Modelling the role of material depletion, grain coarsening and revegetation in debris flow occurrences after the 2008 Wenchuan earthquake

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Abstract

A large amount of debris was generated by the co-seismic mass wasting associated with the 2008 Mw 7.9 Wenchuan earthquake. The abundance of this loose material along the slopes caused more frequent debris flows, triggered by less intense and/or shorter rainfalls. However, both the triggering rainfall and the debris flow frequency seem to have normalised progressively during the past decade. Although changes of rainfall thresholds for post-seismic debris flows were recorded after several major earthquakes, the factors controlling these changes remain poorly constrained. With the aid of a virtual experiment, we investigate the roles of material depletion, grain coarsening and revegetation of the co-seismic debris on the propagation and deposition of debris flows initiated by runoff, as well as their influence on the triggering rainfall thresholds. We employ a Geographic Information System (GIS)-based simulation of debris flow initiation by runoff erosion, which we first calibrate on the 14th August 2010 Hongchun gully event that occurred near the Wenchuan earthquake epicentre. We obtain, by investigating each of the aforementioned processes, changing critical rainfall intensity-duration thresholds for given debris flow runout distances. Grain coarsening appears to play a major role, which is consistent with published laboratory experiments, while material depletion and revegetation do not seem able to account alone for the actual quick decay of debris flow frequency. While the virtual experiment has proven useful in identifying the first-order controls on this decay, model improvements and verification over multiple catchments are needed to make the results useful in hazard assessments.

Keywords: debris flow evolution; material depletion; grain coarsening; revegetation; rainfall thresholds; Wenchuan earthquake
1. Introduction

The 2008 M$_w$ 7.9 Wenchuan earthquake (Sichuan, China) triggered a great number of co-seismic landslides (Fan et al., 2018b; Huang and Fan, 2013), many of which were later remobilised into catastrophic debris flows triggered by rainfalls (Tang et al., 2011). A sharp increase of the frequency of debris flows was observed soon after the earthquake (Domènech et al., 2018; Fan et al., 2018b, 2018a, 2018c; Huang and Fan, 2013) in combination with a reduction of the debris flow-triggering rainfall thresholds (Guo et al., 2016b, 2016a). However, debris flows frequency and rainfall thresholds in the Wenchuan earthquake-struck area seem to have normalised already (Zhang and Zhang, 2017), following a decay similar to that observed in other mountainous regions hit by strong earthquakes (Hovius et al., 2011; Marc et al., 2015).

Kean et al. (2013) grouped the debris flows initiated by runoff into two categories: mass failure of the channel sediment by sliding along a discrete failure plane and grain-by-grain bulking by hydrodynamic forces (runoff erosion). Investigations carried out so far, and discussed in the following paragraphs, suggest that the evolution of debris flow activity is strongly controlled by: (1) the depletion of the erodible material by successive landsliding (e.g., Saito et al., 2014; Zhang and Zhang, 2017); (2) grain coarsening, that increases the hydraulic conductivity, favouring water drainage and limiting bed entrainment (e.g., Abancó and Hürlimann, 2014; Cuomo et al., 2016; Hu et al., 2017; Zhang and Zhang, 2017) and (3) revegetation, that reduces the soil erodibility, increases its shear strength and its infiltration capacity (e.g., Hales, 2018; Reubens et al., 2007; Schwarz et al., 2010; Zhu and Zhang, 2016).

Depletion of the hillslope material is a primary cause of decreasing debris flow volumes under a given hydrological forcing (Saito et al., 2014), which has been observed in the Wenchuan earthquake-affected area also through the decreasing of runout distances and
deposition widths over time (Zhang and Zhang, 2017), and has been reproduced by numerical
simulations of debris flows (van Asch et al., 2014). These led the authors to conclude that
rainfall thresholds increase after successive rain events as a result of a depletion of erodible
material in the channels. Nevertheless, the frequency of debris flows decreased significantly in
the Wenchuan earthquake-affected area even though most of the co-seismic debris is still in
place (Domènech et al., 2018; Fan et al., 2018c).

The preferential washing away of the finest particles and the consequent progressive
coarsening of the debris flow material observed in the Wenchuan earthquake-affected area
(Chen et al., 2014) has been linked with the decreasing runout and deposition distances (Zhang
et al., 2013; Zhang and Zhang, 2017) as soil erodibility decreased progressively (Chang et al.,
2011). Experiments on artificial instrumented slopes demonstrated the controlling role of soil
grading and, particularly, of that of the smallest particles in the initiation and kinematics of
flow-like landslides (Hu et al., 2017; Wang and Sassa, 2003, 2001). Hu et al. (2017) found the
internal erosion of the smallest soil fraction and its effect on the hydraulic conductivity ($k_s$,
m/s) to be a critical factor in the nucleation and development of instability that leads to flow-
like landslides in loose granular assemblies.

Field investigations (Julian and Torres, 2006; Zhu and Zhang, 2016), laboratory tests
(Mamo and Bubenzer, 2001) and numerical simulations (Shen et al., 2017) have been
conducted to analyse the effect of revegetation on soil erosion and slope stability. A significant
increase of the soil shear strength has been observed (e.g., Veylon et al., 2015; Waldron and
Dakkessian, 1981; Wu, 2013), that leads to an increased stability. Shen et al. (2017) modelled
the effects of revegetation on hillslope erosion adopting the approach described by Zhu and
Zhang (2016). They linked the changes of critical erosive shear stress ($\tau_c$, kPa) and coefficient
of erodibility ($k_d$, kPa) with the revegetation using the Root Mass Density ($RMD$, $kg/m^3$). This
quantity describes the ratio between the mass of dry roots and the mass of the root-permeated dry soil:

\[ RMD = \frac{M_R}{M_S} \]  

where \( M_R \) (kg) is the dry mass of roots and \( M_S \) (kg) is the dry mass of the entire sample.

