days). As shown in **Fig. 7**, the sub-tidal water levels obtained by
374 EEMD and VMD are highly consistent with each other. The mean period and mean
375 amplitude of VMD mode 2 are 23.95 h and 0.21 m, respectively, which indicates that
376 mode 2 is dominated by K_1 tide. The mean period and mean amplitude of VMD mode
377 3 are 12.44 h and 0.45 m, respectively, which indicates that mode 3 is dominated by M_2
378 tide. For the rest of VMD modes, based on their mean periods and amplitudes, they
379 correspond to D_3 , D_4 , D_5 , D_6 , D_7 , D_8 , D_9 , D_{10} , and D_{11} tides, respectively. It should be
380 noted that the mean amplitudes of modes 8-12 are less than 0.01 m, which means that
381 they are relatively insignificant to the total water level variations.

382 **Fig. 11** shows the Fourier spectrum maps of modes 2-9 obtained by VMD to
383 compare the energy distribution of the modes with frequencies between D_1 to D_8 tides.
384 Mode 2 only contains D_1 tides, while mode 3 only contains D_2 tides. Modes 4-9 only
385 have $D_3 - D_8$ tides, respectively. Comparing **Fig. 11** to **Fig. 8**, it is clear that the
386 oscillations with different time scales are strictly divided into different VMD modes
387 and no mode mixing exists. All tidal species are perfectly separated from each other,
388 which can be illustrated by **Eq. (13)**. The center frequencies of each VMD mode are
389 respectively estimated based on the center-of-gravity of each mode's power spectrum
390 and they will be allocated to different tidal species. Estimating each VMD mode
391 through the frequency domain enables the VMD method to be less sensitive to noises
392 and have the advantage of avoiding mode mixing.

393 The upper envelope of mode 3 and mode 4 in **Fig. 10** can be regarded as D_2 and

394 D_3 amplitudes, respectively (**Fig. 12**). Both D_2 and D_3 amplitudes show clear
395 semimonthly cycles related to neap-spring variations in bottom friction. These
396 semimonthly cycles in tidal amplitudes are larger when the river discharge decreases,
397 which is consistent with the theory of **Eq. (4)** and **Eq. (5)**. D_2 amplitude is negatively
398 correlated to the river discharge. For example, when the total river discharge of
399 Columbia River and Willamette River peaked in early February 2003 (**Fig. 12b**), the
400 D_2 amplitude reached the minimum at the same time (blue dashed line in **Fig. 12a**).
401 However, **Fig. 12c** shows that the D_3 amplitude did not reach the lowest value when the
402 river discharge peaked in early February 2003. This indicates that the response of D_3
403 tides to river discharge is distinct from D_2 tides. D_2 tides are astronomical, while D_3
404 tides are nearly non-astronomical and mainly generated from the nonlinear interaction
405 between D_1 and D_2 tides. For example, the largest tidal constituent in D_3 tides at
406 Longview is MK_3 which is originated from the nonlinear interaction between K_1 and
407 M_2 tides. For these shallow water tidal constituents, the effect of river discharge is dual.
408 First, river discharge enhances the nonlinear interaction between major tides and
409 transfers the energy from D_1 and D_2 tides to shallow water constituents. Second, river
410 discharge plays a frictional effect on tides and thereby impedes the propagation of tides.
411 The increment of river discharge can enhance the energy transfer from D_1 and D_2 tides
412 to D_3 tides but also play a stronger frictional effect on D_3 tides. The dual effects of river
413 discharge on tides are also reported in previous studies (Guo et al., 2015; Guo et al.,
414 2020). Therefore, the response curve of D_3 amplitudes to river discharge should be non-

415 monotonic and may exist a threshold value. In general, the VMD method captured the
416 non-stationary feature of tides successfully.

417

418 **5. Discussions**

419 **5.1 Detiding river discharge data**

420 In section 4, the performance of VMD on processing estuarine water levels is
421 shown. In fact, in tidal rivers, not only water levels but also river discharge observations
422 are modulated by tides. Such tidal modulations are complicated and present strong non-
423 stationarity. Removing the non-stationary tidal influence from observations is usually
424 called as “detiding” (Hoitink and Jay, 2016). Detiding is a general challenge but a
425 fundamental task. Accurate removal of tidal discharge from observed discharge time
426 series is necessary and vital for numerous proposes, such as climate analyses,
427 freshwater resources management, and coastal ecosystem research (Moftakhari et al.,
428 2013, 2016).

429 **Fig. 13a** displays the observed hourly river discharge (provided by USGS) for a
430 year (October 2007 - October 2008) at Portland, Oregon (**Fig. 2**). Positive discharge
431 values mean that flow propagates seaward, while negative discharge values mean that
432 flow propagates landward. It can be seen from **Fig. 13a** that the flow direction of the
433 observed discharge changes with time. When freshwater discharge is large, tidal
434 discharge is negligible. However, when freshwater discharge becomes weak, tidal
435 discharge becomes significant. To obtain freshwater discharge, the VMD method is

436 used on the river discharge measurements (**Fig. 13a**). **Fig. 13b** shows the freshwater
437 discharge extracted by VMD (red line). VMD accurately removes the non-stationary
438 tidal discharge and obtains reliable freshwater discharge. The Fourier spectrum maps
439 of the related VMD modes 2-9 are displayed in **Fig. 14**. The D_1 to D_8 tides are perfectly
440 divided into different VMD modes, while the energy from freshwater discharge is fully
441 extracted out.

442 The same detiding works are conducted again by EEMD for further comparison.
443 The Fourier spectrum maps of EEMD IMFs 1-4 are displayed in **Fig. 15**. The D_4 tide
444 energy appears in IMF1 and IMF2, while D_2 tide energy resides in IMF2 and IMF3.
445 The D_1 tides majorly exist in IMF4 but partly arises in IMF2. **Fig. 15** clearly shows that
446 the mode mixing phenomenon also exists when the EEMD method is used to
447 decompose the time series of river discharge influenced by tides. Compared to EEMD,
448 it is clear from **Fig. 14** that VMD is more suitable to remove tidal discharge and analyze
449 the multi-time scale tidal variability in discharge time series.

450 **5.2 Advantages and Disadvantages of NS_TIDE, EEMD and VMD**

451 Compared to NS_TIDE which is specially designed for water levels in tidal rivers,
452 both EEMD and VMD are general methods for all kinds of non-stationary and nonlinear
453 time series. In section 5.1, the application of the VMD method to separate freshwater
454 discharge from observed river discharge containing tidal discharge is demonstrated. In
455 fact, not only discharge, water temperature, turbidity, suspended sediment
456 concentration and other parameters in fluvial estuaries are all influenced by tide-river

457 interaction. These parameters can also be analyzed by VMD. In this paper, river tides
458 are used as an instance to illustrate the application of VMD. However, it is fully
459 expected that VMD is also suitable for other non-stationary tides, while NS_TIDE is
460 not suitable. Furthermore, by comparing the results of VMD and NS_TIDE, this study
461 points out again that NS_TIDE cannot accurately reproduce sub-tidal water levels
462 during high-flow events. Gan et al. (2019) proposed a modified NS_TIDE model which
463 replaced the stage model with the frequency-expanded tidal-fluvial model. Although
464 the hindcast of the modified NS_TIDE has been obviously improved compared to the
465 original NS_TIDE model, the accuracy of the predicted water levels obtained by the
466 modified NS_TIDE is virtually reduced due to overfitting.

