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A dual porosity model of high pressure gas flow for geoenergy applications

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7

Abstract

8 This paper presents the development of a dual porosity numerical model of multiphase, multicomponent 9 chemical/gas transport using a coupled thermal, hydraulic, chemical and mechanical formulation. 10 Appropriate relationships are used to describe the transport properties of non-ideal, reactive gas mixtures 11 at high pressure, enabling the study of geoenergy applications such as geological carbon sequestration. 12 Theoretical descriptions of the key transport processes are based on a dual porosity approach considering 13 the fracture network and porous matrix as distinct continua over the domain. Flow between the pore 14 regions is handled using mass exchange terms and the model includes equilibrium and kinetically-15 controlled chemical reactions. A numerical solution is obtained with a finite element and finite 16 difference approach and verification of the model is pursued to build confidence in the accuracy of the 17 implementation of the dual porosity governing equations. In the course of these tests, the time splitting 18 approach used to couple the transport, mass exchange and chemical reaction modules is shown to have 19 been successfully applied. It is claimed that the modelling platform developed provides an advanced 20 tool for the study of high pressure gas transport, storage and displacement for geoenergy applications 21 involving multiphase, multicomponent chemical/gas transport in dual porosity media, such as geological 22 carbon sequestration.

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Keywords: dual porosity, gas flow, high pressure, carbon sequestration, geoenergy

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24 Introduction

25 Climate change poses a great threat to the environment and society, yet there is a growing global demand 26 for energy and energy security is a political priority. Geoenergy technologies are prominent in the 27 strategies for climate change mitigation and adaptation developed as a collective response to these 28 issues. Geological carbon sequestration, for example, is intended to facilitate the decarbonisation of 29 reliable fossil fuel power plants by isolating carbon dioxide emissions in suitable deep rock formations 30 (Scott, Gilfillan et al. 2013). Other examples include enhanced hydrocarbon recovery, the exploration 31 of unconventional gas, and the deep geological disposal of nuclear waste. It is therefore important from 32 an engineering perspective to examine the complex, coupled phenomena governing the transport, storage and displacement of multiphase, multicomponent chemicals and gas in the deep 33 34 geoenvironment. This study addresses the development of a numerical model for this purpose.

35 Fractures and discontinuities are commonly important features in geological formations and can have a 36 significant bearing on the water and gas flows and reactive chemical transport. They effectively divide 37 a geomaterial into two distinct porosities, namely, the fracture network and the porous matrix blocks 38 (Bear 1993). An understanding of the physical and chemical processes involved in multiphase flow in 39 each of these pore regions is important for a rigorous prediction of the phenomena arising in the 40 geoenergy applications mentioned above. Of particular interest are the differences in the fluid transport 41 and displacement behaviour, which may depend strongly on the inter-porosity flows and various 42 physical and chemical interactions between the solid, liquid and gas phases.

43 Several established modelling techniques are available to express the heterogeneous pore structure of a 44 dual porosity geomaterial in a form more amenable to numerical treatment. In broad terms, these may 45 be categorised as: i) discrete fracture network (DFN) models, ii) equivalent continuum models, and iii) 46 dual (or higher) porosity models (Therrien and Sudicky 1996). The selection of the most appropriate 47 type of model depends on the problem scale/conditions, the available input data, the type of output data 48 required, and the available computational resources (Bear 1993, Samardzioska and Popov 2005).

49 DFN models can provide a theoretically rigorous interpretation of a fractured rock, since an attempt is 50 made to explicitly model the flow in each and every hydraulically active fracture. They are attractive 51 provided these fractures can be identified and included within the modelling framework without 52 excessive costs in terms of input data and computation time. Simulation using a DFN model inherently 53 becomes more challenging as the problem scale increases, especially given the complexity of most 54 naturally fractured reservoirs (Samardzioska and Popov 2005, Singhal and Gupta 2010).

55 Equivalent continuum models provide a simpler alternative in which the dual porosity geomaterial is 56 described as a single homogenous medium, thereby reducing the input data requirements, theoretical 57 complexity, and computational cost compared to DFN models. They are suitable provided the 58 homogenisation process adopted can accurately capture the bulk properties of the geomaterial. In 59 practical terms this requires a dense, highly interconnected fracture network to ensure that the flows in 60 the fracture and matrix pore regions remain near equilibrium with each other (Berkowitz 2002). This 61 implies that the accuracy of equivalent continuum models reduces as the partition between the fracture 62 and matrix flows becomes more apparent.

If there is an appreciable partition between the fracture and matrix flows, it is more appropriate to 63 64 employ a dual porosity model where a fracture continuum interacts with a matrix continuum. To reflect 65 the material properties of most fractured rocks, it is generally true that the fracture continuum provides 66 the majority of the flow capacity and the matrix continuum provides the majority of the storage capacity. 67 In other words, the fracture continuum is more highly conductive with a lower porosity and the matrix 68 continuum is poorly (or non-) conductive with a higher porosity (Bear 1993, Xu and Pruess 2001). 69 Provided representative properties can be assigned to the continua and the inter-porosity flow 70 interactions can be accurately theorised, a dual porosity model can capture the salient transport 71 behaviour of both fractured rocks (e.g. Bai, Elsworth et al. 1993, Xu, Sonnenthal et al. 2001, Di Donato 72 and Blunt 2004) and structured soils (e.g. Ray, Ellsworth et al. 1997, Schwartz, Juo et al. 2000).

Figure 1 shows three types of dual (or triple) porosity models that can be formulated to describe the reactive transport processes in highly fractured geomaterials (e.g. coal). A conventional dual porosity model, depicted in Figure 1a, assumes that the matrix porosity contains immobile fluids and chemicals so that there is only a single permeability, i.e. the fracture permeability. In this manner, the matrix porosity acts mainly as a sink/source to the mobile fluids and chemicals in the fractures. If the mobility of the fluids and chemicals in the matrix porosity is considered, the result is the dual porosity, dual permeability model shown in Figure 1b. Finally, the triple porosity model illustrated in Figure 1c may be more appropriate in materials with a multi-modal matrix pore size distribution (e.g. macro-/micropores), as found in some coals (Clarkson and Bustin 1999, Shi and Durucan 2005).

