Electrical load forecasting models: a critical systematic review.

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Highlights

- A systematic review protocol provides unbiased and meaningful meta-information
- A direct model accuracy comparison across studies is meaningless
- A taxonomy for an informed forecasting model’s selection is proposed
- Recommendations on writing electrical load forecasting related paper are given

ABSTRACT

Electricity forecasting is an essential component of smart grid, which has attracted increasing academic interest. Forecasting enables informed and efficient responses for electricity demand. However, various forecasting models exist making it difficult for inexperienced researchers to make an informed model selection. This paper presents a systematic review of forecasting models with the main purpose of identifying which model is best suited for a particular case or scenario. Over 113 different case studies reported across 41 academic papers have been used for the comparison. The timeframe, inputs, outputs, scale, data sample
size, error type and value have been taken into account as criteria for the comparison. The review reveals that despite the relative simplicity of all reviewed models, the regression and/or multiple regression are still widely used and efficient for long and very long-term prediction. For short and very short-term prediction, machine-learning algorithms such as artificial neural networks, support vector machines, and time series analysis (including Autoregressive Integrated Moving Average (ARIMA) and the Autoregressive Moving Average (ARMA)) are favoured. The most widely employed independent variables are the building and occupancy characteristics and environmental data, especially in the machine learning models. In many cases, time series analysis and regressions rely on electricity historical data only, without the introduction of exogenous variables. Overall, if the singularity of the different cases made the comparison difficult, some trends are clearly identifiable. Considering the large amount of use cases studied, the meta-analysis of the references led to the identification of best practices within the expert community in relation to forecasting use for electricity consumption and power load prediction. Therefore, from the findings of the meta-analysis, a taxonomy has been defined in order to help researchers make an informed decision and choose the right model for their problem (long or short term, low or high resolution, building to country level).

KEYWORDS
Electric consumption and load prediction; forecasting models; Machine Learning; Regression; Time Series Analysis; Long-term/short-term forecasting

1 INTRODUCTION
Forecasting models are widely used in different domains; e.g. in finance to forecast stock exchange courses or indices of stock markets (Bianco et al. 2009), in business to schedule
staff, manage inventory and predict demand (Hyndman & Athanasopoulos 2014), in medicine to monitor the spread of diseases (Generous et al. 2014), and in meteorology for predicting weather. Equally, forecasts play an essential role in the control of power plants and electric power exchange in interconnected systems (Mohandes 2002). Forecasting supports energy planners in understanding the influence of some variables on energy consumption and thus inform decision making (Al-Ghandoor et al. 2009). On a temporal scale, forecasts can be short-term for instance for balancing electricity supply; and long-term forecasts, including for capacity expansion, capital investment return studies, and revenue analysis (Parlos et al. 1996). Over the years, many different forecasting models have been applied for electricity and power predictions such as multivariate and multiple regression (Azadeh & Faiz 2011; Filik et al. 2011; Wang 2012; Al-Hamadi & Soliman 2005; Farzana et al. 2014), SVM (Massana et al. 2015; Mohandes 2002; Garulli et al. 2015), time series (including Autoregressive Integrated Moving Average (ARIMA) and the Autoregressive Moving Average (ARMA)) (Fan et al. 1994; Gonzales Chavez et al. 1999; Hoffman 1998; Chujai et al. 2013). Equally, artificial neural networks (ANN) have become widely used for prediction scenarios. ANN has been used for various tasks such as (a) short-term load forecasting (STLF) in microgrids (Hernandez et al. 2014; Hernández et al. 2014; Hernández et al. 2013; Hernández et al. 2012; Twanabasu & Bremdal 2013), (b) optimisation scenarios at building level (Platon et al. 2015; Hsiao 2015), and (c) long term horizon scenarios to determine annual electricity consumption of a region, district or building (Farzana et al. 2014; Azadeh & Faiz 2011). There is no consensus over a particular forecasting model and the use of a method over another is often the result of the expert’s preference. Moreover, in his paper showing the outcomes of the M3 competition (competition comparing the accuracy of different forecasting methods, realised in 1982, 1993 and 2000), Makridakis states that “simple methods developed by practicing forecasters do as well, or in many cases better, than
sophisticated ones” (Makridakis & Hibon 2000). This means that there are no evidences that complex models will outperform “simple” ones. Therefore, it is relevant to identify which model fits a particular situation.

The need for forecasting varies from one scenario to another; the setting of a model is subject to numerous variations: including the available data used as inputs, the timeframe wanted, the time resolution (from every minute to annually), the scale (from a simple building to a whole country consumption). The aim of this review is to critically analyse and identify the quality of a method compared to some other potential solutions in a specific forecasting scenario and to assist users in their forecasting method’s selection by simply answering questions such as “Which model do I need to generate hourly electricity demand/consumption of a building for the next 2 years?”

The paper will first introduce the systematic review process employed (Section 2.1) for the selection of case studies. Equally, a short description of the most commonly encountered forecasting models is given. Each of these forecasting models has advantages and disadvantages and none is 100% efficient. It is important to know their limitations before considering their use. Section 3 gives an overview of the main context characteristics of the study cases across the paper references (e.g. location, year, scale, data used, model used, timeframe considered…) as well as the results of their application in various scenarios and field studies. A taxonomy for the decision making of prediction models is presented as the main output of this review. Finally, a discussion section elaborates on the open questions resulting from the study and suggestions of the authors.

2 METHODOLOGY

The study is based on the critical review of academic research aimed at power and electricity forecasting. The selection of the different papers has followed a rigorous systematic protocol.
In this section the systematic process used for the review is described. The different steps for the papers’ selection are described. The different keywords used and domains’ restrictions are explained for an objective, non-biased papers’ selection. Additionally, some of the most popular forecasting models namely ANN, Time series analysis (including AR, MA, ARMA, ARIMA, SARIMA), SVM and Bottom-up model are briefly explained in this section.

