Synthetic observations of molecular clouds in a galactic centre environment – I. Studying maps of column density and integrated intensity

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ABSTRACT

We run numerical simulations of molecular clouds, adopting properties similar to those found in the central molecular zone (CMZ) of the Milky Way. For this, we employ the moving mesh code AREPO and perform simulations which account for a simplified treatment of timedependent chemistry and the non-isothermal nature of gas and dust. We perform simulations using an initial density of $n_0 = 10^3$ cm⁻³ and a mass of 1.3×10^5 M_{\odot}. Furthermore, we vary the virial parameter, defined as the ratio of kinetic and potential energy, $\alpha = E_{\rm kin}/|E_{\rm pot}|$, by adjusting the velocity dispersion. We set it to $\alpha = 0.5$, 2.0 and 8.0, in order to analyse the impact of the kinetic energy on our results. We account for the extreme conditions in the CMZ and increase both the interstellar radiation field (ISRF) and the cosmic ray flux (CRF) by a factor of 1000 compared to the values found in the solar neighbourhood. We use the radiative transfer code RADMC-3D to compute synthetic images in various diagnostic lines. These are [C II] at 158 µm, [O I] (145 µm), [O I] (63 µm), 12 CO ($J = 1 \rightarrow 0$) and 13 CO ($J = 1 \rightarrow 0$) at 2600 and 2720 μ m, respectively. When α is large, the turbulence disperses much of the gas in the cloud, reducing its mean density and allowing the ISRF to penetrate more deeply into the cloud's interior. This significantly alters the chemical composition of the cloud, leading to the dissociation of a significant amount of the molecular gas. On the other hand, when α is small, the cloud remains compact, allowing more of the molecular gas to survive. We show that in each case the atomic tracers accurately reflect most of the physical properties of both the H_2 and the total gas of the cloud and that they provide a useful alternative to molecular lines when studying the interstellar medium in the CMZ.

Key words: stars: formation-ISM: clouds-Galaxy: centre-galaxies: ISM.

1 INTRODUCTION

The inner few hundred parsecs of our Milky Way, known as the central molecular zone (CMZ), are rich in molecular and dense gas and account for about 5 per cent of the molecular gas content of the Galaxy (Morris & Serabyn 1996). As shown by Longmore et al. (2013), the CMZ contains gas with densities of the order of several 10^3 cm⁻³ and a total mass of $\sim 10^7$ M_{\odot}. Furthermore, it is highly turbulent (Shetty et al. 2012) and illuminated by a strong interstellar radiation field (ISRF) combined with a high cosmic ray flux (CRF; Yusef-Zadeh, Wardle & Roy 2007; Clark et al. 2013).

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It thus provides an excellent laboratory for studying the physics of the interstellar medium (ISM) under extreme conditions (such as those that also occur in distant starburst galaxies) with very high resolution.

Previous observations suggested the existence of copious CO gas in the CMZ near the Galactic Center (GC; Bania 1977; Burton, Liszt & Gordon 1978; Liszt & Burton 1978; Morris & Serabyn 1996; Bitran et al. 1997; Oka et al. 1998; Martin et al. 2004), which might be used to trace the density and velocity structure of the underlying molecular component of the ISM. However, the effect of the extreme physical conditions in the CMZ on the CO distribution within the gas and the degree to which CO is a biased tracer of the underlying cloud properties remain relatively unexplored issues. Previous numerical models of clouds in the CMZ (Clark et al. 2013) or in other harsh environments (Clark & Glover 2015) have shown that the gas is likely to be highly chemically inhomogeneous. This means that molecular tracers might tell us only little about the kinematics, the temperature and density distributions of the cloud and so on. Hence, in order to learn more about the internal physics (e.g. heating, cooling and the chemistry) of the warm gas, which makes up a large fraction of the total mass, we have to use other probes.

Recently, Clark et al. (2013) have shown that the [O I] 63 μ m and the [C II] 158 μ m fine structure lines dominate the cooling in CMZ clouds over a wide range in densities. Moreover, Rodríguez-Fernández et al. (2004) present observations of these fine structure lines in the CMZ, carried out with the ISO satellite. They show that both lines are very strong in this region and can be used to infer important information about the physics of the gas in the CMZ. Hence, using such atomic tracers in order to study the physics of molecular clouds (MCs) in the CMZ seems to be a promising approach.

In this paper, we follow up on this idea and investigate the applicability of atomic tracers to study the properties of the ISM in the CMZ. We aim to provide synthetic observations, readily comparable to observations of fine structure lines. To do so, we compute synthetic observations of MCs in a CMZ-like environment using the radiative transfer code RADMC-3D (Dullemond 2012) for various diagnostic lines, specifically for [CII] (158 um), [OI] (145 um), [O I] (63 μ m), ¹²CO (2600 μ m) and ¹³CO (2720 μ m). We perform simulations of various clouds with the moving mesh code AREPO (Springel 2010) using environmental properties similar to those experienced by a typical CMZ cloud. In particular, we adopt values for the ISRF strength and the CRF comparable to those inferred for the dense CMZ cloud G0.253+0.016, also known as 'The Brick' (see e.g. Güsten, Walmsley & Pauls 1981; Lis et al. 1994, 2001; Lis & Menten 1998; Molinari et al. 2011; Immer et al. 2012; Longmore et al. 2012; Clark et al. 2013; Kauffmann, Pillai & Zhang 2013; Johnston et al. 2014; Rathborne et al. 2014, 2015). We use values for the ISRF and the CRF that mimic the harsh conditions assumed to be found in the CMZ, which are a factor of ~ 1000 larger than the values measured in the solar neighbourhood (Habing 1968; Draine 1978; Mathis, Mezger & Panagia 1983). We simulated clouds with an initial number density of $n_0 = 10^3 \text{ cm}^{-3}$ and studied the impact of different virial α parameters, $\alpha = 0.5, 2.0$ and 8.0, on the physical properties. More information about the simulations can be found in Bertram et al. (2015). Furthermore, we note that this study is the first of two papers which analyse the properties of CMZ-like clouds. In this paper, we focus on maps of column density and integrated intensity, while in Paper II (Bertram et al. in preparation), we study the kinematic properties of our model clouds.

This paper is structured as follows. In Section 2, we present our numerical simulations and the radiative transfer postprocessing tool. In Section 3, we show and discuss the results of our studies. We present a summary and our conclusions in Section 4.

2 METHODS

The numerical simulations studied in this paper are described in more detail in Bertram et al. (2015). However, we summarize the most important aspects of the simulations here and introduce the radiative transfer post-processing, which we use for computing synthetic observational maps of the clouds in various diagnostic lines.

