

# Multivariate forecasting of water storage change for West-Africa using sea surface temperature and GRACE data

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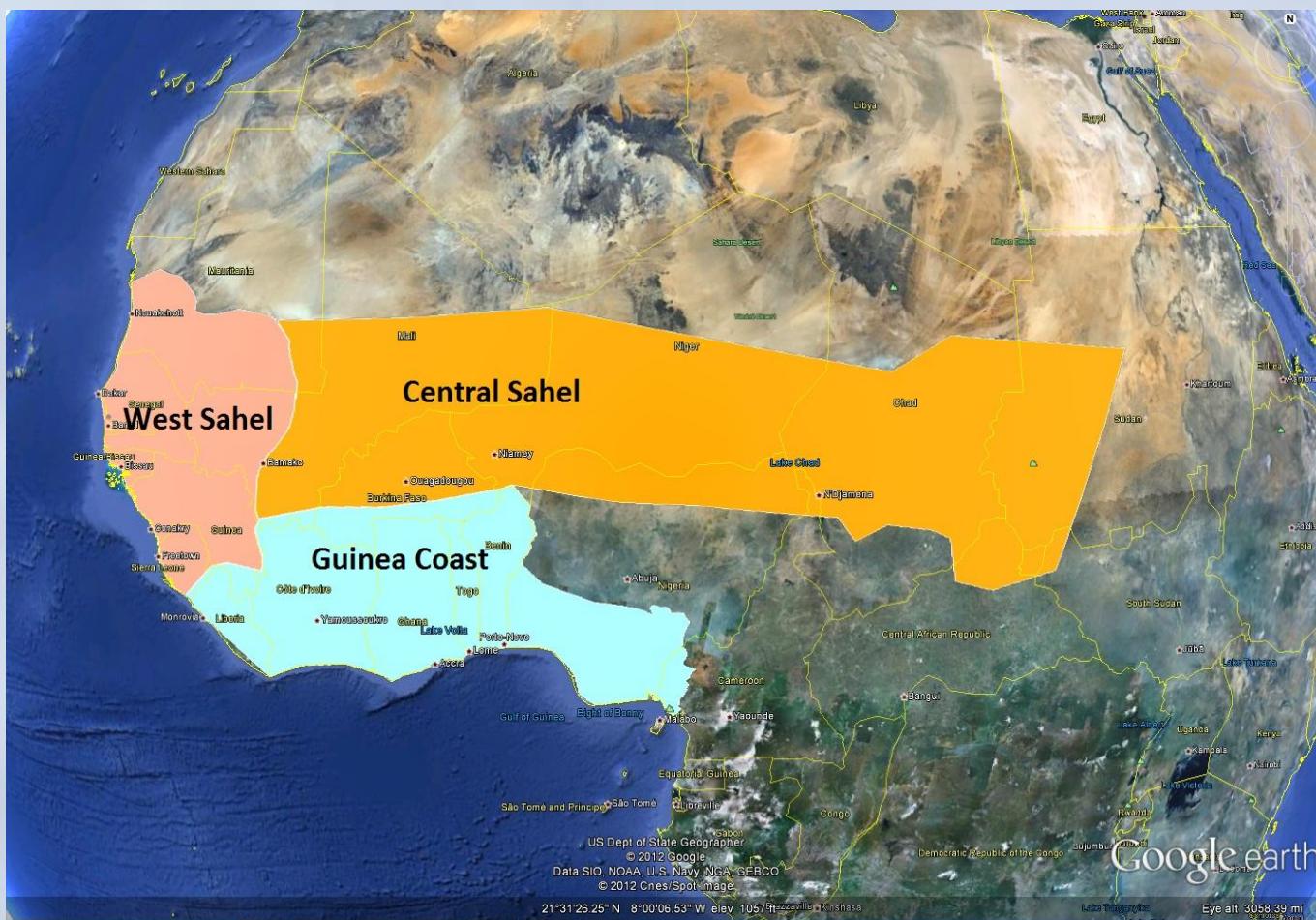
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e) School of Earth Sciences, Ohio State University, Columbus, Ohio, USA

AGU 2012, 3-7 Dec 2012, San Francisco, CA, USA

# Introduction

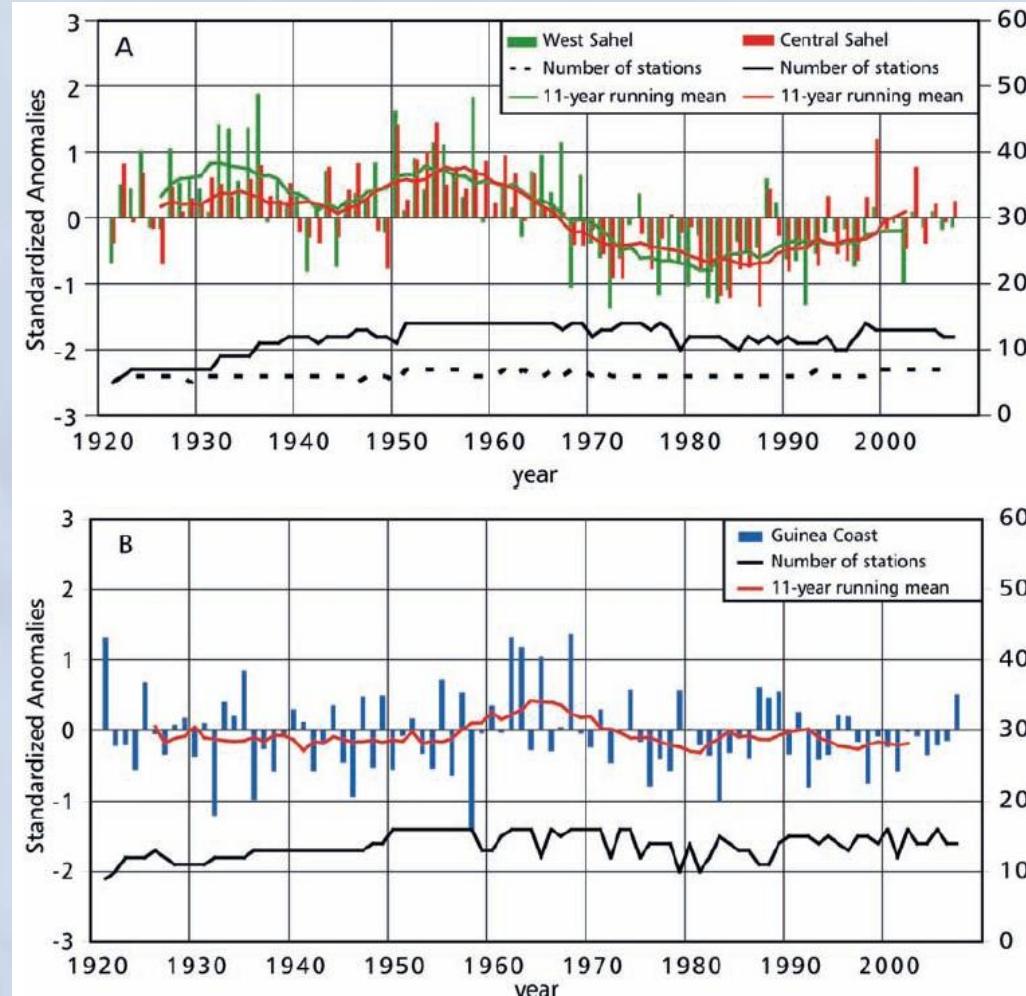
- West African countries are highly water-interdependent, with 17 countries sharing 25 trans-boundary river basins.



