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# Quantum chemical modeling of tri-Mn-substituted W-based Keggin polyoxoanions

Alena Kremleva<sup>a</sup>, Pablo A. Aparicio<sup>b</sup>, Alexander Genest<sup>c</sup>, Notker Rösch<sup>a,b,c,\*</sup>

<sup>a</sup> Department Chemie, Technische Universität München, 85747 Garching, Germany

<sup>b</sup> TUM CREATE Limited, 1 CREATE Way, #10-02 Create Tower, Singapore 138602, Singapore

<sup>c</sup> Institute of High Performance Computing, Agency for Science, Technology and Research, 1 Fusionopolis Way, #16-16 Connexis, Singapore 138632, Singapore

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## ARTICLE INFO

To Professor Maria-Elisabeth Michel-Beyerle, TUM CREATE Singapore, who, over many years, generously shared her deep insight into a broad range of problems in physical chemistry and provided outstanding leadership in forming highly successful, long-term research alliances for solving such problems.

### Keywords:

Polyoxometalates  
Keggin ion  
Redox potentials  
DFT modeling  
Electrolyte environment

## ABSTRACT

Using Density Functional Theory (DFT) calculations, we studied the electrochemistry of polyoxometalates (POMs), specifically the redox properties of Mn in tri-Mn-substituted W-based Keggin ions. For direct comparison with recent cyclic voltammetry results [J. Friedl et al. *Electrochim. Acta*, 141 (2014) 357], we estimated the reversible half-wave potentials of proton- and cation-coupled electron transfer for Mn(IV/III) and Mn(III/II), respectively. The calculated reversible potentials agree well with experiment, reproducing the trend with pH for Mn(IV/III). For adequate DFT energies, it is crucial to apply a reliable description of the electrolyte environment of the POM, accounting also for their rather high charges, up to 7 e. To this end, we included the Li<sup>+</sup> counterions, required for charge neutralization, directly in the quantum chemical models which were embedded in a polarizable continuum. We explored various arrangements of the Li<sup>+</sup> ions around the POMs and their effect on both structural parameters and electrochemical properties of the POMs. Hybrid functionals (TPSSH, B3LYP, PBE0) overestimate the experimental reduction potentials: the larger the exact-exchange contribution, the larger the resulting reduction potential. The best agreement with experiment is achieved with the PBE approach, likely due to fortuitous error cancellation. The results of the present work indicate that a more sophisticated (atomistic) representation of the electrolyte environment will be beneficial for predicting redox potentials in better agreement with experiment.

## 1. Introduction

Polyoxometalates (POMs) are a class of nano-sized compounds formed by linking early transition metal polyhedra via oxygen centers located at their vertices [1–4]. POMs exist in a variety of shapes, sizes, and compositions [2,5,6]. They are stable over a wide range of pH values and temperatures and they are able to undergo reversible multi-electron redox processes [7–9]. Therefore, POMs can be employed in electrocatalysis, including hydrogen evolution reactions [10]. POMs can be regarded as a molecular “electron sponge” due to many-electron redox processes; they have been proposed as a cathode material for high-performance rechargeable batteries, so-called molecular cluster batteries [8,9].

Recently, the use of POMs has also been suggested for large-scale energy storage, in particular in redox flow batteries (RFB)

[11]. In this context, attention focused in particular on so-called Keggin ions, i.e., structures of the type [XM<sub>12</sub>O<sub>40</sub>]<sup>n</sup> [3,4]. The highly symmetric Keggin ion with M = W and X = P was the first such structure to be clarified by X-ray diffraction [3]. Formal replacement of some centers M by another transition metal M<sup>0</sup> generates Keggin-type POMs where redox potentials due to the two types of metals are separated by up to a few Volts [12–14]. As an example, we mention V-exchanged W-based Keggin ions [12], a system which was shown to yield an aqueous 0.8 V battery that could be cycled 100 times, achieving a Coulombic efficiency above 95% [12]. Although the current densities of this prototype were measured at least one order lower than those of common RFBs [15], POMs based systems may offer a new approach to RFBs.

Inspired by this new concept, another substituted POM, namely a tri-Mn-substituted W-based Keggin ion (X = Si) was recently introduced and examined electrochemically [13,16]. The initial oxidation state of this POM has been shown to affect the Mn electrochemistry, whereas the nature of the counterions was found not to influence the resulting electrochemistry [13].

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\* Corresponding author at: Department Chemie, Technische Universität München, 85747 Garching, Germany.

E-mail address: roesch@mytum.de (N. Rösch).

Computational chemistry offers an approach complimentary to experiment, for characterizing the (electrochemical) properties of POMs [17–24]; see also some reviews [25–27] and the references therein. Thus far, structural parameters, electronic properties, and the magnetism of POMs have been computationally examined [17,18,21,25]. Solvation effects on the properties of POMs were also explored in this way [28–30], including those of a surrounding electrolyte [29,30].

To the best of our knowledge, there is only one computational study on the redox properties of singly-substituted Keggin ions [31]. In that work, no explicit counterions were included in the model, and solvation of the highly charged POMs was modeled by the continuum COSMO model [32]. Such simplifications led to significant uncertainties in the absolute reduction potentials. However, shifts of the reduction potentials, relative to the unsubstituted Keggin ion, successfully reproduced the corresponding experimental trends [31]. A similar approach was used to study the redox properties of Dawson-type POMs [33,34].

The present computational study is motivated by experimental investigations on the Mn-redox behavior of tri-Mn-substituted W-based Keggin systems [13]. By means of density functional theory (DFT) calculations, we present a model study of the reversible half-wave redox potentials for two types of reactions, namely proton-coupled electron transfer in the case of Mn(IV/III) and cation-coupled electron transfer in the case of Mn(III/II). For achieving an adequate DFT energetics, we modeled the structure of these systems for various oxidation states of the Mn centers, and we explored structural aspects of the surrounding electrolyte as well as Mn-related standard reduction potentials and their relation to the experimentally measured reversible redox potentials. We also aimed at identifying a consistent DFT approach for modeling

absolute redox potentials by exploring several exchange-correlation functionals.

## 2. Models and Methods

### 2.1. Models of metal-substituted Keggin ions

The original Keggin ion has the general formula of  $[XM_{12}O_{40}]^n$ , with a heteroatom X at the center of a spherical arrangement of metal atoms M; its structure is referred to as **a**-ion [3]. Other isomers (**b**-, **g**-, etc.) are derived from this structure by successive rotations of  $W_3O_{13}$  units by 60° [35]. The present study addresses an **a**-Keggin ion with X = Si, M = W (fully oxidized), where three neighboring M centers directly above the triangular face of the central  $SiO_4$  tetrahedron are substituted by  $M^0 = Mn$ , the latter in oxidation states (IV), (III), or (II) (Fig. 1). Such a substitution pattern is referred to as A-type structure [36]. Fig. 1a shows a sketch of the calculated (optimized) structure of the fully oxidized system  $[Mn(IV)_3(OH)_3(OH)_3(A-a-SiW_9O_{34})]^{4-}$  [16]. Each Mn center exhibits one terminal OH ligand; among each other, the Mn centers are connected by bridging OH groups. Each Mn center is connected to a W center via a binding  $O_W$  center, and to Si via  $O_{Si}$  centers (Fig. 1a).

In an aqueous solution and in the crystal structure, the relatively high charge of the POM is neutralized by counterions. Following the experiment [13], we used  $Li^+$  as counterions. The reduction of Mn centers to oxidation state (III) is coupled with a proton transfer as demonstrated experimentally by the pH dependence of the redox potential for Mn(IV/III) [13]:

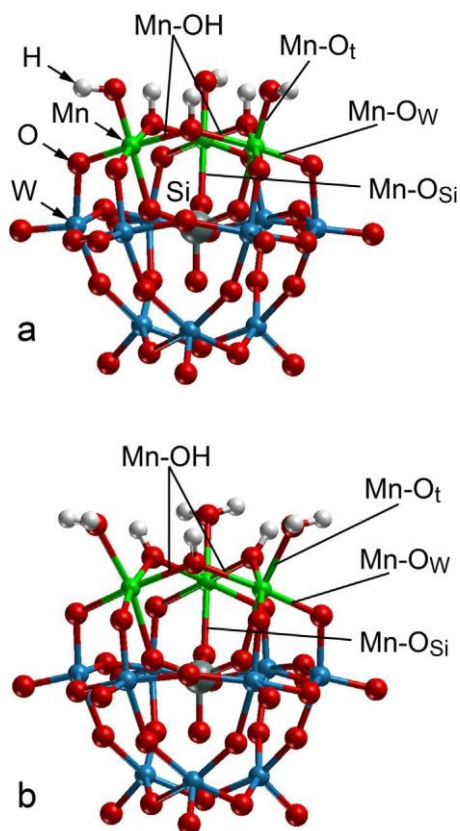
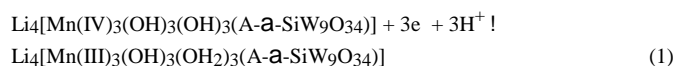
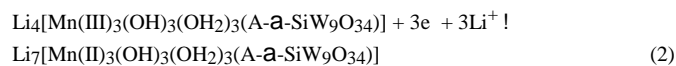


Fig. 1. Schematic representations of tri-Mn-substituted Keggin ions with important Mn-O bonds labeled: (a)  $[Mn(IV)_3(OH)_3]^{4-}$ , (b)  $[Mn(III)_3(H_2O)_3]^{4-}$ . Atom labels shown for structure a.