82 This paper describes an advanced theoretical formulation for multiphase, multicomponent reactive 83 chemical and gas transport in fractured geomaterials, including non-ideal gas behaviour. The dual 84 porosity, dual permeability approach is preferred since it has been quite widely and successfully applied 85 to this class of problems, for example in the study of coal (e.g. King, Ertekin et al. 1986, Clarkson and Bustin 1999, Shi and Durucan 2005, Ozdemir 2009, Wu, Liu et al. 2010, Thararoop, Karpyn et al. 2012), 86 87 which is particularly relevant to the present work. Moreover, from the discussion given above, dual 88 porosity models are seen to offer an attractive balance of accuracy versus practicality, requiring neither 89 large input data sets nor excessive computational effort as the problem scale increases. Theoretical 90 features relating to the coupled hydraulic, chemical, gas and mechanical behaviour have been included 91 in the formulation presented. An example is the swelling of coal in response to gas adsorption, which 92 can have a considerable feedback effect on the porosity and permeability (Clarkson and Bustin 2010).

93 The theoretical formulation has been implemented in an existing coupled thermal, hydraulic, chemical and mechanical (THCM) model, COMPASS, developed incrementally at the Geoenvironmental 94 95 Research Centre by Thomas and co-workers (Thomas and He 1998, Cleall, Seetharam et al. 2007, 96 Seetharam, Thomas et al. 2007, Thomas, Sedighi et al. 2012, Sedighi, Thomas et al. 2016). COMPASS 97 has a background of high performance simulations of three-dimensional multiphase, multicomponent 98 reactive transport in single porosity geomaterials, based on a theoretical formulation that can be 99 described as a mechanistic approach. Geochemical reactions between components in the liquid, gas and 100 solid phases are considered via the coupling of COMPASS to the geochemical model, PHREEQC 101 (version 2) (Parkhurst and Appelo 1999), with the COMPASS-PHREEQC platform having been applied 102 to study a range of problems including the performance of engineered barriers for the deep geological 103 disposal of nuclear waste. This paper presents recent developments that extend the existing capabilities 104 towards the aforementioned areas of geoenergy engineering, particularly carbon sequestration, achieved principally through the introduction of the dual porosity framework and the inclusion of non-ideal gas behaviour (Hosking 2014). A series of benchmark tests have been performed on the new model to verify the correctness of the numerical implementation, with the results of these tests also being presented in this paper.

By incorporating the new developments into the pre-existing THCM framework of COMPASS, this work has yielded an advanced model of high pressure gas transport, storage and displacement for geoenergy applications involving multiphase, multicomponent chemical/gas transport in dual porosity media. Beyond being a predictive tool, the mechanistic approach adopted allows for a detailed insight into the underlying coupled processes that govern the overall system behaviour, as well as providing flexibility for the continued development of the model.

115 **Dual porosity theoretical formulation**

116 The fracture network and porous matrix blocks are handled as distinct continua over the domain and 117 each flow variable has fracture and matrix values at every analysis point. This yields a system of 118 governing equations expressed in terms of six primary variables, namely, the pore water pressure in the 119), the concentrations of chemical components in the aqueous phase in fractures () and matrix (120 the fracture () and matrix (), and the concentrations of chemical components in the gas phase in 121) and matrix (). The gas phase is thereby modelled by considering the coupled the fracture (122 behaviour of its constituent chemical components. Mechanical behaviour is not explicitly considered in 123 the present work, with the feedback of deformation instead considered implicitly using constitutive 124 relationships describing the evolution of porosity and permeability as effective stress and chemo-125 mechanical conditions change.

126 Chemical flow through the continua is considered by advection, diffusion and dispersion mechanisms. 127 Darcy's law is used to describe the advective flow due to pressure and gravitational gradients and Fick's 128 law is used to describe molecular diffusion, with mechanical dispersion treated analogously to molecular 129 diffusion (Bear and Verruijt 1987). Sink/source terms are included to: i) handle equilibrium and 130 kinetically-controlled chemical reactions, and ii) define the mass exchange processes which couple the 131 flows in the fracture and matrix continua.

132 The governing equations for coupled thermal, hydraulic and aqueous chemical behaviour in unsaturated soils have been covered in detail elsewhere (Thomas and He 1998, Cleall, Seetharam et al. 2007, 133 134 Thomas, Sedighi et al. 2012, Sedighi, Thomas et al. 2016). In addition, the governing equations for the 135 reactive transport of multicomponent gas in a single porosity unsaturated soil have been presented by 136 Masum (2012) and Sedighi et al. (2015), assuming ideal gas behaviour. Thus, the focus of this paper is 137 on presenting the governing equations and model development for water transfer and multicomponent 138 reactive chemical transport in dual porosity geomaterials. In addition, the theoretical aspects 139 implemented in the model in relation to non-ideal gas flow at high pressure are presented.

140 General form of the governing equations

Based on the principle of conservation of mass, the temporal derivative of the water content and chemical accumulation is equal to the spatial gradient of the relevant fluxes. Sink/source terms are included allowing for chemical reactions and mass exchange between the fracture and matrix continua. The dual porosity governing equations for water transfer (equation (1)) and the reactive transport of the dissolved or gaseous chemical component (equation (2)) are then given by:

where the subscript is the phase identifier for chemical components and becomes to denote dissolved 146 147 chemical components and to denote gaseous chemical components. Similarly, the subscript is the 148 continuum identifier and becomes to denote the fracture network and to denote the porous matrix. 149 denotes the component number of the chemical and gas species present in the The superscript multiphase, multicomponent system. Accordingly, if if 150 or , where 151 and are the number of dissolved and gas components, respectively. On the left hand side of 152 equations (1) and (2), the parameter is the volumetric water (if) or gas (if) content. is the density of liquid water, and 153 is the sink/source term for the accumulation/generation of the

154 chemical component due to chemical reactions. The flux components are included on the right hand 155 side of the governing equations, where represents the advective velocity, is the effective 156 is the coefficient of mechanical dispersion. In the final terms, diffusion coefficient and and 157 represent the sinks/sources for mass exchange between the continua, with if if or 158 .