2.1 Hydrodynamical and chemical model

We use the moving mesh code AREPO (Springel 2010) in order to run numerical simulations of various model clouds. We have added to AREPO a detailed atomic and molecular cooling function, described in detail in Glover et al. (2010) and Glover & Clark (2012), and a simplified treatment of the basic chemistry of the gas. The chemical network is based on the work of Nelson & Langer (1997) and Glover & Mac Low (2007), and allows us to follow the formation and destruction of H₂ and CO self-consistently within our simulations. The network tracks the abundances of six species and follows 14 chemical reactions. The simplified Nelson & Langer (1997) network is known to somewhat overestimate the rate at which CO forms, owing to its neglect of atomic carbon (see the detailed discussion in Glover & Clark 2012). It also neglects the reaction

$$CO + He^+ \to C^+ + O + He, \tag{1}$$

which plays an important role in regulating the CO abundance in gas exposed to a high CRF (see e.g. Bisbas, Papadopoulos & Viti 2015; Clark & Glover 2015). Our simulations thereby overestimate the CO abundance in the simulated clouds, and hence potentially underestimate the C^+ and O abundance in regions where the CO abundance is large. Therefore, in order to establish the effect that this has on the synthetic maps, we make two versions of each map: one in which we use values for the fractional abundances of C⁺ and O taken from the simulations and a second version in which we assume that all of the carbon is in the form of C⁺ and all of the oxygen is present as O. This can be achieved by assuming zero CO abundances in our simulations. As discussed in more detail in Appendix C, we find only minor differences in the [O1] (145 µm) emission probability density function (PDF) and negligible differences in the [O I] (63 μ m) and [C II] (158 μ m) PDFs. We therefore conclude that the known weaknesses of our simplified chemical model have little influence on the results we obtain for [C_{II}] and [O_I]. Full details of the chemical model with a description of how the chemistry interacts with the ISRF via the TREECOL algorithm can be found in Clark, Glover & Klessen (2012). Further examples of the use of our chemical model with the AREPO code can be found in Smith et al. (2014a) and Smith, Glover & Klessen (2014b).

We assume that the gas has a uniform solar metallicity and adopt the standard ratio of helium to hydrogen. The abundances of carbon and oxygen are taken from Sembach et al. (2000). We use $x_{\rm C}$ = 1.4×10^{-4} and $x_0 = 3.2 \times 10^{-4}$, where x_c and x_o are the fractional abundances by number of carbon and oxygen relative to hydrogen. We note that the CMZ has supersolar metallicity. Nevertheless, we use a uniform solar value in order to be conservative regarding the cooling rates in our runs. When we start the simulations, hydrogen, helium and oxygen are in atomic form, while carbon is assumed to be in singly ionized form, as C⁺. We adopt the standard local value for the dust-to-gas ratio of 1:100 (for further discussion see e.g. Glover et al. 2010). We set the cosmic ray ionization rate of atomic hydrogen to $\zeta = 3 \times 10^{-14} \text{ s}^{-1}$ (Clark et al. 2013). This value is a factor of ~ 1000 higher than the value measured in dense clouds in the solar neighbourhood (van der Tak & van Dishoeck 2000) and is comparable to the high value that has previously been inferred in the CMZ (Yusef-Zadeh et al. 2007; Clark et al. 2013). Note, however, that it is only around a factor of 100 higher than the value derived in more diffuse gas in the solar neighbourhood (Indriolo et al. 2015). For the ISRF, we adopt the same spectral shape as given in Draine (1978). We denote the strength of the Draine ISRF as $G_0 = 1$ and perform simulations with a field strength $G_0 = 1000$ (Clark et al. 2013). This corresponds to an integral flux in the energy range 6–13.6 eV of 2.7×10^{-3} erg cm⁻² s⁻¹.

2.2 Model parameters

The clouds that we model are initially spherical and located at the centre of a large box of low-density gas. For the box, we use periodic boundary conditions. However, this is simply a convenient choice, since the boundaries do not influence the dense cloud evolution, because the size of the box is taken to be much larger than the size of the cloud. The cloud has a uniform initial hydrogen nuclei number density, which we set to 10^3 cm⁻³, and a total mass of M_{tot} = $1.3 \times 10^5 \,\mathrm{M_{\odot}}$. The initial cloud radius is $R \approx 8.9 \,\mathrm{pc}$. In all of our simulations, the density of the gas surrounding the cloud is ≈ 1 cm⁻³, but we note that our results are insensitive to this value provided that it is much smaller than the mean cloud density. The cubic side length of the total simulation domain is set to $5 \times$ the individual cloud radius of 8.9 pc, i.e. 44.5 pc in total. All clouds have zero bulk velocity and are placed in the centre of the box. The Voronoi cells initially have approximately constant volumes. We initially start with 2×10^6 cells in total. The initial cell mass within the cloud corresponds to $\approx 2 M_{\odot}$.

We make use of a Jeans refinement criterion in order to accurately refine dense and collapsed gas regions in the box over the whole simulation time. We use a constant number of 8 cells per Jeans length, which is sufficient to avoid artificial fragmentation (see e.g. Truelove et al. 1998, Greif et al. 2011 as well as Federrath et al. 2010b). Our code also includes a sink particle formation algorithm (Bate, Bonnell & Price 1995; Jappsen et al. 2005; Greif et al. 2011) to properly track the formation of stars during each run. Although our numerical models show active star formation by the end of the simulations, we ignore the sink particles in this study, since we only want to focus on the physical properties of the different gas phases. A more detailed analysis of the star formation history of our runs and the sink particle algorithm that we use can be found in Bertram et al. (2015).

We assume that the gas has a turbulent velocity field with an initial power spectrum $P(k) \propto k^{-4}$ and consists of a natural mixture of solenoidal and compressive modes (see e.g. Federrath et al. 2010a). The strength of the turbulence is set by our choice of the initial virial α parameter. This is defined as $\alpha = E_{kin}/|E_{pot}|$, i.e. the kinetic energy $E_{\rm kin} = 1/2M_{\rm tot}\sigma_v^2$ divided by the potential energy $E_{\rm pot} =$ $-3GM_{tot}^2/(5R)$ measured at the beginning of each run. The quantity σ_v denotes the 3D rms velocity dispersion in the cloud. We note that the virial parameter is also often calculated as $\alpha = 2E_{\rm kin}/|E_{\rm pot}|$ in the literature, which is different from the notation used in this paper (see, e.g. Federrath & Klessen 2012). With our definition, a value of $\alpha = 0.5$ corresponds to a cloud in virial equilibrium and $\alpha > 1.0$ describes clouds that are gravitationally unbound. In order to span a large range in the virial parameter space, we analyse models with $\alpha = 0.5, 2.0$ and 8.0. Note that although it is convenient to parametrize the models in terms of α , the underlying physical quantity that changes as we change α is the turbulent velocity dispersion of the gas, since we keep M_{tot} and the initial radius R fixed in all three models. It is therefore the changes to the velocity field, and the consequent changes to the density distribution of the gas, that dictate the observed trends seen in our simulations. However, for simplicity and clarity, we will simply refer to the different α models in our discussions in the following sections.