(According to: Fink et al., 2002)

- Drier conditions for the West Sahel and Central Sahel since the 1970s to at least 2000.

Rainfall Anomalies:



(Source: West African Atlas, Fink et al., 2002)

Knowledge concerning the hydrological cycle all in relation to climate change is essential for West African water resource management.

## Data:

- Direct (in-situ) observations → data are sparse
- Remote sensing observations

## Model:

- Climate models → uncertain (FAO, 2008)  
e.g. phase problem of rainfall predictions
- Hydrological models → not accurate within inter-annual time scales (Grippa et al., 2011)



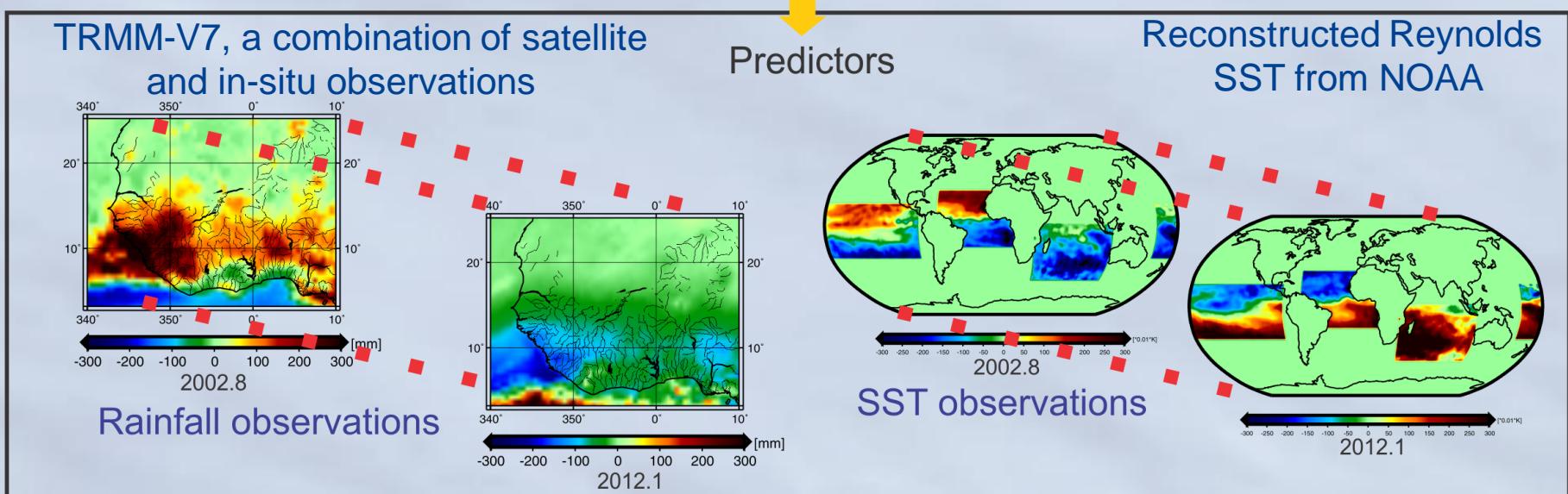
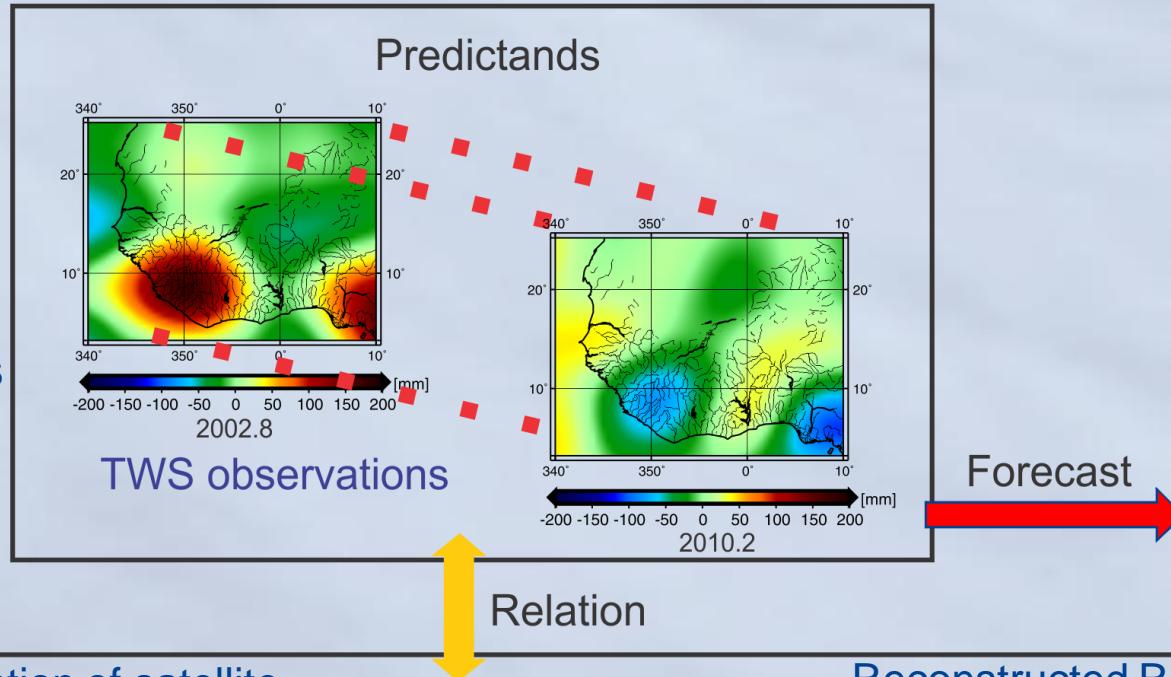
## Goal

Forecasting Total Water Storage (TWS) variations of West Africa using remote sensing observations.