467 Compared to EMD, although the results of EEMD are improved and the problem
468 of mode mixing is partly solved to some extent, there is still room for further
469 improvement. In comparison with EEMD, VMD perfectly eliminates mode mixing and
470 each mode only contains oscillations with similar frequencies. When applied to
471 estuarine tide levels, each VMD mode has a physical meaning and is related to tidal
472 species. The non-stationary features captured by the VMD model are generally
473 consistent with the theory of tide-river interplay.

474 Although powerful and useful, VMD also has potential limitations. VMD can only
475 separate different tidal species from each other and cannot extract specific tidal
476 constituents such as the M_2 , S_2 , K_1 and O_1 tidal constituents. This is actually the
477 common limitations of signal analysis tools because they need to make a tradeoff

478 between the resolutions in time domain and frequency domain. All signal analysis
479 methods follow the Heisenberg Principle (Flinchem and Jay, 2000). With the increase
480 of the resolution in the time domain, their resolution in the frequency domain should
481 decline. M_2 and S_2 tidal constituents belong to D_2 tides due to their close frequency.
482 They are divided into the same VMD mode (Mode 3 in **Fig. 10**). However, they can not
483 be further separated because of the resolution limitation of the VMD model in the
484 frequency domain. Relative to the signal analysis methods such as the VMD and EEMD
485 models, NS_TIDE may be the only tool to extract specific tidal constituents but also
486 keep the time-dependent tide properties. In other words, the NS_TIDE model has the
487 finest resolution in the frequency domain.

488

489 **6. Conclusions**

490 The VMD method has been widely used to analyze various signals, but to our
491 knowledge, the application of VMD to non-stationary tides is nonexistent. Application
492 of the VMD method to analyze river tides is a new idea that is verified in this research
493 for the first time. VMD strictly divides different tidal species into different modes, and
494 thus avoids mode mixing. The non-stationary characteristics of tides induced by tide-
495 river interaction are captured accurately. The sub-tidal water levels obtained by VMD
496 are highly consistent with those obtained by EEMD and more accurate than those
497 obtained by NS_TIDE. As the first effort to adopt the VMD method to separate tidal
498 discharge from freshwater discharge, it is found in this study that VMD is superior to

499 EEMD when dealing with non-stationary tidal time series.

500 Both VMD and NS_TIDE are useful non-stationary signal analysis tools. The
501 biggest advantage of NS_TIDE over the VMD method is the capacity to resolve specific
502 tidal constituents. Compared to NS_TIDE, a great advantage of the VMD is that it is a
503 general method and can be applied to analyze non-stationary tidal time series with
504 dynamic mechanisms unclear. The combination of VMD and NS_TIDE can help us
505 know more about water level dynamics in tidal rivers, and thus better protecting people
506 who live nearby the river. It is expected that the VMD method can prove its value in
507 future studies of the non-stationary and nonlinear processes like internal tides or tidal
508 influence on the environment.

509

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526

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529

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Tables:

530 Table 1. Tidal constituents at Longview (rkm 107) with amplitudes greater than 0.05
 531 m and signal-to-noise ratios (SNRs) greater than two (extracted from the data of 2003
 532 by the CHA method).

Tidal Constituent	Amplitude (m)	Phase (deg)	Signal-to-noise ratio (SNR)
Sa	0.38	257.22	21
Ssa	0.13	302.57	3.3
Msf	0.17	312.29	5.7
O ₁	0.10	347.25	410
P ₁	0.05	274.76	160
K ₁	0.20	265.75	1800
N ₂	0.08	225.39	98
M ₂	0.43	331.31	3200
S ₂	0.10	284.68	150
K ₂	0.05	86.67	44
MO ₃	0.05	231.23	80
MK ₃	0.07	156.76	89
M ₄	0.08	230.00	300

533
 534

535 Table 2. Selected 26 tidal constituents in the NS_TIDE model for the water levels at
 536 Longview in 2003.

Tidal species	Tidal constituents
D ₁	ALP ₁ , SIG ₁ , Q ₁ , O ₁ , NO ₁ , K ₁ , J ₁ , SO ₁ , UPS ₁
D ₂	EPS ₂ , N ₂ , M ₂ , S ₂
D ₃	MO ₃ , MK ₃ , SK ₃
D ₄	MN ₄ , M ₄ , MS ₄ , SK ₄
D ₅	2MK ₅
D ₆	2MN ₆ , M ₆ , 2MS ₆
D ₇	3MK ₇
D ₈	M ₈

537

538 Table 3. Mean amplitudes and periods of EEMD modes at Longview station for the

539 water levels of 2003

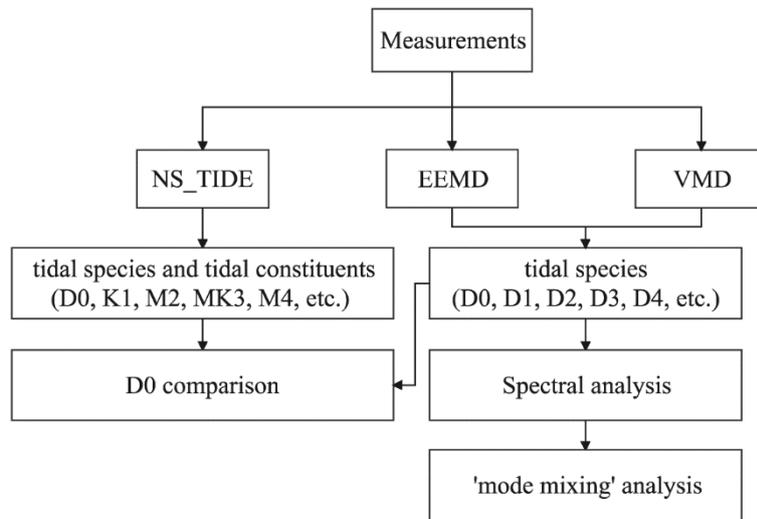
Mode	Number of peaks	Mean period (day)	Mean amplitude (m)
1	2089	0.18	0.04
2	705	0.52	0.43
3	372	0.98	0.18
4	223	1.64	0.03
5	89	4.10	0.05
6	37	9.87	0.11
7	20	18.26	0.08
8	8	45.66	0.13
9	4	91.32	0.08
10	1	365.30	0.23
11	1	365.30	0.00
12	1	365.30	0.00
13	-	-	-