The turbulence is not driven and hence decays throughout the simulation (Mac Low et al. 1998). The timesteps between the individual snapshots are $\Delta t_{\text{snap}} \approx 7$ kyr, corresponding to ~200 snapshots per

simulation in total. Table 1 summarizes the initial conditions of our clouds. We note that due to the high computational cost of our $\alpha = 0.5$ model, we had to stop our run already at $t \approx 0.7 t_{\rm ff}$, while the other runs end at one free-fall time. This is due to an intense refinement of dense gas regions within the cloud. Furthermore, regarding the densities in the CMZ, we have to keep in mind that a significant number of CMZ clouds have densities higher than those modelled in our simulations, which would lead to even larger turbulent velocities in our simulations for the same constant total mass.

2.3 Radiative transfer

We post-process our data in order to generate synthetic line emission maps for the atomic and molecular tracers listed in Table 2, using the radiative transfer code RADMC-3D¹ (Dullemond 2012). We use the large velocity gradient (LVG) approximation (Sobolev 1957) to compute the C⁺, O and CO level populations. The LVG implementation in RADMC-3D is described in Shetty et al. (2011a). We use the rate coefficients for collisional excitation and de-excitation by atomic and molecular hydrogen tabulated in the Leiden data base (Schöier et al. 2005).

At the moment, RADMC-3D cannot deal with AREPO data directly. Thus, we have to map the simulation output on to a cubic grid. For that, we adopt a resolution of 512 cells in all three spatial dimensions, corresponding to a cell size of $\Delta x = \Delta y = \Delta z =$ 0.087 pc. Moreover, we also use 512 channels in velocity space for our radiative transfer post-processing, corresponding to a spectral resolution of 0.057, 0.066 and 0.102 km s⁻¹ for our models with α = 0.5, 2.0 and 8.0. Our choice of spatial resolution is determined by technical limitations within RADMC-3D: as it is a serial code, our grid size is limited by the requirement that the data should all fit within the memory of the computer that we use to carry out the postprocessing. However, for most of our tracers, we find only minor differences in the emission as we increase the grid resolution. In particular, we find that a resolution of 512³ grid cells is enough in order to properly recover the emission of the cloud for all of the tracers apart from the [O1] 63 µm line (see Appendix A). Hence, our main conclusions are not strongly affected by our choice of spatial resolution.

Our simulations do not explicitly track the abundance of ¹³CO and so we need a procedure to relate the ¹³CO number density to that of ¹²CO. A common assumption is that the ratio of ¹²CO to ¹³CO is identical to the elemental abundance ratio of ¹²C to ¹³C (see e.g. Roman-Duval et al. 2010). We make the same assumption and set the ¹²CO to ¹³CO ratio to a constant value, $R_{12/13} = 60$. In reality, physical effects like chemical fractionation (Watson, Anicich & Huntress Jr. 1976) and photodissociation (Visser, van Dishoeck & Black 2009) will alter the abundances of ¹³CO relative to ¹²CO, leading to a variable value of $R_{12/13}$ within the cloud. However, Szűcs, Glover & Klessen (2014) have shown that the resulting ¹³CO maps do not differ greatly from those that we would obtain by assuming a constant ratio of ¹²CO to ¹³CO, and so we expect this approximation to be adequate.

The radiative transfer calculation yields position–position–velocity cubes of brightness temperatures $T_{\rm B}$, which are related to the intensity via the Rayleigh–Jeans approximation,

$$T_{\rm B}(\nu) = \left(\frac{c}{\nu}\right)^2 \frac{I_{\nu}}{2k_{\rm B}},\tag{2}$$

¹ www.ita.uni-heidelberg.de/~dullemond/software/radmc-3d/

Model name	Virial α	Initial number density n_0 (cm ⁻³)	3D velocity dispersion σ_v (km s ⁻¹)	Radius <i>R</i> (pc)	Free-fall time <i>t</i> _{ff} (Myr)	Simulation end <i>t</i> _{end} (Myr)
GC-0.5-1000	0.5	1000	5.4	8.9	1.40	1.00
GC-2.0-1000	2.0	1000	10.8	8.9	1.40	1.40
GC-8.0-1000	8.0	1000	21.6	8.9	1.40	1.40

Table 1. Overview of the initial conditions for our different cloud models.

Table 2. Tracer name and type, quantum mechanical transition, wavelength λ and frequency ν of various fine structure lines, which we model with the radiative transfer code RADMC-3D.

Tracer	Туре	Transition	λ (μm)	v (GHz)
¹² CO	Molecular	$J = 1 \rightarrow 0$ $J = 1 \rightarrow 0$ ${}^{2}P_{3/2} \rightarrow {}^{2}P_{1/2}$ ${}^{3}P_{1} \rightarrow {}^{3}P_{2}$ ${}^{3}P_{0} \rightarrow {}^{3}P_{1}$	2600	115
¹³ CO	Molecular		2720	110
[C II]	Atomic		158	1900
[O I]	Atomic		63	4744
[O I]	Atomic		145	2060

where I_{ν} is the specific intensity at frequency ν and $k_{\rm B}$ the Boltzmann constant. For each run, we carry out the post-processing for each of the tracers listed in Table 2 along an arbitrary line of sight (LoS), using the last snapshot of each model. Since we use isotropic turbulence without magnetic fields, we do not expect our results to significantly depend on the specific choice of the LoS and hence we only focus on emission observed along the *z*-direction (see also Appendix B).

3 RESULTS

In this section, we analyse various physical cloud parameters using the latest time snapshot (see Table 1). We start with the thermal state of the MCs (Section 3.1) and investigate which chemical components best trace the total shape of the cloud (Section 3.2). Afterwards, we estimate the effective cloud radii by using synthetic observations in various diagnostic lines (Section 3.3). We then explore the ability of the lines listed in Table 2 to trace dense MC regions (Section 3.4) and continue with a quantitative estimate of the mass fraction of the cloud that is traced by the line emission (Section 3.5). At the end, we discuss the X_{CO} -factor of the MCs.

3.1 Thermal state of the clouds

In Fig. 1, we show the two-dimensional PDFs of gas temperatures and densities within the clouds for the different virial parameters and for all chemical components: total mass, molecular hydrogen, atomic oxygen, ionized carbon and carbon monoxide. These PDFs are mass-weighted, with the colour-coding indicating the fraction of the total mass of the cloud (in the upper row of panels) or of the species of interest (in the remaining panels) located at each point in density–temperature space. The number densities shown in the upper row of panels are the total number density of particles; in the remaining panels, we show instead the number density of the species of interest (n_{H_2} , n_0 , etc.). Fig. 1 demonstrates that the thermal state of the clouds for all of the components only weakly depends on the virial parameter. However, we find strong differences in the PDFs between the various tracers.