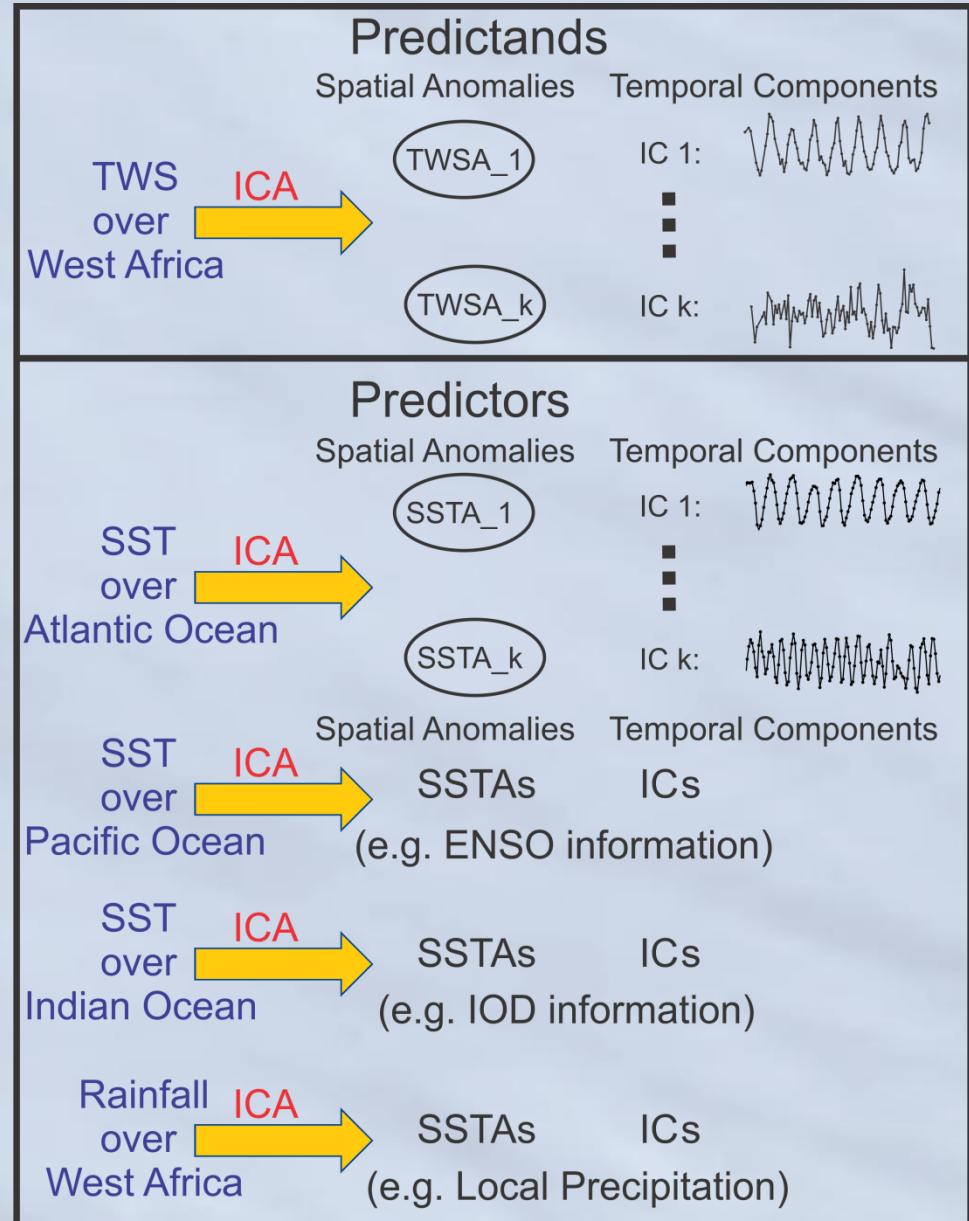
- Spatial scale: few-hundred kilometer
- Temporal scale: monthly based, up to a few years
- Why TWS?  GRACE provide accurate TWS
  - TWS is a key component of the hydrological cycle
  - It can be used for understanding the long-term effects of drought (Houborg et al., 2011)

The suggested method can be used for gap-filling of GRACE-TWS products over West Africa!

GRACE-TWS  
variations from GFZ  
centre, smoothed by  
Kusche et al. (2009)'s  
DDK2 filter

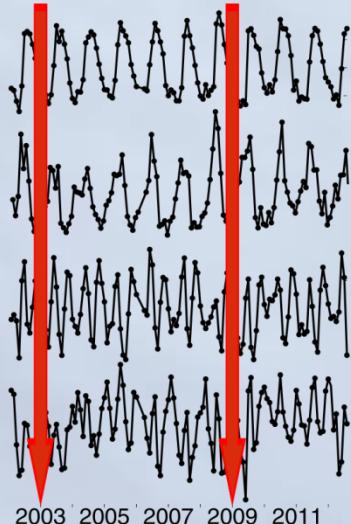


- Using the higher order statistical method of Independent Component Analysis (ICA) for transforming predictands and predictors (Forootan and Kusche, 2012a)
- The forecast model is univariate in the “Predictand Space”.
- The forecast model is multivariate in the “Predictor Space”.

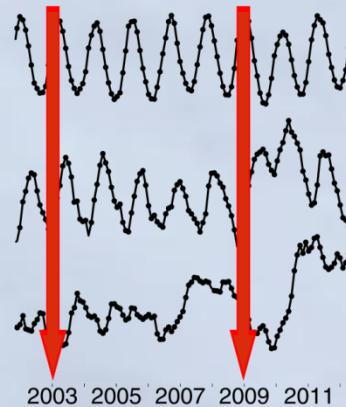


# Modeling Concept

IC s of Rainfall-West Africa

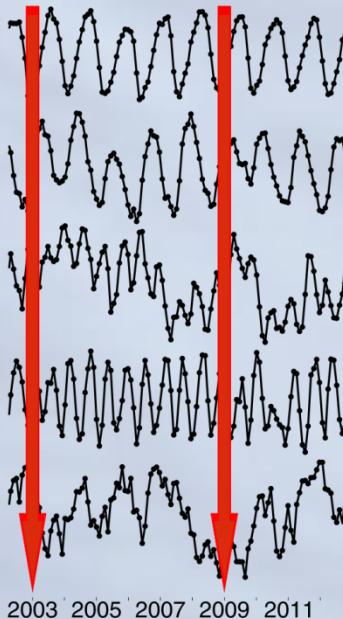


IC s of SST-Pacific Ocean

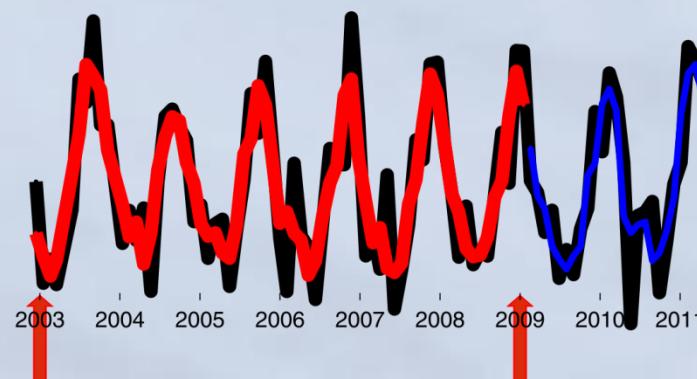
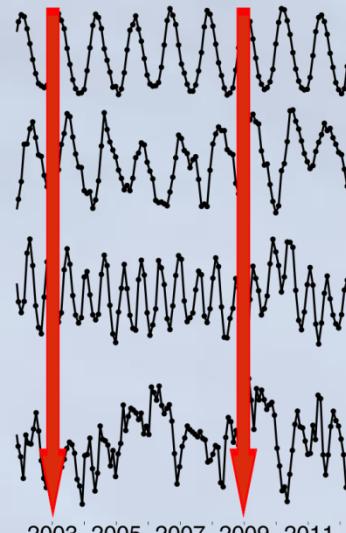


■ Predicted TWS  
■ Used data  
■ GRACE TWS

IC s of SST-Atlantic Ocean



IC s of SST-Indian Ocean



- Statistical modeling: Relating predictors and predictands, using an AutoRegressive (AR) Process

## Step1: PCA

$$\mathbf{F}(t, s)_{n \times m} = \mathbf{P} \Lambda \mathbf{E}^T$$

## Step2: Rotation

$$\mathbf{F}(t, s)_{n \times m} = \mathbf{F}(t, s)_{n \times m} = \mathbf{P} \mathbf{R} \Lambda \mathbf{R}^T \mathbf{E}^T = \mathbf{A} \mathbf{S}^T$$

Selected: diagonality of 4<sup>th</sup>-order cumulants

(Forootan and Kusche, 2012a,b)

## Error estimation

A Monte Carlo error estimation can be used to estimate the uncertainties of the derived independent components.