159 The volumetric water or gas content, , can be expressed in terms of the porosity and the degree of160 saturation, as:

(3)

(4)

(5)

where is the porosity and is the degree of water or gas saturation. In the absence of water vapour,
the volumetric liquid and gas contents, and , in a two phase system are bound by the
relationship:

Application of Darcy's law yields the following expression for in equations (1) and (2) (Bear andVerruijt 1987):

where is the elevation and , the unsaturated hydraulic or gas conductivity, can be expanded togive:

_____ (6)

168 where is the intrinsic permeability, is the phase relative permeability, and is the absolute169 phase viscosity.

In determining the bulk gas phase velocity, , the bulk gas pressure, i.e. , can be expressed in
terms of the sum of the concentrations of the chemical components in the gas phase using the non-ideal
gas law, given by:

7

where is the compressibility factor, i.e. the ratio of the actual molar volume to that predicted by theideal gas law, is the universal gas constant, and is the temperature.

The effective diffusion coefficient, , in equation (2) is derived from the free fluid diffusion
coefficient, , to account for the tortuous diffusion paths in a porous medium. This relationship can
be written as (Cussler 1997):

(8)

(7)

178 where is the tortuosity factor.

Mechanical dispersion in the gas phase is considered negligible compared to diffusion since gas diffusion coefficients are around four orders of magnitude greater than those of dissolved chemicals (Cussler 1997). Hence, . Furthermore, Therrien and Sudicky (1996) reported that mechanical dispersion of dissolved chemicals in rock matrix blocks is generally weak compared to diffusion and by experience may also be neglected, giving .

184 *Porosity and permeability*

It is important to clearly define how the porosity and permeability of the fracture and matrix continua 185 186 are assigned, since characterisation tests conventionally do not (or cannot) distinguish between the 187 different pore regions (Schwartz, Juo et al. 2000). With reference to Figure 2, the matrix continuum is 188 assigned the properties of the unaltered porous rock matrix, ignoring any minor splay fractures. The 189 properties in the local region of an open fracture are more complex since fractures are not necessarily 190 clear flow conduits. Open fractures can be partially or completely blocked by infilling minerals such as 191 carbonates, quartz and clays (Ward 2002), and the presence of a fracture may also give rise to a zone of 192 altered porous matrix surrounding the discontinuity. The extent of this zone is likely to be larger in softer 193 rocks, such as coal, compared to harder rocks, such as granite. In this work, an attempt has been made 194 to assign properties to the fracture continuum that represent those of the fracture 'zone' comprising open 195 fractures, mineral infillings and the altered porous matrix.

196 The fracture continuum porosity, , is the fraction of the total porosity associated with the fracture197 zone, expressed mathematically as (Gerke and van Genuchten 1993, Zheng and Samper 2015):

(9)

198 is the local fracture porosity given by the volume of the pores in the fracture zone divided by where 199 . This becomes 1.0 in a clean fracture, but may be less the total volume of the fracture zone, i.e. 200 due to mineral infillings and the presence of altered porous matrix surrounding the fracture. The 201 is the volumetric weighting factor, defined as the total volume of the fracture zone divided parameter 202 by the total volume, i.e. (Zheng and Samper 2015), analogous to the following expression 203 if the matrix blocks have a more or less regular cubic geometry:

_____ (10)

204 where and are the fracture aperture and matrix block half-width, respectively.

Equation (9) allows the matrix continuum porosity, , to be expressed in terms of the total porosity, 206 , and , as:

(11)

207 Therefore, provided the values of can be measured or estimated, the distribution of the . and 208 porosity can be defined. While the measurement of via experimental techniques (e.g. porosimetry) 209 does not present a major challenge, it is more difficult to distinguish between the fracture and matrix 210 values. Nonetheless, equation (10) may be applied to estimate , and there are some field and 211 laboratory techniques available to estimate the fracture porosity, i.e. (Singhal and Gupta 2010).

Similarly, the total intrinsic permeability, , can be readily measured in the laboratory via core flooding experiments. In order to distribute the observed permeability between the dual pore regions, it is useful to consider the wide body of literature supporting the notion that the fracture network permeability is typically several orders of magnitude greater than the porous matrix permeability (Tsang and Pruess 1987, Bear 1993, Bandurraga and Bodvarsson 1999, Philip, Jennings et al. 2005). As an example, it is up to eight orders of magnitude greater in coal (Robertson 2005). It is therefore assumed that the total permeability, , determined in a laboratory test belongs to the fracture network, i.e. , where
is the intrinsic permeability of the fracture network. The permeability of the fracture continuum, ,
is then conveniently expressed as:

The local matrix permeability, , is subsequently set to several orders of magnitude less than and
may be determined via model calibration against laboratory data (Bandurraga and Bodvarsson 1999).
The permeability of the matrix continuum, , is given by:

(13)

(12)

Equations (9) to (13) together define the approach used to assign the porosity and permeability under the dual continuum framework considered in this work.

226 Mass exchange between the fracture and matrix continua

227 Expressions for the sink/source terms controlling the exchange rates of inter-porosity water and 228 chemical components in the liquid and gas phases are presented in this section. It is assumed that quasi-229 steady state distributions of pore water pressure and chemical concentrations prevail across the porous 230 matrix block thickness at all times. This assumption is strictly only valid once the pressure or 231 concentration front due to a change in conditions in the fracture network has reached the centre of the 232 matrix block, and so may not be valid over all time scales (Lemonnier and Bourbiaux 2010). However, 233 it allows the mass exchange terms to be conveniently expressed as linear functions of the differences 234 between the fracture and average matrix pressures and concentrations (Barenblatt, Zheltov et al. 1960, 235 Warren and Root 1963, Hassanzadeh, Pooladi-Darvish et al. 2009).