We find a significant amount of warm gas at densities $n \lesssim 1000 \text{ cm}^{-3}$ and temperatures between $T \approx 300-10^4 \text{ K}$. We also note

that there is a substantial scatter in the temperature at every value of the density in this regime. This gas corresponds to the warm and tenuous envelope in the outer regions of the clouds with low extinction. It is heated by the strong external ISRF via the photoelectric effect. For densities higher than $n \gtrsim 1000 \,\mathrm{cm^{-3}}$, we find an inverse relationship between the temperature and the density. The temperature decreases with increasing density, owing to the efficient self-shielding of the dense gas from the external radiation field. Such high densities only occur in the inner regions of the clouds with temperatures of $T < 100 \,\mathrm{K}$, which are cold enough to result in active star formation (for further information about the star formation history of our numerical simulations, we refer the reader to Bertram et al. 2015). These are also the parts of the cloud in which we find molecular H₂ and CO gas in our simulations.

If we compare the thermal state of the total mass to the thermal state of the other tracers, we find that only the atomic oxygen and ionized carbon show a similar behaviour over the whole range of temperatures. This is because these components exist in the diffuse cloud regions as well as in the denser, more shielded gas. We also see that molecular hydrogen is strongly dissociated in the diffuse, warm envelope of the cloud. It only reaches maximal temperatures of ~4000 K, which is lower than the warmest regions observed for the total gas. In the case of CO, the range of temperatures (30–300 K) is even smaller. This suggests that CO traces a denser, colder part of the cloud than [C II] or [O I]. We will examine the consequences of this in more detail in the following sections.

3.2 Tracing the shape of the MC

Fig. 2 shows logarithmic column density maps for the total density and the H₂ density computed along the LoS in the z-direction for virial parameters $\alpha = 0.5$, 2.0 and 8.0 for the last time snapshots (see Table 1). We see that as we increase α , and hence the velocity dispersion of the gas, the structure of the cloud changes significantly. When $\alpha = 0.5$ and the cloud is gravitationally bound, it remains relatively compact. It is therefore able to shield itself relatively well from the effects of the high external ISRF, with the result that the H₂ column density traces the total column density fairly well. In the runs with $\alpha = 2$ and 8, however, the cloud is not gravitationally bound and hence starts to expand. In addition, the strong turbulence opens up large channels into the cloud by lowering the column density locally, allowing radiation to penetrate deeper into the MC, leading to enhanced photodissociation of the molecular hydrogen. Hence, we do not find a good correlation between the total and the H_2 column density in the $\alpha = 2.0$ and 8.0 runs. Molecular hydrogen can only exist in the most dense regions of the cloud, where it is best able to self-shield from the strong external radiation field.

This is also illustrated in Fig. 3, which shows the corresponding column density PDFs for three virial parameter models. If we compare the H₂ column density PDFs with each other, we find that the peak column density in the $\alpha = 0.5$ model is shifted to larger values compared to the $\alpha = 8.0$ model by about one order of magnitude. This is because the turbulent kinetic energy in the virialized $\alpha = 0.5$



Figure 1. Physical state of the clouds at the end of our simulations. We show two-dimensional PDFs of gas temperature and number density for various chemical components for runs with $\alpha = 0.5$ (left-hand column), 2.0 (middle column), and 8.0 (right-hand column). In the upper row, the number densities shown are the total particle number density. In the remaining rows, on the other hand, they are the number density of the chemical species indicated in the panel (e.g. n_{H_2} , n_0 , etc.). Note that the scaling of the density axis therefore differs from panel to panel. The colour coding shows the fraction of the total gas mass in each logarithmic density and temperature bin.



Figure 2. Logarithmic column density maps computed along the LoS in the z-direction for the total density (top row) and the H₂ density (bottom row) for different virial parameters: $\alpha = 0.5$ (left-hand column), 2.0 (middle column) and 8.0 (right-hand column). Each side has a length of 44.5 pc. The initial cloud radius of 8.9 pc is indicated in the bottom panels.

run is much smaller than in the $\alpha = 8.0$ run, leading to denser cloud regions and thus to larger average column densities. Moreover, the fraction of H₂ gas in the total box decreases with increasing virial parameter, owing to the high external ISRF, which photodissociates those molecular components more effectively as the radiation can penetrate deeper into the cloud's interior. Furthermore, we see that the H₂ gas generally extends to much lower column densities than the total gas. This is because the total gas consists of both atomic and molecular hydrogen and thus does not fall below lower values than $N_{\text{tot}} \approx 10^{21} \text{ cm}^{-2}$ due to the H₁ background, while the fraction of H₂ gas can continuously decrease in the outer regions due to photodissociation.

In analogy to Fig. 2, Fig. 4 shows velocity-integrated intensity maps computed along the LoS in the z-direction for the same virial parameters and the different tracers presented in Table 2. We again find that the molecular tracers ¹²CO and ¹³CO are photodissociated at the edges of the MC by the strong external ISRF. This effect is even stronger if the amount of turbulent kinetic energy in the box is high. Comparing the different tracers to the total gas column in Fig. 2, we find that the cloud's shape is well reproduced by all atomic tracers, although the integrated brightness temperatures of these lines are significantly smaller than those of the ¹²CO and ¹³CO lines. This holds for all three virial parameter models. Conversely, in the case of CO, we find that neither of its isotopologues describes the total gas distribution of the cloud. However, we observe that they do remain reasonably good tracers of the dense H₂, owing to the effect of self-shielding. We will quantify this finding in Section 3.5.

3.3 Estimating the effective cloud radii

In the previous section, we established that carbon monoxide is not a good tracer for the total column density, while the atomic species better reflect the distribution of the total gas mass. In this context, CO tends to significantly underestimate the radius of the total cloud in such an extreme environment. This can compromise any observational estimates of the virial parameter α , which requires an accurate estimate for the cloud's radius (see also our follow-up study in Paper II). However, we note that it is generally complicated to define a proper cloud radius. MCs are complex hierarchical systems and estimates of cloud radii always come with some assumptions of how to define outer cloud boundaries. Hence, if we refer to the effective cloud radius in the following, we always mean the radius of a spherical cloud with the same surface area.