Therefore, after reducing all Mn centers to oxidation state (III), one obtains  $[\text{Mn(III)}_3(\text{OH})_3(\text{OH}_2)_3(\text{A-a-SiW}_9\text{O}_{34})]^{4-}$ , Fig. 1b. The most obvious difference to the POM with Mn(IV) centers are the terminal ligands, OH<sub>2</sub> instead of OH, of the Mn centers, Fig. 1. The systems with the three Mn centers further reduced corresponds to  $[\text{Mn(II)}_3(\text{OH})_3(\text{OH}_2)_3(\text{A-a-SiW}_9\text{O}_{34})]^{7-}$ :



This equation reflects the fact that almost constant values of the Mn(III/II) redox potential were measured over a pH range [13]. These findings suggested a cation-coupled electron transfer mechanism for the latter reduction process.

Eqs. (1) and (2) are written for a single transfer step of 3 e<sup>-</sup>, but in experiment electron transfer occurs in a one-by-one fashion [13]. At least for the reduction Mn(IV/III), these 1 e<sup>-</sup> transfer steps have been discriminated; see Fig. 3b in Ref. [13]. In the present study, we considered simplified models representing the simultaneous transfer of 3 e<sup>-</sup>; see Eqs. (1) and (2). We also tested non-symmetrical structures with only one or two Mn centers reduced. A charge analysis showed that the corresponding charges were well localized for all exchange-correlation functionals studied, including the generalized gradient approximation (GGA) PBE [37] where sometimes self-interaction artifacts are observed [38]. Then the redox potentials calculated for the transfer of a single e<sup>-</sup> (Section 3.3) have to be compared to suitable averages of experimental values. The corresponding experimental redox potentials, however, are rarely distinguished. For the system under study experiments revealed very close lying peaks, differing by 0.2 V only [13]. Therefore, it seemed justified to employ simplified models, formally connected by the simultaneous transfer of 3 e<sup>-</sup>. The fragment (A-a-SiW<sub>9</sub>O<sub>34</sub>) comprises the W centers and the central SiO<sub>4</sub> tetrahedron. This moiety does not participate directly in the redox reaction processes under study, Eqs. (1) and (2). For improved readability, we therefore will not carry this fragment in the labels used in the following. In the same spirit, we will also drop from the simplified labels the bridging OH groups connecting neighboring Mn centers. Hence, in the following, we will refer to the systems with all Mn centers in the same oxidation state as Li<sub>4</sub>[Mn(IV)<sub>3</sub>(OH)<sub>3</sub>], Li<sub>4</sub>[Mn(III)<sub>3</sub>(OH)<sub>2</sub>]<sub>3</sub>, and Li<sub>7</sub>[Mn(II)<sub>3</sub>(OH)<sub>2</sub>]<sub>3</sub>.

## 2.2. Computational Method

We carried out first-principles DFT calculations with the software package TURBOMOLE 6.6 [39–41]. We employed the GGA functional PBE [37] as well as the hybrid approaches B3LYP [42,43], PBE0 [44], and TPSSH [45]. To accelerate the DFT calculations, we applied the resolution-of-identity (RI-J) approximation for evaluating the Coulomb part of the electron-electron interaction together with a suitable auxiliary basis set [46]. We represented the Kohn-Sham orbitals using standard triple-zeta basis sets [47] together with effective core pseudopotentials for Mn [48] and W [49]. All systems studied are open-shell systems; therefore we used the unrestricted Kohn-Sham (UKS) formalism. In the geometry optimizations, the total energy was converged to 10<sup>-6</sup> au. For the structure optimizations, the energy gradients on all atomic centers were required to be less than 10<sup>-3</sup> au. All stationary structures of complexes in the gas phase were confirmed as local minima by a normal mode analysis.

The total Gibbs free energy *G* of a system was calculated as follows:

$$G = E_{\text{el}} + D_{\text{solv}} G + RT \ln(q_{\text{trans}} q_{\text{rot}} q_{\text{vib}}) \quad (3)$$

Here, *E<sub>el</sub>* is electronic energy of the system in the gas phase, *D<sub>G<sub>solv</sub></sub>* is the free energy of solvation; both quantities were evaluated for each of the functionals mentioned above. The thermochemistry was evaluated for room temperature, *T* = 298.15 K, and normal pressure, 1 atm. The term *RT ln(q<sub>trans</sub>q<sub>rot</sub>q<sub>vib</sub>)* accounts for thermal corrections to the enthalpy and entropic terms (including zero-point energy). The latter correction term in Eq. (3) was evaluated for structures in the gas phase, optimized at the PBE level, using harmonic vibrational frequencies; the same values were also applied for correcting the energy quantities determined with the hybrid functionals.

The free energy of solvation *D<sub>G<sub>solv</sub></sub>* was estimated using the polarized continuum solvation model COSMO as implemented in TURBOMOLE [32]. The solute was embedded in a dielectric medium, water in the present study. The dielectric constant of water was set to 78.4. The molecular cavity in the dielectric medium was constructed from overlapping spheres with radii *R<sub>i</sub>* + *R<sub>solv</sub>* for all atoms *i*. We used *R<sub>solv</sub>* = 130 pm and the atomic radii *R*(Si) = 220 pm, *R*(W) = *R*(Mn) = 222 pm, *R*(O) = 172 pm, *R*(H) = 130 pm, and *R*(Li) = 157 pm. More details on the construction of the cavity can be found in Ref. [32]. To reduce the uncertainties associated with the polarized continuum description of solvation

[50] (of small charged species), we used experimental values for the enthalpies of solvation of a proton, 1104.5 kJ mol<sup>-1</sup>, and of a Li<sup>+</sup> ion, 519 kJ mol<sup>-1</sup> [51,52], when deriving the corresponding free energies of solvation.

Model-related computational details describing how we calculated the redox potentials are given below in the corresponding sections.

## 3. Results and Discussion

An important aspect of modeling POMs and their redox potentials is the role of the counterions in the surrounding electrolyte, or, in other words, the screening effect of the electrostatic field due to the electrolyte. The (average) number of counterions in the immediate vicinity of the POM is estimated from the charge of the POM, i.e. the number of Li<sup>+</sup> counterions to render the nanooxidic cluster plus its immediate environment neutral. The interaction of various Keggin ions with their surrounding counterions in aqueous solution has been studied by means of molecular dynamics simulations using a force field

[29]. These simulations showed that POMs and counterions may form configurations in analogy to contact ion pairs (inner-sphere interaction) as well as configurations in analogy to solvent-separated ion pairs (outer-sphere interaction). We decided to include the counterions into our quantum chemical model cluster, thus representing inner-sphere adsorbed Li<sup>+</sup> ions. For test purposes, we also calculated redox potentials for bare (and therefore highly charged) substituted Keggin ions and obtained a negative value for the reduction potential of the Mn(III/II) reduction. In view of this artifact, we decided to include explicitly an appropriate number of counterions in the models.

Section 3.1 describes various arrangements of the Li counter-ions chosen around the POM structure. In Section 3.2 we present the calculated results for the structural parameters of the neutral POMs and their dependence on the Li arrangements. In Section 3.3 we discuss how the Li cation arrangements affect the calculated standard redox potentials. Finally, in Section 3.4, we compare the calculated results for reversible redox potentials with experiment.

