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The Molpro Quantum Chemistry package

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Molpro is a general purpose quantum chemistry software package with a long development history. It was originally focused on accurate wavefunction calculations for small molecules, but now has many additional distinctive capabilities that include, inter alia, local correlation approximations combined with explicit correlation, highly efficient implementations of single-reference correlation methods, robust and efficient multireference methods for large molecules, projection embedding and anharmonic vibrational spectra. In addition to conventional input-file specification of calculations, Molpro calculations can now be specified and analysed via a new graphical user interface, and through a Python framework.

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I. INTRODUCTION

Molpro is a general purpose quantum chemistry software package with a development history of over 50 years. It was started in the late 1960s by the pioneering work of Wilfried Meyer and Peter Pulay; Meyer developed the pseudo-natural configuration interaction (PNO-CI)¹ and coupled-electron pair (PNO-CEPA)² methods and Pulay the first Hartree-Fock analytical energy gradient program.³ These methods have been used in the 1970s for numerous calculations of molecular properties of small molecules with unprecedented accuracy.^{4–9} Since then, the main focus of Molpro has been on high accuracy treatments of electron correlation. Perhaps most widely used and distinctive are the internally contracted multireference configuration interaction (IC-MRCI) methods^{10–14} in Molpro, which allowed for the first time to compute global potential energy surfaces (PES) for electronic ground and excited states with unmatched precision. In many cases these calculations also included non-adiabatic and spin-orbit couplings.¹⁵ The PES were used in many studies of molecular spectroscopy, as well as in quasi-classical and quantum mechanical treatments of inelastic and reactive collision dynamics. Molpro is also well known for its highly efficient coupled cluster modules with single, double, and triple excitations [CCSD(T)]. Through the inclusion of explicitly correlated (F12) terms in the MP2-F12^{16,17} (explicitly correlated second-order Møller-Plesset perturbation theory), CCSD(T)-F12,^{18–20} CASPT2-F12²¹ (explicitly correlated second-order complete active space perturbation theory), and MRCI-F12,^{22–24} programs, the basis set limits of the corresponding methods can be closely approached using triple- ζ basis sets.^{19,25–30} Typically, this reduces the basis set incompleteness errors of relative energies and molecular properties by at least one order of magnitude at rather little additional cost. Molpro also contains an efficient implementation of Kohn-Sham DFT that supports, as well as the standard hybrid functionals, extensions including dispersion corrections, range-corrected wavefunction hybrids and exact-exchange functionals.

The traditional functionality of Molpro has been summarized in an earlier review article³¹ and will therefore be outlined only briefly. The main focus of the current paper is on new methods, and the current authors are those who contributed significantly to these developments. The full list of contributors is given in Ref. 32. We describe improvements of coupled cluster methods (distinguishable cluster^{33–37} and quasi-variational coupled-cluster^{38–43}), as

well as recent developments of accurate electron correlation treatments for large molecules. This includes highly accurate explicitly correlated local coupled cluster methods based on pair natural orbitals [PNO-LCCSD(T)-F12]^{44–58} and embedding methods.⁵⁹ In the multireference area, a new multiconfiguration (complete active space) self-consistent field (MC-SCF/CASSCF) program has been developed,^{60,61} which allows efficient optimizations of wavefunctions for large systems, such as transition metal clusters. The CASSCF orbitals can be used in subsequent single-state⁶² or multi-state⁶³ PNO-CASPT2 calculations to include dynamical correlation effects in large systems.

The paper is organized as follows: in sections II and III we describe the many wave-function and density functional methods, respectively, which are available in Molpro. Section IV B presents projection-based wavefunction-in-dft embedding methods, which allow combination of both worlds. Section V summarizes the treatment of scalar-relativistic and spin-orbit effects, and section VI describes methods to compute molecular properties and molecular spectra. Section VII gives an overview of methods to compute and analyze intermolecular interaction energies, either with supermolecular approaches or using symmetry adapted perturbation theory (SAPT). Finally, in section VIII we describe a new graphical user interface (GUI) and further interfaces, which can be used for connecting Molpro with other programs or for postprocessing molecular orbitals and molecular properties.

II. WAVE FUNCTION METHODS

A. Canonical single reference methods

1. Hartree-Fock and Kohn-Sham

Closed-shell and open-shell Hartree-Fock programs are available with and without spin-restriction (RHF, UHF), and with or without a Kohn-Sham density functional (KS). The programs can run in conventional mode using integrals stored on disk, or in integral-direct mode. For large molecular systems we recommend using the density fitting (DF) implementation, which is most efficient. These programs have been described in Ref. 31 and this is not repeated here. More recently, a new parallel version with local approximations has