## Temporal vs. Spatial ICA

Temporal ICA: Rotation of PCs

$$\mathbf{x} = \mathbf{P}_k \mathbf{R}$$

Spatial ICA: Rotation of EOFs

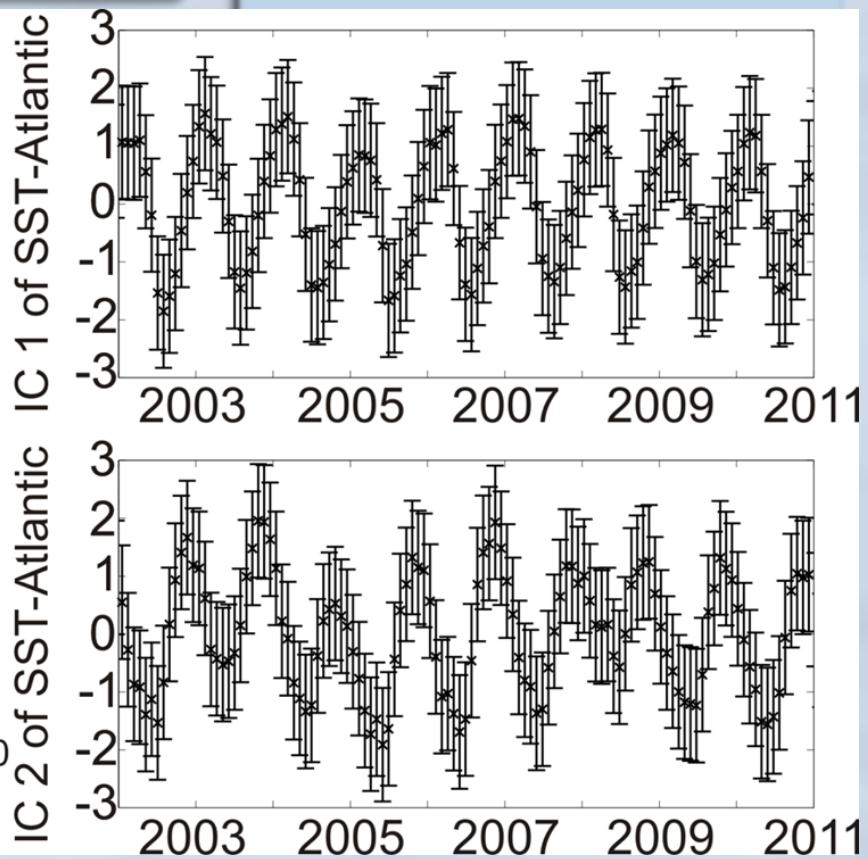
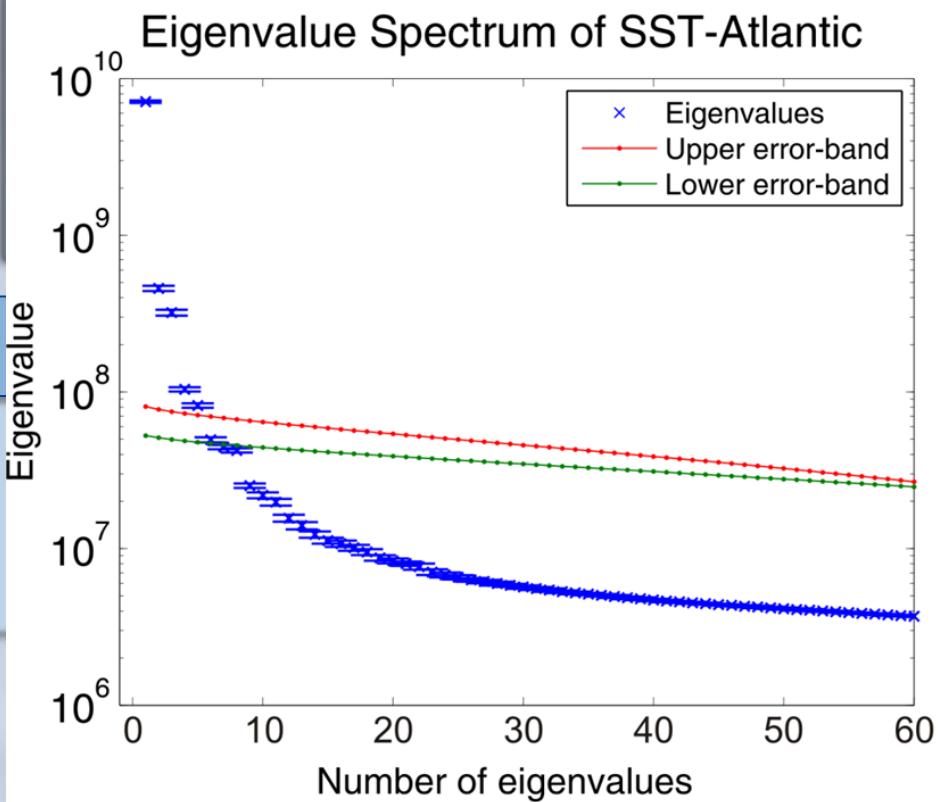
$$\mathbf{x} = \mathbf{E}_k \mathbf{R}$$

(see Forootan et al., 2012)