Below, we try to estimate the effective cloud radius $R_{\rm eff}$ in a similar fashion to what would be applied to observational data sets. At first sight, this seems to be complicated, since all clouds shown in Fig. 4 are far away from a spherical geometry. Nevertheless, we can estimate an effective radius by adopting an integrated intensity threshold W_{thresh} for each map and counting the number of cells N, which fulfil $W_{\text{cloud}} > W_{\text{thresh}}$. The values for W_{thresh} are listed in Table 3 and are chosen so that there is a clear separation between emission from the cloud and from the diffuse gas in which it is embedded. Our results are not particularly sensitive to the exact value chosen for W_{thresh} , as long as it is large enough to not be contaminated by the diffuse emission, but not so large that we miss significant emission from the cloud itself. For example, in the case of model GC-0.5-1000, values of W_{thresh} anywhere in the range 2 $< W_{\rm thresh} < 10 \,{\rm K \ km \ s^{-1}}$ give essentially the same results for $R_{\rm eff}$. For comparison, we also give the effective radii of the clouds that incorporate ~ 80 per cent of the total gas mass.

We have also verified that our adapted thresholds are comparable or greater than the practical thresholds that we would obtain using modern instruments to measure the line emission. For example, in a single pointing, the GREAT instrument (German REceiver for Astronomy at Terahertz Frequencies; Heyminck et al. 2012) on-board



Figure 3. Total mass per unit logarithmic column density for the total and the H₂ gas as shown in Fig. 2 for our different virial parameters: $\alpha = 0.5$ (top), 2.0 (middle) and 8.0 (bottom).

the Stratospheric Observatory for Infrared Astronomy (SOFIA) can measure integrated intensities of the [C II] line down to around ~0.06 K km s⁻¹ in around one hour of integration time,² although multipixel array detectors are available today that become more and more efficient. Mapping an entire cloud using multiple pointings obviously allows one to spend much less time per pointing, yielding a higher threshold, but it remains plausible to map extended regions with a sensitivity comparable to or better than the adopted threshold.

We compute the effective cloud radius $R_{\rm eff}$ by assuming an effective cloud area $A_{\rm eff} = \pi R_{\rm eff}^2$, where $A_{\rm eff} = N\Delta x^2$ and Δx is the cell size introduced in Section 2.3. Thus, we get

$$R_{\rm eff} = \sqrt{\frac{A_{\rm eff}}{\pi}} = \Delta x \sqrt{\frac{N}{\pi}}.$$
(3)

Table 4 shows the different effective radii of the various clouds presented in Fig. 4, computed via equation (3). If we compare

the different values listed in Table 4, we find that the cloud radii measured with the integrated intensities of ¹²CO and ¹³CO are significantly smaller by a factor of 1.5–2.5 compared to the values measured with the integrated intensities of the atomic tracers. This is because the strong ISRF and high CRF destroy the molecular tracers in the more diffuse regions, leading to smaller effective radii. Conversely, the radii measured with the atomic components roughly agree with each other for one specific virial parameter model and give the best radius estimate for the total cloud that incorporates ~80 per cent of all gas. These values confirm our assumption that the atomic species accurately reflect the spatial distribution of the total gas column and that they yield a robust estimate of the effective radius of the cloud.

3.4 Tracing the total and H₂ column density

Now we turn to the densest parts of the cloud, because this is where stars are formed, and we study how well atomic fine-structure lines can be used to trace this regime. Figs 5 and 6 show velocityintegrated intensities plotted against the total column density and H_2 column density for the different virial parameters and all tracers presented in Table 2. In these plots, we also show the mean value at each column density, which is indicated by a black solid line. The small fluctuations at high column densities in each plot are caused by the small number of cells available to compute an average value of W.

We find clear differences for the various chemical components. For the total density in Fig. 5, we observe that the ¹²CO and ¹³CO tracers fall off sharply with decreasing column density below $\sim 10^{22}$ cm⁻², which is due to photodissociation of the gas in the diffuse cloud regions, owing to the strong external radiation field. On the other hand, at high column densities, we find a saturation of the ¹²CO emission due to the effect of the line opacity, while the ¹³CO emission is a significantly better tracer of the column density than ¹²CO. This is because ¹³CO is optically thin and consequently can better trace compact regions within the cloud. However, even in a small regime where N_{tot} and W_{CO} show some degree of correlation, we find a substantial amount of scatter around the mean value for both ¹²CO and ¹³CO. Furthermore, we also show the scatter plots for the different atomic species in Fig. 5. As expected, we see that all atomic components extend to significantly lower column densities of $\sim 10^{21}$ cm⁻² compared to carbon monoxide. Hence, both atomic carbon and oxygen are much better tracers of the low column density material of the total gas in the cloud. However, both the [C II]158 µm and the [O I] 63 µm line saturate at higher column densities, owing to the effect of the line opacity and thus either ¹³CO or the [O1] 145 µm line is to be preferred as tracers for the dense cloud material.

For the H₂ column density in Fig. 6, we find a different result. First, we see that both ¹²CO and ¹³CO extend to significantly lower H₂ column densities of $\sim 5 \times 10^{20}-10^{21}$ cm⁻², reflecting the fact that CO is a better tracer of molecular mass than of total mass. At higher column densities, we find a qualitatively similar behaviour as for the total gas in Fig. 5, again owing to the effect of the line opacities. Moreover, we also show the scatter plots for the different atomic species. We note that both the atomic oxygen and carbon extend over a much larger range in H₂ column density than in total gas column density, showing that those components can also be used in order to accurately trace a large fraction of the molecular hydrogen mass. However, the correlation between the emission of [C II] 158 µm, [O I] 63 µm and $N_{\rm H_2}$ breaks down at H₂ column densities above $\sim 10^{20}-10^{21}$ cm⁻², owing to the optical depth of

² https://great.sofia.usra.edu/cgi-bin/great/great.cgi



Figure 4. Velocity-integrated intensity maps computed along the LoS in the *z*-direction for different virial parameters: $\alpha = 0.5$ (left-hand column), 2.0 (middle column) and 8.0 (right-hand column). From top to bottom: integrated intensity maps for ¹²CO ($J = 1 \rightarrow 0$), $[O I] (G3 \mu m)$, [O I] (145 μ m) and [C II] (158 μ m). Note the different scaling in the colour bars at the right-hand side. Each side has a length of 44.5 pc. The initial cloud radius of 8.9 pc is indicated in the bottom panels. The contour lines show the threshold values given in Table 3.

Table 3. Threshold values W_{thresh} used for the integrated intensity maps in Fig. 4 in order to estimate the effective cloud radius R_{eff} . The values are chosen such that the denser cloud regions can be clearly separated from the diffuse gas phase around it, leading to a reasonable estimate for the effective cloud radii presented in Table 4.

Model	[C π] (158 μm) (K km s ⁻¹)	[O 1] (145 µm) (K km s ⁻¹)	[O I] (63 µm) (K km s ⁻¹)	¹² CO (2600 μm) (K km s ⁻¹)	¹³ CO (2720 μm) (K km s ⁻¹)
GC-0.5-1000	3.0	1.0	0.6	1.0	1.0
GC-2.0-1000	3.0	1.0	0.6	0.3	0.3
GC-8.0-1000	3.0	0.8	0.5	0.1	0.1

Table 4. Effective radii of the clouds shown in Fig. 4, as inferred from equation (3), based on the threshold intensities given in Table 3. For comparison, we also give the effective radii of the clouds that incorporate \sim 80 per cent of the total gas mass in the second column.