2.1 Systematic review protocol

For the study, a systemic approach of the literature has been employed. Systematic reviews vary from the traditional review by extensive literature searches and meta-analysis of the finding, reducing the effect of chance and biases (Tranfield et al. 2003). A systematic review must follow a well-defined protocol introduced to bring more clarity, rigour and repeatability. The author must first define the research question(s); then define the research criteria to apply in order to select accurate publications. Once the selection done, the author can analyse the data and finally discuss the results (Righi et al. 2015; Higgins JPT, Green S 2006). In this process, the selection of the criteria is particularly important. The research criteria have been selected according to the research question. While developing the research question some keywords appeared naturally like “electricity forecasting models”, “electricity prediction models” or “electricity demand models”. Using the online database Scopus, one of the established abstract and citation databases of reviewed literature (Anon n.d.), and its advanced search tool, the search results were first limited to these keywords. The appearance of the keywords in the main text has been excluded as criteria due to a high probability of occurrences. The threefold Title-Abstract-Keyword provides more relevant results because it targets better the global content of the text. On this 1st search, 10 667 results were returned. A statistical analysis shows the distribution of the returned results by area of study. From the 10 667 results 39.1% are from Engineering; 38.1% are from Energy; 16.3% from Computer
Science and 14.6% from Environment science. The other areas are not relevant in this study and therefore have been excluded (Figure 1).

Texts in languages other than English have been excluded. The reduction to the four areas: Engineering, Energy, Computer science and Environmental Science leads to a new selection of 5845 papers. In order to fit even better to the desired topic, other keywords were targeted within the previous results. The texts including the keywords “building”, “dwelling” or “household” inside the title, abstract or keywords have been selected. 900 papers have been identified under these criteria. Finally, Scopus provides the overall of the keywords allocated to each paper. A quick overview on the keywords has enabled the identification of some irrelevant papers like “electric vehicles”, “wind power” or “global warming”. In order to avoid irrelevant studies, papers associated to the specific keywords “electricity demands” and “electric load forecasting” have been selected. At the end, 153 have been identified and will constitute the study basis. The whole process is shown in Figure 2.

Among the 153 studies, 76 are articles, 68 are conference papers, five are reviews, three are articles found in the press and one is a short survey; all from 44 different countries. Among the 153 references found on the topic, 41\(^1\) have been reviewed in depth. Within the 41 references, 113 different implementations of forecasting models have been identified. Having explicit criteria against which to assess studies helps to avoid hidden bias, by having clear consistent rules about which studies are being used to answer the review’s specific research.

questions (Eppi 2007). Thus, the systematic review approach allows the reduction of biases and to consider the distribution of the cases as a good representation of the overall framework.

2.2 Cases comparison

From this point, the cases have been rigorously studied following specific characteristics. A relevant selection of a case characteristic is important because it is the starting point for an accurate and meaningful comparison between different electricity forecasting models. The idea is to best represent a particular situation through those characteristics without leaving out aspects that could influence the forecasting performance. A first analysis of the references helped in this matter. The authors have identified the different characteristics to take into account by considering the aspects that repeatedly appeared in the literature in order to describe a case. Table 1 gives the characteristics considered and a description of their suitability.

From there, a second analysis has been done and an excel spreadsheet has been populated with all the needed information for every case.

2.3 Forecasting models highlights

From the 113 cases studied, 16 different models have been identified. The first observation is that some models can be categorised under a same label. For example, AR, MA, ARMA, ARIMA, seasonal or not, with or without exogenous variables can be seen as a part of time series analysis model. Therefore, they will be gathered into the label “Time Series”.

It is interesting to study the models’ distribution through all the references in order to have a representation of the current trend in the forecasting model use. If the models’ distribution does not give an exact representation of the practices of the expert community, it still
provides a good overview. Figure 3 illustrates the distribution of the different analysed forecasting models. Because one paper can proceed to several applications on one specific prediction model, the distribution of each forecasting model through the reviewed papers provides a better representation of the actual trend. Therefore, distribution will always be considered as a number of papers in which a particular forecasting model is used rather than the number of application.

A clear trend is observed in the use of forecasting models. The regression model (most often multiple regressions or multivariate regressions) is the most widely used, and is present in 17 papers out of 41 (43.6% of the papers), followed by the artificial neural networks (ANN) present in 15 papers (38.5%). Time series models are present in 30.8% of the papers, i.e. 12 papers. In a lesser proportion, SVM and Bottom up models are used in 15.4% and 10.3%, respectively. The other models are singularities. The relatively high quantity of regression, ANN and time series models can be explained by their popularity in the research community. This observation strengthens their status as leading models in the field. SVM and bottom up model are present in a lesser extent but there is a clear framework developed around these models sustained by an increasing number of studies. Overall, five main models were identified from the review of the articles. A short description of the most encountered forecasting models is given below.