The mass exchange of water is treated as an advective flow, whereas for chemicals both advective and diffusive mechanisms are considered (Gwo, Jardine et al. 1995, Ray, Ellsworth et al. 1997, Kohne, Mohanty et al. 2004). Accordingly, first-order mass exchange terms can be written for water and the dissolved chemical or gas component, expressed in a general form as (Gwo, Jardine et al. 1995, Ray, Ellsworth et al. 1997):

241 is the resident concentration, for which if mass exchange is from the fracture where 242 continuum to the matrix continuum and if the exchange is reversed. and are the first-243 order exchange rates relating to advection and diffusion, respectively. These parameters can be expanded considering the relevant geometrical and material properties, including the matrix block shape and 244 dimensions, the permeability and diffusivity of the fracture-matrix interface (i.e. the fracture zone in 245 Figure 2) and the fluid transport properties, giving expressions of the form (Schwartz, Juo et al. 2000): 246

247 where is the typical half-width of a matrix block, is the effective hydraulic conductivity between 248 the fracture and matrix pore regions, and is a dimensionless factor related to the geometry of the 249 matrix blocks, which can range from 3 for rectangular slabs to 15 for spherical aggregates (Gerke and 250 van Genuchten 1993, Kohne, Mohanty et al. 2004), but otherwise in practice may also be lumped with 251 the remaining parameters in equations (16) and (17) to form an empirical coefficient for calibration 252 using observed laboratory or field data. Gerke and van Genuchten (1993) evaluated a number of methods 253 for obtaining and concluded that an arithmetic mean approach is the most practical, giving:

254 Chemical reactions

Previous works have coupled the transport model (COMPASS) with chemical models, for example MINTEQA2 (Cleall, Seetharam et al. 2007, Seetharam, Thomas et al. 2007) and PHREEQC (version 2) (Thomas, Sedighi et al. 2012, Sedighi, Thomas et al. 2015), enabling the study of a range of geoenvironmental and geoenergy problems involving multiphase, multicomponent chemical transport in single porosity geomaterials with homogenous and heterogeneous reactions. While an extension of 260 this coupling to the dual porosity framework is not part of the present developments, which are more 261 concerned with transport processes than chemical reactions, it is considered for future development as 262 has already been accomplished in other applications of COMPASS (e.g. Sedighi, Thomas et al. 2016). 263 Nonetheless, the adsorption and desorption of multicomponent chemicals is important in geoenergy applications including carbon sequestration in coal, enhanced hydrocarbon recovery, and 264 265 unconventional gas exploration. Hence, the development of the chemical reactions presented is limited 266 here to adsorption and desorption in the solid, and it is acknowledged that a more general geochemical modelling approach will be required when a further complicated multiphase, multicomponent system is 267 268 of interest.

269 The sink/source terms, , in equations (1) and (2) can be expanded to give:

where is the dry bulk density, is the adsorbed amount of the chemical component. The factors
and are used to partition the adsorption sites between the fracture network and porous
matrix blocks.

Adsorption inherently depends on the available surface area of the adsorbent (solid phase) over which interactions with the adsorbate can occur. In fractured rock, such as coal, the majority of the surface area exists in the porous matrix blocks (Clarkson and Bustin 2010). It is therefore assumed that the matrix continuum provides all of the adsorption capacity, so that equations (19) and (20) become:

A kinetic chemical reaction is formulated to describe the adsorption/desorption phenomena, similar to that presented in the previous section for inter-porosity mass exchange. This yields a first-order model describing sorption in the matrix continuum, as (King, Ertekin et al. 1986): where is the rate of adsorption/desorption and is the adsorbed amount at equilibrium with the
free-phase adsorbate. is evaluated using an appropriate adsorption isotherm, which may be a
simple linear relationship or a nonlinear relationship such as a Langmuir isotherm.

283 Multiphase coupling

284 Changes in the degree of water saturation, , influence the physical and chemical behaviour in 285 partially saturated fractured rock, most notably through feedback to the phase relative permeability, 286 . An important characteristic of fractured rock is that the fracture network is more free-draining 287 than the porous rock matrix, making it important to define the water retention behaviour appropriately 288 in the respective continua. The rate of change of is affected by the difference between pore water 289 pressure and pore gas pressure, known as matric suction (Mitchell and Soga 2005), as well as changes to the void ratio caused by deformation (Gallipoli, Wheeler et al. 2003). The effect of the latter is less 290 291 clearly defined and often neglected in the study of fairly rigid porous media (Mašín 2010), such as coal, 292 giving:

(24)

where is the matric suction, expressed in terms of the primary variables with substitution fromequation (7), leading to (Mitchell and Soga 2005):

(25)

From equations (24) and (25), the temporal derivative of the degree of water saturation can be expandedto yield:

- ____ (26)

297 where the partial derivative of with respect to is analogous to the specific water capacity and 298 defined as the gradient of the water retention curve via the van Genuchten (1980) model, given by: where is the effective volumetric water content, and are the residual and saturated
volumetric water contents, respectively, and , and () are constants based on the
water retention characteristics of each continuum.

302 The phase relative permeability, , is evaluated from , giving:

(28)

where the function on the right hand side is given by the van Genuchten-Mualem model (Mualem 1976,
van Genuchten 1980) for , with the extended model by Parker et al. (1987) used for , giving:

(29)

(30)

305 The main limitation of this approach in the dual porosity framework is the lack of experimental data 306 available to determine the parameters of the hydraulic functions given in equations (27), (29) and (30). 307 Nonetheless, it is possible to estimate water retention curves for the fracture and matrix continua based 308 on the characteristics of the respective pore regions, most notably the pore size distributions (e.g. Zhang 309 and Fredlund 2003). Moreover, Köhne et al. (2002) presented a procedure for estimating the dual 310 permeability water retention and conductivity functions using bulk soil data, based on the notion of 311 volumetric weighting. Since volumetric weighting is also used in this formulation, future work could 312 look at applying the Köhne et al. procedure for modelling fractured rock.