Model	80 per cent of total mass (pc)	[C II] (158 μm) (pc)	[O I] (145 µm) (pc)	[O I] (63 μm) (pc)	¹² CO (2600 μm) (pc)	¹³ CO (2720 μm) (pc)
GC-0.5-1000	11.0	9.0	8.7	8.1	6.6	6.2
GC-2.0-1000	13.1	13.8	13.0	12.2	7.6	6.8
GC-8.0-1000	17.5	20.1	19.9	19.7	8.4	6.9

these lines in this density regime. This means that one has to rely on other probes in order to infer information about the compact gas regions. On the contrary, the correlation between the [O I] 145 μ m emission and $N_{\rm H_2}$ seems to be provide a better way to study the dense H₂ clumps in the cloud.

We also analyse the impact that our overestimation of the CO abundance may have on the relationship between the integrated intensity of the atomic tracers and the column density (see Appendix C). However, the influence of this turns out to be small.

3.5 Mass fraction traced by the emission

In Section 3.2, we speculated that a significant fraction of the total gas mass may not be traced by ¹²CO or ¹³CO. To quantify this finding, Fig. 7 shows the fraction of total and H₂ gas mass observed along the LoS having velocity-integrated intensities greater than a minimum value W_{min} for our various tracers. Furthermore, we analyse how this mass fraction changes as we vary W_{min} . In this context, Fig. 7 defines a theoretical limit for detecting gas above a given sensitivity threshold, e.g. determined by the telescope or the detector.

We see that all lines are a strong function of the minimum velocity-integrated intensity and of the virial parameter. In case of the mass fraction of the total gas, we find that our different atomic tracers recover almost all of the total mass if the minimum integrated intensity is $W_{\rm min} \approx 0.1 \, {\rm K \ km \ s^{-1}}$ in the lpha = 0.5 model and $W_{\rm min} \approx 1.0 \,\rm K \,\, km \,\, s^{-1}$ in the $\alpha = 2.0$ and $\alpha = 8.0$ models. Furthermore, as already indicated in Section 3.2, we see that in the case of very small threshold values W_{\min} in the $\alpha = 0.5$ model, both ¹²CO and ¹³CO only trace about 75 per cent of the total mass or less. This fraction decreases even further for higher α values. For example, if we adopt $W_{\rm min} \approx 0.1 \, {\rm K \ km \ s^{-1}}$ in the cloud with $\alpha = 8.0$, we find that only ~40 per cent of the total mass is traced by CO, while all atomic tracers recover almost 100 per cent of the total gas mass. Furthermore, we observe narrow emission ranges for some of the atomic components, which trace almost 100 per cent of the total mass. For example, regarding our intermediate $\alpha = 2.0$ model and the [O1] 63 µm tracer, almost 100 per cent of the total mass lies in the narrow emission range between $0.5 < W_{\min} < 3.0$. In the case of the other α models, we find a similar behaviour. This is because there are almost no lines of sight having higher values of integrated intensity (see also Figs 5 and 6), which may be different in even denser clouds.

Regarding the H_2 mass, we see that both ¹²CO and ¹³CO trace a higher H₂ mass fraction compared to the total mass of the cloud. This is because the molecular hydrogen can only exist in dense regions of the cloud, owing to the ability to self-shield from the external radiation field. This is similar to our finding for the carbon monoxide. Furthermore, we observe that the atomic components recover almost 100 per cent of the H₂ mass if we set $W_{\rm min} \approx$ 0.5 K km s⁻¹. Hence, we find that those components again trace a significantly higher mass fraction of the gas compared to the carbon monoxide. Regarding both ¹²CO and ¹³CO, we see that the amount of mass recovered by those molecular tracers decreases with higher virial parameter for a fixed minimum value of the integrated intensity. For example, if we adopt a value of $W_{\min} \approx 0.1$ K km s⁻¹, almost 98 per cent of the H₂ mass is traced by ¹²CO for our α = 0.5 model, while ~90 per cent is traced in our $\alpha = 2.0$ and only \sim 70 per cent can be recovered in the $\alpha = 8.0$ model. Moreover, similar to the mass fraction of the total gas mass, we also find a narrow emission range for the various atomic lines in all α models, which trace about 100 per cent of the H₂ mass. In contrast, the emission of the ¹²CO and ¹³CO molecules is extended over a much wider range in integrated intensities. Hence, a much larger emission range is needed in order to trace the whole mass of molecular hydrogen in the cloud.

In summary, we conclude that CO is only a good tracer for the molecular content of the cloud, but can miss a significant fraction of the total gas mass, particularly for unbound clouds.

3.6 Estimating the CO-to-H₂ conversion factor

Based on our maps of column densities for H₂ (Fig. 2) and velocityintegrated intensities for ¹²CO (Fig. 4), we also estimate the value of the CO-to-H₂ conversion factor, X_{CO} , in our various models. X_{CO} is a widely used quantity in particular in extragalactic astronomy to derive H₂ column densities from CO observations (Bolatto, Wolfire & Leroy 2013). It is defined via

$$X_{\rm CO} = \frac{N_{\rm H_2}}{W_{\rm CO,1-0}},\tag{4}$$

where $N_{\rm H_2}$ denotes the H₂ column density and $W_{\rm CO, 1-0}$ the velocityintegrated brightness-temperature. Previous studies tried to estimate



Figure 5. Log-log plot showing velocity-integrated intensities against total column density for different virial parameters: $\alpha = 0.5$ (left-hand column), 2.0 (middle column) and 8.0 (right-hand column). Shown are all our tracers presented in Table 2. In each plot, the mean value is indicated by a black solid line.

the X_{CO} -factor in both observations and numerical simulations (see e.g. Solomon et al. 1987; Polk et al. 1988; Young & Scoville 1991; Dame, Hartmann & Thaddeus 2001; Liszt, Pety & Lucas 2010; Glover & Mac Low 2011; Leroy et al. 2011; Glover & Clark 2012; Bolatto et al. 2013; Narayanan & Hopkins 2013; Clark & Glover 2015). For example, Shetty et al. (2011a,b) investigated the X_{CO} -

factor in numerical simulations of turbulent clouds, varying environmental properties such as the initial number density, the metallicity and the external UV field, finding cloud average values $X_{\rm CO} \approx 2-4$ $\times 10^{20}$ cm⁻² K⁻¹ km⁻¹ s for solar-metallicity models. Moreover, Bolatto et al. (2013) review the efforts to measure the CO-to-H₂ conversion factor for MCs in the Milky Way disc, recommending a



Figure 6. Same as Fig. 5, but with the column density of H_2 .

similar factor $X_{\rm CO} \sim 2 \times 10^{20} \,{\rm cm}^{-2} \,{\rm K}^{-1} \,{\rm km}^{-1}$ s with ±30 per cent uncertainty. However, all these studies arrived at the conclusion that the $X_{\rm CO}$ -factor in the Galaxy is remarkably constant, having a value of $X_{\rm CO} \approx 2-4 \times 10^{20} \,{\rm cm}^{-2} \,{\rm K}^{-1} \,{\rm km}^{-1}$ s.