2.3.1 Artificial Neural Network

Conventional models such as regression are limited and can sometime lead to unsatisfactory solutions (Aggarwal & Song 1997). The reasons include the too high number of computational possibilities leading to large solution times and the complexity of certain non-linear data patterns (Aggarwal & Song 1997). On this type of challenges, artificial neural
networks and intelligent machine learning technique, provide a promising and attractive alternative. The increasing computational power has facilitated forecasting in a large set of power system management from load forecasting to security assessment or fault diagnosis (Wehenkel 1997). However, on some problems, the use of conventional models lead to unsatisfactory solutions due to the high complexity of variables' relationships and the extent of computation power requirements (Landau & Taylor 1998). It is in these cases that artificial neural networks (ANN) are used. Two references have been mainly used for the ANN description: the work of Raj Aggarwal and Yonghua Song that gives an introduction to the field of ANN via three tutorials which are proposed to engineers with an application in power systems (Aggarwal & Song 1997; Song & Aggarwal 1998a; Song & Aggarwal 1998b); and the book of Lawrence Jay Landau and John Gerald Taylor that gives a broad view on the concept of neural networks. It explains the basics of artificial neural networks and the mathematical underpinnings (Landau & Taylor 1998). ANN is an intelligent machine learning method based on the structure of the human brain. As the human brain, ANN is composed of neurons and interactions within multiple layers. Even if current ANNs are far from reflecting the complexity of a human brain, they remain powerful tools in pattern recognition. A neuron is the main element of the ANN, it can receive or send a normalised signal from and to the other neurons of the network. The wires between neurons are called “weight” $w_{kp}$, one for each wire coming to a neuron from another one. Overall, there are three main features that determine an ANN: the architecture of the net (feedforward or recurrent), the learning rule used for defining the weights during training (perceptron, Hebbian, etc.), the activation function between neuron input and output. One of the most commonly used ANN is the Multi-Layer-Perceptron. This multilayer network is based on a backpropagation rule which evaluates the output’s error and reduces it, adjusting the weights by back-propagating the error from the output to the hidden layer. ANNs are particularly
suited for energy forecast. They provide a good estimation in cases where data is incomplete (Aggarwal & Song 1997), and can address complex nonlinear problems while demonstrating robustness and fault tolerance (Zhai 2005). More, it is a data-driven self-adaptive model (Zhai 2005; Pantic 2000) that (a) includes pattern recognition and captures subtle relationships (Aggarwal & Song 1997; Pantic 2000), (b) deals with noise (Aggarwal & Song 1997), (c) does not depend on the programmer's prior knowledge of rules (Song, 1997); and (d) identical and independent operations can be done simultaneously (Aggarwal & Song 1997). However, ANN’s results cannot be easily explained as (a) they are not mathematically based (Aggarwal & Song 1997), (b) it is computation time consuming (Aggarwal & Song 1997), (c) the training process optimisation is complex (Askarzadeh & Rezazadeh 2013), (d) extended data is required (Zhai 2005) and (e) the model may never converge in some cases (Zhai 2005).

2.3.2 Time series analysis

Some of the most widely used methods for time series analysis and forecasting are the Autoregressive Integrated Moving Average (ARIMA) and the Autoregressive Moving Average (ARMA). The ARMA and ARIMA have been introduced in 1970 by two statisticians, George Box and Gwilym Jenkins (Box et al. 2008). The basic ARMA model is composed of an autoregressive model (AR) and a moving average model (MA). The autoregressive model is a linear regression of the current value based on one or more previous values. Just as an AR, the MA is a linear regression, at the difference that it regresses current values against the white noise or errors of one or more past values. Note that an essential condition to process an ARMA model is that the time series is stationary. If not, the stationarity is achieved by differencing a non-stationary series in first place. The introduction of this step lead to a new model called ARIMA with the “I” standing for “Integrated”. In order to deal with the seasonality, Box and Jenkins introduced a new model,
the seasonal ARIMA or SARIMA. The most commonly used seasonal ARIMA is probably the ARIMA\((0,1,1)x(0,1,1)\) which corresponds to a seasonal exponential smoothing model. Overall, Box-Jenkins forecasting model is (a) adaptable, (b) can deal with seasonality and with non-stationarity and (c) only requires the past value of a time series (Zhai 2005). Nevertheless, it is unlikely to perform well on long-term prediction (Zhai, 2005), is computation time-consuming (Zhai 2005), is subjective and requires a good understanding of the underlying statistics (Zhai 2005).

2.3.3 Bottom up end-use approach

We call “bottom up approach” the construction of a complex system by aggregating elementary systems. Applied to the electricity consumption, it is simply the aggregation of all appliances loads within a household in order to determine the overall load of this household. The bottom up approach the most commonly cited is the Capasso bottom up model (Capasso et al. 1994). This approach evaluates the probability for a specific appliance to be “on” at every time step of a day by considering various factors involving the appliances and household members’ characteristics. Each appliance is related to one or more activities. The probability that an appliance is “on” is then linked with the probability for an activity to be done at a certain time of the day by one or more members. A calibration is applied to this probability taking into account (i) if the activity can be done by the person available, (ii) how many people the activity requires, and (iii) can the activity be done simultaneously with another activity. Once the activity probability is computed, socio-economic criteria are used to determine the penetration of appliances in the household. The power requirement and duration of each of these appliances is extracted and used to determine if they are suitable for a given activity and building type. For that, the minimum duration of usage of an appliance has to fit the activity probability in which the appliance is involved and the power required has to be smaller than \(P_{\text{limit}}\), the maximum power load allocated to the household.
(considering that other appliances might be used in the exact same time). These steps lead to the creation of the appliance load profile and finally the daily load profile of the household. The bottom up model has the advantage to consider behaviour of the various types of customer and lifestyle-related psychological factors. It describes interrelations between appliances and members of the household and is easily understandable. Moreover, it can deal with missing values and its maintenance is simple. Among its disadvantages are the large number of data and tenants behaviour surveys required, the lack of information regarding customers’ behaviours in the long-term, thus inherently inaccurate in the long-term (Ghods & Kalantar 2011) and that the model assumes a constant relationship between electricity consumption and end-use (Ghods & Kalantar 2011).