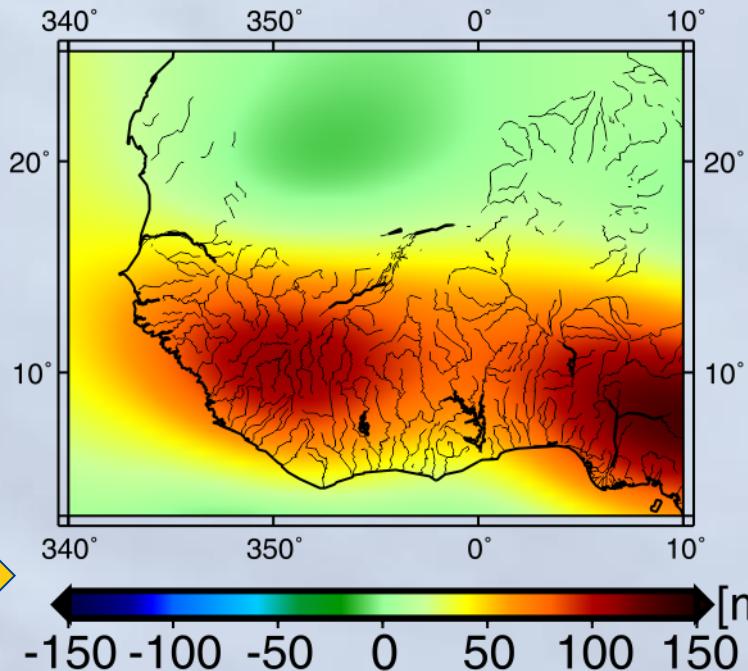
## Step1: PCA

$$\mathbf{F}(t, s)_{n \times m} = \mathbf{P} \Lambda \mathbf{E}^T$$

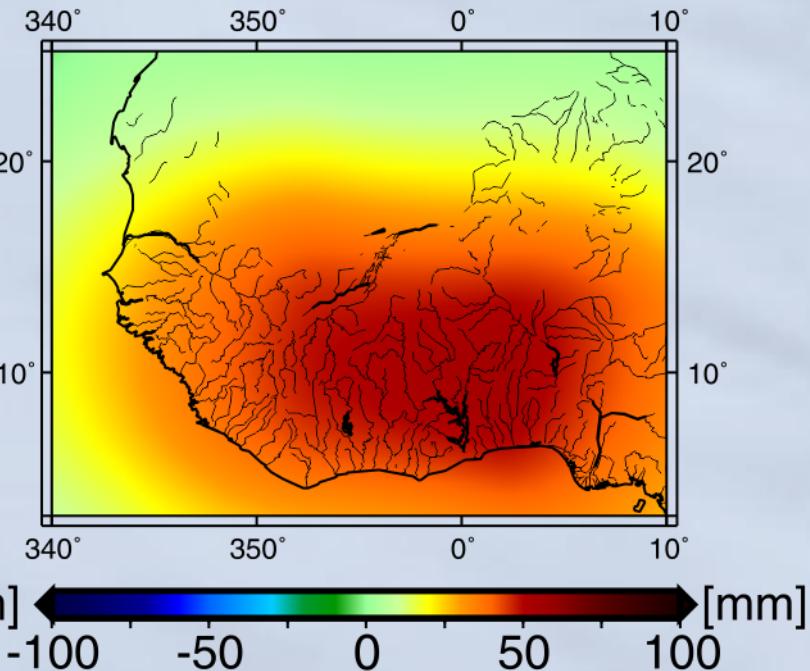
## Step2: Rotation



Spatial pattern of IC 1-GRACE

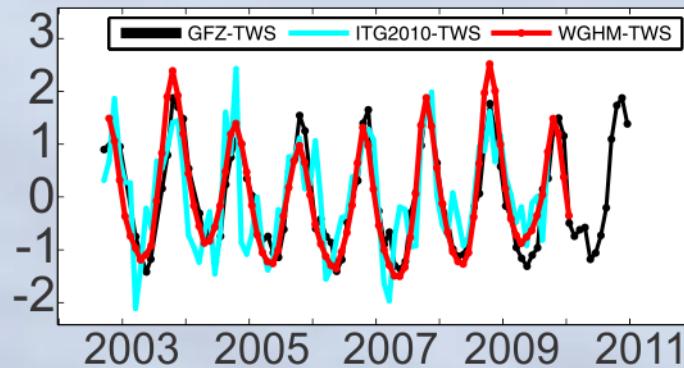


Spatial pattern of IC 2-GRACE

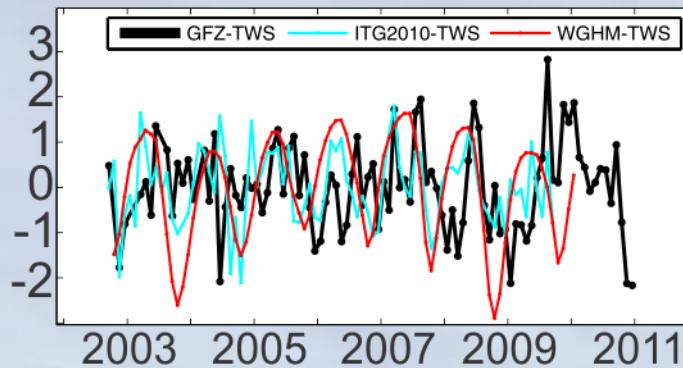


ICA of  
TWS

## Temporal pattern of IC 1-GRACE

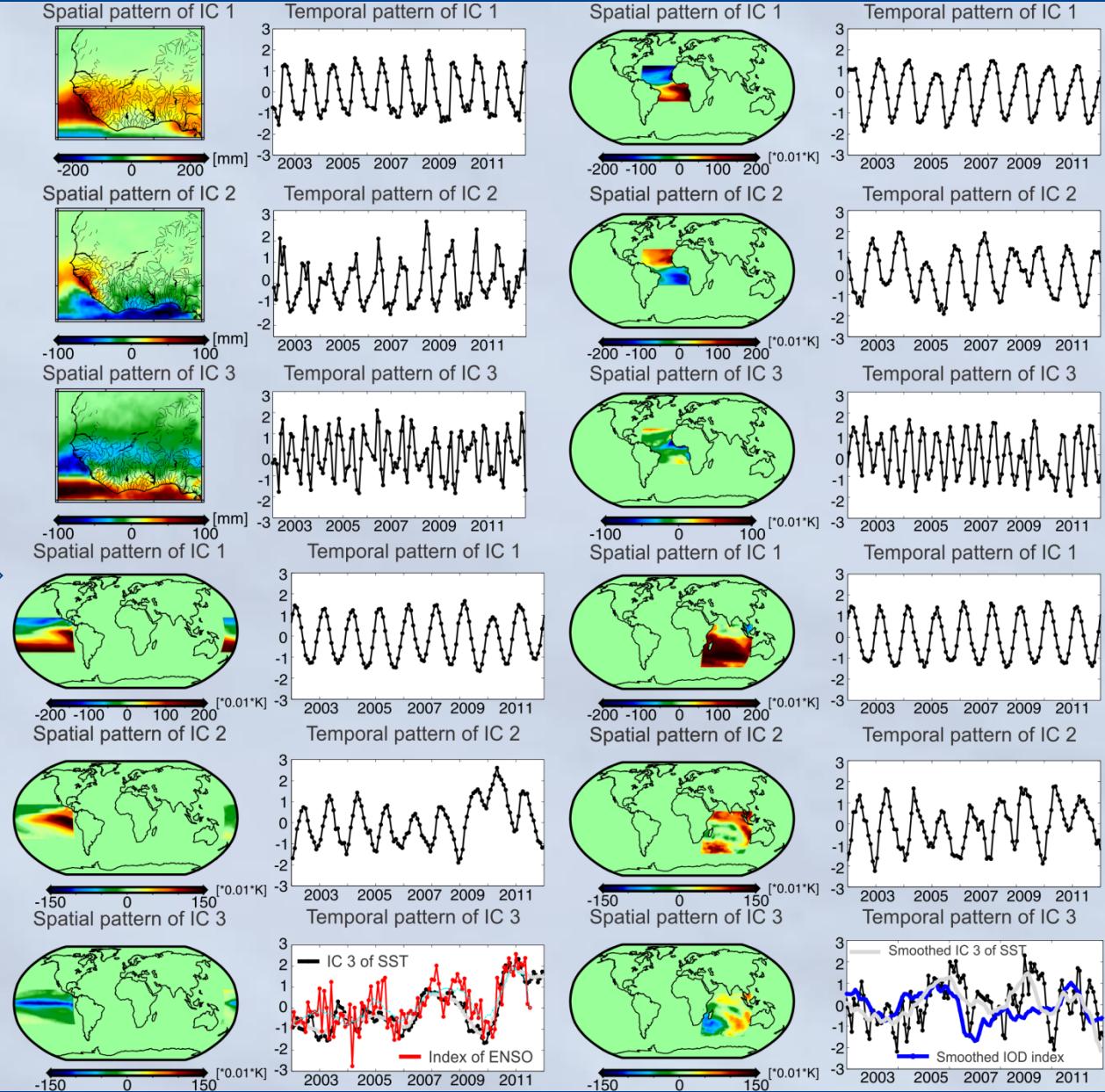


## Temporal pattern of IC 2-GRACE



# ICA Results - TWS

ICA of  
Predictors



El Niño  
Southern  
Oscillation  
(ENSO)

Highly correlated with the annual variability of TWS (TWS-IC1)