While independent studies investigated the effects of the aforementioned processes individually, a comparative quantification of their role is lacking. By means of a virtual experiment, here we analyse the role of material depletion, grain coarsening and revegetation of the co-seismic debris at catchment scale. We compare their influence on the propagation and deposition of debris flows, initiated by runoff, as well as on the rainfall thresholds. Even though we use a site-specific setting as our baseline, we follow the input of Weiler and McDonnell (2004, 2006), who proposed the use of virtual experiments for a systematic examination of the first-order controls on complex and coupled hydro-mechanical processes. Virtual experiments, defined as numerical experiments with a model driven by collective field intelligence, can allow to assess the main and essential process constraints, whereas the irregular bedrock and surface topography and the spatial variability in soil properties make the isolation of causes and effects challenging in field studies (Weiler and McDonnell, 2006). A number of physically-based models have been proposed to simulate rainfall-induced soil erosion, transportation and deposition (Cuomo et al., 2015): the Water Erosion Prediction Project (WEPP) model (Nearing et al., 1989), the Limburg Soil Erosion Model (LISEM; De Roo, 1996), the EUROpean Soil Erosion Model (EUROSEM; Morgan et al., 1998), and the Erosion-Deposition Debris flow Analysis (EDDA 1.0) model (Chen and Zhang, 2015), among others. In this parametric study, aimed at identifying the first-order process constraints, a modified version of van Asch et al. (2014)’s model, implemented in PCRaster GIS environment (Karssenberg et al., 2001), has been chosen for its simplicity and ease to use and modify. An early version of this model was
applied by van Asch et al. (2014) to our study area, proving itself useful in reproducing the main features of the actual debris flow event, on which it was calibrated. In this work, we first re-calibrated the model on the 14th August 2010 debris flow event that occurred at Hongchun gully (Sichuan, China). Then, relations from the literature that characterise the three aforementioned processes are integrated into the model and used to simulate possible scenarios of evolutions of debris flow activity. The results are then discussed in terms of debris flow volumes and runout and of changes of the critical rainfall thresholds.

2. Study area

The Hongchun gully (103°30′21″ E, 31°4′12″ N) is a left-bank tributary of the upper course of the River Min (Minjiang). Its outlet is located just upstream of the urban centre of the town of Yingxiu, very close to the epicentre of the 2008 Wenchuan earthquake. (Fig. 1a). It subtends a catchment area of 5.35 km², with elevations ranging from 880 to 1700 m a.s.l. (Fig. 1b). The bedrock is mainly composed of deeply fractured and highly weathered granitic rock, Sinian pyroclastic rock, Carboniferous limestone and Triassic sandstone (Tang et al., 2011). The volume of co-seismic debris generated by the co-seismic mass wasting in the catchment can be quantified in about 9.3 x 10⁶ m³.

On 14th August 2010 at 03:00 h, a large debris flow occurred in the gully (Fig. 1c). It was preceded by 162.1 mm precipitation accumulated during 33 h (from 17:00 h on 12th August to 02:00 h on 14th August, local time). During the hour prior to the debris flow initiation, a rainfall intensity of 16.4 mm/h was recorded (Fig. 1d). The debris flow initiated in the erosive rills on the co-seismic deposits in the upper reaches of the catchment, due to the overland flow that progressively eroded the deposits and transported the debris into the gully (Tang et al., 2011). Eyewitnesses indicated that the largest surge moved between 03:00 h and 04:30 h. It resulted in a volume of about 7.11 x 10⁵ m³ (Tang et al., 2011) forming a deposition fan at the
outlet of the catchment, with about $4 \times 10^5$ m$^3$ reaching the River Min (Li et al., 2013), obstructing its course and thus flooding the newly reconstructed Yingxiu town and causing dozens of victims.

Figure 1. Study area and triggering rainfall. a) General view of the epicentral area of the Wenchuan earthquake and its location in Sichuan, China. The study area is indicated by a black square; b) map of the Hongchun gully displaying the co-seismic landslide deposits; c) aerial
photo taken on 15th August 2010 showing the depositional fan of the 14th August 2010 debris
flow; d) hourly and cumulative rainfall between 12th and 14th August 2010 recorded in Yingxiu.

3. Data and methods

3.1 Topography, co-seismic deposits and rainfall data

The model runs on a 10 m resolution Digital Elevation Model (DEM). Information on
the landslide deposits was obtained from a detailed inventory compiled through polygon-based
visual interpretation of high-resolution satellite images and aerial photographs (Fig. 1b)
(Domènech et al., 2018; Fan et al., 2018c). A total of 202 co-seismic landslides were identified
in the study area. The average depth of the deposits of co-seismic debris ($d$, m) was estimated
for each mapped area using the empirical relationship proposed by Tang et al. (2011),
calibrated through the analysis of 62 deposits of various size in Hongchun gully and in the
nearby Shaofang gully:

$$d = 1.2 \ln S_L - 5.6$$

where $S_L$ (m$^2$) is the individual landslide area. $d$ is thus estimated to range from 0.4 to 8.6 m,
with an average value of 4 m. It results in a range of volumes of the individual deposits between
59 m$^3$ and over 1.2x10$^6$ m$^3$. The total volume results approximately equal to 9.1x10$^6$ m$^3$.

Rainfall data with hourly resolution were retrieved from a rain gauge installed in
Yingxiu. It is located at 800 m a.s.l., 600 m from the Hongchun gully outlet (Fig. 1d).