2.3.4 Support Vector Machine

Support Vector Machines have been first introduced by Vladimir Vapnik with a paper at the COLT 1992 conference (Boser et al. 1992). Then, in 1995, the soft margin classifier was introduced by Cortes and Vapnik in the paper Support Vector Networks (Cortes & Vapnik 1995). Originally, SVMs were created to deal with pattern classification problems like character recognition, face identification and text classification. In 1995, Vladimir Vapnik extends SVM to a regression algorithm in his book, The Nature of Statistical Learning Theory (Cherkassky 1997). Over the years various applications were found in the literature; e.g. time series prediction problem. The purpose of an SVM is to create an optimal separating hyperplane in a higher dimensional feature space such that subsequent observations can be classified into separate subsets. In practice, real data are not as perfectly separable. In order to provide a hyperplane, one has to relax the requirement that a separating hyperplane will perfectly separate every training observation. For that, a soft margin classifier (SVC) has been constructed. In the case of non-linear boundaries, the use of SVM is convenient (Auria & Moro 2008). Indeed, the SVM allows non-linear decision boundaries by using an
appropriate transformation that makes them linear on a higher dimensional feature space. Unfortunately, computation on high dimension feature space can be very costly and SVM depend a lot on the proper selection of the hyper-parameters (Adhikari & Agrawal 2013). To improve the computation efficiency, a solution also called the “Kernel trick” is used (Adhikari & Agrawal 2013). Kernels are functions used to represent inner products between observations rather than observations themselves. Thus, it modifies how we calculate "similarity" between two observations in a more flexible way, allowing to change and solve a non-linear problem by a linear problem on a higher-dimensional space.

2.3.5 Regression

A regression is the simple statistical method that allows the observation of relationship between variables. Thus, the response, outcome, or dependent variable can be defined by other variables called predictor, explanatory, or independent variables. The most common form of regressions analysis used for prediction are the linear regressions and the polynomial regressions. The linear regression links the response $y$ and the predictor $x$ by the simple linear model:

$$y = \beta_0 + \beta_1 x + \epsilon.$$  

Where $\beta_0, \beta_1$ and $\epsilon$ are the intercept and the slope of the line and the random “error” respectively (Hyndman & Athanasopoulos 2014). The extension of the simple linear regression is the multiple linear regression. The difference between simple and multiple linear regression being the number of variables introduced as predictors that goes from one variable in the simple model to several in the multiple. Thus, the regression can not only be time related but also integrate some other independent variables. Four conditions, however, must be taken into account: the mean of the response at each set of values of the predictors is a linear function of the predictors, errors are independent, errors at each set of values of the
predictors are normally distributed, errors at each set of values of the predictors have equal variances (Anon n.d.). In the same way, the polynomial regression is a regression analysis where the predictor is related to the response via a polynomial of degree \( n \). It is used to fit nonlinear data.

3 FORECASTING MODELS COMPARATIVE ANALYSIS

The initial phase involves analysing each paper’s scope and scenario objectives. The focus is then on the analysis of the forecasting models used, prediction horizon, variables and processes employed. Finally, key patterns in the use of the selected forecasting models are described.

In term of application, the objectives are various. The most frequently encountered objective is the demand response for production and distribution of electricity. This objective requires short-term horizon predictions with high-resolution data in order to have a fast response to the electrical loads. This can be applied to a single building when several electricity sources are involved (Mathieu et al. 2011; Mena et al. 2014) or at district level with the increasing development of smart grids (Garulli et al. 2015; Hernandez et al. 2014; Hernández et al. 2014). Another application is associated with mid to long term forecasting (1 week to a year) where the prediction is employed for power system planning (Al-Hamadi & Soliman 2005), maintenance or production and resell market (Filik et al. 2011). Long term prediction (several years) with large time step are often applied for policy making (Azadeh & Faiz 2011), large scale planning (Gonzales Chavez et al. 1999), statistical prevision (Bianco et al. 2009) or business plan (Wang 2012). Some applications are more household orientated with a great emphasis on appliances’ running time and on occupancy (Ciabattoni et al. 2013; Fischer et al. 2015; Widen & Wackelgard 2010; Richardson et al. 2010). In the latter cases, the researcher seeks a reproducible model that can fit several household types. Thus, the prediction can
apply from a single house up to an entire district by aggregation. Finally, some studies attempt to cover all the previously cited applications with high a resolution model that has a long-term horizon (Filik et al. 2011).

3.1 Scope and scenario objectives

This section presents the different use cases found in the literature by giving their main features such as if they have been pre-processed, the timeframe, inputs, and resolution. This gives a better insight of the references listed.

3.1.1 Forecasting data pre-processing

Many studies have concerns about the variables they present as inputs of their models. Indeed, many studies support the use of data pre-processing in order to improve forecasting accuracy ((Chujai et al. 2013; Hsiao 2015; Azadeh & Faiz 2011)), especially when using machine learning algorithms (Crone et al. 2006; Huang et al. 2015; Suhartono & Subanar 2006). It appeared than in 66.0% of the cases, a pre-processing has clearly been done. Note that the remaining 33% do not necessarily mean a lack of pre-process but simply that it has not been mentioned. Overall, data pre-processing is a common practice for forecasting. Four different kinds of pre-processing can be identified: (1) smoothing and filling missing values, (2) measurement of variables dependency and significance, (3) data decomposition and classification and (4) check order of integration and stationarity. For that, several mathematical and statistical tools are used, the most widely spread are principal component analysis (PCA), which uses principles to transforms a number of possibly correlated variables into a smaller number of variables called principal components, Pearson correlation (PCC) which show the interdependency of sets of variables, \( p \)-value that is used for testing a
statistical hypothesis, analysis of variance (ANOVA), Kernel density estimation (KDE) which is a non-parametric density estimator and Canonical Correspondence Analysis (CCA).

3.1.2 Forecasting timeframe and resolution

Another important characteristic is the time-term considered for the prediction. Indeed, the timeframe and resolution that are chosen for a prediction will highly influence the results and the choice of a model over another. The timeframe has been classified into 4 categories such as “very short term” (less than an hour), “short term” (1 hour to several days), “mid-term” (1 month to a season) and “long term” (a year or more). The time resolution represents the time-step considered for the prediction. It goes from every minutes to annually. Table illustrates the term distribution through the different papers and cases. The distribution in percentage is based on the number of paper in which the timeframe is used.