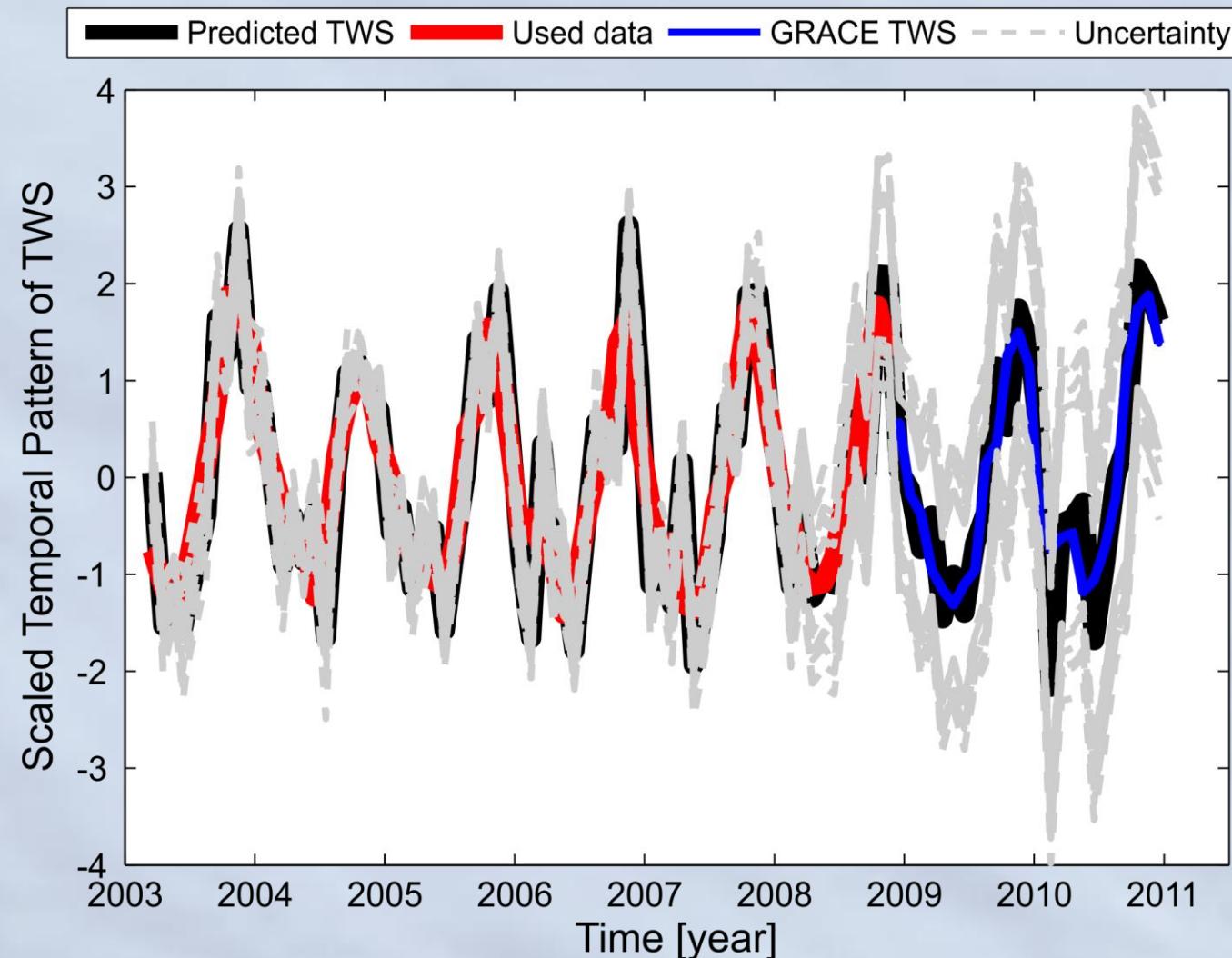
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Indian Ocean Dipole (IOD)

# Forecasting Results

Simulation Fit: 92%

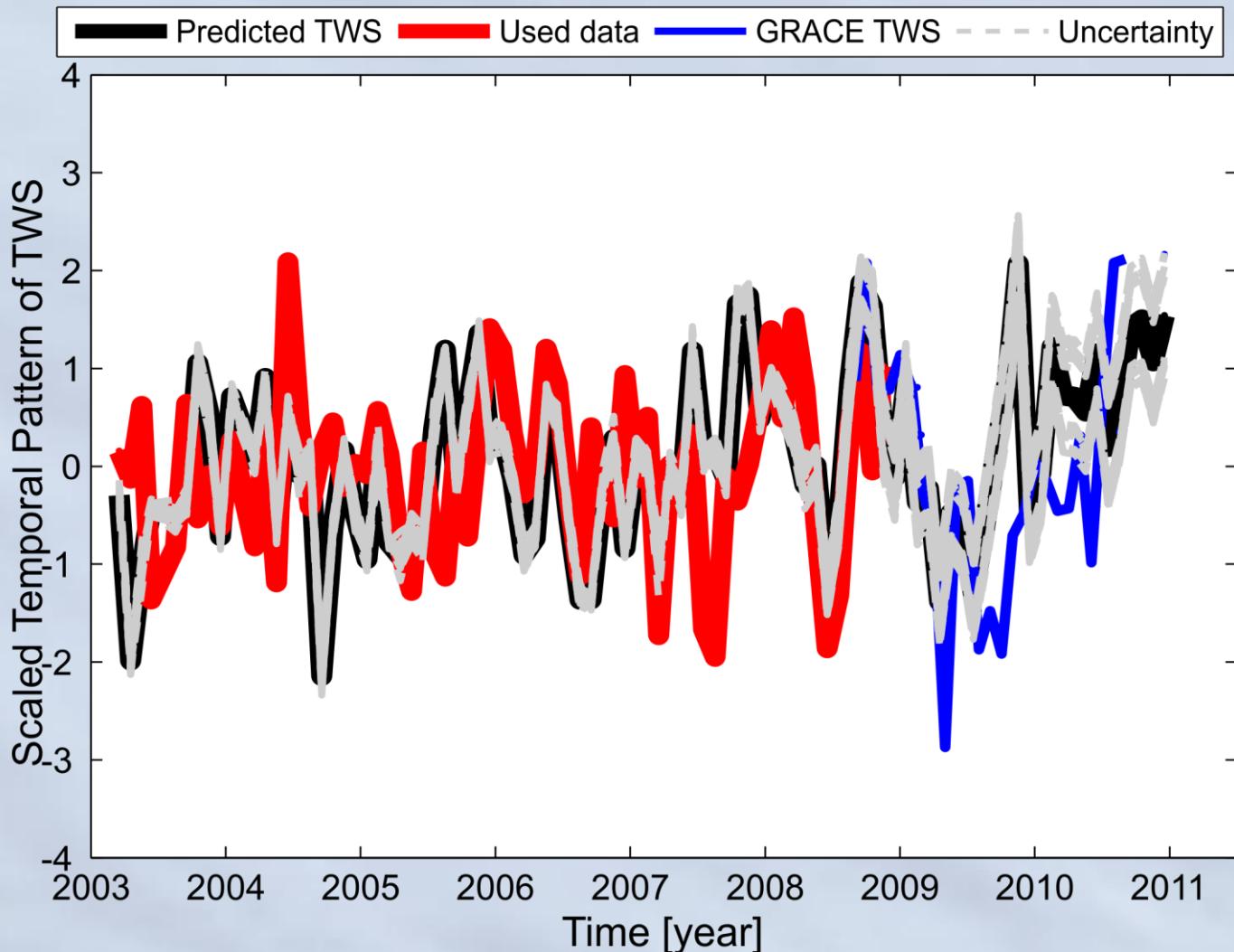
1-year Forecast Fit: 79%    2-year Forecast Fit: 63%



# Forecasting Results

Simulation Fit: 83%

1-year Forecast Fit: 67%    2-year Forecast Fit: 58%



- The amplitude of annual TWS variations over West-Africa is mainly correlated to SST variations of the Atlantic Ocean
- The long-term and inter-annual variability of West-African TWS is controlled with the ENSO phenomenon
- A Multivariate Statistical Forecast can be used for forecasting TWS over West Africa