### 3.1. Distributing Li counterions on the surface of a Keggin ion

The models of tri-Mn-substituted POMs studied here exhibit 4 Li<sup>+</sup> counterions for the structures with Mn(IV) and Mn(III) centers and 7 Li<sup>+</sup> counterions for the structures with the fully reduced

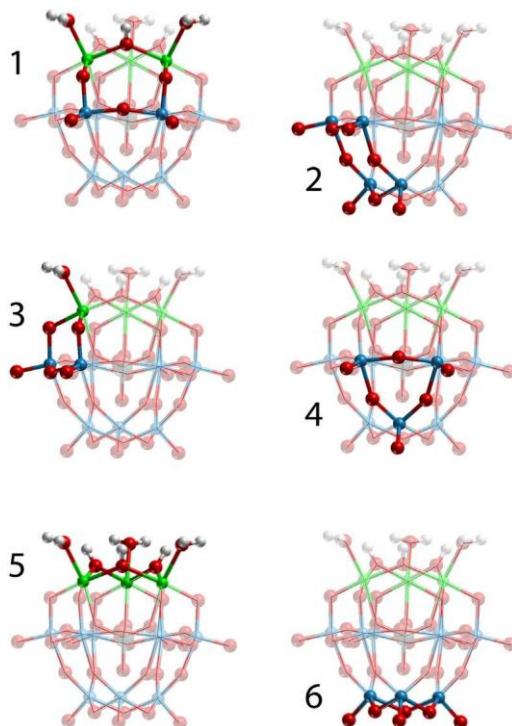


Fig. 2. Schematic representation of sites 1 to 6, for  $\text{Li}^+$  inner-sphere adsorption on the tri-Mn-substituted Keggin ion  $[\text{Mn}(\text{III})_3(\text{H}_2\text{O})_3]^{4-}$  as example.

centers Mn(II). To explore the effect of how the Li cations are distributed around the POM structure within the present computational approach and to understand which sites on the surface of the tri-Mn-substituted POM anions under study may be occupied by Li ions, we first calculated the energies of a single  $\text{Li}^+$  ion at six sites on the surface of this POM structure (Fig. 2). As discussed in Section 2, we focused on models where the three Mn centers were uniformly in one of the three oxidation states under study. On the surface of a tri-Mn-substituted Keggin ion, there are two 4-fold hollow sites (pockets), namely site 1 and site 2 (Fig. 2); these sites exhibit four nearby O centers of POM surface that are able to coordinate a Li cation. Sites 3 to 6 are 3-fold hollow sites, with three nearby O centers for Li coordination.

To quantify the site stability, we estimated binding energies  $E_b$  of a Li cation to POM as the reaction energy of the following formal transformation:

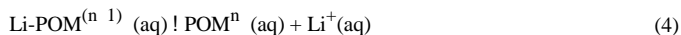


Table 1 collects the corresponding  $E_b$  values for  $\text{Li}[\text{Mn}(\text{IV})_3(\text{OH})_3]^{3-}$ ,  $\text{Li}[\text{Mn}(\text{III})_3(\text{OH}_2)_3]^{3-}$ , and  $\text{Li}[\text{Mn}(\text{II})_3(\text{OH}_2)_3]^{6-}$ . The cation  $\text{Li}^+$  always binds stronger to a specific site of  $[\text{Mn}(\text{II})_3(\text{OH}_2)_3]^{7-}$  than to the analogous sites of  $[\text{Mn}(\text{III})_3(\text{OH}_2)_3]^{4-}$  and  $[\text{Mn}(\text{IV})_3(\text{OH})_3]^{4-}$ , because of the Coulomb interaction. The total formal charge of the bare Keggin ion is 7 e of Mn(II) centers and 4 e in the case of Mn(III) and Mn(IV). For all sites except site 5, the binding strength increases when Mn is reduced. For example, Li binds with  $E_b = 0.90$  eV to site 1 of  $[\text{Mn}(\text{IV})_3(\text{OH})_3]^{4-}$ , with  $E_b = 1.06$  eV to the analogous site of  $[\text{Mn}(\text{III})_3(\text{OH}_2)_3]^{4-}$ , and with  $E_b = 1.62$  eV to  $[\text{Mn}(\text{II})_3(\text{OH}_2)_3]^{7-}$ . At site 5,  $\text{Li}^+$  binds stronger to  $[\text{Mn}(\text{IV})_3(\text{OH})_3]^{4-}$ ,  $E_b = 1.03$  eV, than to  $[\text{Mn}(\text{III})_3(\text{OH}_2)_3]^{4-}$ ,  $E_b = 0.90$  eV. In that case, the terminal OH ligands of  $[\text{Mn}(\text{IV})_3(\text{OH})_3]^{4-}$  coordinate to  $\text{Li}^+$  ( $\text{Li-O}_t = 282$  pm) in addition to the bridging hydroxyls ( $\text{Li-OH}_b = 202$  pm) and thus render the binding of the counterion with the POM overall stronger. In contrast,  $[\text{Mn}(\text{III})_3(\text{OH}_2)_3]^{4-}$  exhibits  $\text{OH}_2$  terminal ligands and therefore is able to provide only weaker coordinative bonds to a Li cation at site 5

( $\text{Li-O}_t = 294$  pm,  $\text{Li-OH}_b = 202$  pm). Note that these effects in part are a consequence of our model which does not offer any explicit solvation by water molecules. In a more realistic model, the terminal OH ligands would be shielded ("saturated") by nearby solvation water molecules. Therefore, we consider the unusual trend for site 5 as a model artifact.

Next, we compare the binding energies at different sites for a given structure with a uniform oxidation state of the Mn centers. For each oxidation state, sites 3, 4, and 6 are less favorable than the other sites (Table 1). For  $[\text{Mn}(\text{IV})_3(\text{OH})_3]^{4-}$  the most favorable Li position is site 5 with  $E_b = 1.03$  eV (Table 1) which may reflect some aspects of the model, as just discussed. Sites 1 and 2 are rather close in energy, 0.90 and 0.81 eV, with site 1 being slightly favored. For  $[\text{Mn}(\text{III})_3(\text{OH}_2)_3]^{4-}$ , site 2 is the most favorable site for coordinating a single  $\text{Li}^+$ ,  $E_b = 1.10$  eV, site 1 is only 0.04 eV less favorable. Site 5 is 0.20 eV less favorable, compared to site 2 (Table 1). In conclusion, for both  $[\text{Mn}(\text{IV})_3(\text{OH})_3]^{4-}$  and  $[\text{Mn}(\text{III})_3(\text{OH}_2)_3]^{4-}$ , we consider sites 1 and 2 as primary Li locations.

On the surface of the POM, there are three sites 1 and three sites 2, to be occupied by 4 Li cations, thus giving rise to several arrangements of Li counterions. We examined four of them, Fig. 3a–d. First, we assumed that all three sites 1 are occupied by Li cations, and the fourth Li occupies site 2 (Fig. 3a). We refer to this arrangement by the label  $1_32_1$  and we assume that the three structures of this type are essentially equivalent. A structurally different arrangement is  $1_12_3$ , with three sites 2 and one site 1 occupied by  $\text{Li}^+$  (Fig. 3b). In addition, we studied configurations

Table 1  
Calculated binding energies<sup>a</sup>  $E_b$  (in eV) for a single Li cation probed on six sites of a tri-Mn-substituted Keggin ion with Mn in oxidation states (IV), (III), and (II).

Site <sup>b</sup>	1	2	3	4	5	6
Mn(IV)	0.90	0.81	0.62	0.53	1.03	0.24
Mn(III)	1.06	1.10	0.86	0.84	0.90	0.47
Mn(II)	1.62	1.59	1.16	1.26	1.64	0.90

<sup>a</sup> Results for the PBE exchange-correlation functional.

<sup>b</sup> For the site designations, see Fig. 2.

where two Li cations adsorb at sites 1 and two more at sites 2. There are two such isomers, with the Li cations positioned in symmetric or antisymmetric fashion (Fig. 3c, d), labeled 1222 sym and 1222 asym. We probed these four Li arrangements for both  $\text{Li}_4[\text{Mn(IV)}_3(\text{OH})_3]$  and  $\text{Li}_4[\text{Mn(III)}_3(\text{OH}_2)_3]$ .