With respectively 61.5% and 43.6%, the long-term and short term prediction represents the actual needs for electrical loads forecasting in buildings. In the vast majority of cases, the use of forecasting model is for 1 hour, 1 day or 1 year ahead prediction. Very short-term and mid-term prediction are not highly represented within the cases. This can be explained by the needs of the industry for short term and long-term prediction. Indeed, short-term prediction has a direct application for quick electricity demand response while long term prediction are often used for prevision and strategies.

3.1.3 Forecasting input variables

For electricity and power prediction, a forecasting model can be implemented with a large range of inputs. Independent variables such as income, occupancy, electricity price,
temperature, building size, rainfall, dwelling type, GDP, population are just few examples of the various possible inputs. For the purpose of the study, the different exogenous variables have been classified into 4 categories: “Socio-economic” related to the socio-economic situation of the zone considered, “Environmental” related to the weather conditions, “building and occupancy” related to the building type and activity and “time index”. Table presents the input used distribution across the papers and cases. The building characteristics are, with 48.7% of paper considering them, the most used exogenous variables. Environmental variables and socio-economic variables follow and are present in respectively 41.0% and 38.5% of the papers. The time index data, which are simply the date stamps series introduced as an input, are used in a lesser proportion with 28.2% of papers found. Finally, models without exogenous inputs are present in 30.8% of the papers.

In order to fully understand this distribution, it is important to look at when these inputs are used. Figure 4 illustrates how the inputs are split into the different timeframe. In the same way, Figure 5 shows the repartition of the input depending on the scale of the study. Some trend can be identified. Indeed, socio-economic variables are in a high majority of cases used for long-term prediction as well as large-scale studies (from a city level to entire country). Environmental variables are implemented in models that aim to predict short-term and small to mid-scale studies (building to district level). Overall, electricity historical data (past patterns) are equally present in short or long term, small or big scale studies. If building and occupancy inputs are almost equally used for short-term and long-term prediction, they are mainly employed for small and mid-scale level (building to district). Finally, time index are mainly introduced for short-term and small-scale prediction.
One of the reasons for input variables selection is the meaning that the developer wants to give to his/her model. Indeed, some studies target some particular variables to highlight the relationship between them and impact for instance on electricity consumption.

Finally, the introduction of a time index in certain cases has proven improving the accuracy when time series have been clustered (Hernandez et al. 2014; Yoo & Hur 2013) or when the model highly depends on the occupancy such as in (Ciabattoni et al. 2013).

3.2 Key observations

The study aims to identify which forecasting model best fits particular situations and variables. Indeed, following the situation and the variables available, the use of a model will be preferred in order to obtain the best accuracy possible. This section presents the different observations done on the use of forecasting models by highlighting potential correlation between a scenario parameter such as timeframe and/or inputs variables and a particular model. The outcome is the overall representation of the practices within the expert community. Those practices are assumed as being representatives of the good use of the models.

3.2.1 Model vs timeframe

In this section, the models have been compared by considering the timeframe they are meant to predict. Only the five most commonly encountered models that are ANN, bottom up, time series analysis, regression and SVM are being compared. The singularity of the other models listed in Figure 3 does not allow any interpretations about the case they best fit. Figure 6 shows the number of papers in which a timeframe is considered given a certain model. The
majority of the regression models are used for long-term prediction, one year or more. Only four on 19 configurations are against short or very short-term prediction. On the other hand, ANN is mainly used for short-term prediction with 10 papers studying this configuration. In a lesser extent, the use of ANN for a long or mid-term prediction follows with a total of 6 papers. Likewise, the time series analysis and SVM models have been mainly applied for a short and very short-term prediction with respectively 10 and 6 different references considering this configuration. The bottom up model seems to be slightly preferred for long term forecast.

The regression remains widely used for long term forecasts due to its simplicity and accuracy on this timeframe, especially when the time resolution is large as states AlRashidi in Section 2 of his paper “Long term electric load forecasting based on particle swarm optimization” (AlRashidi & EL-Naggar 2010). Short term predictions require more sophisticated models such as machine learning or ARIMA because the variables interrelationship are more complex and sensitive on this time scale (Hippert et al. 2001; Ho et al. 2002).

3.2.2 Model vs input

This last section presents the repartition of the inputs implemented within the model following the model.

Figure 7 shows the number of papers in which input variables are introduced in a given model. The regression models have been mainly set up with socio-economic inputs. Note that if regressions models are using socio-economic variables, a direct correlation between the model and the variable is debatable. Indeed, regression models are widely used for long-term
forecasts (see section 3.2.1) and long-term forecasts are correlated with the use of socio-
economic variables (see section 3.1.3). ANN shows a preference for environmental, building
and time index inputs. Overall, ANN has been implemented with a relatively large range of
variables which indicates flexibility of the models toward the data introduced as inputs. In the
case of the ANN and SVM, the relatively high amount of time index data introduced is
mainly due to a possible need in order to increase their accuracy. Time series analysis is most
often set up without exogenous variables. In this model, exogenous variables are introduced

for a better performance but are not mandatory for its proper functioning. Finally, the bottom
up model systematically uses building related data such as available appliances or occupancy,
due to the nature of the model itself (see section 2.3.3).

3.2.3 Model vs output resolution

Lastly, it is interesting to look at the time step considered for the prediction. Indeed, forecasts
serve different purposes that may require a specific resolution. From less than an hour to
yearly, several examples have been found in the literature. Often a model is test on different
output resolution since its accuracy will be relative to those. Thus, a model can show poor
performance on an hourly basis but overall good accuracy on a weekly or monthly resolution.

Figure 8 shows the repartition of the different models according to the timeframe and
resolution considered. If there is no evident clear trend, some observation can be done.
Firstly, the graph confirms the observation done in the section 3.2.1 where ANN, SVM and
time series analysis are preferred for short-term forecasts while regression and bottom up for
long-term. Secondly, hourly resolution on short-term forecast represents slightly more cases and those in every model applied. Lastly, on long-term forecasts, regression is favoured on an annual resolution of predictions over several years while bottom up is slightly preferred on lower time steps.