3.2 Model description

In the model, erosion by runoff occurs when the bed shear stress ($\tau$, kPa) is larger than
the critical erosive shear stress at initiation of soil erosion ($\tau_c$, kPa), and the volumetric
concentration of solids in the debris flow \( (C_v) \) is smaller than an equilibrium value \( (C_{v\infty}) \). We use the expression for the latter as proposed by Takahashi et al. (1992):

\[
C_{v\infty} = \frac{\rho_w \tan \theta}{(\rho_s - \rho_w)(\tan \phi_{bed} - \tan \theta)}
\]  

(3)

where \( \rho_w \) (kg/m\(^3\)) is the density of water, \( \rho_s \) (kg/m\(^3\)) is the density of the solids, \( \phi_{bed} \) (\(^\circ\)) is the internal friction angle of the bed material and \( \theta \) (\(^\circ\)) is the slope angle. The erosion rate can be expressed as (Takahashi et al., 1992):

\[
i = \delta_e \frac{a_c}{d_L} U = \delta_e \frac{C_{v\infty} - C_v}{C_{v_s} - C_{v\infty}} q_t
\]  

(4)

where \( \delta_e \) is a non-dimensional coefficient of erosion rate that has been obtained through back-analysis, \( a_c \) (m) is the depth within the sediment layer where \( \tau_c = \tau \), \( d_L \) is assumed to be the same as that of the source material of the debris flow, \( U \) (m/s) is the sectional mean velocity of the flow, \( C_{v_s} \) is the volumetric fraction of solids in the erodible bed and \( q_t \) (m\(^2\)/s) is the total discharge of the sum of sediment and water per unit width expressed as (van Asch et al., 2014):

\[
q_t = (H_s + H_w)V = (H_s + h_r T_s)V
\]  

(5)

where \( H_s \) (m) is the equivalent height of solids, \( H_w \) (m) is the equivalent height of water, \( V \) (m/s) is the flow velocity, and \( T_s \) (s) is the time step duration. \( h_r \) is calculated using a simple-lumped infiltration model that ignores the effect of the initial moisture content and sorpetivity of the soil (van Asch et al., 2014):

\[
h_r = (r - k_s)
\]  

(6)

where \( r \) (m/s) is the rain intensity.
The solid materials of a debris flow begin to deposit when \( V \) is smaller than a critical flow velocity \( (V_e, \text{m/s}) \), and at the same time \( C_v \) is larger than \( C_{v\infty} \). We use the \( V_e \) proposed by Takahashi et al. (1992):

\[
V_e = \frac{2}{5d_L} \left( \frac{g \sin \theta_e \rho}{0.02 \rho_s} \right)^{0.5} \lambda^{-1} h^{1.5}
\]  

(7)

where \( g \) (m/s\(^2\)) is the gravity acceleration, \( h \) (m) is the flow height, \( \theta_e \) (º) is the flattest slope on which a debris flow that comes down through the change in slope does not stop, and \( \rho \) (kg/m\(^3\)) is the bulk density of the debris flow. \( \theta_e \) and \( \rho \) are defined as:

\[
\theta_e = \arctan \left( \frac{C_v (\rho_s - \rho_w) \tan \phi_{bed}}{C_v (\rho_s - \rho_w) + \rho_w} \right)
\]  

(8)

\[
\rho = C_v (\rho_s - \rho_w) + \rho_w
\]  

(9)

Moreover:

\[
\lambda^{-1} = \left( \frac{C_v}{C_{v\infty}} \right)^{1/3} - 1
\]  

(10)

The deposition rate \( (i, \text{m/s}) \) can be expressed as (Takahashi et al., 1992):

\[
i = \delta_d \left( 1 - \frac{V}{p_{V_e}} \right) \frac{C_{v\infty} - C_V}{C_V} \cdot V
\]  

(11)

where \( \delta_d \) is a non-dimensional coefficient of deposition rate obtained through back-analysis and \( p(<1) \) is a non-dimensional coefficient to describe the initiation of the depositing process. A value of 0.67 for the latter is recommended by Takahashi et al. (1992).

Assuming turbulent flow conditions, which seem likely in steep and rough channels (Montgomery and Buffington, 1997), \( V \) is calculated using the Manning’s equation when \( C_v \) is below an arbitrarily chosen limit of 0.4 (van Asch et al., 2014).

\[
V = \frac{h^{2/3} \sin \theta^{1/2}}{n}
\]  

(12)
where \( n \) (m\(^{1/3}\)/s) is the Manning’s number equal to 0.04 (van Asch et al., 2014). For \( C_v > 0.4 \) (van Asch et al., 2014), a simple equation of motion is used:

\[
\frac{\partial v}{\partial t} = g\left( \sin \theta \cos \theta - k \tan \theta - S_f \right)
\]

(13)

where \( k \) is the lateral pressure coefficient (taken equal to 1; van Asch et al. (2014), and \( S_f \) is a resistant factor depending on the rheology of the flow:

\[
S_f = \cos^2 \theta \tan \varphi' + \frac{1}{\rho g h} \left( \frac{3}{2} \tau_c + \frac{3 \mu}{h} V \right)
\]

(14)

where \( \varphi' (\degree) \) is the apparent friction angle of the flow for a certain pore water pressure, and \( \mu \) (kPa·s) is its dynamic viscosity.

3.3 Model calibration

The model simulates the initiation of debris flow by surface runoff. It is an improved version of the model written by van Asch et al. (2014). \( \delta_e \) and \( k_s \) were calibrated by back analysis to match the volume and shape (by visual estimation and matching degree (Fan et al., 2018a) of the 14\(^{th}\) August 2010 debris flow fan deposit at the outlet of the catchment, and the time that the debris flow reached the River Min (as reported in Tang et al., 2011). In the model, the River Min was assumed to be flowing below 895 m a.s.l. (Ouyang et al., 2015).

3.4 Effects of material depletion, grain coarsening and revegetation

In order to analyse the effect of the decreasing availability of erodible material due to successive debris flows events in the catchment, the parameters calibrated through back analysis were kept unchanged, while the output of one simulation was used as the input for the next simulation. For simplicity, and to eliminate the effect of rainfall variability, we kept using the 14\(^{th}\) August rainfall pattern in all simulations. We repeated the simulations until the runoff-
eroded material was insufficient to generate a debris flow that reached the outlet of the catchment.