Further to the water retention behaviour and phase relative permeability described in this section, the option to include gas-liquid phase transformations exists through the coupling of COMPASS with PHREEQC. However, this option has not been explored in the present work owing to the focus on carbon sequestration in coalbeds, in which the adsorbed phase tends to dominate gas storage. Coalbeds are also quite often dewatered during primary methane recovery prior to the injection of carbon dioxide (CO₂) for enhanced recovery. Further applications of the model considering problems such as carbon sequestration in saline aquifers would require an elaboration of the gas-liquid phase transformation.

320 Gas properties

Appropriate constitutive relationships are employed in the model to accurately describe the evolution of the key gas transport properties as the pressure, temperature and composition vary. In relation to the formulation described above, these properties are the non-ideal gas compressibility and the gas viscosity. Non-ideal gas compressibility is considered using the Peng and Robinson (1976) equation of state (EoS) with van der Waals mixing rules. This approach has been widely applied with a proven accuracy and requires little input data (Wei and Sadus 2000). The EoS expresses the bulk gas pressure as:

where is the effective volume of the molecules contained in one mole of bulk gas and is a coefficient accounting for the intermolecular interactions in the mixture, both of which are obtained via the van der Waals mixing rules (Kwak and Mansoori 1986). The parameter is the molar volume of the gas mixture predicted by the ideal gas law.

For an ideal gas, the factors and are zero and equation (31) reduces to the ideal gas law. However, the ideal gas law does not accurately describe the pressure-volume-temperature characteristics of gas under the majority of conditions (Dake 1978). Deviations from the ideal gas law are described by the compressibility factor, , which is determined by rewriting equation (31) as a cubic equation according to Peng and Robinson (1976):

336 where:

(33)

(32)

(34)

Of the three roots to Equation (32), the selection of depends on the number of real roots and the phase
composition of the pore fluid, as outlined by Chen et al. (2006).

339 Gas mixture viscosity is included using the semi-empirical model proposed by Chung et al. (1988). The

340 model is based on the kinetic theory of gases in combination with empirical density-dependent functions 341 and has been chosen ahead of simpler interpolative models because it describes the evolution of the 342 mixture viscosity not only with composition, but also with pressure and temperature. Moreover, the 343 model retains accuracy near the critical point and has shown absolute deviations of no more than 9% for 344 non-polar dense gas mixtures. The model is expressed as:

(35)

where is a function of the gas mixture viscosity at low pressure and is an adjustment fordense gases. These terms are fully expanded and described in Chung et al. (1988).

347 Deformation feedback

While mechanical behaviour is not explicitly considered in this work, the feedback of deformation on fluid transport is considered implicitly since it can be important in some cases of dual porosity flow. For example, the porosity and permeability of rock can be strongly influenced by effective stress changes and certain chemo-mechanical phenomena, including sorption-induced swelling/shrinking of the rock matrix. These changes in porosity and permeability are described in a general form as (Xu and Pruess 2001):

_____(36)

where the subscript denotes the initial condition, is the effective stress, and is the total sorption
strain of the matrix blocks, equal to the sum of the strains induced by each component, i.e.

Relationships in the form of equation (36) apply in the study of geomaterials which can be described as fractured sorptive elastic media (e.g. coal). A number of relationships have been presented in the literature (Palmer and Mansoori 1988, Shi and Durucan 2004, Robertson and Christiansen 2008), with an adsorption isotherm-type relationship conventionally being used to obtain . This approach has proven accurate based on comparison with the results of experimental studies (Harpalani and Chen 1995, Levine 1996).

362 **Computational approach**

363 Substitution of the pore fluid velocity from equation (5), the porosity and permeability relationships 364 from equations (9) to (13), the mass exchange sink/source terms from equations (14) and (15), and the 365 chemical reaction sink/source term from equations (22) and (23) into equations (1) and (2) produces 366 equations of the form:

367 where and are lumped coefficients of the governing equations, and and are terms 368 representing the gravitational body forces for the water and chemical terms, respectively.

369 The numerical solution of the governing equations is achieved by applying the finite element method 370 with Galerkin weighted residuals for spatial discretisation and an implicit mid-interval backward-371 difference scheme for temporal discretisation. This solution procedure follows works on the coupled 372 THM and THCM behaviour of single porosity media presented in detail by Thomas and He (1998) and 373 See tharam et al. (2007). A time splitting technique, namely the sequential non-iterative approach 374 (SNIA), is employed in which the conservative transport formulation, mass exchange and chemical reactions are solved sequentially in each time step. In other words, each time step first involves solving 375 376 the conservative transport equations in each continuum assuming no mass exchange and no reactions. Once this system has converged, the values of the primary flow variables are updated in the mass 377 378 exchange and chemical reaction modules. Although such an approach has proven successful for 379 sufficiently small time steps (Seetharam, Thomas et al. 2007, Thomas, Sedighi et al. 2012), the use of a 380 split time step via the SNIA is acknowledged as a limitation of the present work and other approaches, 381 including the sequential iterative approach (SIA) and global implicit approach, are available.

382 Model verification

383 A set of verification tests has been performed to assess the correctness of the numerical implementation

384 of the theoretical and numerical developments in the model, with benchmarks provided by analytical or 385 alternative numerical solutions presented in the literature. The first test deals with multiphase flow, 386 considering the evolution of the degree of saturation as water and gas flow in a partially saturated porous medium. In the second test, two simulations are performed for multicomponent gas transport at high 387 pressure with kinetically-controlled adsorption/desorption. The results are compared with the results of 388 389 an alternative numerical model presented in the literature. This also provides an opportunity to verify 390 the performance of the constitutive relationships implemented for non-ideal gas behaviour, most notably 391 in the case of CO₂ transport, which is highly non-ideal under the simulation conditions. A further sets of tests is then presented to examine the coupling scheme (SNIA) between the chemical transport and 392 393 inter-porosity mass exchange modules of the developed model.