Discussion

The accuracy of each studies has been investigated in order to define which model performs the best in a given scenario context. However, a direct comparison of the study cases seems irrelevant because of the numerous variables influencing their performance. Indeed, models are implemented for different locations, in different time periods, with data of more or less good quality and supported by scripts more or less well written. Even the mean for accuracy determination are different (mean absolute percentage error, mean percentage error, root mean square error (RMSE), coefficient of variance of RMSE) making comparison difficult. Overall, none of the model clearly outperforms the others and seeking the most accurate is meaningless in this case. Instead, the study assumes that the most commonly used practices by the expert community are representative of the best use of forecasting models. If the position of the author is in favour of this theory, it remains obviously debatable. The above elements of response following the analysis of the critically reviewed papers have informed the development of a simple taxonomy summarizing the use of "major" models (ANN, regression, time series analysis, bottom up, SVM) in particular scenarios / applications. It is designed to answer the following type of questions:

"Which model do I need to generate hourly electricity demand/consumption of a building for the next 2 years?"
Figure 9 presents a first taxonomy faithful to the cases found in the literature. Associated with Table, it gives real cases found in the literature in order to solve a specific problem. Thus, this taxonomy does not necessarily generalized on the model that need to be used but leads the user to references they can consult.

A broader taxonomy can be developed according to the results of the previous analysis. In the same way, the user can refer to the taxonomy and choose between the recommended models. All colours superior to a particular case can be applied to this one. Table explains the values of each colour and the model associated. For instance, the daily electricity consumption on a long term period at the building level can be forecasted using a regression or a bottom up model with building related data for instance.

It should be noted that the use of the bottom up model highly depend on the availability of precise data concerning the building(s) and their appliances.

Overall, the authors suggest that the researcher tries the few models given by the forecasting models’ taxonomies fitting his or her situation (term, scale, available inputs). Thus, to the above question:

“Which model do I need to generate hourly electricity demand/consumption of a building for the next 2 years?”

we can answer:

“A bottom up model introduced with high resolution and disaggregated (by appliances) historical data that have been smoothed and building data such as occupancy, appliance
availability etc., as exogenous inputs. Environmental data such as weather condition and time index can eventually be introduced (see Ciabattoni et al. 2013; Fischer et al. 2015).”

Last concern is about the writing of academic papers. Indeed, information retrieval had been particularly difficult and the authors suggest that while presenting his or her work, the researcher provides explicitly the frame of the forecasting implementation (timeframe, time resolution, scale, inputs, outputs, pre-processing…). Moreover, the researcher should present several means for error measurement (mean absolute percentage error, mean percentage error, root mean square error (RMSE), coefficient of variance of RMSE) in order to facilitate a direct comparison across studies.

4 CONCLUSION

In this review, 113 different applications of various forecasting models distributed into 41 international papers have been studied. Many criteria have been checked such as the scale of the project, the time-term, time resolution, input employed, data pre-processing, error etc. Overall, if the models ‘selection via a direct accuracy comparison appeared to be meaningless in this study because of external elements that can interfere, some patterns in the use of the models are interesting. Considering the numerous use cases and papers studied, it is reasonable to assume that recurrence in the use of forecasting models reflects good practices. Some models seem to be favoured for electricity and power forecasting such as multivariate regression or Multiple Linear Regression, Artificial neural network and Time series analysis. Regression models are often employed for long-term prediction where periodicity and changes are less significant. This long-term predictions are often associated with socio-economic variables and building characteristics reflecting the correlation between these variables and electricity consumption on the long–term. ANN and Time series analysis are
mainly used for short-term predictions where electricity and power consumption patterns are more complex. Time series analysis leans principally on past electrical loads data while ANN are mainly set up with past values, Environmental and building/occupancy data. Support vector machine and bottom up models are present in a significant amount of paper showing increasing interest thereof. In the case of SVM, they are similar to the ANN in their usage (short-term with Environmental, past values and occupancy inputs). In the case of bottom up models, they have the advantage to be easily understandable and can be used for 1 day to 1 week ahead prediction at building level. However, the model requires a well detail dataset about appliances electricity consumption and occupancy. In some cases, a time series index is introduced in order to increase the accuracy of certain models. A time index is particularly useful when a model strongly depends on occupancy such as the bottom up model or when the time series has been decomposed in underlying patterns. Additionally, a pre-analysis and pre-processing of the input data is recommended in order to have better results. Indeed, it is recommended to smooth time series from errors and to fill missing values. A measurement of variables dependency and significance can help both on speed of computation and accuracy. Data decomposition and classification allow breaking down complex series into simpler models and thus give better performance on forecasting. Two simple taxonomies are presented therefore, one that leads to real cases found in the literature and a second that generalizes the outcomes of the study. When a researcher has to make a choice on the model to use, one can refer to the general taxonomy, going across the different branches of the tree that fit his or her situation and then try the recommended forecasting models. Equally, one can refer to the 1st taxonomy to have real use cases of the model coming from the literature. If these taxonomies do not have the ambition to reflect all the complexity of electricity power and consumption prediction, they nevertheless give a good overview and can lead to the selection of a potential model solution.


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http://dx.doi.org/10.1016/j.enbuild.2010.05.023.


http://digital-library.theiet.org/content/journals/10.1049/pe_19980110.