Nevertheless, in the last few years concerns have been raised that the X_{CO} -factor may be significantly different from the canonical value in MCs located in the GC. For example, Narayanan et al.

(2012) have shown that large gas temperatures and velocity dispersions can increase the CO intensity, thus decreasing X_{CO} . On the other hand, the strong ISRF and CRF can also destroy the carbon monoxide, increasing X_{CO} (Clark & Glover 2015). In addition, observational measurements of X_{CO} at the centre of other nearby spiral galaxies typically find values that are lower than the canonical Galactic value (Sandstrom et al. 2013). Moreover, conditions in the



Figure 7. Cumulative fraction of the total (top row) and H₂ (bottom row) mass in the cloud for different virial parameters $\alpha = 0.5$ (left-hand column), 2.0 (middle column) and 8.0 (right-hand column), traced by our various chemical components presented in Table 2, as a function of the minimum velocity-integrated intensity in the line.

Table 5. Values of the CO-to-H₂ conversion factor, relating the amount of 12 CO ($J = 1 \rightarrow 0$) emission W_{CO} to the H₂ column density N_{H_2} for all our α runs. For the computation of the X_{CO} -factor, we only include pixels where the velocity-integrated intensity for carbon monoxide is larger than the corresponding threshold given in Table 3. Thus, X_{CO} only accounts for regions with a significant amount of CO emission in the cloud.

Model	$(\text{cm}^{-2} \text{ K}^{-1} \text{ km}^{-1} \text{ s})$
GC-0.5-1000	3.9×10^{20}
GC-2.0-1000	2.6×10^{20}
GC-8.0-1000	1.3×10^{20}

GC are somewhat similar to those found in ultra-luminous infrared galaxy (ULIRGs), and there is considerable observational evidence that X_{CO} is smaller in ULIRGs than in normal spiral galaxies (see e.g. the detailed discussion in Bolatto et al. 2013). So far, we are still missing a reliable picture of the X_{CO} -factor in different (and extreme) physical environments.

In the following, we evaluate the $X_{\rm CO}$ -factor for our three α models and list our results in Table 5. In general, the $X_{\rm CO}$ -factors given in Table 5 are computed by taking the ratio of the mean values of the H₂ column density and the velocity-integrated intensity of CO. We only include pixels where the velocity-integrated intensity for carbon monoxide is larger than the corresponding threshold given in Table 3. These are 1.0, 0.3 and 0.1 K km s⁻¹ for the models with $\alpha = 0.5$, 2.0 and 8.0. Thus, $X_{\rm CO}$ only accounts for regions with a significant available amount of CO emission in the cloud, as illustrated in Fig. 4.

We find a range of values for the CO-to-H₂ conversion factor in Table 5, reaching from $\sim 1-4 \times 10^{20} \text{ cm}^{-2} \text{ K}^{-1} \text{ km}^{-1}$ s. Our estimates are in good agreement to estimates of the canonical X_{CO}- factor in the Milky Way. However, we again emphasize that our Nelson & Langer (1997) network overestimates the rate at which CO forms (see also Section 2.1) and hence we expect that our $X_{\rm CO}$ -factors listed in Table 5 are lower limits.

Furthermore, we show logarithmic maps of the $X_{\rm CO}$ -factor for all our α models in Fig. 8. Here, the $X_{\rm CO}$ -values are evaluated by computing the ratio of the H₂ column density and the velocity-integrated intensity of CO for each individual pixel. The grey background denotes regions where the CO emission is zero. Hence, it is impossible to compute a value for $X_{\rm CO}$ there. We find significantly different values for the inner and the outer parts of the clouds. While the inner cloud regions reproduce the canonical $X_{\rm CO}$ -factor value on average, we find that the outer cloud regions exhibit significantly larger $X_{\rm CO}$ values compared to the canonical one. This is because the carbon monoxide is photodissociated at the edges of our clouds by the strong ISRF, leading to an increase in $X_{\rm CO}$. In contrast, the molecular CO is better able to self-shield in the dense parts of the cloud and hence we observe that those regions fairly reproduce the canonical value.

4 SUMMARY AND CONCLUSIONS

In this paper, we have analysed synthetic images of MCs in a CMZlike environment. For this purpose, we have performed numerical simulations of model clouds with the moving mesh code AREPO (Springel 2010) using environmental properties comparable to those experienced by typical CMZ clouds. We adopted values for the ISRF and the CRF that are a factor of ~1000 larger than the values measured in the solar neighbourhood (Clark et al. 2013). We simulated clouds with an initial number density of $n_0 = 10^3$ cm⁻³ and studied the impact of different virial α parameters of $\alpha = 0.5$, 2.0 and 8.0. The total cloud mass was set to a constant value of $M_{\text{tot}} =$ 1.3×10^5 M_☉. Furthermore, we used the radiative transfer code



Figure 8. Logarithmic maps of the CO-to-H₂ conversion factor, $X_{CO} = N_{H_2}/W_{CO}$, for the three models: $\alpha = 0.5$ (top), 2.0 (middle) and 8.0 (bottom). The average X_{CO} -factor values are given in Table 5. We see that only the inner parts of the cloud yield the canonical X_{CO} -factor value on average, while the outer cloud regions exhibit significantly larger X_{CO} values. The grey background denotes regions where the CO emission is zero. Hence, it is impossible to compute a value for X_{CO} there.

RADMC-3D (Dullemond 2012) to compute synthetic maps of our clouds in important diagnostic lines, i.e. we model the emission of the cloud in [C II] (158 µm), [O I] (145 µm), [O I] (63 µm), ^{12}CO (2600 µm) and ^{13}CO (2720 µm). We report the following findings.

(i) Atomic carbon and oxygen are found in both cold and warm regions in the clouds, but CO only traces cold regions (see Section 3.1).

(ii) If the cloud is virialized ($\alpha = 0.5$), the H₂ gas is much better able to self-shield from the high external ISRF compared to other runs with a larger α value. This is because the gravitational pressure compresses the gas to much higher densities because the amount of turbulent kinetic energy in the box is smaller in the low α models than in the high virial parameter models. In the latter case, radiation can penetrate deeper into the MC, leading to photodissociation of the molecular hydrogen (see Section 3.2).