Grain coarsening was accounted for in the model by increasing the mean diameter of the solid grains \((d_{50})\) and, consequently, the \(k_s\) of the granular assembly. As a matter of fact, research carried out in the Wenchuan earthquake-affected area (Chen et al., 2014; Zhang et al., 2014; Zhang and Zhang, 2017) indicates that actual successive debris flows events were characterised by increasingly coarser material due to the preferential loss of the finest particles. Evidence of this was provided experimentally by Hu et al. (2017) on artificial slopes. For loose granular slopes prepared at a given relative density, the authors evaluated significant changes of \(k_s\) and \(d_{50}\) in dependence of the progressing erosion of the granular fraction that can be transported by seepage through the soil pores. In this research, the model calibration was performed using \(d_{50}\) resulting from the highest percentage of small particles (dimension smaller than 0.5 mm). For the successive simulations, \(d_{50}\) was increased to account for the decreasing proportion of small erodible particles, until they were completely washed away. In parallel, \(k_s\) increases due to the increasing pore size and pore network connectivity. To reproduce this, we associated to each \(d_{50}\) a value of \(k_s\) following the trend observed by Hu et al. (2018, 2017). The different values of \(d_{50}\) and \(k_s\) were later compared and discussed with those obtained from other studies performed in the study area. For all simulations, we used each time the input layer containing the full amount of co-seismic material.

Regarding the revegetation effect, Zhu and Zhang (2016) simulated the process by increasing \(\tau_e\), and decreasing \(k_d\):

\[
i = k_d (\tau - \tau_e)
\]

(15)

Changes of \(\tau_e\) are introduced in eq. 14 accordingly.
To quantify the effect of the revegetation, we used the results obtained by Shen et al. (2017) in the Xiaojiagou Ravine, 5 km away from our study area. The authors quantified the revegetation on a hillslope in the years 2010, 2013 and 2015 using the $RMD$ (Zhu and Zhang, 2016). Then, they related the changes of $RMD$ with those of $\tau_c$ and $k_d$ using the empirical relationships proposed by Zhang et al. (2013) and Zhu and Zhang (2016), and considering the 2010 condition as that of a bare slope:

\[
\tau_{c\text{ coeff}} = \frac{\tau_{c\text{ for a given } RMD}}{\tau_{c\text{ for a bare slope}}} \\

k_{d\text{ coeff}} = \frac{k_{d\text{ for a given } RMD}}{k_{d\text{ for a bare slope}}}
\]

(16) (17)

Shen et al. (2017) found an increase of $RMD$ by 0.16% in 2013 (mid-level revegetation) and of 0.4% in 2015 (high-level revegetation). For 2013, this was translated into an increase of $\tau_c$ by 80% and a decrease of $k_d$ by 40%. In 2015, the increment of $\tau_c$ was of 140% and a decrease of $k_d$ by 60% compared to 2010.

### 3.5 Assessment of the changing rainfall thresholds

A parametric analysis was conducted to analyse the influence of material depletion, grain coarsening and revegetation on the critical rainfall in terms of intensity-duration (ID) thresholds. Taking the result of the calibrated model as the initial condition, the evolution of the ID curves was analysed, separately, for each process. For instance, the ID curves for the years 2010, 2013 and 2015 were calculated to analyse the effect of the revegetation. Each curve refers to the amount of rainfall, within a given period of time, necessary to generate a debris flow by runoff erosion that reaches the outlet of the gully.
4. Results

4.1 Model calibration

The best-fit model parameters used during the calibration at Hongchun gully are listed in Table 1. $d_{50}$, $\rho_s$, $C_v$, $\phi_{bed}$, $\tau_c$, $\delta_d$, $\mu$, and $n$ have been taken from the literature as specified below. On the other hand, $\delta_e$ and $k_s$ were calibrated by back analysis. Assuming a high proportion of small particle content in the co-seismic deposits of the Wenchuan earthquake (between 2% and 26% (Wang et al., 2017)), the grain size distribution obtained by Hu et al. (2017) in a co-seismic deposit from Wenjia gully, which range from 0.1 to 22% of small particle content, has been used. Therefore, a $d_{50}$ of 1.9 mm of the source material that corresponds to the maximum percentage of small particle contents (22%), i.e. the co-seismic situation before the erosion started, was chosen. It is of the same order of magnitude as the $d_{50}$ obtained by Zhang et al. (2014) in the 24th June 2008 debris flow events occurred in Pubugou Ravine (0.7 mm), which is approximately 5 km away from Hongchun gully with a similar geology mainly composed of igneous rocks such as granodiorite and diorite and quaternary deposits. $C_v$ and $\phi_{bed}$ were chosen equal to 0.65 and 35°, respectively. The first one is based on the flume experiments carried out by Takahashi et al. (1992) and later used by Chen and Zhang (2015) and Shen et al. (2017) during their simulations. Shen et al. (2017) obtained the $\phi_{bed}$ from field and laboratory tests carried out in the Xiaojiagou Ravine, located beside Pubugou Ravine, at 6.0 km from Hongchun gully and composed of igneous rocks as well. $\delta_d$ was chosen based on the results obtained by van Asch et al. (2014) which is equal to 0.0001. Both $\tau_c$ and $\mu$ are based on the results of simulations carried out in Hongchun gully (Ouyang et al., 2015) and Shuida gully (van Asch et al., 2014), with 1 kPa and 1 kPa-s. Regarding $\delta_e$ and $k_s$, a sensitivity analysis has been carried out to check their influence (Fig. 2). Results for three different values of $\delta_e$ (0.01, 0.1 and 1) and $k_s$ (0.0015 m/h, 0.003 m/h and 0.006 m/h) are presented in Fig. 2a-c and Fig. 2d-f, respectively. It can be seen as the amount of debris flows generated and its velocity of the
flow increases for higher values of $\delta_e$. Conversely, for higher values of $k_s$ the generated volume of debris flow and its velocity decreases. Considering the volume of debris flow at the depositional fan (red dot), calculated by Tang et al. (2011) from field investigations, and the time of arrival of the main event at the river (dashed red line), described also by Tang et al. (2011), the best fit has been found to be with $\delta_e = 0.1$ and $k_s = 0.003$ m/h.