- Applying an Auto-Regressive (AR) algorithm,

Predictors: ICs of SST over the Atlantic, Pacific and Indian Oceans

Predictors: ICs of rainfall over West Africa

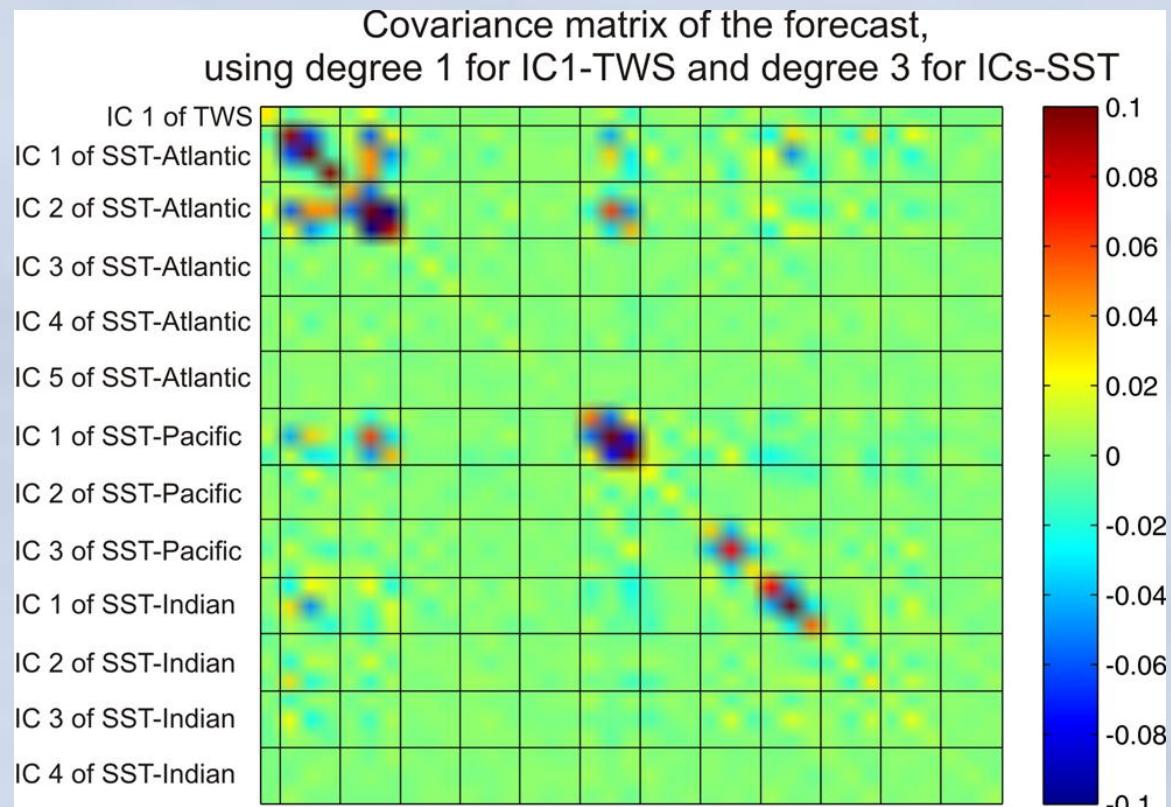
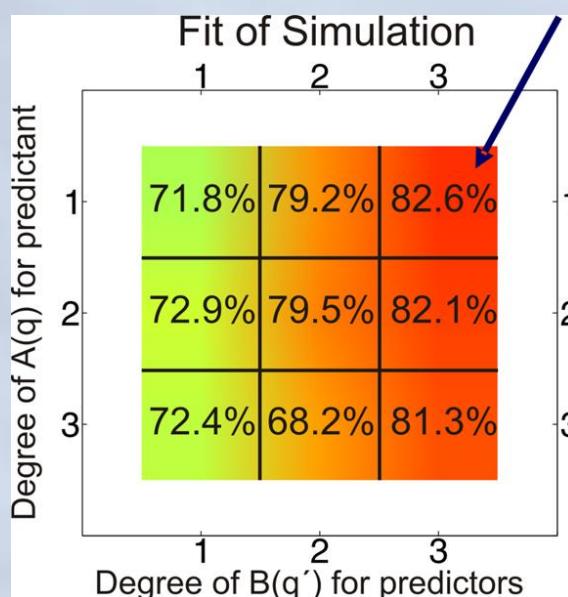
Predictands: ICs of GRACE-TWS over West Africa

- Results showed a reliable performance of the forecast up to two years
- The forecasting method can be used for gap-filling of GRACE-TWS over West Africa

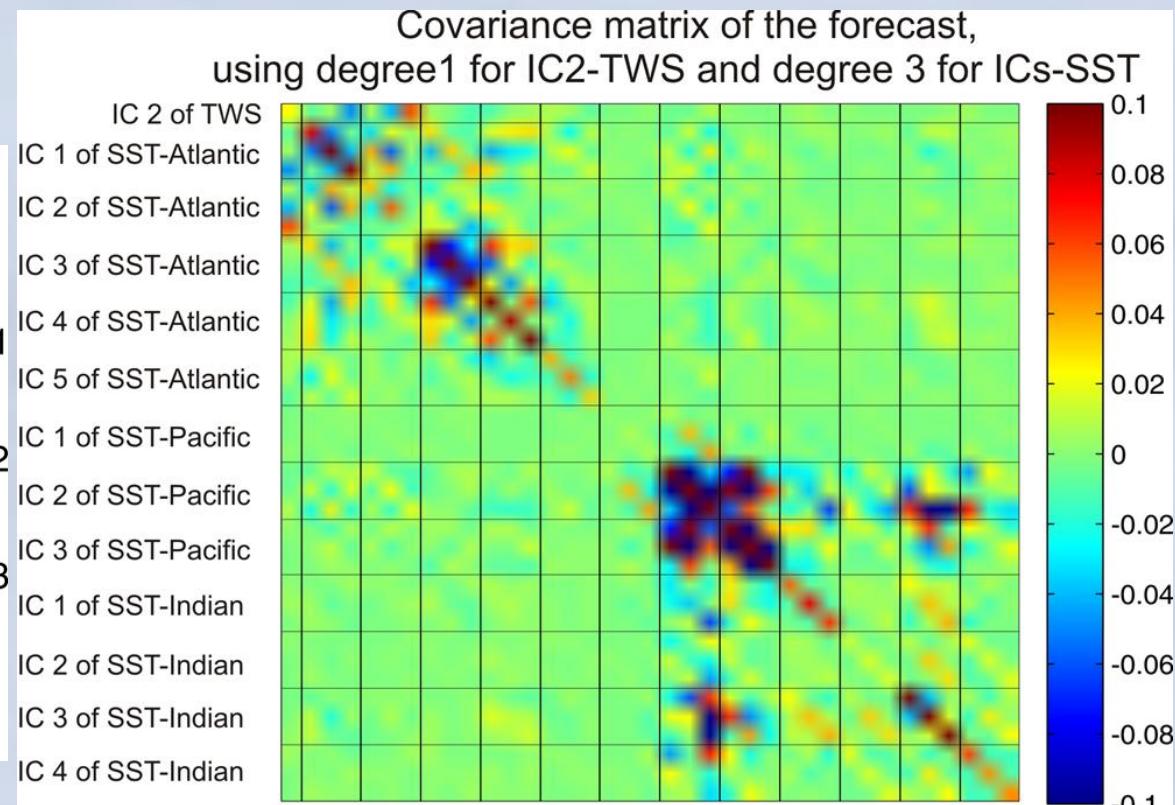
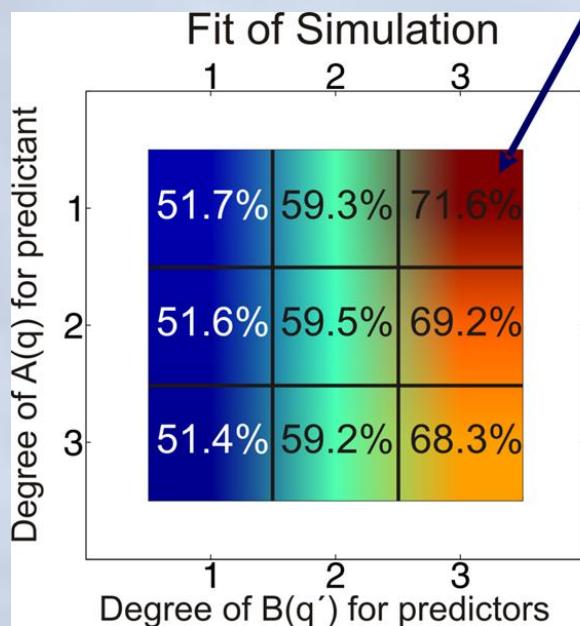
# Thanks for your attention