On the surface of  $[\text{Mn(II)}_3(\text{OH}_2)_3]^{7-}$ , sites 1, 2, and 5 exhibit rather similar binding energies  $E_b$  per Li cation, between 1.59 eV and 1.64 eV (Table 1). Therefore, one may assume all seven available sites of types 1, 2, and 5 to be occupied by 7  $\text{Li}^+$

counterions, required for a charge balance of  $[\text{Mn(II)}_3(\text{OH}_2)_3]^{7-}$ . In this case we studied arrangement 132351 with 7 Li occupying sites 1, 2, and 5 (Fig. 3e). In addition, we optimized the structure where site 6 occupied instead of site 5, i.e., arrangement 132361 (Fig. 3f).

### 3.2. Structural parameters of the neutral oxide moiety

For each POM with a uniform oxidation state of the Mn centers, Table 2 presents results of PBE calculations for important

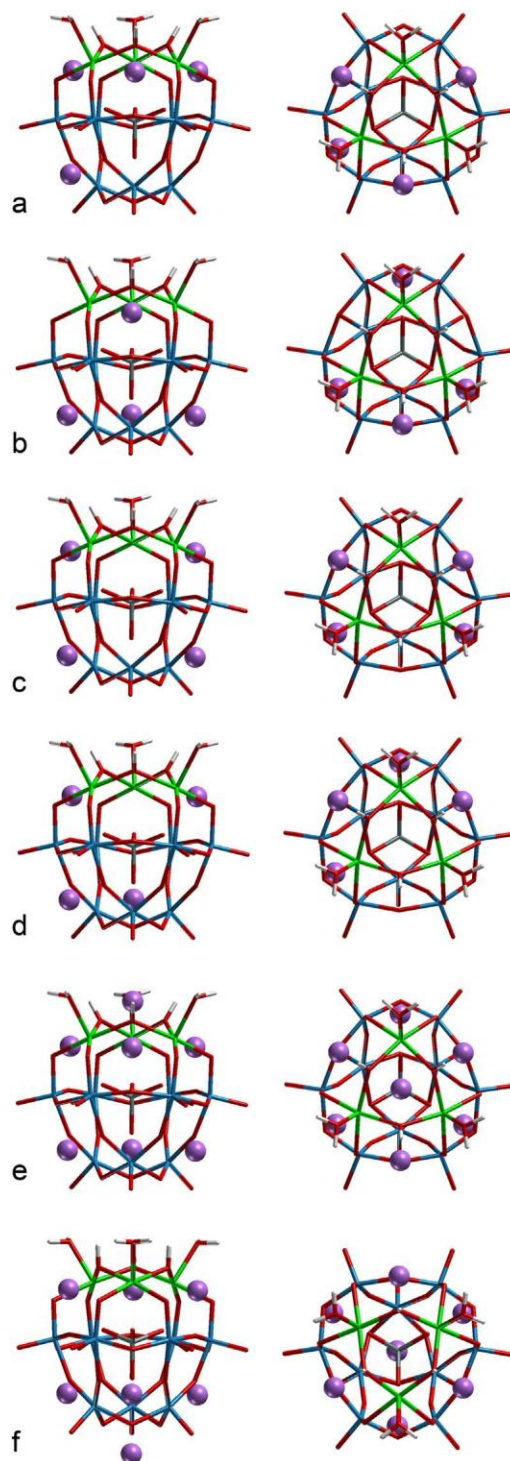


Fig. 3. Schematic representation of various Li arrangements for  $\text{Li}_4[\text{Mn(IV)}_3(\text{OH})_3]$  and  $\text{Li}_4[\text{Mn(III)}_3(\text{OH}_2)_3]$  systems: (a) 1321, (b) 1123, (c) symmetric arrangement 1222 sym, (d) antisymmetric arrangement 1222 asym. Analogous sketches for  $\text{Li}_7[\text{Mn(II)}_3(\text{H}_2\text{O})_3]$  system: (e) 132351 and (f) 132361. Left column side view, right column top view. Li ions are shown as spheres, while the POM structure is represented by lines. For the atom labels, see Fig. 1.

Table 2  
Structure parameters<sup>a</sup> (in pm) of Li<sub>4</sub>[Mn(IV)<sub>3</sub>(OH)<sub>3</sub>], Li<sub>4</sub>[Mn(III)<sub>3</sub>(OH<sub>2</sub>)<sub>3</sub>], and Li<sub>7</sub>[Mn(II)<sub>3</sub>(OH<sub>2</sub>)<sub>3</sub>] for various Li arrangements, calculated at the PBE level of theory. Relative total energies E<sub>rel</sub> (in eV) are also given. For the site designations, see Figs. 2 and 3.

	Ion configuration	Mn-O <sub>t</sub>	Mn-OH	Mn-O <sub>w</sub>	Mn-O <sub>Si</sub>	E <sub>rel</sub>
Li <sub>4</sub> [Mn(IV) <sub>3</sub> (OH) <sub>3</sub> ]	1321	180(0)	202(1)	186(1)	204(0)	0.00
	1123	180(0)	198(2)	188(2)	205(1)	0.23
	1222, sym	180(0)	201(2)	187(2)	205(1)	0.15
	1222, asym	180(0)	201(2)	187(2)	205(1)	0.16
	Average	180(0)	201(2)	187(1)	205(1)	
Li <sub>4</sub> [Mn(III) <sub>3</sub> (OH <sub>2</sub> ) <sub>3</sub> ]	1321	226(0)	204(0)	190(1)	221(0)	0.15
	1123	225(0)	200(2)	192(2)	222(1)	0.00
	1222, sym	226(0)	202(3)	191(1)	221(0)	0.21
	1222, asym	225(0)	202(2)	191(2)	221(0)	0.04
	Average	225(1)	202(2)	191(1)	221(1)	
	Exp. <sup>b</sup>	217(2)	194(1)	192(2)	225(3)	
Li <sub>7</sub> [Mn(II) <sub>3</sub> (OH <sub>2</sub> ) <sub>3</sub> ]	132351	225(0)	221(0)	211(0)	230(0)	0.02
	132361	227(0)	213(0)	219(0)	232(0)	0.00
	Average	226(1)	217(4)	215(4)	231(1)	
	Exp. <sup>b</sup>	217(0)	201(1)	198(1)	233(0)	

<sup>a</sup> Mn-O<sub>t</sub> bonds to the terminal ligand, H<sub>2</sub>O for Mn(II) and Mn(III), OH for Mn(IV), Mn-OH bonds to the bridging OH groups, Mn-O<sub>w</sub> bonds to the O centers connecting Mn and W, Mn-O<sub>Si</sub> bonds to the O centers of the central Si tetrahedron.

<sup>b</sup> Ref. [16].

structural parameters of optimized structures, representing isomers of various Li arrangements, together with the total energy differences E<sub>rel</sub> relative to the most stable isomer. Bond lengths are averaged over all incidents: Mn-O<sub>t</sub> and Mn-O<sub>Si</sub> are averaged over 3 values, Mn-OH and Mn-O<sub>w</sub> over 6 values; standard deviations are given in parentheses. For each oxidation state of Mn, the relative energies among the isomers differ at most by 0.23 eV. This suggests that all these arrangements may coexist in solution. For the POM with Mn(IV) the most favorable structure is the one with the Li arrangement 1321; Li prefers the site 1, close to Mn centers (Fig. 2). The least favorable structure is the one with the Li arrangement 1123 where three Li cations occupy sites of type 2 and only one a site of type 1. For the POM with Mn(III) the energetic preference is opposite: arrangement 1123 is favored over 1321 (Table 2). Interestingly, both arrangements studied, 132351 and 132361 for the POM with Mn(II), are very close in energy, differing by only 0.02 eV in total energy. Although a single Li cation clearly favors site 5 over site 6, the two structures with seven Li cations are essentially degenerate in energy.

The arrangement of the Li counterions only slightly affects the Mn-O distances of the POMs with Mn in oxidation states (IV) and (III). For Li<sub>4</sub>[Mn(IV)<sub>3</sub>(OH)<sub>3</sub>] the average Mn-O<sub>t</sub> bond lengths are not affected by the Li arrangement; it is 180 pm without any standard deviation for all arrangements studied. The average values of Mn-O<sub>w</sub> and Mn-O<sub>Si</sub> do not exceed 2 pm among the various arrangements of the counterions (Table 2), and the corresponding standard deviations are at most 2 pm. The average Mn-O<sub>w</sub> distances of the O bridges to the W centers vary in a similarly narrow margin, from 186(1) pm to 188(2) pm; the Mn-O<sub>Si</sub> bonds are equally stable, between 204(0) and 205(1) pm.