540 Table 4. Mean amplitudes and periods of VMD modes at Longview station for the

541 water levels of 2003

Mode	Number of peaks	Mean period (day)	Mean amplitude (m)
1	77	4.74	1.69
2	366	1.00	0.21
3	705	0.52	0.45
4	1072	0.34	0.09
5	1411	0.26	0.10
6	1762	0.21	0.03
7	2122	0.17	0.01
8	2479	0.15	0.008
9	2830	0.13	0.007
10	3194	0.11	0.005
11	3622	0.10	0.002
12	4142	0.09	0.002

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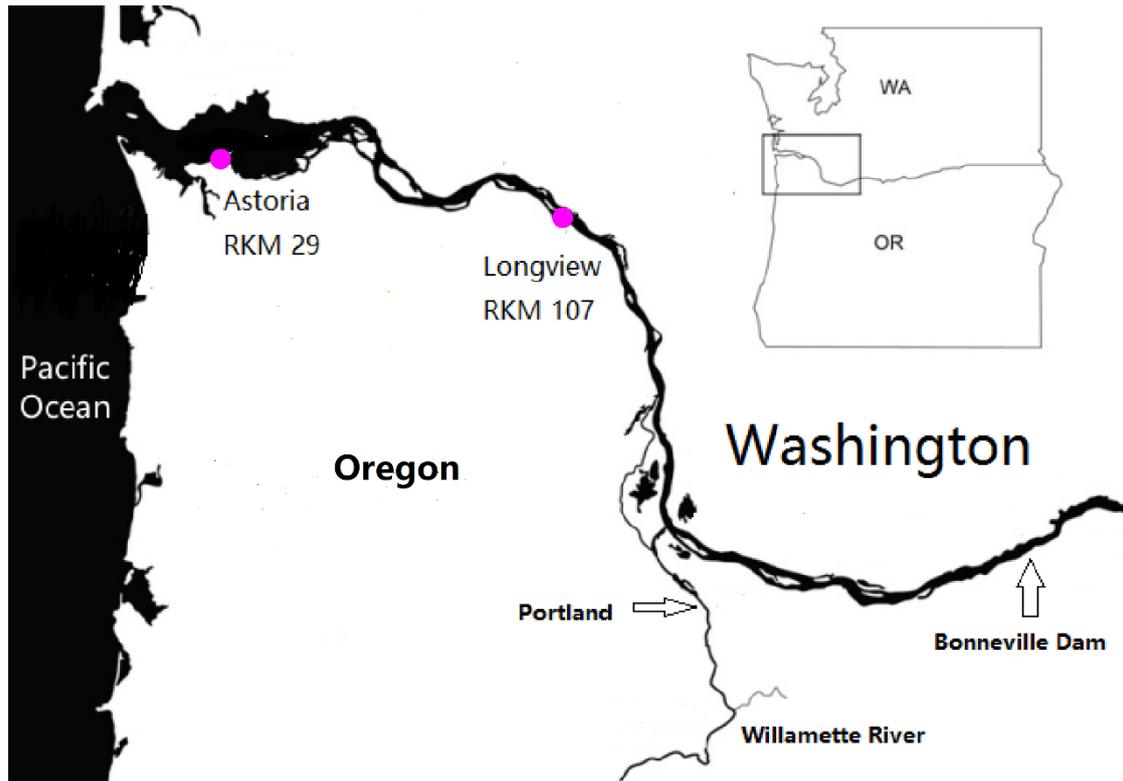


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544

Fig. 1. Flowchart of this study.

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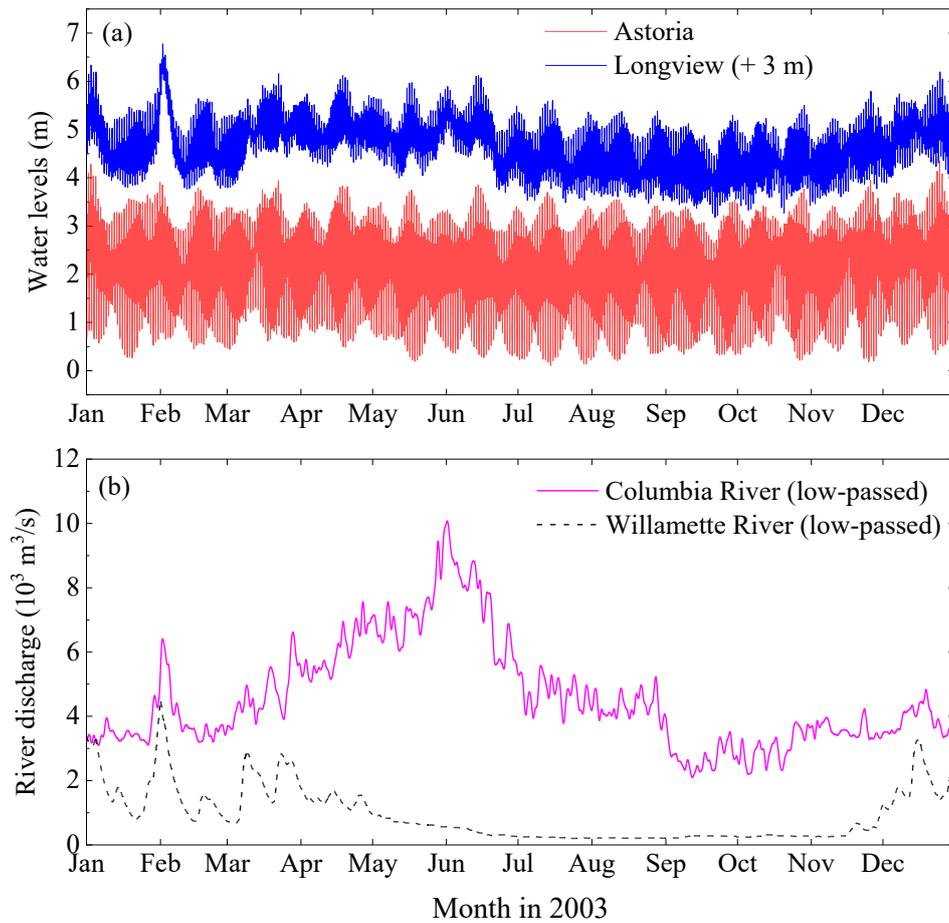


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Fig. 2. Map of the Columbia River Estuary and the location of the tide gauges.