Table 1. Parameters used during the calibration of the 14th August 2010 debris flow event in Hongchun gully. $d_{50}$, $\rho_s$, $C_{v*}$, $\phi_{bed}$, $\tau_c$, $\delta_d$, $\mu$ and $n$ have been taken from the literature. On the other hand, $\delta_e$, $k_s$ were calibrated by back analysis.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>$d_{50}$ (mm)</th>
<th>$\rho_w$ (kg/m$^3$)</th>
<th>$\rho_s$ (kg/m$^3$)</th>
<th>$C_{v*}$</th>
<th>$\phi_{bed}$ ($^\circ$)</th>
<th>$\tau_c$ (kPa)</th>
<th>$\delta_e$</th>
<th>$\delta_d$</th>
<th>$k_s$ (m/h)</th>
<th>$\mu$ (kPa·s)</th>
<th>$n$</th>
</tr>
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<td>1.9</td>
<td>1000</td>
<td>2600</td>
<td>0.65</td>
<td>35</td>
<td>1</td>
<td>0.1</td>
<td>0.0001</td>
<td>0.003</td>
<td>1</td>
<td>0.04</td>
<td></td>
</tr>
</tbody>
</table>

$d_{50}$ = mean grain size; $\rho_w$ = density of water; $\rho_s$ = density of solid particles; $C_{v*}$ = volume fraction of solids in the erodible bed; $\phi_{bed}$ = friction angle of soil; $\tau_c$ = yield strength; $\delta_e$ = coefficient of erosion rate; $k_s$ = soil infiltration capacity; $\mu$ = dynamic viscosity; $n$ = Manning’s number
Figure 2. Temporal evolution of the calculated volume at the depositional fan (dashed black line) and part of the deposit that reached the river (black line) for the 14\textsuperscript{th} August 2010 event in Hongchun gully using PCRaster. The debris flow simulation started on 13\textsuperscript{th} August 2010 at 14:00 h and lasted for 24 h. Coefficient of erosion rate $\delta_e = 0.01$ (a), $\delta_e = 0.1$ (b), $\delta_e = 1$ (c). Soil infiltration capacity $k_s = 0.0015$ (d), $k_s = 0.003$ (e), $k_s = 0.006$ (f). The red dot indicates the volume estimated by Tang et al. (2011) in the depositional fan. The time of arrival of the main debris flow is indicated by a dashed red line (03:00 am, Tang et al., 2011).
The results of the calibrated model are presented in Fig. 3. The debris flow event simulation started from 13th August 2010 at 14:00 h and lasted for 24 h. The code is able to reproduce the deposition of the debris flow, mostly accumulated along the main channel and at the outlet of the catchment, blocking the River Min (Fig. 3a). The simulated debris flow fan has an area of 113,280 m², which is larger than the 75,740 m² mapped from observations made by Tang et al. (2011) (depositional fan in Fig. 3a) representing a matching degree (Fan et al., 2018a) of 0.67. This mismatch could be partly due to the fact that the mapping has been done using an aerial image that prevents the identification of some parts of the fan submerged into the river and that the picture was taken one day after the event, being some material from the fan already eroded. Actually, the part of the simulated deposit that does not match with the field mapping (Tang et al., 2011) is the one located downstream with a maximum flow height between 1 and 4 m. With this height, the material flooded into the River Min is submerged and thus the area of the fan mapped in the field is underestimated. On the other hand, it also could be due to the fact that the model is not able to reproduce, exactly, the spreading of the depositional fan as it was already observed by van Asch et al. (2014). The simulated debris flow reached the river 14 hours after the initiation of the simulation, i.e., around 14th August 2010 at 04:00 h (Fig. 3b). It represents one hour of delay regarding the observations made by the eyewitness who indicated that the most important debris flows started around 03:00 h (Tang et al., 2011). This delay could be due to the failure of a debris dam upstream in the Hongchun gully, that the code is not able to simulate, and which increased the flow discharge, the transported debris volume (Tang et al., 2011) and consequently, its velocity and capacity of erosion. This effect was already observed during the calibration of the model when increasing the non-dimensional coefficient of erosion rate (Fig. 2a-c). The total volume simulated on the depositional fan is about $6.5 \times 10^5$ m³ from which, about $5.7 \times 10^5$ m³ reached the river with a
maximum thickness of 17 m (Fig. 3b). There is an underestimation of the material deposited in the fan of about 9% with respect to the one mapped by Tang et al. (2011), i.e. $7.11 \times 10^5$ m$^3$. The difference could be a result of other processes observed during the debris flow propagation. As a matter of fact, entrainment, collapses of the sidewalls, channel damming and breaching can enhance the debris flow volume (Chen et al., 2006; Hu et al., 2016) but cannot be accounted for in our simplified model. Nevertheless, the 9% of difference indicates that they were not very relevant in this case and our model is able to reproduce the amount of material transported at the depositional fan satisfactorily.