The most sensitive structure parameter of the Keggin ions is the Mn-OH bond to the bridging OH group. It is calculated at 202(1) pm for 1321 and at 198(2) pm for 1123 (Table 2). The bridging OH ligands coordinate to Li cations when they occupy sites 1. Therefore, changes in the average Mn-OH bonds reflect some bond competition. When 3 Li ions occupy sites 1 and coordinate to all three bridging OH, the corresponding average Mn-OH is 202.1 pm. In contrast, when only one site 1 is occupied, together with the three sites 2, the average Mn-OH distance is 4 pm shorter, 198.2 pm (Table 2). For the arrangements 1222, both sym and asym, when two Li<sup>+</sup> occupy sites 1, the average Mn-OH results in an intermediate value, 201(2) pm. Assuming that all arrangements are present in solution to similar amounts allows one to average

over all Li arrangements. The resulting averaged bond distances are also given in Table 2. The largest standard deviation, 2 pm, is again calculated for the Mn-OH bonds.

Similar trends as for Mn(IV) are obtained for the system Li<sub>4</sub>[Mn(III)<sub>3</sub>(OH<sub>2</sub>)<sub>3</sub>]. None of the standard deviations exceeds 3 pm (Table 2). The average values of Mn-O<sub>w</sub> and Mn-O<sub>Si</sub> vary by 2 pm at most. The largest deviations again result for Mn-OH bond, 4 pm (Table 2), between the Li arrangements 1321 and 1123, due to bond competition as just discussed. In contrast to Mn(IV), the Mn-O<sub>t</sub> distance of the Mn(III) systems is notably larger, varying from 225(0) pm to 226(0) pm. This is a consequence of the fact that, for Mn(III), the distance Mn-O<sub>t</sub> represents a coordinative bond of an aqua ligand whereas for Mn(IV) this distance is a bond to an OH ligand. The weaker (and longer) Mn-O<sub>t</sub> bonds to H<sub>2</sub>O ligands are more prone to vary, compared to the stronger (and shorter) Mn-O<sub>t</sub> bonds to OH ligands.

The averaged Mn-OH and Mn-O<sub>w</sub> bond lengths also increase when Mn is reduced from (IV) to (III), but only slightly, by 1 pm and 4 pm, respectively (Table 2). Interestingly, the averaged Mn-O<sub>Si</sub> distance increases by 16 pm when Mn is reduced from (IV) to (III). It is one of the longest Mn-O bonds and therefore more prone to react to the change of Mn charge. When the charge of the Mn center is decreased from +4 to +3 (reduction), this coordinative Mn-O<sub>Si</sub> bond to the central [SiO<sub>4</sub>]<sup>4-</sup> fragment naturally gets longer.

Structural changes due to different Li<sup>+</sup> arrangements are more pronounced for Li<sub>7</sub>[Mn(II)<sub>3</sub>(H<sub>2</sub>O)<sub>3</sub>]. While the Mn-O<sub>t</sub> and Mn-O<sub>Si</sub> bond lengths vary by 2 pm, the Mn-OH and Mn-O<sub>w</sub> change significantly, when only one Li<sup>+</sup> changes its position, from site 5 to site 6. The distance Mn-OH is 8 pm longer for the arrangement 132351, compared to 132361. The bridging OH moieties for Li<sup>+</sup> occupying site 5, exhibit longer Mn-OH distances for 132351. The average distance Mn-O<sub>w</sub> shows the opposite trend; it is shorter for the arrangement 132351, 211(0) pm, and 8 pm longer for 132361 (Table 2). Averaging over these Li arrangements results in the largest standard deviations, 4 pm for the distances Mn-OH and Mn-O<sub>w</sub>; the distances Mn-O<sub>t</sub> and Mn-O<sub>Si</sub> exhibit standard deviations of 1 pm.

All calculated Mn-O distances, except Mn-O<sub>t</sub>, increase when Mn is reduced from (III) to (II). Averaged Mn-OH, Mn-O<sub>w</sub>, and Mn-O<sub>Si</sub> increase by 15 pm, 24 pm, and 10 pm, respectively (Table 2). The charge of the Mn centers decreases from +3 e to +2 e under the reduction (III/II) and one can expect Mn-O bonds to elongate due to lower Coulomb attraction. However, the Mn-O<sub>t</sub> distance to the

terminal OH<sub>2</sub> ligands almost does not change in this situation; it is 225.1 pm on average for the POM with Mn(III) and 226.1 pm for the POM with Mn(II). The same trend is observed in experiment (discussed below) [16]. The reason for such structural invariance is unclear.

To identify potential effects of various exchange-correlation functionals on the structure parameters of the POMs, we analyzed and compared the structural parameters obtained from calculations with the functionals B3LYP, PBE0, and TPSSh; see Table S1 of the Supplementary Data (SD). Overall, the effect of the exchange-correlation functional on the structures is rather small. Average bond lengths vary at most by 3 pm. PBE and B3LYP results are slightly longer, by 1–2 pm, than the results of PBE0 and TPSSh calculations. Previous studies found that experimental structural parameters of Keggin-type polyoxometalates are best reproduced in PBE0 calculations [17,18]. However, the average absolute errors of the functionals PBE0, B3LYP, and PBE, do not exceed 3 pm [17,18]. In conclusion, calculations with GGA and various hybrid functionals yield rather similar structural parameters, in contrast to the resulting energy characteristics [17,18]. In consequence, we refrain from comparing here the structural results for the POMs calculated with hybrid methods; for details, see the SD.

Tri-Mn-substituted Keggin ions with Mn in oxidation states (II) and (III) were synthesized and characterized by Al-Oweini et al. [16]. The experimentally determined bond lengths are also given in Table 2, for comparison. For Li<sub>4</sub>[Mn(III)<sub>3</sub>(OH<sub>2</sub>)<sub>3</sub>], the distances Mn-O<sub>w</sub> and Mn-O<sub>s</sub>i are very well reproduced (Table 2), while calculated distances Mn-O<sub>t</sub> and Mn-OH are overestimated by 8 pm at the PBE level. For Li<sub>7</sub>[Mn(II)<sub>3</sub>(OH<sub>2</sub>)<sub>3</sub>] only the Mn-O<sub>s</sub>i distance is well reproduced. The calculated Mn-O<sub>t</sub> distance are 9 pm longer than the corresponding experimental value. The distances Mn-OH and Mn-O<sub>w</sub> deviate even more from experiment; they are calculated 16–17 pm longer (Table 2). Note that the experiment examined crystal structures where several POMs are linked to each other by counterions, K<sup>+</sup> and Na<sup>+</sup> [16]. In our model calculations we addressed systems in aqueous solution, employing a polarizable continuum method to represent the solvent; no interaction among POMs is taken into account. Not unexpectedly, only Mn-O<sub>s</sub>i bonds are well reproduced for both types of POMs; these bonds are not directly affected by the electrolyte surrounding the POMs.

However, the calculated distances reproduce trends of experimental structural parameters that occur upon reduction Mn(III/II). For such a reduction, the experimental distances Mn-O<sub>t</sub> does not change, just as the calculated Mn-O<sub>t</sub> values which change by 1 pm only. Mn-O<sub>s</sub>i bond lengths increase due to Mn reduction by 8 pm in experiment and by 10 pm in our calculations (Table 2). The experimental distances Mn-OH and Mn-O<sub>w</sub> increase by 6–7 pm, the calculated values increase by 20 pm (Table 2).

Thus, our analysis of structural parameters of POMs with Mn in various oxidation states has shown that most Mn-O bonds do not vary much among different Li arrangements. The exchange-correlation approximation also hardly affects the Mn-O bonds, by 2–3 pm on average. Our findings agree with those of earlier studies on POMs [17,18] where similarly small variations of structure parameters had been determined for different exchange-correlation functionals. This similarity did not carry over to calculated chemical shifts [18] and energies of frontier molecular orbitals [17]. The present comparison with experimental crystal structure data showed that the structural changes due to Mn(III/II) reduction are well reproduced by the model calculations. However, most calculated Mn-O distances are overestimated compared to experiment, with the exception of the Mn-O<sub>s</sub>i bonds that are not directly affected by the counterions and the surrounding solvent. These latter findings may be a harbinger for the need to strive ultimately for a more sophisticated modeling of the interaction of a POM with its electrolyte environment.