Suhartono & Subanar, 2006. The Effect of Decomposition Method As Data Preprocessing on


Figure 1 Fields' distribution through the papers

10 667
electricity forecasting model" OR "electricity prediction model" OR "electricity demand model" in TILT-ABS-KEY

5 845
reduction to 4 areas: "Engineering", "Energy", "Computer Science", "Environmental Science" ENGLISH language

899
building" OR "dwelling" OR "household" in TILT-ABS-KEY

153
Limited to "electric load forecasting" AND "Energy demand"

Figure 2 Selection procedure
Figure 3 Classified forecasting models distribution

Figure 4 Input distribution depending of the time horizon

Figure 5 Input distribution depending of the scale
Figure 6 Models vs time horizon distribution

Figure 7 Models vs inputs distribution
Figure 8 Models distribution by time horizon and resolution
Term: Very-Short = VS; Short = S; Mid = M; Long = L
Scale: Building = B; District = D; City = Ct; Region = R; Country = C
Resolution: Subhourly = Sh; Hourly = H; Daily = D; Weekly = W; Monthly = M; Seasonal = S; Annual = A

Figure 9 Study taxonomy
Figure 10 General taxonomy
Table 1 Cases characteristics

<table>
<thead>
<tr>
<th>Frame</th>
<th>Describe the context of the study and give an overview of the study purposes.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Location</td>
<td>Country of the case.</td>
</tr>
<tr>
<td>Scale</td>
<td>Scale of the study, from a single building to an entire country. Size of the sample are taken into account.</td>
</tr>
<tr>
<td>Term</td>
<td>From very short (1 min ahead) to very long term (several years ahead), gives the timeframe of the case.</td>
</tr>
<tr>
<td>Time resolution</td>
<td>Gives the time step considerate in the forecast: every minute, hours, day, years...</td>
</tr>
<tr>
<td>Inputs</td>
<td>Inputs implemented in the forecasting model.</td>
</tr>
<tr>
<td>Historical Data</td>
<td>Gives the length of the data sample used for the prediction as well as their origin (meters, statistical...).</td>
</tr>
<tr>
<td>Pre-processing</td>
<td>Indicates if the data have been pre-processed before being introduced into the forecasting model and which type of pre-process have been done.</td>
</tr>
<tr>
<td>Forecasting model</td>
<td>Gives the forecasting model employed</td>
</tr>
<tr>
<td>Error</td>
<td>Gives the type of error measured (CV(RMSE), MAPE, RMSE...).</td>
</tr>
</tbody>
</table>
Table 2 Term distribution through the reviewed papers and cases

<table>
<thead>
<tr>
<th>Term</th>
<th>nb studies</th>
<th>nb papers</th>
<th>Distribution percentage</th>
</tr>
</thead>
<tbody>
<tr>
<td>Very Short-Term</td>
<td>5</td>
<td>1</td>
<td>2.6%</td>
</tr>
<tr>
<td>Short-term</td>
<td>40</td>
<td>17</td>
<td>43.6%</td>
</tr>
<tr>
<td>Mid-term</td>
<td>9</td>
<td>3</td>
<td>7.7%</td>
</tr>
<tr>
<td>Long-Term</td>
<td>58</td>
<td>24</td>
<td>61.5%</td>
</tr>
</tbody>
</table>

Table 3 Inputs distribution through the papers and cases

<table>
<thead>
<tr>
<th>Exogenous Input</th>
<th>nb studies</th>
<th>nb paper</th>
<th>Distribution percentage</th>
</tr>
</thead>
<tbody>
<tr>
<td>None</td>
<td>36</td>
<td>12</td>
<td>30.8 %</td>
</tr>
<tr>
<td>Socio-economic</td>
<td>42</td>
<td>15</td>
<td>38.5%</td>
</tr>
<tr>
<td>Environmental</td>
<td>41</td>
<td>16</td>
<td>41.0%</td>
</tr>
<tr>
<td>Building</td>
<td>44</td>
<td>19</td>
<td>48.7%</td>
</tr>
<tr>
<td>Time index</td>
<td>33</td>
<td>11</td>
<td>28.2%</td>
</tr>
</tbody>
</table>
### Table 4 Taxonomy references