548



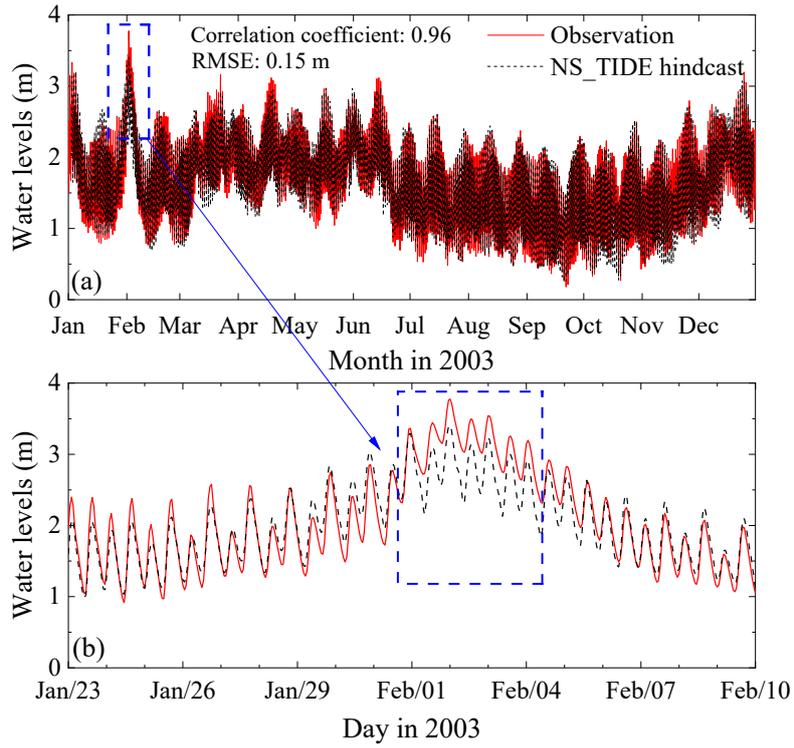
550

551 Fig. 3. (a) Water level observations at Astoria and Longview (increased by 3 m) in

552 2003. (b) Synchronous river discharge for the Willamette River and the main stem of

553 the Columbia River (at Bonneville Dam).

554

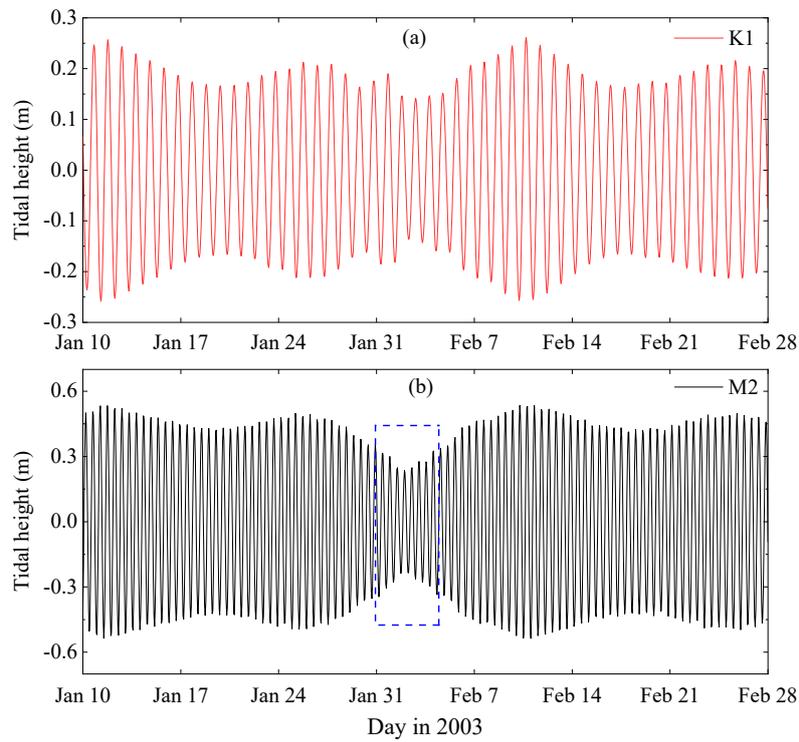


555

556 Fig. 4. (a) Water level observations in 2003 of Longview station and the synchronous

557 hindcast results of the NS_TIDE model. (b) Same as (a), but in early February 2003.

558



560

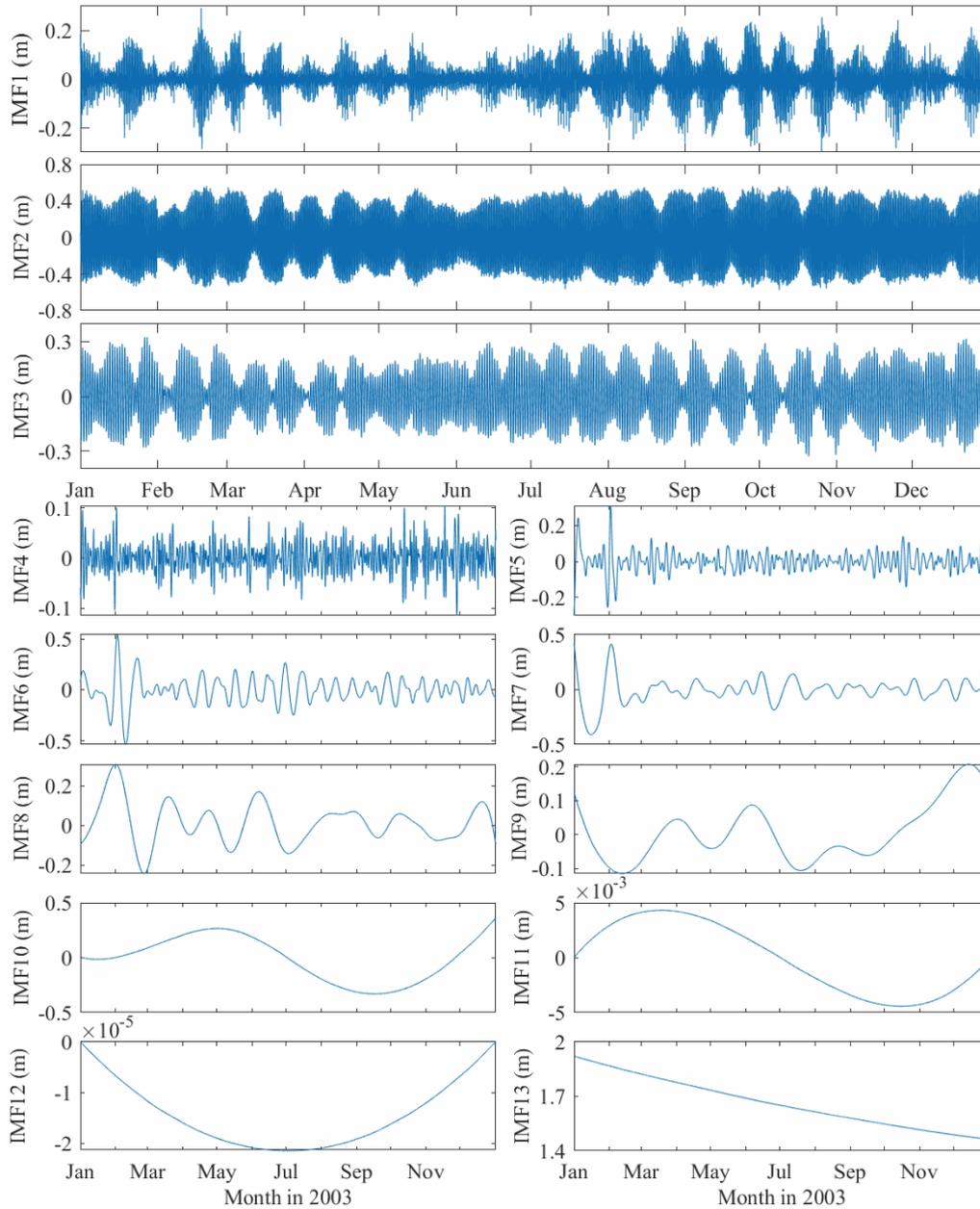
561 Fig. 5. Extracted time-dependent K_1 (a) and M_2 (b) tidal heights between January 10