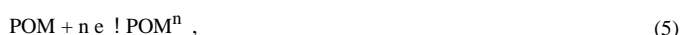
Table 3

Standard reduction potentials  $U_{\text{red}}^0$  vs NHE (eV) for the redox processes Mn(IV/III) and Mn(III/II), estimated from Eq. (6), calculated at various levels of theory: PBE, B3LYP, PBE0, and TPSSh. Also shown are the average values  $\langle U_{\text{red}}^0 \rangle$  over the various Li arrangements. For the site designations, see Figs. 2 and 3.

	Ion configuration	PBE	TPSSh	B3LYP	PBE0
Mn(IV/III)	1321	0.86	1.25	1.66	1.78
	1123	0.81	1.17	1.60	1.71
	1222, sym	0.85	1.21	1.63	1.74
	1222, asym	0.85	1.21	1.63	1.75
	$\langle U_{\text{red}}^0 \rangle$	0.84 0.03	1.21 0.04	1.63 0.04	1.74 0.04
Mn(III/II)	1321	0.44	0.78	1.12	1.24
	1123	0.33	0.65	1.00	1.11
	1222, sym	0.43	0.70	1.05	1.16
	1222, asym	0.36	0.68	1.04	1.15
	$\langle U_{\text{red}}^0 \rangle$	0.39 0.07	0.70 0.08	1.05 0.07	1.16 0.08

### 3.3. Standard reduction potentials

Having clarified structural aspects of the tri-Mn-substituted Keggin ion and its electrolyte environment, we now turn to determining electrochemistry characteristics and how they are affected by the Li arrangements. From the reaction free energy change  $\Delta G$  of the reaction



we calculate the standard reduction potential

$$U_{\text{red}}^0 = \frac{\Delta G}{nF} \approx \frac{\delta \epsilon}{nF}$$

Here,  $F$  is the Faraday constant and  $n$  the number of electrons transferred,  $n = 3$  in the present case. We determine reduction potentials with respect to the normal hydrogen electrode (NHE), with the reduction potential  $U(\text{NHE}) = 4.28$  eV [53]. Table 3 provides the values  $U_{\text{red}}^0$  vs NHE for the reduction steps Mn(IV/III) and Mn(III/II), assuming various arrangements of the Li counterions and for the exchange-correlation functionals selected for this study.

Similar to the structure characteristics, also the standard reduction potentials are rather similar for all Li arrangements studied if evaluated at the same level of theory (Table 3). However, these values vary notably among the different exchange-correlation approximations used, in contrast to the calculated structural parameters. At a given level of theory, the calculated values  $U_{\text{red}}^0$  for the reduction Mn(IV/III) vary by up to 0.08 eV among the Li arrangements examined. The standard reduction potentials  $U_{\text{red}}^0$  evaluated for the reduction step Mn(III/II) vary somewhat more, by up to 0.11–0.13 eV (Table 3). The largest value  $U_{\text{red}}^0$  is always calculated for the counterion arrangement 1321, and the lowest one for the arrangement 1123; the value  $U_{\text{red}}^0$  obtained with the two arrangements 1222 lie in between and are very similar (Table 3). In view of the rather small deviations, one may also discuss average values  $\langle U_{\text{red}}^0 \rangle$  of the standard reduction potentials over the various Li arrangements studied (Table 3).

With the pure GGA functional PBE, one estimates the lowest values  $\langle U_{\text{red}}^0 \rangle = 0.84$  0.03 eV for the reduction Mn(IV/III) (Table 3). A notably larger value  $\langle U_{\text{red}}^0 \rangle = 1.21$  0.04 eV is calculated using the hybrid functional TPSSh. The two other hybrid functionals, B3LYP and PBE0, yield even larger values  $\langle U_{\text{red}}^0 \rangle$ , 1.63 0.04 eV and 1.74 0.04 eV, respectively (Table 3). Thus, one finds an interesting trend: the value  $\langle U_{\text{red}}^0 \rangle$  increases with the fraction of the exact exchange in the functional. The pure GGA functional PBE does not contain any exact exchange and yields the lowest reduction potential. The hybrid functionals TPSSh, B3LYP, and PBE0 feature 10%, 20%, and 25% of exact exchange, respectively.



The corresponding averages  $\langle U_{\text{red}}^0 \rangle$  of the reduction potentials increase in the same order (Table 3).

A similar trend in  $\langle U_{\text{red}}^0 \rangle$  is observed for the reduction step Mn (III/II). The PBE calculations yield the lowest value,  $\langle U_{\text{red}}^0 \rangle = 0.39$  0.07 eV. The results for the hybrid functionals again increase in the order TPSSh, B3LYP, and PBE0, namely 0.70 0.08 eV, 1.05 0.07 eV, and 1.16 0.08 eV, respectively (Table 3). This effect of the amount of exact exchange on calculated redox potentials has previously been noted for the Mn center of superoxide dismutase [19]; in that case, the hybrid B3LYP functional yields a redox potential that is 0.6 eV larger than the corresponding PBE result [19].

The standard oxidation potential  $U_{\text{ox}}^0$  can be calculated in an analogous fashion:



$$U_{\text{ox}}^0 = \frac{\text{DG}}{nF} \quad (8)$$

To facilitate comparison with experiments, more precisely with the measured reversible half-wave potential  $U_{\text{rev}}$ , one has to take the average of  $U_{\text{red}}^0$  and  $U_{\text{ox}}^0$ . As test, we calculated  $U_{\text{ox}}^0$  for the oxidation Mn(III/IV) of the Li arrangement 1321: 1.96 eV for PBE and 2.80 eV for B3LYP. Therefore, the estimated reversible half-wave potential  $U_{\text{rev}}$  for the redox process Mn(IV/III) is 1.41 eV at the PBE level and 2.23 eV at the B3LYP level. The experimental value changes from 0.85 eV to 1.05 eV for pH values ranging from 6.0 to 4.2 [13]. Both results, from PBE and B3LYP calculations overestimate the experimental values quite notably, by at least 0.4 eV and 1.2 eV, respectively.

The computational approach just described for estimating redox potentials is rather straightforward, but it has notable disadvantages. Foremost, the computational procedure does not account for any pH dependence. First,  $U^0$  depends on solvation energies of the charged species as can be seen from Eqs. (5) and (7). We used the COSMO approach for calculating free energies of solvation. The accuracy of this method is known to deteriorate for systems with high molecular charge (3 e in our case) due to incomplete description of electrostatics, hydrogen bonds, dispersion, and other solvation effects [50]. Thus, inaccuracies in  $\text{DG}_{\text{solv}}$  calculations can be a limiting factor for a quantitative prediction of redox potentials, when highly charged species are involved. Another factor affecting the accuracy of calculated redox potentials is the mechanism of the redox reaction, e.g., a protonation of the reduced POMs, or a deprotonation of the oxidized species. Taking this into account will also introduce a pH dependence which is missing so far in modeling but seen in experiment [13]. The next section, focusing on a comparison of calculated and measured redox potentials, describes alternative ways for estimating the reversible potential  $U_{\text{rev}}$  as measured in cyclic voltammetry.

#### 3.4. Comparison with experiment

The measured reversible half-wave redox potentials,  $E_{\text{rev}}$ , [13] (we use E to distinguish experimental potentials from calculated ones to which we refer as U) do not only depend on the electron transfer itself, but also on other processes occurring simultaneously in the solution. For the reduction Mn(IV/III), the proton transfer accompanying the electron transfer has to be taken into account, while for the reduction Mn(III/II) the cation transfer should be accounted for. To include the redox mechanism in the model, we take the Gibbs free energies of the full reduction reactions, Eqs. (1) and (2), that directly include proton/cation transfer. We use these free energy values in Eq. (6) to obtain the standard reduction potentials,  $U_{\text{red}}^0$ . Eqs. (1) and (2) correspond to

Table 4

Calculated reversible redox potentials<sup>a</sup>  $U_{\text{rev}}$  vs. NHE (eV) for the cation-coupled redox process Mn(III/II), estimated from Eqs. (2) and (6), for results obtained at various levels of theory: PBE, TPSSh, B3LYP, and PBE0.

Initial configuration <sup>b</sup>	PBE	TPSSh	B3LYP	PBE0	Exp. <sup>c</sup>
1321	0.32, 0.34	0.68, 0.70	1.04, 1.06	1.17, 1.20	
1323	0.28, 0.30	0.63, 0.65	0.99, 1.01	1.12, 1.14	
1222, sym	0.36, 0.38	0.66, 0.67	1.01, 1.03	1.15, 1.17	
1222, asym	0.29, 0.31	0.65, 0.66	1.00, 1.03	1.14, 1.16	
$\langle U_{\text{rev}} \rangle$ <sup>d</sup>	0.32 0.04	0.66 0.02	1.02 0.02	1.16 0.03	0.65

<sup>a</sup> The first value of each entry refers to the Li arrangement 132351 in the final state of Eq. (2), Li7[Mn(II)3(OH)2]3, the second value to the Li arrangement 132361; see Figs. 2 and 3.