(iii) We show that the atomic components trace the shape of the total cloud very well even in diffuse cloud regions (see Section 3.2).

(iv) On the other hand, the molecular gas (H $_2$ as well as CO) is photodissociated at the edges of the MC by the strong external ISRF.

(v) As a consequence, the photodissociation has a strong impact on measurements of the effective MC radius using a molecular tracer, which tend to significantly underestimate the radius of the total cloud in environments where the external radiation field and the turbulent kinetic energy is high. However, we find that the atomic tracers recover a significantly larger fraction of the total cloud mass (see Section 3.3).

(vi) We find a large dynamical range for the [O₁] 145 μ m line in column density space, which traces both the H₂ and the total gas up to the most dense regions in the cloud. In contrast, the [O₁] 63 μ m and [C₁₁] 158 μ m lines already saturate at significantly lower column densities. Hence, we would not expect that those components trace the compact MC regions very well (see Section 3.4).

(vii) We find that all atomic components trace almost 100 per cent of the H₂ and the total gas mass above a sensitivity threshold of $W_{\rm min} \approx 0.1$ K km s⁻¹ for the velocity-integrated intensities. However, we also find that CO only traces a significantly lower mass fraction of H₂ and the total density compared to the atomic components (see Section 3.5).

(viii) We compute values of the CO-to-H₂ conversion factor $X_{\rm CO} = N_{\rm H_2}/W_{\rm CO}$, which relates the H₂ column density $N_{\rm H_2}$ to the amount of ¹²CO ($J = 1 \rightarrow 0$) emission $W_{\rm CO}$. We find values in the range $X_{\rm CO} \approx 1-4 \times 10^{20}$ cm⁻² K⁻¹ km⁻¹ s, in good agreement to the canonical $X_{\rm CO}$ -factor values obtained in observations of MCs in the Milky Way (see Section 3.6). However, we caution that simplifications in our chemical model mean that these values are lower limits.

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APPENDIX A: RADIATIVE TRANSFER POST-PROCESSING: INFLUENCE OF GRID RESOLUTION

Since RADMC-3D cannot deal with AREPO data directly, we have to map the simulation output on to a cubic grid. The results presented in this paper are all based on a grid resolution of 512³ cells. However, we examine the sensitivity of our results to the choice of the number of grid cells in each dimension. Therefore, we run a similar radiative transfer post-processing with RADMC-3D, using resolutions of 256³ and 128³ grid zones. In Fig. A1, we compare the PDFs of the velocity-integrated intensities for our various tracers for the different grid resolutions, while using the intermediate $\alpha = 2.0$ cloud models as an example. We find that a resolution of 512^3 grid cells is enough in order to properly recover the emission of the cloud for all of the tracers apart from the $[O_1]$ 63 μ m line. In the case of $[O_1]$ 63 µm, the maps are well converged for integrated intensities of below 1.5 K km s⁻¹, but at higher integrated intensities, increasing the resolution depresses the PDF. However, as we have already seen in Section 3.4, integrated intensities of this magnitude are only recovered for [O1] 63 µm along lines of sight where the line is already optically thick. The precise values of the integrated intensity that we recover in this regime therefore do not significantly affect our conclusions.

For all of the tracers, we find that the differences between the PDFs we recover from the 256^3 and 512^3 runs are always significantly smaller than the differences between the 128^3 and 256^3 models. Thus, we do not expect to find larger differences in the PDFs for models with even higher resolution, e.g. between 512^3 and 1024^3 . Hence, due to the significant increase of the computational costs for the radiative transfer post-processing for even higher resolution



Figure A1. Emission PDFs for our various tracers for different resolution models with 128^3 , 256^3 and 512^3 grid cells for clouds with $\alpha = 2.0$.



Figure B1. Example of emission PDFs for the ¹²CO tracer for the resolution model with 512^3 grid cells. We choose the intermediate cloud model with $\alpha = 2.0$. The above figure shows the emission PDF for the *x*-, *y*- and *z*-direction. Although there are slight variations in the different PDFs, the bulk emission is the same for all directions.

runs, we focus on models with a resolution of 512^3 grid cells in this paper, which is enough to demonstrate our basic conclusions.

APPENDIX B: DEPENDENCE ON VIEWING ANGLE

When constructing our synthetic emission maps, we choose to focus on a LoS parallel to the *z*-axis of the simulation volume. However, as the turbulence in our simulations is isotropic, we expect our results to be insensitive to this choice. To test this, we have also made maps of ¹²CO for LoS parallel to the x – and y-axes, using our standard grid resolution of 512³ zones, for the run with α = 2.0. The resulting integrated intensity PDFs are shown in Fig. B1. Although there are slight variations in the different PDFs for x, yand z, the bulk emission is the same for all directions. We find a similar behaviour also for the other atomic tracers. Hence, we conclude that it is enough to focus on one specific LoS, for example the *z*-direction, in order to get an idea about the underlying physical parameters of the cloud. We note, however, that for magnetized clouds this is not necessarily true, as in this case the turbulence will no longer be isotropic, unless the field is very weak.

APPENDIX C: INFLUENCE OF THE CO ABUNDANCE ON THE LINE EMISSION OF [C II] AND [O I]

In Section 2.1, we emphasize that the simplified Nelson & Langer (1997) network that we use in our study is known to somewhat overestimate the rate at which CO forms in our simulations. Thus, we may expect that this has a consequence on the distribution of the line emission of [C II] and [O I]. In order to quantify this, we perform additional runs of radiative transfer post-processing with updated abundances of carbon and oxygen for comparison by assuming zero CO abundances in our simulations. As an example, we plot the different line emission PDFs for our various atomic tracers for a fixed resolution of 512^3 grid cells for clouds with $\alpha = 2.0$. The result is shown in Fig. C1. We find that the [C II] 158 µm and [O I] 63 µm line emission are unaffected by the changed abundances. This suggests that in the region where the CO abundance are in sensitive to this uncertainty. Support for this interpretation



Figure C1. Emission PDFs for our various atomic tracers for a fixed resolution of 512^3 grid cells for clouds with $\alpha = 2.0$. Shown are the PDFs given in Fig. A1 (with CO) together with PDFs computed from additional runs of radiative transfer post-processing with updated abundances of carbon and oxygen assuming zero CO abundances in our simulations (without CO). We do not find significant changes in the different emission PDFs of the atomic tracers.

comes from the behaviour of the [O I] 145 μ m line. As we have already seen, this has a much smaller optical depth, and hence is more strongly altered by the changed abundances. However, even in this case, the effect is relatively small: the brightest regions become around 0.1 dex brighter, but the majority of the PDF remains unaffected. We can therefore conclude that the inaccuracy introduced into our predicted [C II] and [O I] maps by our simplified chemical model is unimportant.

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