- Main references:
1. Forootan, E., Kusche, J. (2012a). Separation of global time-variable gravity signals into maximally independent components, *Journal of Geodesy*, Vol.86 (7), 477-497, doi:10.1007/s00190-011-0532-5.
  2. Forootan, E., Kusche, J. (2012b). Separation of deterministic signals, using independent component analysis (ICA). *Journal of Studia Geophysica et Geodaetica*, doi: 10.1007/s11200-012-0718-1.
  3. Forootan, E., Awange, J., Kusche, J., Heck, B., Eicker, A. (2012). Independent patterns of water mass anomalies over Australia from satellite data and models. *Journal of Remote Sensing of Environment*, Vol.124, 427-443, doi:0.1016/j.rse.2012.05.023.
  4. Kusche ,J., Schmidt ,R., Petrovic, S., Rietbroek, R. (2009). Decorrelated GRACE time-variable gravity solutions by GFZ, and their validation using a hydrological model. *Journal of Geodesy*, Vol.83, 903–913.,doi:10.1007/s00190-009-0308-3

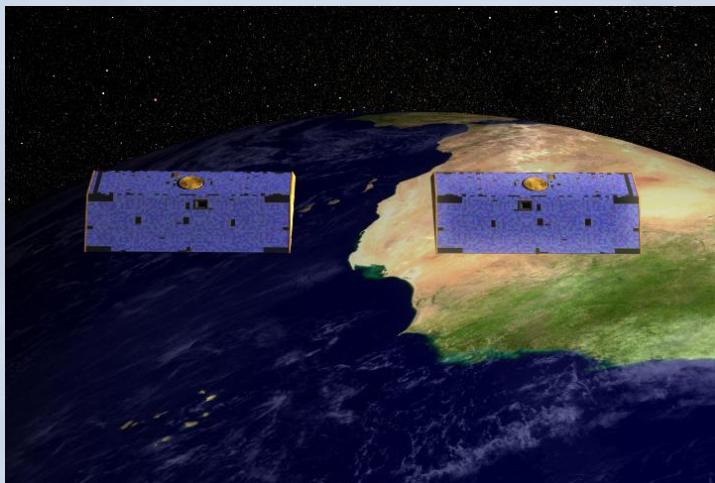
# Fit of the Model



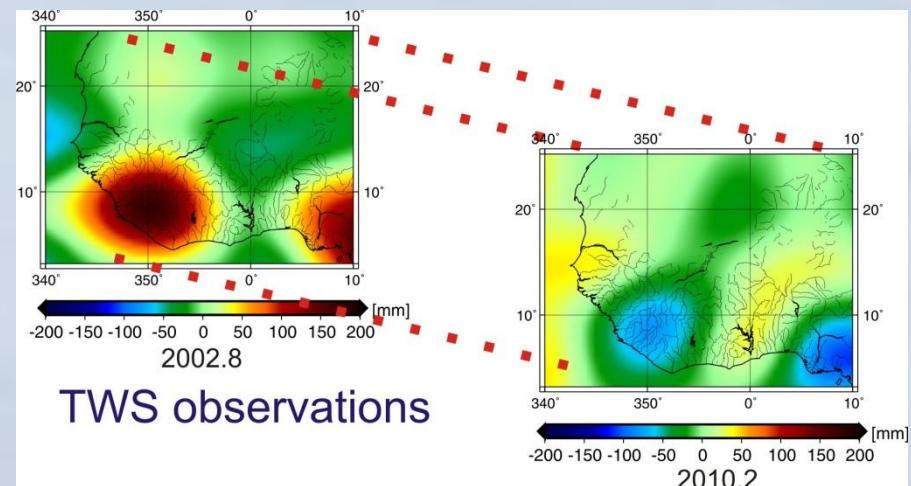
# Fit of the Model



## Predictands



## TWS changes



TWS observations

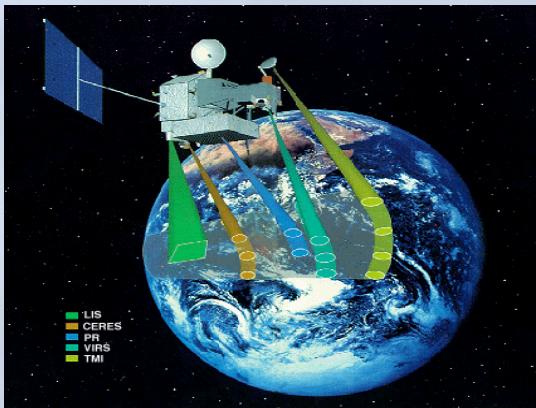
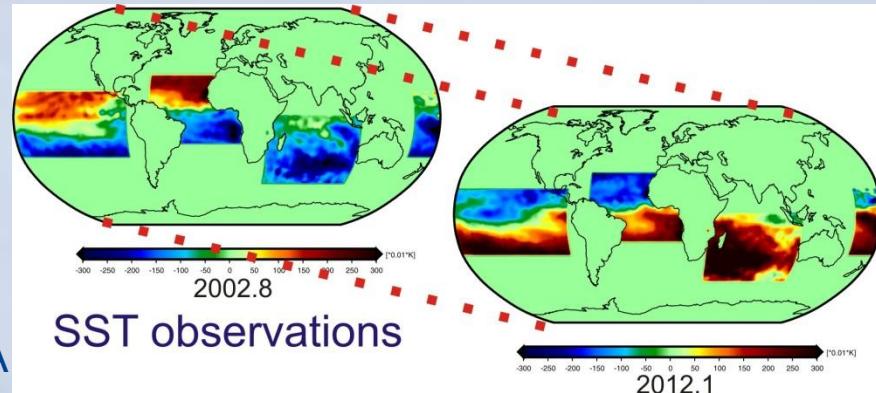
GRACE-TWS variations from GFZ centre,  
smoothed by Kusche et al. (2009)'s DDK2 filter

## Predictors (Indicators)



Reconstructed Reynolds SST from NOAA

## Monthly SSTs



TRMM-V7, combination of satellite and in-situ observations

## Monthly Rainfalls