<sup>b</sup> Initial arrangement of the Li counterions.

<sup>c</sup> Ref. [13].

<sup>d</sup> Average result of all Li arrangements studied, including the standard deviation.

the reduction process; the corresponding oxidation process can be described by the reversed equations. Then, with Eq. (8), one obtains the standard oxidation potential  $U_{\text{ox}}^0$ . Yet, the corresponding Gibbs free energies differ only by the sign which cancels out in Eq. (8). Therefore the standard  $U_{\text{red}}^0$  and  $U_{\text{ox}}^0$  calculated from the full reactions will be the same. Therefore, we drop the subscripts and simply write  $U^0$ . Next, we apply the Nernst equation, which relates the cell potential to the standard potential and to the activities of the electroactive species [54]:

$$U = U^0 - \frac{RT}{nF} \ln Q \quad (9)$$

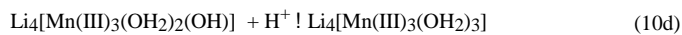
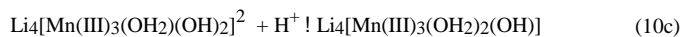
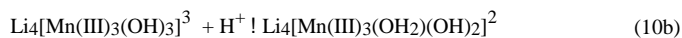
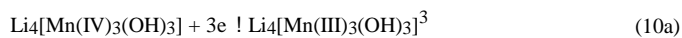
Here, U is the redox potential at the temperature T of interest,  $U^0$  is the standard redox potential, Q is the reaction quotient, i.e., the ratio of activities of products and reactants of the reaction; activities are commonly replaced by concentrations [54]. Recall that the half-wave potential  $E_{\text{rev}}$  measured by cyclic voltammetry corresponds to the condition, at which the concentrations of oxidants and reductants are equal; to the redox potential at this condition, we refer to as  $U_{\text{rev}}$ . We will first discuss the redox process Mn(III/II). Subsequently, we will turn to the process Mn(IV/III).

When considering Eq. (2) to describe the redox process Mn(III/II), one should recall that the experimental concentration of  $\text{Li}^+$  is 1 M [13]. Therefore, Q = 1 when the concentration of the oxidant is equal to the concentration of the reductant and the Nernst correction vanishes. Hence, for Mn(III/II),  $U^0$  represents the computationally estimated  $U_{\text{rev}}$  and can be directly compared to the experimentally measured value  $E_{\text{rev}}$ .

In Table 4 we present this direct comparison of the calculated  $U_{\text{rev}}$  to the measured results for the redox process Mn(III/II), for all Li ion configurations in the initial as well as the final state of Eq. (2). For each functional, the calculated redox potentials  $U_{\text{rev}}$  vary at most by 0.1 eV, from 0.28 to 0.38 eV for PBE, from 0.63 to 0.70 eV for TPSSh, from 0.99 to 1.06 eV for B3LYP, and from 1.12 to 1.20 eV for PBE0 (Table 4). Thus, for a chosen exchange-correlation potential, the Li arrangement does not affect the value  $U_{\text{rev}}$  in a significant way. Not unexpectedly (Section 3.3), the PBE functional yields the lowest average value for the reversible potential,  $U_{\text{rev}} = 0.32$  0.04 eV. The largest such value was calculated with the PBE0 functional,  $U_{\text{rev}} = 1.16$  0.03 eV. The functionals TPSSh and B3LYP yield intermediate values of  $U_{\text{rev}}$ , 0.66 0.02 and 1.02 0.02 eV, respectively. The best agreement with the measured redox potential  $E_{\text{rev}}$  of 0.65 eV [13] is obtained with the functional TPSSh (Table 4). The PBE results underestimate the experimental result by 0.3 eV, while both B3LYP and PBE0 results overestimate the experiment by 0.4–0.5 eV (Table 4).

The situation is different in the case of the redox process Mn(IV/III) because Q for the reaction described in Eq. (1) deviates from 1 due to the variable proton concentration (pH of the solution). For

estimating the reversible redox potential  $U_{\text{rev}}$  of the proton-coupled redox process, we consider a step-wise addition of protons [55]:



Eq. (10a) describes the standard reduction potential  $U_{\text{red}}^0$ , Eqs. (10b), (10c), and (10d) describe the reversed dissociation reactions of the possible reductant complexes formed in each of the three steps; the latter are represented by the dissociation constants  $K_1$ ,  $K_2$ ,  $K_3$ , respectively. The measured reversible redox potential  $E_{\text{rev}}$  [13] corresponds to the condition at which the concentrations of oxidized, [Ox], and reduced, [Red], species are equal. From Eq. (10a),  $\text{Ox} = \text{Li}_4[\text{Mn(IV)}_3(\text{OH})_3]$ ,  $\text{Red} = \text{Li}_4[\text{Mn(III)}_3(\text{OH})_3]$ . The  $\text{pH}$  of the solution defines the degree of protonation of the reduced complex. At different  $\text{pH}$  of the solution there are various reduced complexes, namely  $\text{Red}^3$ ,  $\text{RedH}^2$ ,  $\text{RedH}^1$ ,  $\text{RedH}_3$ . Therefore, in experiment the reversible half-wave redox potential  $E_{\text{rev}}$  for the process Mn(IV/III) is measured at the condition where

$$[\text{Ox}] = [\text{Red}]_{\text{total}} = [\text{Red}^3] + [\text{RedH}^2] + [\text{RedH}^1] + [\text{RedH}_3]. \quad (11)$$

Therefore, one has for the calculated reversible potential  $U_{\text{rev}}$  of the redox process Mn(IV/III) [55]:

$$U_{\text{rev}} = U_{\text{red}}^0 + \frac{RT}{3F} \ln \left( \frac{1}{1 + \frac{K_1 \text{H}^{\text{p}}}{K_1} + \frac{K_1 K_2 \text{H}^{\text{p}^2}}{K_1 K_2} + \frac{K_1 K_2 K_3 \text{H}^{\text{p}^3}}{K_1 K_2 K_3}} \right) \quad (12)$$

Table 5 compares the corresponding computationally estimated values  $U_{\text{rev}}$  to the measured results  $E_{\text{rev}}$  [13]. The corresponding calculated dissociation constants are provided as SD.

First of all, all exchange-correlation functionals examined reproduce the pH dependence. At  $\text{pH} = 4.2$  the computed redox potential is 0.1 eV higher than the corresponding redox potential at  $\text{pH} = 6$  (Table 5). The corresponding measured difference between the two  $E_{\text{rev}}$  at  $\text{pH} = 4.2$  and 6 is 0.2 eV [13]. Different from Mn(III/II), where the hybrid exchange-correlation functional TPSSh shows the best agreement with experiment, for Mn(IV/III) the PBE results agree best with experiment. TPSSh overestimates the measured potentials by 0.6 eV, and B3LYP and PBE0 by 1 eV (Table 5). This is in contrast to the common expectation of a better performance of the hybrid DFT methods, compared to the pure GGA approach. Predicting the accuracy of DFT methods for particular systems is difficult [56,57]. For the first-row transition metals, it has been shown [58] that pure GGA and hybrid functionals tend to deviate from experiment in opposite directions, e.g. for calculated bond lengths and, more importantly in the present context, for ionization potentials and dipole moments. Roy

Table 5

Calculated reversible redox potentials  $U_{\text{rev}}$  vs. NHE (in eV) for the proton-coupled redox process Mn(IV/III), estimated from Eq. (12), for results obtained at various levels of theory: PBE, TPSSh, B3LYP, PBE0. The numbers are given for Li arrangement 1321.

	PBE	TPSSh	B3LYP	PBE0	Exp. <sup>a</sup>
Mn(IV/III)					
$U_{\text{rev}}$ , pH 4.2	1.05	1.61	1.91	2.12	1.05
$U_{\text{rev}}$ , pH 6	0.98	1.51	1.81	2.01	0.85

<sup>a</sup> Ref. [13].

et al. [59] calculated redox potentials for various redox couples for a series of small transition metal compounds of the first-, second-, and third-row elements. They also obtained better alignment with experiment for the pure GGA functionals BP86 and PBE,  $R^2 = 0.97$ ; the hybrid methods yielded  $R^2 = 0.83$  only [59]. These authors suggested that the better performance of pure GGA may be due to error cancellation of the additional solvent and/or metal electrode surface effects taking place in experiment [59].