394 Multiphase flow

395 This section presents a verification test (Test I) for the coupled flow of water and ideal gas in a single 396 porosity medium. The test considers a two-dimensional domain of 1 m length and 0.1 m height, spatially 397 discretised using 200 quadrilateral elements concentrated towards the upstream and downstream faces. 398 Under the simulation conditions shown in Figure 3, the isothermal system is initially partially saturated 399 with fixed pore water and gas pressures at the downstream boundary. An influx of gas begins at the 400 upstream boundary after 1 day, rising linearly from zero to 0.01 mol s⁻¹ by the end of the S 401 simulation period. The aim of the test is to verify the initial ingress of water from the downstream boundary and its subsequent displacement due to the gas influx at the upstream boundary. 402

A benchmark for the simulation results is provided by comparing the predicted changes in the degree of water saturation to the conditions expected with reference to the water retention and relative permeability functions in Figure 4 and Figure 5, respectively, based on the material parameters provided in Table 1. Similar to the approach of Köhne et al. (2002), the parameters adopted for the hydraulic functions are taken from van Genuchten (1980) and compare an un-fractured rock matrix to a finetextured porous medium, in this case "Touchet silt loam".

Figure 6 shows the predicted evolution of the degree of water saturation, , at the mid-point of the
domain, i.e. m. The first point of reference for is under the initial conditions, given as 0.81

411 by the flat section of Figure 6 at early times before water ingress from the downstream boundary. 412 Considering the initial suction of 18.1 kPa, the initial predicted in the numerical simulation agrees 413 with the expected value given by Figure 4. After this initial period, rises towards the fully saturated 414 condition as the flow of water from the downstream boundary reaches the mid-point of the domain, with 415 this condition prevailing until the onset of gas injection after 1 day (s). As expected, the gas 416 influx from the upstream boundary causes a decline in , initially sharp before tailing as it tends towards 417 the residual value of 0.405. Noting the logarithmic scales used for the time axes, the tailing of in 418 Figure 6 as the gas flux increases is comparable to that of the water retention curve in Figure 4. In other 419 is declining in the manner expected as the pore gas pressure in the system steadily increases. words.

Test I demonstrates the capability for simulating two-phase flow under the conditions considered, namely, the re-saturation of a partially saturated porous medium and the subsequent displacement of pore water through gas injection. The test therefore forms the basis for further verification of multiphase flow in future work, particularly for the dual porosity case, where inter-porosity flow and the bi-modal nature of the hydraulic functions are of relevance.

425 *Multicomponent reactive gas transport at high pressure*

Two scenarios of high pressure gas injection and displacement are simulated and the results are compared with those obtained in the numerical modelling study by Pini et al. (2011). Both scenarios deal with the enhanced displacement of methane (CH₄) due to gas injection in a 100 m long coalbed with unit cross section. The first scenario (Test II-a) considers the displacement of CH₄ during CO₂ injection, i.e. carbon sequestration, whereas the second scenario (Test II-b) considers nitrogen (N₂) injection.

Since the exercise is mainly concerned with verifying the non-ideal, multicomponent reactive gas transport behaviour, the system is treated as a single porosity medium with kinetically-controlled adsorption/desorption. The domain is discretised using 500 equally-sized 4-noded quadrilateral elements and is initially saturated with CH_4 at a pressure of 1.5 MPa at a temperature of 318 K. The amount of gas stored in the adsorbed phase is initially at equilibrium with the free gas phase and calculated using the extended Langmuir isotherm (ELI), which for the component in a gas mixture is given by(Ruthven 1984):

439 where is the Langmuir capacity and is the reciprocal of the Langmuir pressure. Equation (39) is 440 used in equation (23) to calculate the changes in the adsorbed phase as CO_2 or N_2 displaces CH_4 in the 441 coalbed.

442 The injection boundary pressure for CO₂ and N₂ is 4 MPa at , with an atmospheric pressure
443 production boundary condition prescribed at . A schematic representation of this system is

Injection boundary conditions	Initial conditions	Production boundary conditions
	Free gas (mol m ⁻³):	
Test II-a:	$c_g^{CO_2} = c_g^{N_2} = 0.0$	$RT\sum_{i=1}^{n_g} c_g^j$
$c_g^{CO_2} = 1,881.9 \text{ mol m}^{-3}$	$c_g^{CH_4} = 582.4$	$= 0.1 \times 10^6 \text{Pa}$
Test II-b:	Adsorbed gas (mol kg ⁻¹):	
$c_g^{N_2} = 1,522.5 \text{ mol m}^{-3}$	$s_{gM}^{CO_2} = s_{gM}^{N_2} = 0.0$	$\sum_{i=1}^{n_g} \frac{\partial c_g^j}{\partial t} = 0.0$
	$s_{gM}^{CH_4} = 0.75$, -

444 provided in _____

Figure 7, where the stated pressures are expressed as the equivalent gas concentrations. All of the gas properties required in the Peng and Robinson EoS have been taken from IEAGHG (2011).

447 As adopted by Pini et al. (2011), in equation (36) is expanded using the relationship proposed
448 by Gilman and Beckie (2000), giving:

(40)

where is Poisson's ratio, is Young's modulus, is the confining pressure, and the coefficientsand are defined in Table 2.

450 and are defined in rable 2.

451 along with a summary of the other physical and chemical parameters used in the simulations, including

- 452 the component viscosities, , adopted from Linstrom and Mallard (2001). The parameter is the
- 453 swelling fraction, i.e. , with given by:

454 where is the Langmuir strain and is the reciprocal of the Langmuir swelling pressure.