562 to February 28 of 2003 from the NS_TIDE model hindcast results of Longview

563

station.

564



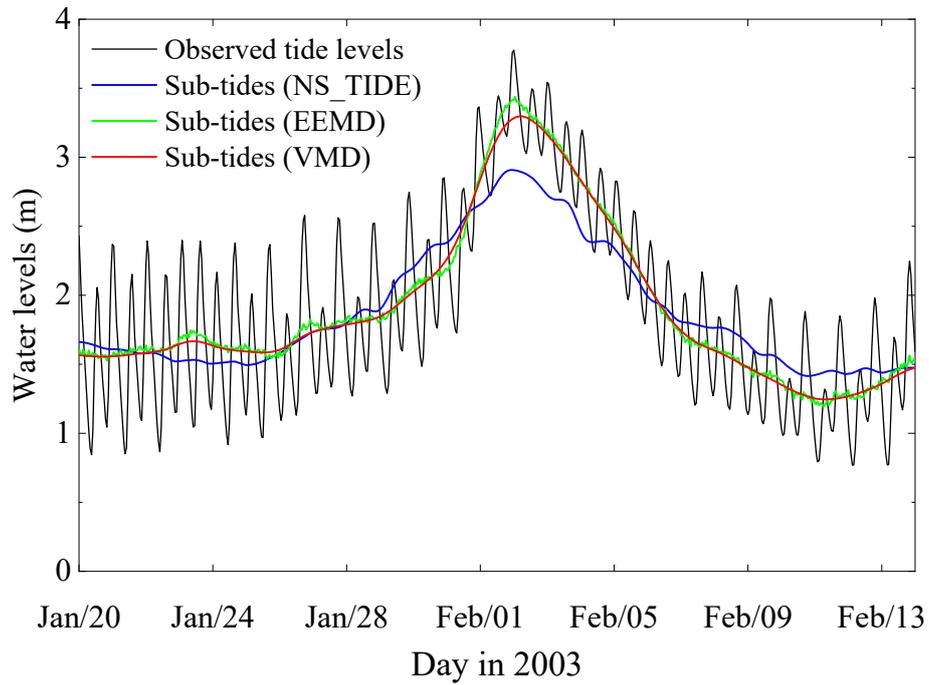
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566

Fig. 6. The EEMD modes for the water levels of Longview station in 2003.

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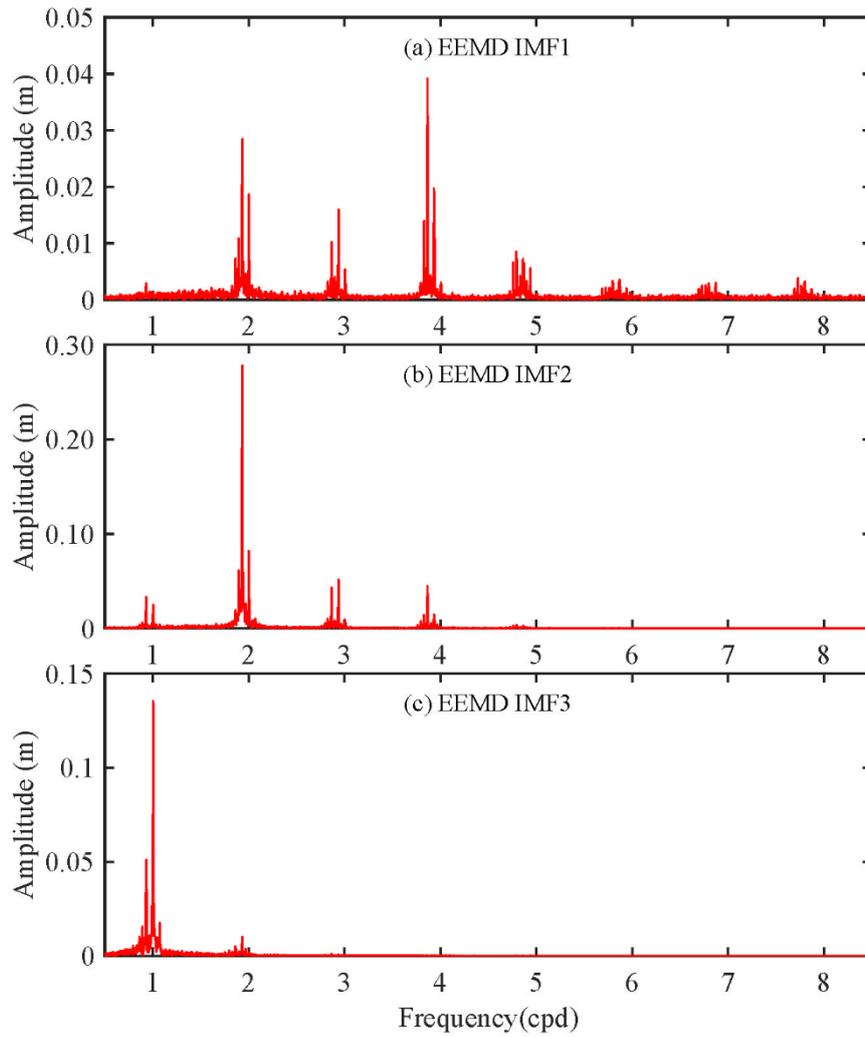


569

570 Fig. 7. Comparison of the sub-tidal water levels between January 20 and February 13

571 of 2003 obtained by the NS_TIDE, EEMD, and VMD models.