However, the better performance of a pure GGA functional, compared to the hybrid methods, may be fortuitous as other approximations may affect the computational results, e.g., the solvation model. As mentioned in Section 3.3, solvation energies of highly charged species may suffer from larger uncertainties.

Besides the solvation model itself, an accurate description of the electrolyte structure can be also crucial. The popular COSMO approach may not suffice for reflecting the solvation effects on the Li cations; rather, some water molecules may have to be explicitly described. Using the COSMO method for calculating redox potentials of the aqua complexes of Ru(III/II) and Os(III/II), Srncic et al. indicated [60] that in that case solvation energies may be quite inaccurate (up to 1 eV for the Ru complexes) unless the second solvation sphere (12–14 H<sub>2</sub>O molecules) is taken explicitly into account [60]. In the present case of POMs, such models will be computationally quite demanding.

We probed this effect by introducing one explicit water molecule for each Li cation of the arrangement 1321 of the POM models for Mn(IV) and Mn(III), and the arrangement 132351 of the POM model for Mn(II). For the process Mn(III/II) the reversible redox potential  $U_{\text{rev}}$  was calculated at the PBE level at 0.19 eV as compared to 0.32 eV for the corresponding model without explicit solvation. Similarly, at the TPSSh level, the calculated value  $U_{\text{rev}}$  was reduced to 0.58 eV compared to 0.68 eV for the non-solvated model. While the explicit solvation decreases the calculated reversible potential for Mn(III/II) by 0.1 eV, the TPSSh result still compares very well with the experimental result  $E_{\text{rev}} = 0.65$  eV [13]. For Mn(IV/III) the calculated  $U_{\text{rev}}$  decreased by 0.06 eV at the PBE level and by 0.04 eV at the TPSSh level. These rather simple test calculations suggest that the effect of the second solvation shell of the POM is larger for Mn(III/II) than for Mn(IV/III). For Mn(III/II) the initial and final structures of the near field electrolyte change considerably; three Li<sup>+</sup> ions are added to the structure when Mn(III) is reduced to Mn(II). Therefore, a change in the description of the solvation effects, namely adding explicit water molecules directly in the quantum-chemical model, can noticeably affect the calculated redox potential. As for the redox process Mn(IV/III) the electrolyte environment does not change in such a drastic way, the number of Li<sup>+</sup> ions near the POM does not change under reduction/oxidation. Therefore, one expects that the present model is more appropriate for Mn(IV/III) than for Mn(III/II).

In the present models we represented Li<sup>+</sup> ions as inner-sphere adsorbates on the surface of the POM, and we chose the strongest adsorption sites. This is yet another simplification of the electrolyte environment near a POM. In solution, the cations may occupy over time different sites and they may even be adsorbed in outer-sphere fashion. To explore this aspect, we carried out an additional test, examining how the distance between Li cations and the surface of the POM may affect the redox potentials. For this purpose, we moved the Li<sup>+</sup> ions of the optimized 1321 arrangement by 50 pm along the Si-Li axes away from the surface of the POM. For these structure, we calculated the reversible redox potentials  $U_{\text{rev}}$  at the PBE level. For Mn(IV/III), the value decreased from 1.05 eV to 1.01 eV and, for Mn(III/II), from 0.32 eV to 0.06 eV. This model consideration indicates once again that a correct description of the electrolyte is crucial for calculating redox potentials, especially for cation-coupled electron transfer where the structure of near field electrolyte changes notably.

## 4. Conclusions

We studied computationally the tri-Mn-substituted W-based Keggin ion. By means of DFT calculations, we determined the structure of these polyoxometalates (POMs), focusing on three systems with all Mn centers uniformly in the same oxidation state, (IV), (III), and (II). To neutralize the highly charged POMs, we followed the experiment [13,16] and designed model systems with the POMs in an aqueous electrolyte containing  $\text{Li}^+$  ions. Therefore, we added an appropriate number of Li cations to the quantum chemical models, placing them near the surface of the POM in various arrangements. Hence, we added four Li cations to the models of  $[\text{Mn}(\text{IV})_3(\text{OH})_3]^{4-}$  and  $[\text{Mn}(\text{III})_3(\text{OH}_2)_3]^{4-}$  as well as seven cations to the model of  $[\text{Mn}(\text{II})_3(\text{OH}_2)_3]^{7-}$ . We tested a pure GGA exchange-correlation functional and several hybrid DFT approaches. As a result, we found out that, for each of the Mn oxidation states studied, the main structural parameters of the POMs were not affected by the Li arrangement nor the exchange-correlation functional. While the calculated structural parameters were found to overestimate some of the experimental interatomic distances, the calculations successfully reproduced the geometric trends [16] upon reduction of the Mn centers from (III) to (II).

Similarly, the standard reduction potentials were found to be not sensitive to the Li arrangement, but the calculated results depend strongly on the exchange-correlation functional. The lowest standard reduction potentials were determined with the pure GGA functional, PBE. The three hybrid functionals tested, TPSSh, B3LYP, and PBE0, yield higher reduction potentials which increase (in that order) with the contribution of exact exchange in the hybrid functional.

For comparison with experiment we used the full redox reactions, including the transfer of protons or cations coupled with the electron transfer. For the cation-coupled redox process Mn(III/II), the reversible redox potential  $U_{\text{rev}}$  calculated with TPSSh compares best with experiment. The GGA functional PBE yields a result that underestimates the measured value of  $E_{\text{rev}}$  [13] by 0.3 eV, while results of B3LYP and PBE0 overestimate it by 0.5 eV. For the proton-coupled electron transfer of the redox process Mn(IV/III), we corrected the standard reduction potential using the dissociation constants of the protonated POMs and the Nernst equation. The resulting  $U_{\text{rev}}$  values reproduce the experimental pH dependence [13]. Surprisingly, the PBE result shows the best agreement with experiment, while the  $U_{\text{rev}}$  results of the hybrid functionals explored notably overestimate experimental  $E_{\text{rev}}$  by 0.6–1 eV.

The good performance of the pure GGA approach compared to hybrid methods seems to be due to fortuitous error cancellation [59]. Another source of uncertainty is the solvation model that may lead to smaller redox potentials if a more realistic description based on explicit solvation is included in the quantum chemical model. One expects that models with such an improved description of solvation (e.g., by solvated counterions) affect more noticeably the calculated  $U_{\text{rev}}$  values for Mn(III/II) than for Mn (IV/III) because the near field electrolyte changes more notably in the former case as the number of Li cations close to the POM varies during the reduction Mn(III/II).

Obtaining accurate results for redox potentials of POMs apparently is still a challenge for computational chemistry methods. Preliminary simple model studies indicated that the structure of the electrolyte near a POM, especially the distances to the counterions as well as the screening of these ions by water molecules, may be essential for achieving quantitative agreement between theoretical and experimental data. The results of the present study point to a crucial need for a more refined atomistic representation of the (average) effective potential due to the electrolyte environment. The approximate nature of the effective

potential used here, although going beyond a straightforward polarizable continuum model, seems to be a major reason for the limited accuracy of the calculated redox potentials. Experimental conditions, not reflected by the present type of computational models, may also affect the calculated redox properties, e.g., the nature of the electrolyte and the working electrode. On the computational side, uncertainties remain regarding the choice of the exchange-correlation functional [57,58], and the description of the electrolyte. In the latter case, one may have to resort to more elaborate methods, e.g., by describing the electrolyte via a solution of the generalized Poisson-Boltzmann equation. Here, recent advances for computational methods seem to be promising [61–64].

Alternatively, one may use an internal reference, either from experiment or a calculation, that allows quantitative predictions of redox potentials with standard deviations that are comparable to typical experimental errors of cyclic voltammetry [20,31]. Results of this work, therefore, besides being pioneering, can be used further as a reference.

In summary, the present study confirms the experimentally determined electrochemical behavior of a tri-Mn-substituted Keggin ion. This computational work provides a protocol for calculating redox potentials that, to a certain degree, can be compared to measured redox potentials of other POMs. However, the present results also show where the computational approach has to be improved in order to achieve a more reliable modelling.

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Supplementary data associated with this article can be found, in the online version, at <http://dx.doi.org/10.1016/j.electacta.2017.02.046>.

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