Figure 3. Best simulation of the 14th August 2010 debris flow event at Hongchun gully using PCRaster: (a) General view of the calculated flow height and zoom in of the depositional fan at the outlet of the catchment. Parameters used in the simulation are described in Table 1. (b) Temporal evolution of the calculated volume at the depositional fan (dashed black line) and part of the deposit that reached the river (black line). The red dot indicates the volume (Tang et al., 2011) in the depositional fan. The time of arrival of the main debris flows at the river is indicated with a dashed red line (3:00 am, Tang et al., 2011).
4.2 Effects of material depletion, grain coarsening and revegetation on the debris flow volumes

Regarding the material depletion, the volumes of debris flow triggered in 5 successive simulations, accounting for the erosion of the co-seismic deposits after each simulation, are presented in Fig. 4a. The largest events were generated during the first three simulations, where 648,431 m$^3$, 631,560 m$^3$ and 609,605 m$^3$ were deposited at the depositional fan, consecutively. Then, for the following two simulations, the eroded material decreased dramatically until no erosion occurred during the fifth simulation. In general, most of the erosion was given in the main channels where a larger amount of accumulated water is present (Fig. 5). The amount of material evacuated from the catchment after four simulations represents only the 25% of the total co-seismic landslides triggered by the earthquake (Table 2). Therefore, there is still a 75% of material remaining along the hillslopes that is not mobilized as debris flow under the chosen input rainfall event. In this case, since the erosion is mostly given in the main channels, once the material has been washed away, the runoff in the remaining deposits is not enough to generate a debris flow. However, in other settings (e.g. Zhang and Zhang, 2017), it is likely that the erosion of the debris deposits toes that are located in steep slopes induce an instability in the whole deposit, providing additional material to the main channel that could enlarge the final total volume or contribute to the next simulation.

Table 2. Results obtained during the simulation of the material depletion. Each simulation was computed using the remaining material in the loose deposits that was not eroded in the previous one. The debris flow at the depositional fan and the accumulated loose material evacuated from the catchment after each simulation are listed.
<table>
<thead>
<tr>
<th>Simulation number</th>
<th>Volume of depositional fan (m³)</th>
<th>Accumulated material evacuated from the catchment (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>648,431</td>
<td>7</td>
</tr>
<tr>
<td>2</td>
<td>631,560</td>
<td>14</td>
</tr>
<tr>
<td>3</td>
<td>609,605</td>
<td>20</td>
</tr>
<tr>
<td>4</td>
<td>438,108</td>
<td>25</td>
</tr>
<tr>
<td>5</td>
<td>0</td>
<td>25</td>
</tr>
</tbody>
</table>

**Figure 4.** Evolution of the simulated debris flow volumes that reach the outlet of Hongchun gully for each process: a) material depletion after each simulation (Table 2). The available erodible material before each simulation is represented; b) grain coarsening in terms of small particles content (Table 3); c) revegetation for a given RMD (Table 4). The corresponding year for each RMD, according to Shen et al. (2017), is also shown.
Figure 5. Simulated evolution of the co-seismic deposits due to material depletion. Initial thickness (in meters) of the co-seismic landslide deposits before simulating the 14th August 2010 debris flow event in Hongchun gully (a). Non-eroded material after four simulations using the calibrated parameters in PCRaster (Table 1) and using the remaining material of the previous simulations as input for the following one (b).

The influence of the grain coarsening is shown in Fig. 4b. With the decreasing of the small particles content (dimension smaller than 0.5 mm), and consequent increase of $d_{50}$, and $k_s$ (Fig. 6), there is a reduction of the total volume of debris flow. From a content of small particles of 22% to a content of 18%, the simulated volume at the depositional fan decreases from 648,431 m$^3$ to 602,556 m$^3$ (Table 3). With the content decreasing to 16%, 14% and 12%, the volume decrease becomes more pronounced, down to a minimum amount of just 51,511
m³. For lower contents of small particles, erosion of the co-seismic deposits does not occur at all in our test conditions. These results reveal the prime control of the small particles content on the hillslope erosion. This is in agreement with the experimental results presented by Hu et al. (2017), who suggested that the small particles play an important role in the initiation and runout of debris flows. In this regard, a high content of small particles may be the key to the generation and the sustainment of large positive pore pressure excess, which is a key contributor to the initiation and runout of debris flow (Iverson et al., 1997). However, the numerical approach used in this research focuses on the initiation of debris flows by runoff erosion, while it does not account for the generation of pore water pressures directly. Thus, it cannot offer an explicit simulation of the internal instability phenomena triggered by the reduction of the available shear strength upon reduction of suction, saturation and generation of positive pore water pressures (Fredlund and Rahardjo, 1993). The decreasing of the small soil fraction, and the consequent increasing of \( d_{50} \) and \( k_s \) is translated into a reduction of \( i \) (eq. 4) and of \( h_r \) (eq. 6). Conceptually, the increase of \( k_s \) hinders the generation of excess of rain and the consequent runoff with sufficient capacity of erosion. On the other hand, the larger the \( d_{50} \) the higher the energy (runoff) necessary to destabilize the sediment layer is. In terms of time, the rate at which the grain coarsening proceeds should mostly depend on the rain and on the debris flow events that wash away the smaller particles. In this research, the \( d_{50} \) corresponding to the exhaustion of fine particles is 3.5 mm. According to the observations made by Zhang et al. (2014) in the Pubugou Ravine, this mean grain size is in the range between the debris flow occurred in 2008 and 2010 suggesting that: 1) the washing away of fine particles in the Wenchuan earthquake-affected area is a rapid process that might be completed in less than two years, and 2) this process produces an increase of the critical rainfall thresholds after this period of time (Guo et al., 2016a; Yu et al., 2014; Zhou and Tang, 2014).
Table 3. \( d_{50} \) and \( k_s \) used for each small particle content (dimension smaller than 0.5 mm) (Fig. 5). The resulting simulated volume at the depositional fan is shown.