<table>
<thead>
<tr>
<th>#</th>
<th>Model</th>
<th>Input resolution</th>
<th>Exogenous Inputs data</th>
<th>Pre-process recommended</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Bottom up</td>
<td>Subhourly</td>
<td>Building &amp; time index</td>
<td>Smoothing</td>
<td>(Ciabattoni et al. 2013; Fischer et al. 2015)</td>
</tr>
<tr>
<td>2</td>
<td>Bottom up</td>
<td>Subhourly</td>
<td>Building &amp; socio-economic</td>
<td>None</td>
<td>(Fischer et al. 2015)</td>
</tr>
<tr>
<td>3</td>
<td>Regression</td>
<td>Monthly</td>
<td>Building</td>
<td>Dependency &amp; significance</td>
<td>(Wang 2012)</td>
</tr>
<tr>
<td>4</td>
<td>Bottom up</td>
<td>Subhourly</td>
<td>Building &amp; environmental</td>
<td>Smoothing</td>
<td>(Widen &amp; Wackelgard 2010; Richardson et al. 2009)</td>
</tr>
<tr>
<td>5</td>
<td>Regression</td>
<td>Daily</td>
<td>Socio-economic, environmental, building</td>
<td>Dependency &amp; significance</td>
<td>(Fan et al. 2015)</td>
</tr>
<tr>
<td>6</td>
<td>Bottom up</td>
<td>Subhourly</td>
<td>Building</td>
<td>None</td>
<td>(Richardson et al. 2009)</td>
</tr>
<tr>
<td>7</td>
<td>ANN</td>
<td>Annual</td>
<td>Socio-economic &amp; building</td>
<td>None</td>
<td>(Aydinalp et al. 2004; Farzana et al. 2014)</td>
</tr>
<tr>
<td>8</td>
<td>Regression</td>
<td>Annual</td>
<td>Socio-economic &amp; building</td>
<td>None</td>
<td>(Farzana et al. 2014)</td>
</tr>
<tr>
<td>9</td>
<td>ANN</td>
<td>Subhourly</td>
<td>None</td>
<td>Clustering</td>
<td>(Koprinska et al. 2011)</td>
</tr>
<tr>
<td>10</td>
<td>TSA</td>
<td>Monthly</td>
<td>None</td>
<td>None</td>
<td>(Abdel-aal &amp; Al-Garni 1997; Gonzales Chavez et al. 1999)</td>
</tr>
<tr>
<td>11</td>
<td>Regression</td>
<td>Hourly</td>
<td>None</td>
<td>Smoothing, Clustering</td>
<td>(Filik et al. 2011; Al-Hamadi &amp; Soliman 2005)</td>
</tr>
<tr>
<td>13</td>
<td>TSA</td>
<td>Subhourly</td>
<td>None</td>
<td>Smoothing, Clustering</td>
<td>(Chujai et al. 2013)</td>
</tr>
<tr>
<td>14</td>
<td>ANN</td>
<td>Subhourly</td>
<td>None</td>
<td>Clustering</td>
<td>(Koprinska et al. 2011)</td>
</tr>
<tr>
<td>15</td>
<td>Regression</td>
<td>Subhourly</td>
<td>None</td>
<td>Clustering</td>
<td>(Koprinska et al. 2011)</td>
</tr>
<tr>
<td>16</td>
<td>SVM</td>
<td>Subhourly</td>
<td>None</td>
<td>Clustering</td>
<td>(Koprinska et al. 2011)</td>
</tr>
<tr>
<td>17</td>
<td>SVM</td>
<td>Hourly</td>
<td>None</td>
<td>Smoothing, Clustering</td>
<td>(Mohandes 2002)</td>
</tr>
<tr>
<td>18</td>
<td>ANN</td>
<td>Hourly</td>
<td>Environmental, building &amp; time index</td>
<td>Clustering</td>
<td>(Hernández et al. 2014; Marvuglia &amp; Messineo 2012)</td>
</tr>
<tr>
<td>19</td>
<td>SVM</td>
<td>Subhourly</td>
<td>Socio-economic, environmental, time index</td>
<td>Smoothing, Clustering</td>
<td>(Garulli et al. 2015; Hsiao 2015)</td>
</tr>
<tr>
<td></td>
<td>Model</td>
<td>Resolution</td>
<td>Inputs</td>
<td>Pre-process</td>
<td></td>
</tr>
<tr>
<td>---</td>
<td>-------</td>
<td>------------</td>
<td>--------</td>
<td>-------------</td>
<td></td>
</tr>
<tr>
<td>20</td>
<td>ANN</td>
<td>Subhourly</td>
<td>Socio-economic, environmental, time index</td>
<td>Smoothing, Clustering</td>
<td>(Garulli et al. 2015; Hsiao 2015)</td>
</tr>
<tr>
<td>21</td>
<td>ANN</td>
<td>Hourly</td>
<td>Environmental, building &amp; time index</td>
<td>Smoothing, Dependency &amp; significance</td>
<td>(Platon et al. 2015; Jurado et al. 2015; Twanabasu &amp; Bremsd 2013; Massana et al. 2015; Beccali et al. 2008)</td>
</tr>
<tr>
<td>22</td>
<td>SVM</td>
<td>Hourly</td>
<td>Environmental, building &amp; time index</td>
<td>Smoothing eventually</td>
<td>(Twanabasu &amp; Bremsd 2013; Massana et al. 2015)</td>
</tr>
<tr>
<td>23</td>
<td>TSA</td>
<td>Hourly</td>
<td>Environmental</td>
<td>Smoothing</td>
<td>(Newsham &amp; Birt 2010; Jurado et al. 2015; Yoo &amp; Hur 2013; Twanabasu &amp; Bremsd 2013)</td>
</tr>
<tr>
<td>24</td>
<td>ANN</td>
<td>Subhourly</td>
<td>Environmental, building &amp; time index</td>
<td>Dependency &amp; significance</td>
<td>(Mena et al. 2014)</td>
</tr>
</tbody>
</table>

**Table 5 General taxonomy references**

<table>
<thead>
<tr>
<th>Colour</th>
<th>Model</th>
<th>Resolution</th>
<th>Inputs</th>
<th>Pre-process</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Regression</td>
<td>Subhourly to Hourly</td>
<td>Building data can eventually be introduced for better performance.</td>
<td>Smoothing high-resolution dataset is recommended. Clustering dataset in seasonal pattern can eventually be done to improve performance.</td>
</tr>
<tr>
<td></td>
<td>Regression</td>
<td>Hourly to Annual</td>
<td>Socio-economic data are often introduced</td>
<td>Dependency &amp; significance in order to lower the amount of input data</td>
</tr>
<tr>
<td></td>
<td>Bottom Up</td>
<td>Subhourly</td>
<td>Building data are always introduced due to the nature of the model. Environmental data and time index can eventually be introduced for better performance.</td>
<td>Smoothing high resolution data is recommended</td>
</tr>
<tr>
<td></td>
<td>ANN</td>
<td>Subhourly to Hourly</td>
<td>Can be set with a large variety of data. Mainly environmental, building and time index. Time index often improve performance.</td>
<td>Dependency &amp; significance in order to lower the amount of input data. Smoothing high-resolution data is recommended.</td>
</tr>
<tr>
<td></td>
<td>SVM</td>
<td>Subhourly to Hourly</td>
<td>Can be set with a large variety of data. Mainly environmental, building and time index</td>
<td>Smoothing high-resolution data is recommended.</td>
</tr>
<tr>
<td>Time series analysis</td>
<td>Subhourly to Hourly</td>
<td>Environmental and time index data can eventually be introduced for better performance.</td>
<td>Clustering dataset in seasonal pattern can eventually be done to improve performance.</td>
<td>Smoothing high-resolution data is recommended.</td>
</tr>
</tbody>
</table>