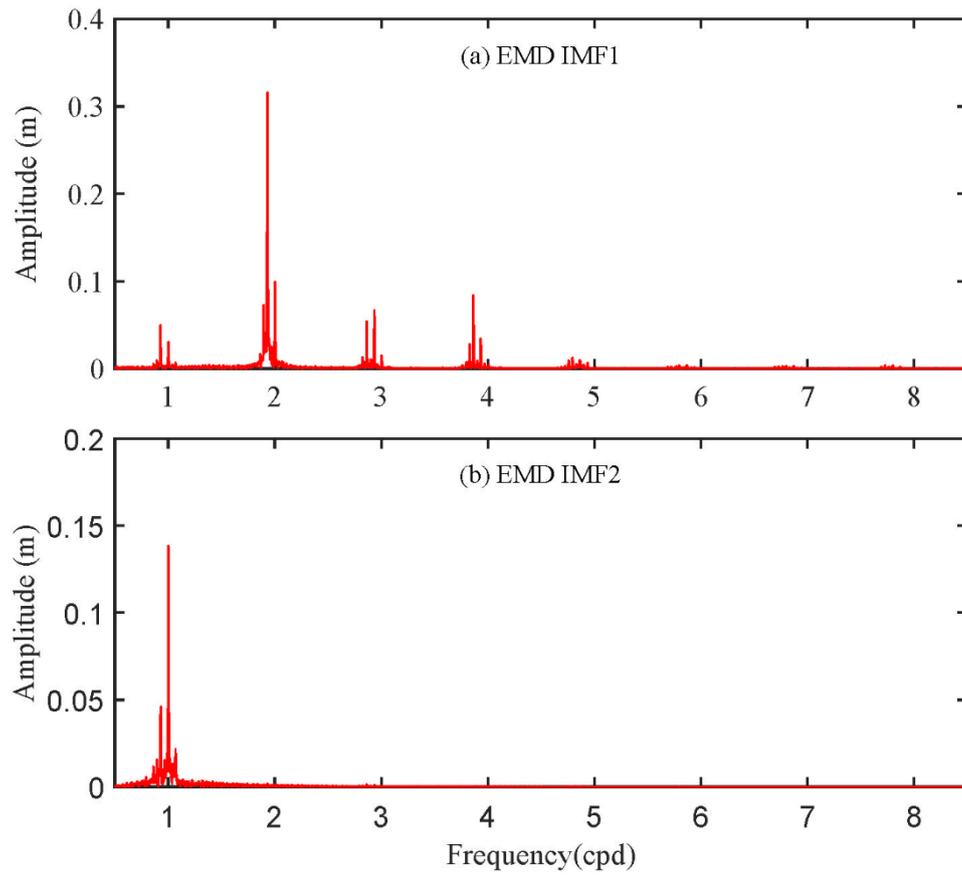
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573

574 Fig. 8. Fourier spectra map for (a) EEMD IMF 1, (b) IMF 2, and (c) IMF 3 for the
 575 water levels of Longview station in 2003.

576



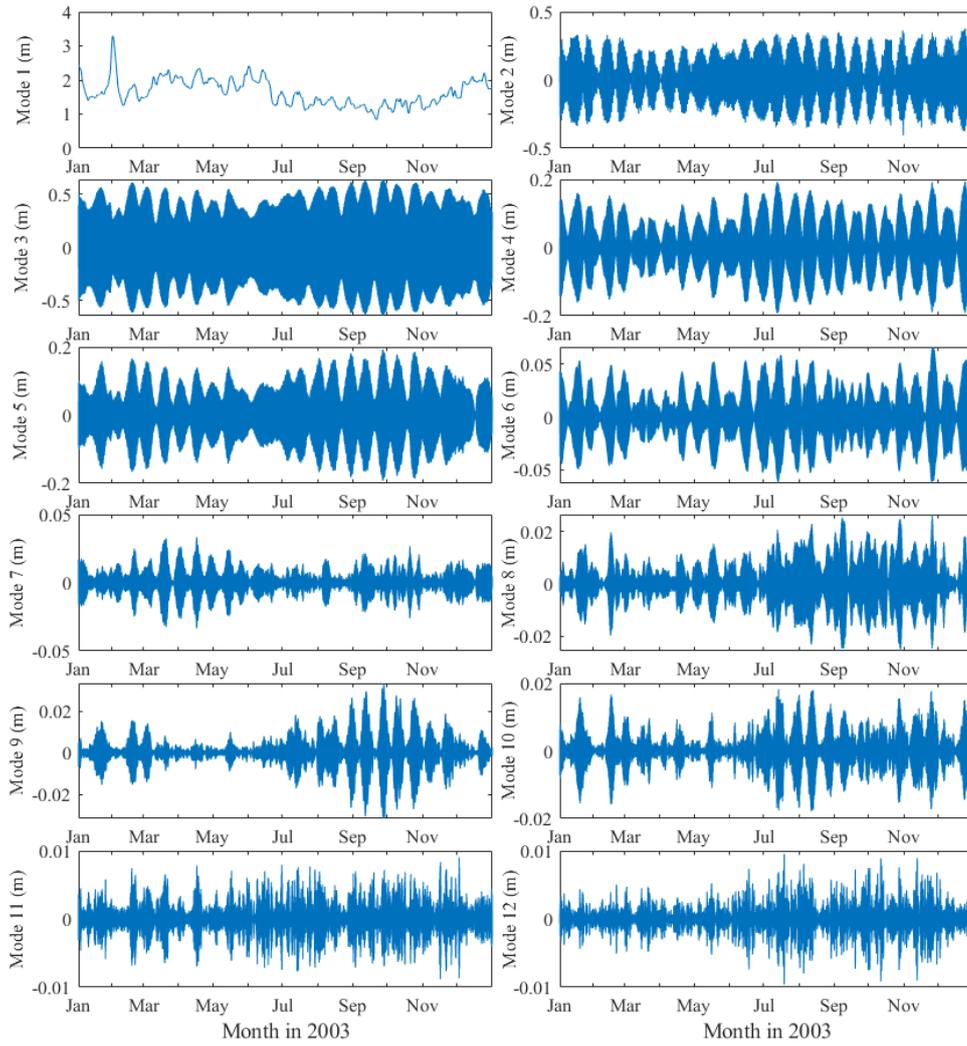
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578 Fig. 9. Fourier spectra map for (a) EMD mode 1 (b) mode 2 for the water levels of

579

Longview station in 2003.