<table>
<thead>
<tr>
<th>Small particle content (%)</th>
<th>( d_{50} ) (mm)</th>
<th>( k_s ) (m/h)</th>
<th>Volume of depositional fan (m³)</th>
</tr>
</thead>
<tbody>
<tr>
<td>22</td>
<td>1.9</td>
<td>0.003</td>
<td>648,431</td>
</tr>
<tr>
<td>18</td>
<td>2.3</td>
<td>0.003</td>
<td>602,556</td>
</tr>
<tr>
<td>16</td>
<td>2.4</td>
<td>0.004</td>
<td>447,907</td>
</tr>
<tr>
<td>14</td>
<td>2.5</td>
<td>0.005</td>
<td>289,602</td>
</tr>
<tr>
<td>12</td>
<td>2.7</td>
<td>0.007</td>
<td>51,511</td>
</tr>
<tr>
<td>9</td>
<td>2.9</td>
<td>0.008</td>
<td>0</td>
</tr>
<tr>
<td>6</td>
<td>3.1</td>
<td>0.009</td>
<td>0</td>
</tr>
<tr>
<td>4</td>
<td>3.2</td>
<td>0.010</td>
<td>0</td>
</tr>
<tr>
<td>2</td>
<td>3.3</td>
<td>0.012</td>
<td>0</td>
</tr>
<tr>
<td>0</td>
<td>3.5</td>
<td>0.018</td>
<td>0</td>
</tr>
</tbody>
</table>

Figure 6. Relationship between the content of small particles (dimension smaller than 0.5 mm), \( k_s \) (at a given relative density (Hu et al., 2018)) and \( d_{50} \): this relationship has been used to simulate the effect of the grain coarsening (Fig. 4b).
The effects of the vegetation restoration over time (2010, 2013 and 2015) are shown in Fig. 4c. There is a decrease of the calculated total volume of debris flows. From 2010 to 2013 the decrease is of about 27% which is higher than that from 2013 to 2015 (6%). The reason relies on the higher increment of $\tau_c$ and decrease of $\delta_e$ from 2010 to 2013 than that from 2013 to 2015 (Table 4). Nevertheless, the results indicate that although the vegetation restoration is reducing the hillslopes erosion, the calculated debris flow volume is still considerable with 459,765 m$^3$ of material that reach the depositional fan in 2015. This may be related to the fact that the arboreal revegetation is a slow processes and in 2015 the vegetation has not fully recovered to the pre-seismic levels (Yang et al., 2018). At this point, it is important to stress that these results are based on the values obtained by Shen et al. (2017) in another area which is close to Hongchun gully. Nevertheless, the entire gully may not follow the same history of the study area analysed by Shen et al. (2017) as the revegetation can proceed at different rates depending on terrain conditions such as aspect, slope, soil type, etc. Furthermore, vegetation restoration takes place only where landslide remobilisations no longer occur or slope movements are very low (e.g. creep deformation). In other words, if substantial remobilisations are observed via satellite imagery during the period 2010-2015, these slopes cannot be considered with the same degree of vegetation as the dormant ones during the analysis of 2015. Hence, these results must be taken only as a first approach that indicates the potential of the revegetation in mitigating the hillslope erosion.

Table 4. $\delta_e$ and $\tau_c$ used to reproduce the effect of the revegetation. The values refer to the co-seismic deposits in the years 2010, 2013 and 2015 according to the RMD obtained by Shen et al. (2017). The simulated debris flow at the depositional fan is listed.
In summary, among the three analysed processes, grain coarsening of the loose deposits is the factor that reduces the hillslope erosion the most, and hence limits the consequent generation of debris flows in the short term (from 2008 to 2015).

### 4.3 Influence of material depletion, grain coarsening and revegetation on the critical rainfall thresholds

The changes on the critical rainfall threshold as a consequence of material depletion, grain coarsening and vegetation restoration have been calculated by a power law (Fig. 7): \( I = \alpha D^{-\beta} \) (18)

where \( I \) (mm/h) is the intensity of a rainfall event of a duration \( D \) (h) from the beginning until the occurrence of the debris flow and \( \alpha \) and \( \beta \) are constants.

The curves have been built by interpolating simulated rainfall events, with a given intensity and duration, and considering whether they produced a debris flow at the depositional fan or not. The effect of the antecedent rainfall has not been considered in the analysis directly: it can influence the initial moisture content, especially for the short and intense events just before the triggering rain (some hours to 1 day), and thus the critical threshold curves (van Asch et al., 2014). Furthermore, the antecedent rainfall does not play an important role for high intensity rains triggering debris flow by runoff. Additionally, the antecedent rainfall that occurred in Hongchun gully within the last 24 hours preceding the debris flow was relatively small (see Fig. 1).
The changes on the critical rainfall threshold as a consequence of the material depletion are shown in Fig. 7a. There is a shift of the ID curve after two simulations due to the depletion of material in the main channels. However, for the further simulations, the critical rainfall to generate sufficient runoff for a given runout distance until the outlet of the catchment cannot be calculated because of the lack of material to be eroded. After four simulations, the exhaustion of most of this material prevents the generation of debris flow until the depositional fan. As mentioned earlier, this effect is partly a consequence of the limitations of the code as a strong erosion at the toe of the co-seismic landslides at the main channels would lead to their collapse bringing additional material for the next events.

Conversely, the effects of the grain coarsening on the rainfall thresholds are much more evident (Fig. 7b). As expected, the critical rainfall threshold increases with the decreasing of the content of small particles. In other words, the fines of the co-seismic deposits are washed away, over time, and the rainfall necessary to generate sufficient runoff increases. From 22% to 2% of small particle content, we observe a gradual increase of the critical rainfall threshold. This increase is even more accentuated between 2% and 0.1%. This large increase, which relates to the corresponding large increase of $k_s$ (Fig 6), reveals that the runoff erosion is very sensitive to small changes of the small particles content where this content is very low.