455



Figure 9 show the results obtained using the numerical model after 42 days of analysis for Tests II-a and II-b, respectively. There are considerable differences in the predicted CH_4 displacement profiles, with CO₂ producing a sharper yet less advanced front compared to the results for N₂ injection. Whilst both gases physically sweep free CH_4 from the pore space, these differences arise due to the sorption and sorption-induced swelling phenomena. In particular: i) coal has a higher affinity for CO₂ adsorption than for CH_4 , whereas a lower affinity for N₂ adsorption, and ii) CO₂ adsorption results in a swelling-induced permeability loss. Hence, in Test II-b, N₂ does not displace the adsorbed CH_4 as efficiently as CO_2 in

465 Test II-a, less N_2 is immobilised via adsorption, and the system permeability remains higher. The 466 displacement of the free CH₄ therefore occurs more rapidly in Test II-b, causing breakthrough of N_2 at 467 the production boundary. The significant spreading of the injection front can be attributed to the more 468 gradual displacement of the adsorbed CH₄ by N_2 compared to CO₂.

469 In both tests, the results show agreement with the benchmarks provided by Pini et al. (2011). A degree 470 of deviation is noted and may be attributed to differences in the prescribed gas viscosities. Whereas Pini 471 et al. adopted Wilke's dilute gas mixture method (Poling, Prausnitz et al. 2001) using unspecified pure 472 component viscosities, the same method has been used here for Test II but with viscosities taken from Linstrom and Mallard (2001). Hence, there may be some degree of disagreement between these 473 474 viscosities and those used by Pini et al. Based on the results achieved and under the conditions of the 475 problems described, it can be reasonably concluded that the transport behaviour of multicomponent gas, including kinetically-controlled adsorption/desorption, is accurately implemented in the numerical 476 477 model.

478 Dual porosity, dual permeability chemical transport and exchange

This section presents three verification tests (Tests III-a, III-b and III-c) for dual porosity, dual permeability chemical transport. The tests consider the transport of a chemical component in a fully saturated dual porosity geomaterial subject to steady state water flow, equilibrium adsorption, and various mass exchange rates. The simulation results are presented as chemical breakthrough curves at an analysis point and comparisons are made with the results obtained by Šimunek and van Genuchten (2008) using the HYDRUS-1D numerical model.

A two-dimensional domain of 1 m length and 0.1 m height is spatially discretised using 50 equally-sized 4-noded quadrilateral elements, with the analysis point for chemical breakthrough located at m. Each test is performed for a simulation period of 10 days with initial and maximum time steps of 100 and 3,600 seconds, respectively. The arbitrary chemical component is introduced into the system with a fixed concentration of mol m⁻³ at m and a far field concentration of mol m⁻³ at m.
Diffusion of the chemical was not considered by Šimunek and van Genuchten (2008) and equilibrium 491 adsorption was modelled using a retardation factor, . Under these conditions, the governing equation492 in equation (2) reduces to:

			(42)
493	with the coefficient of mechanical dispersion,	, given by:	

494 where is the longitudinal dispersivity.

495 Since the pore water pressures in the fracture and matrix continua are assumed to remain equilibrated,
496 the advective component of chemical mass exchange in equation (15) becomes zero. Šimunek and van
497 Genuchten (2008) then used a lumped mass exchange rate for the diffusive component, given by:

(44)

498 with the mass exchange rate, , defined as:

(45)

499 where is the chemical mass exchange rate.

500 HYDRUS-1D handles the dual porosity, dual permeability framework in a slightly different form to that 501 described in this work. Based on the work of Gerke and van Genuchten (1993), the material parameters 502 in the governing equations are defined at the local scale (e.g.), whereas in this work they are 503 defined at the bulk scale (e.g.). A discussion on the background and procedures for converting 504 between the local and bulk scales was provided in the "Porosity and permeability" section of the 505 theoretical formulation. Importantly, both approaches produce the same overall behaviour.

As an example, Šimunek and van Genuchten (2008) set as 0.1 and prescribed steady pore water velocities of $m s^{-1}$ and $m s^{-1}$ at the local scale in the fracture and matrix continua, respectively. The corresponding bulk scale hydraulic conductivities are back-calculated from

(43)

these velocities using equation (5) (m) by prescribing a pressure drop of 10 Pa over the length
of the domain and using to convert to the equivalent bulk scale conductivities, giving:

511 where is the pore water velocity at the local pore region scale, is the length of the domain, i.e. 1 m, 512 and Pa, giving $m s^{-1}$ and $m s^{-1}$.

Table 3 provides a summary of the physical and chemical parameters used in the simulations for verification Tests III-a, III-b and III-c. No mass exchange is considered in Test III-a so that the fracture and matrix continua behave as independent flow conduits. The effects of different mass exchange rates are then examined in Tests III-b and III-c, with the rate in Test III-c being five times greater than that applied in Test III-b.



Figure 10 shows the chemical breakthrough in the fracture and matrix continua with no mass exchange. It can be seen that the breakthrough in the fracture continuum occurs earlier and is sharper than in the matrix continuum. This results from a combination of the higher pore water velocity in the fracture continuum and the considerably lower chemical storage capacity provided by its porosity.



523 The breakthrough curves in

Figure 11 and Figure 12 show the role of lower (Test III-b) and higher (Test III-c) mass exchange rates 524 525 on chemical transport, respectively. Most notable are the more gradual fracture breakthrough and earlier 526 matrix breakthrough which follow an increase in the mass exchange rate. This is the expected trend 527 since the rapid chemical advance in the fracture continuum resulted in higher fracture concentrations 528 than matrix concentrations, thereby driving chemical exchange from the fracture continuum into the 529 matrix continuum. At higher mass exchange rates the resistance to these flow interactions between the 530 continua reduces. The breakthrough curves then tend towards that which would be predicted by an 531 equivalent single porosity, single permeability model.





534 Figure 10,

Figure 11 and Figure 12, it can be concluded that the sink/source term for mass exchange between the fracture and matrix continua produces the expected behaviour. Further confidence is provided by the close agreement of the results with the benchmarks provided by Šimunek and van Genuchten (2008) for HYDRUS-1D.

539 The set of verification tests presented above establish a good level of confidence regarding the accurate 540 numerical implementation of the theoretical framework for reactive flow in dual porosity geomaterials. 541 Building upon this work, the application of the model in the study of geoenergy applications, such as 542 geological carbon sequestration, will be considered in future work.