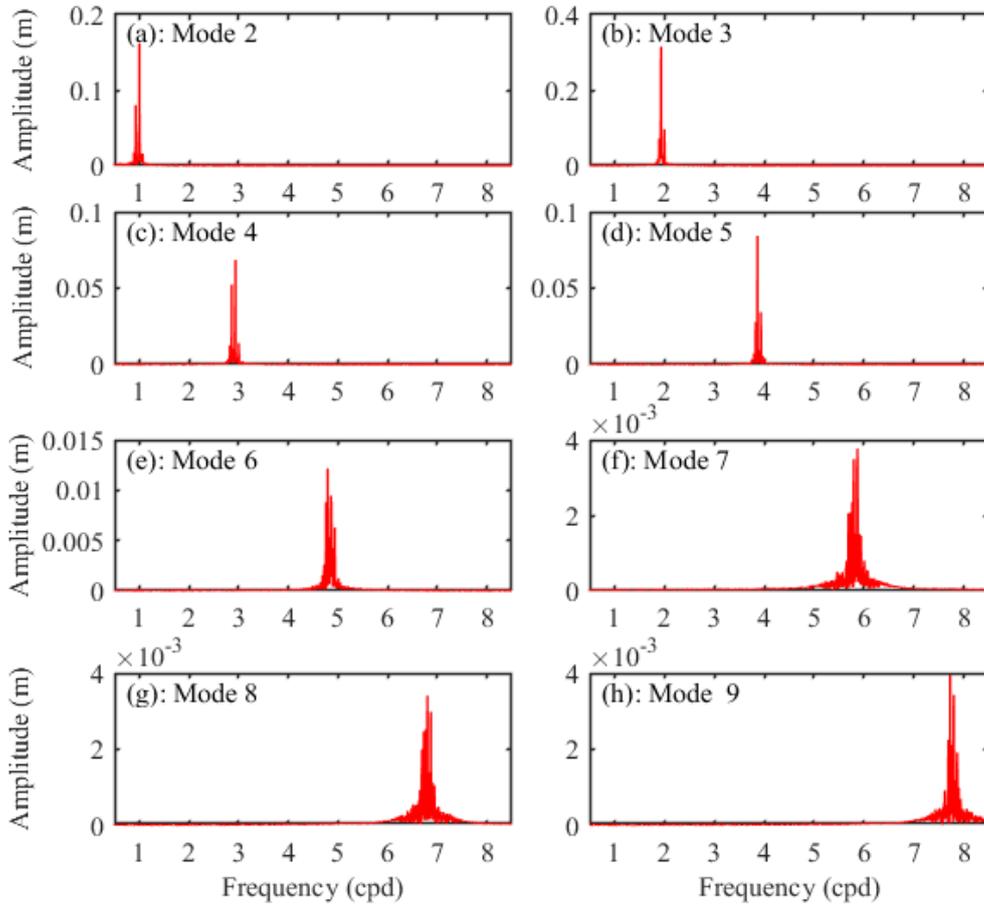
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581

582 Fig. 10. The 12 VMD modes for the water levels of Longview station in 2003.

583

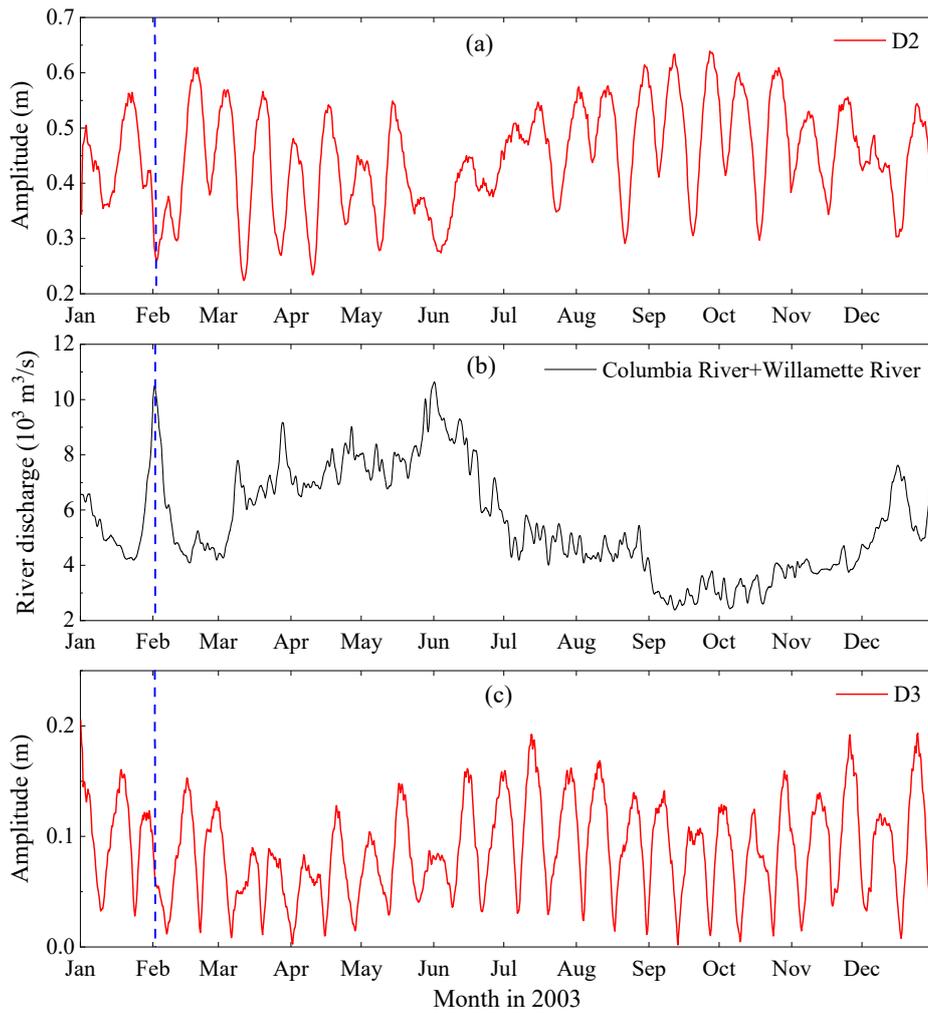


584

585 Fig. 11. Fourier spectra map of the VMD model from mode 2 to mode 9 for the water

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levels of Longview station in 2003.



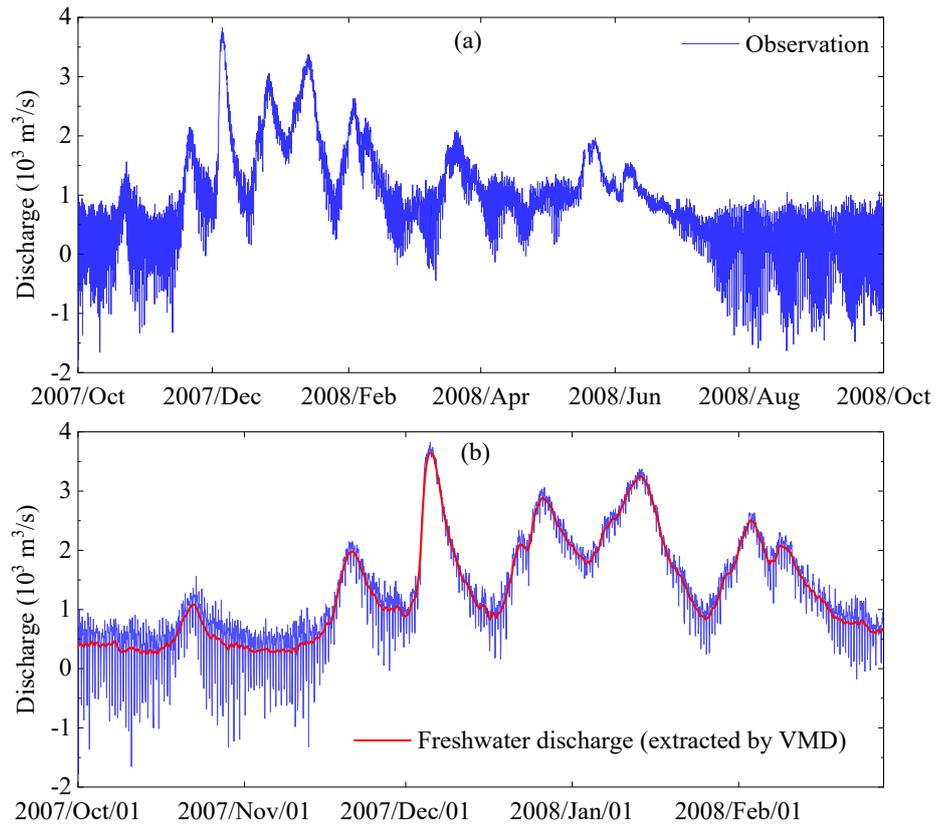
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588 Fig. 12. (a) D2 amplitudes at Longview (b) Discharge forcing in the lower Columbia