For the revegetation of the co-seismic deposits, the evolution of the ID curve is shown in Fig. 7c. The lowest critical rainfall threshold is given for the bare ground case (2010) and it increases as the vegetation colonises the loose deposits in 2013 (mid-level revegetation) and 2015 (high-level revegetation). This increment is more evident from 2010 to 2013 where the differences between $\delta_e$ and $\tau_c$ are more significant than between 2013 and 2015. On the one hand, the period from 2010 to 2013 comprises one year more than the 2013-2015, thus the time allowed for the vegetation to recover is longer. On the other hand, in the revegetation analysis carried out by Yang et al. (2018) in the Wenchuan earthquake-affected area from 2008 to 2015,
the vegetation recovery trend tends to slow down for the years 2014 and 2015, which would agree with the lower increment of the critical rainfall threshold in 2015.

Figure 7. Evolution of the rainfall thresholds for debris flows with deposition at the outlet of Hongchun gully as a consequence of: (a) material depletion of the co-seismic deposits; (b) grain size coarsening of the co-seismic deposits. The grain size evolution has been quantified in terms of percentage of small particle content (dimension smaller than 0.5 mm) (from 22% to 0.1%); (c) revegetation of the co-seismic deposits. The equation of the best-fitted power law and its coefficient of determination are shown for the lowest and highest rainfall threshold of each process.
The values of the ID threshold constant $\alpha$ (eq. 18) found for the three analysed parameters range from 65 to 90 and $\beta$ from -0.86 to -0.555. They fit with those calculated by van Asch et al. (2014) in Wenjia ($\alpha = 62; \beta = -0.705$) and Shuida gullies ($\alpha = 83; \beta = -0.71$) during the events that occurred between September 2008 and 2010, and during August 2010, respectively. Conversely, $\alpha$ values are much higher than the ones obtained by other authors at regional scale indicating that the mean rainfall intensity required is higher. Exponent values, which define the variation of the rainfall intensity threshold towards higher rainfall durations, remain in the same order of magnitude: Guo et al. (2016b) found that the threshold increased annually from $I = 5.46D^{-0.75}$ in 2008 to $I = 17.14D^{-0.75}$ in 2013 for rainfall durations of 1 to 135 h after analysing data for 252 rainfall-induced debris flows in the Wenchuan earthquake-affected area. The upper limit of rainfall conditions that did not trigger debris flows was determined as $I = 45.91D^{-0.63}$. Guo et al. (2016b) proposed an ID threshold for the Wenchuan earthquake-affected area as $I = 4.2D^{-0.62}$ (2 h $< D < 56$ h) for the post-earthquake debris flow events and $I = 11.8D^{-0.87}$ (2 h $< D < 56$ h) for debris flow during the period of 2009-2013. On the other hand, Ma et al. (2017) obtained $I = 41D^{-0.33}$ for Dujiangyan and $I = 15.2D^{-0.8}$ and $I = 26D^{-0.7}$ for Yingxiu. In contrast with the study presented here and the one performed by van Asch et al. (2014), which correspond to two large events with large triggering rainfalls, the ID thresholds calculated at regional scale are usually defined by the lowest triggering rainfall (Guo et al., 2016b) being mandatory the smallest debris flow events that require the smallest amount of rainfall. Furthermore, due to the high temporal and spatial variability of rainfalls in mountainous areas, it is difficult to determine the exact triggering rainfall event, which is commonly underestimated (Abancó et al., 2016; Nikolopoulos et al., 2014).
5. Discussion and conclusion

We used an improved version of the code written by van Asch et al. (2014) in PCRaster environmental modelling language (Karssenberg et al., 2001) to analyse the influence of material depletion, grain coarsening and revegetation of the co-seismic deposits on the triggering condition and characteristics of runoff-generated debris flows. We calibrated the model on the 14th August 2010 debris flow event that occurred in Hongchun gully and ran it parametrically in the same catchment.

Grain coarsening has been found to be the most limiting factor for the generation of debris flows, as progressive grain coarsening and the related increase of hydraulic conductivity produce a significant increase of the critical rainfall thresholds. Field observations suggested that the wash-away of the finest soil fraction can be a rather quick process that occurs over just a few years (Zhang et al., 2014) and during a few consecutive debris flows occurring in the same area. This hinders the generation of additional debris flows even though most of the co-seismic debris remains in place. On the other hand, our quantification of the influence of the material depletion might be biased by the abundance of co-seismic debris in the selected study area. It also might be underestimated because of limitations of the code, which lacks the modelling of sediment supply from further slope instabilities and entrainment of bed material. Revegetation of the co-seismic deposits seems to have a little influence on debris flow occurrence in the short term, as large increases in soil strength seem only achievable by extensive root systems that take several years to develop. However, it also influences hydraulic properties of the soil, and this was not accounted for in this study.

The modelling approach is affected by several limitations, some of which are intrinsic to the simplified nature of numerical approaches in general. The initiation of debris flow by runoff is an underlying hypothesis of the study, made to limit the number of variables and focus
on the relative importance of the investigated processes. Obviously, initiation by runoff is not granted in other areas and in time, as it depends on the nature and state of the debris and bed material, its degree of saturation, its water retention behaviour, and its (evolving) hydraulic conductivity (Cuomo and Della Sala, 2013). Moreover, the relatively small size of the study area, including only one catchment, challenges the representativeness of the results for the much wider Wenchuan earthquake-affected region. However, it is apparent that the modelling approach, regarded as a conceptual, parametric, virtual experiment has been able to identify and rank the first-order controls on the post-earthquake evolution of runoff-generated debris flow occurrence and characteristics in a way consistent with observations and with experimental results from the literature. The approach can be considered as a prototype study to be expanded and improved in studies targeting larger areas and aimed at providing usable insight in post-earthquake debris flow hazard assessments.

Acknowledgments

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