543 Conclusions

A theoretical and numerical modelling platform has been developed for studying the coupled behaviour of geoenergy systems involving the transport, storage, and displacement of multiphase, multicomponent chemicals and gas in the deep geoenvironment. Specifically, the capabilities of a coupled thermal, hydraulic, chemical and mechanical (THCM) model have been enhanced to consider hydraulic, chemical, gas and deformation behaviour based on a dual porosity, dual permeability framework.

Appropriate constitutive relationships have been included to provide an accurate description of the properties of high pressure, non-ideal gas mixtures. Additional theoretical features have also been included to allow the study of physically and chemically complex geomaterials, such as coal. There are terms in the governing equations to describe equilibrium or kinetically-controlled adsorption/desorption in the porous matrix, and an implicit approach has been employed to consider the feedback of physico-and chemo-mechanical deformation on the transport processes.

A set of verification tests of the model provided further confidence in: i) the approach taken to multiphase coupling, ii) the accuracy of the numerical implementation of the dual porosity governing equations, and iii) the effectiveness of the technique employed for coupling the transport module with the mass exchange and chemical reaction modules. The tests have been accompanied by analyses of the relevant behaviour considered, lending further confidence to the verification process.

560 The compositional structure of the model developed provides a flexible scientific tool for both present 561 and future applications in the geoenergy field. The developments are most relevant to the simulation of 562 high pressure gas transport, storage, and displacement in fractured rock during geological carbon 563 sequestration, the enhanced recovery of conventional oil and gas, the exploration of unconventional gas, 564 and the deep geological disposal of nuclear waste. Nonetheless, the model can be more generally applied 565 in the study of other geoenvironmental problems in structured soils, including groundwater flow and 566 contaminant transport. Hence, future work will focus on the application of the model to enhance the 567 current understanding in these geoenergy and geoenvironmental areas.

568

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Tables

Parameter	Value
Residual volumetric water content,	
Saturated volumetric water content,	
Hydraulic constant, (m ⁻¹)	
Hydraulic constant, (-)	
ntrinsic permeability, (m ²)	
Absolute viscosity of water, (Pa s)	
Absolute viscosity of gas, (Pa s)	
Density of liquid water, (kg m ⁻³)	

 Table 1 Material parameters used for verification Test I.

Parameter	Value		
Initial porosity, (-)			
Initial permeability, (m ²)			
Sorption rate, (s^{-1})			
Poisson's ratio, (-)			
Young's modulus, (Pa)			
Confining pressure, (Pa)			
Coal density, (kg m ⁻³)			
(-)			
	CH4	CO ₂	N2
Viscosity, (Pa s)			
(-)			
Langmuir capacity, (mol kg ⁻¹)			
Langmuir constant (sorp.), (Pa ⁻¹)			
Langmuir strain, (-)			
Langmuir constant (swell.), (Pa ⁻¹)			

 Table 2 Material parameters used for verification Tests II-a and II-b (Pini, Storti et al. 2011).

Material parameter		Relationshi	p / value	
Volumetric weighting factor, (-)				
Degree of water saturation, (-)				
Retardation factor, (-)				
Longitudinal dispersivity, (m)				
		Fracture	Matrix	
Porosity, (-)				
Hydraulic conductivity, (m s ⁻¹)				
Coeff. of mechanical dispersion,	(m ² s ⁻¹)			
		Test III-a	Test III-b	Test III-c
Solute mass exchange rates, (s ⁻¹)				

Table 3 Material parameters used for verification Tests III-a, III-b and III-c.

Figures



Figure 1 Illustration of the types of dual/triple porosity models (adopted and redrawn from Šimůnek and van Genuchten (2008)). Spheres represent the matrix porosity, including the partition of the macro- and micro-porosity where indicated. Gaps between the spheres represent the fracture porosity. Larger arrows denote permeability pathways and smaller arrows denote inter-porosity mass exchange.



Figure 2 Schematic of a segment of a fractured rock, including open and minor fractures, mineral infillings, unaltered rock matrix, and altered rock matrix (adopted and redrawn from MacQuarrie and Mayer (2005)).

[COLOUR NOT REQUIRED IN FIGURE 2]

Upstream boundary conditions	Initial conditions	Downstream boundary conditions
$0 \le t \le 1 \text{ day}$ $Q_g = 0 \text{ mol s}^{\cdot 1}$ $1 \text{ day} \le t \le 11.6 \text{ days}$ Linear increase of Q_g to $1.0 \times 10^{-2} \text{ mol s}^{\cdot 1}$	$T=298~{ m K}$ $u_l=-1.8 imes10^4~{ m Pa}$ $u_g=RTc_g=100~{ m Pa}$	$u_{l} = 100 \text{ Pa}$ $u_{g} = RTc_{g} = 100 \text{ Pa}$ $\frac{\partial u_{l}}{\partial t} = RT \frac{\partial c_{g}}{\partial t} = 0.0$

Figure 3 Schematic of the initial and boundary conditions used for Test I.



Figure 4 Water retention curve for Test I.



Figure 5 Phase relative permeability curves for Test I.



Figure 6 Predicted evolution of the degree of water saturation at the mid-point of the domain (m) for Test I.



Figure 7 Schematic of the initial and boundary conditions used for Test II-a (CO2 injection) and Test II-b (N2 injection).



Figure 8 Gas composition of CO₂ and CH₄ (Test II-a) after 42 days compared to Pini et al. (2011).



Figure 9 Gas composition of N₂ and CH₄ (Test II-b) after 42 days compared to Pini et al. (2011).



Figure 10 Chemical breakthrough for Test III-a (no mass exchange), obtained using the numerical model and by Šimunek and van Genuchten (2008) using HYDRUS-1D.



Figure 11 Chemical breakthrough for Test III-b (s-1), obtained using the by Simunek and van Genuchten (2008) using HYDRUS-1D.





Figure 12 Chemical breakthrough for Test III-c (by Šimunek and van Genuchten (2008) using HYDRUS-1D.

s-1), obtained using the numerical model and