589 River (sum of river discharge at Bonneville Dam of Columbia River and Portland of

590 Willamette River); (c) D3 amplitudes at Longview for the data in 2003.

591



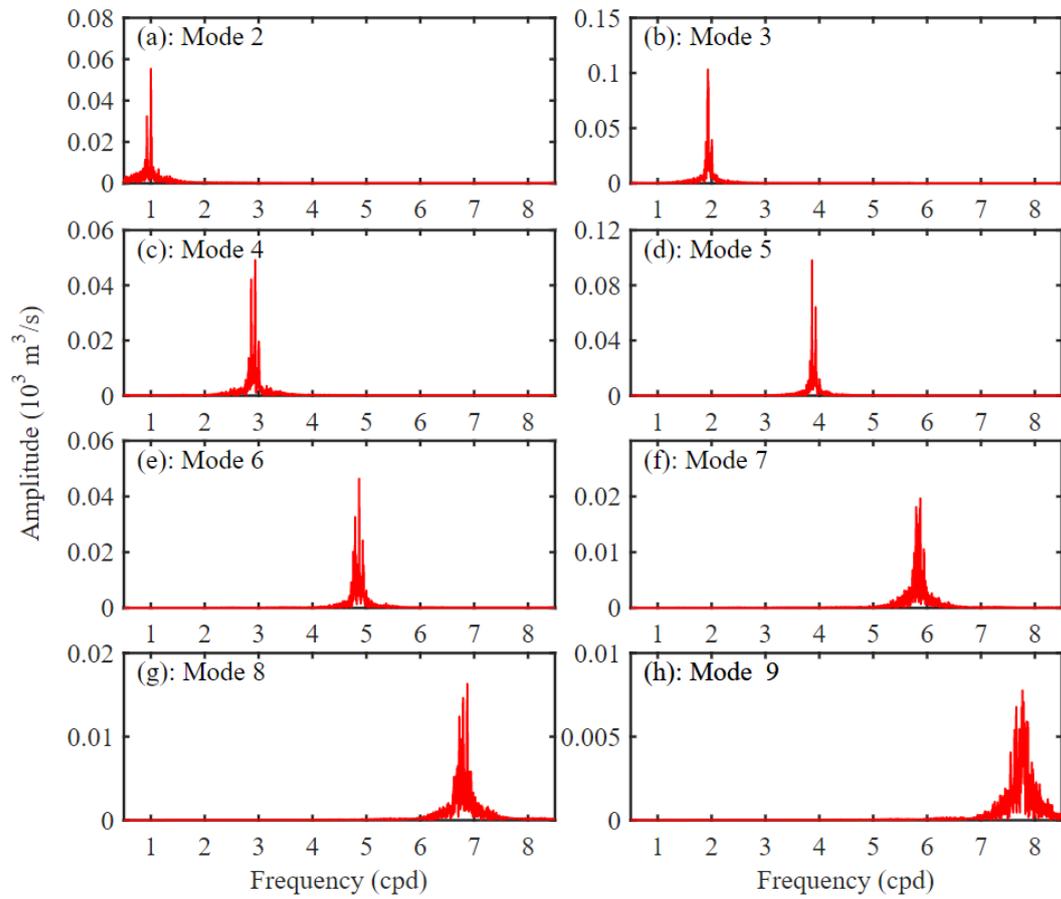
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593 Fig. 13. (a) Portland discharge observations from 2007 October to 2008 October. (b)

594 Freshwater discharge obtained by VMD from October 2007 to February 2008.

595

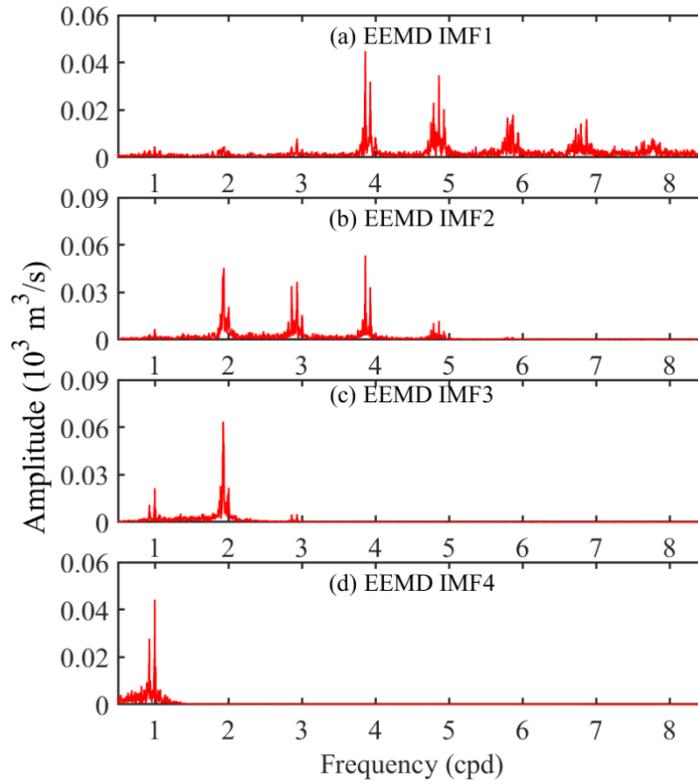
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597

598 Fig. 14. Fourier spectra map of the VMD model from mode 2 to mode 9 for the
599 observed river discharge of Portland station between 2007 October and 2008 October.

600



601

602

Fig. 15. Fourier spectra map of the EEMD model from IMF 1 to IMF 4 for the

603

observed river discharge of Portland station between 2007 October and 2008 October.