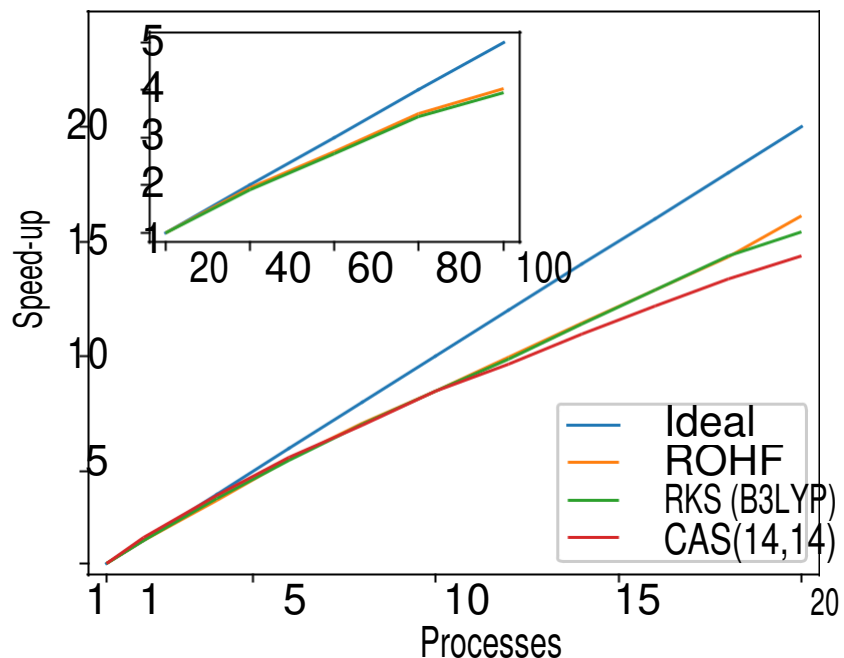


FIG. 1. Parallel speed-ups for spin-restricted Hartree-Fock and hybrid Kohn-Sham (B3LYP) calculation of the 7A state of $\text{Co}_2\text{ON}_4\text{C}_{70}\text{H}_{106}$ ⁶⁷ with the def2-tzvp basis. Additionally shown is the parallel speed-up for the CASSCF calculation of the 1A state. The main figure shows parallel speed-up relative to a single MPI process on a single 20-core node; the subfigure shows the speed-up on multiple nodes relative to a single node computation, with 20 processes used on each node.

been developed,⁶⁴ which can considerably speed up calculations for large molecules. Furthermore, a configuration averaged Hartree-Fock (CA-HF) program^{65,66} has been added, which is available with and without local approximations. This is equivalent to state-averaged CASSCF that includes all possible states, of any overall spin, within the active space. The method is useful for the calculation of crystal field splittings in transition metal and lan-thanide complexes. The latest version⁶⁶ is also applicable to polynuclear complexes. A new density fitting module for computing the Coulomb and exchange parts of the Fock matrices with much improved parallelization has also been provided. This program can be used on multi-node computer systems. An example demonstrating the efficiency and speed-ups is shown in Fig. 1. We note that it is sometimes difficult to achieve convergence in ROHF calculations for large open-shell transition metal complexes. In such cases we recommend

the use of our new MCSCF program (cf. Section II B 1), which converges more rapidly and robustly, and is only slightly more expensive per iteration.

2. MP2, Coupled-Cluster

Molpro includes highly efficient implementations of all important single reference methods for closed-shell and open-shell electron correlation treatments. These range from MP2 to CCSD(T), with variants such as Brueckner coupled cluster [BCCD, BCCD(T)],⁶⁸ quadratic configuration interaction [QCISD(T)], distinguishable cluster either with orbital optimization (ODCD and BDCD) or with single and double excitations (DCSD),^{33–35,37} and quasi-variational coupled-cluster [QVCCD(T)].^{38–43} The latter two methods extend the application area of single-reference coupled-cluster theory to situations where multireference effects become important, see section II A 3 for more details. Excited states can be treated using CC2^{69–73} and EOM-CCSD⁷⁴ methods. Spin-component scaling approximations⁷⁵ are available for MP2 and DCSD.³⁷ The open-shell methods (except spin-unrestricted MP2, UMP2) are based on ROHF orbitals, and partially spin restricted [RCCSD(T)]⁷⁶ as well as unrestricted coupled-cluster implementations [ROHF-UCCSD(T)] are available. Explicitly correlated (F12) variants^{18–20,35,77} are implemented for all the mentioned ground-state methods [except QVCCD(T)]. As already mentioned, the F12 terms greatly reduce the basis set incompleteness errors and are therefore highly recommended. For most of the methods also analytical energy gradients are implemented, as described in section VI A.

Traditionally, the MP2 and coupled-cluster methods use 2-electron integrals stored on disk. Integral direct implementations, in which the integrals are computed on the fly whenever needed, are available for QCISD and CCSD.⁷⁸ Alternatively, density fitting (DF) can be used, and DF-MP2 and closed-shell DF-CCSD(T)-F12 methods are also implemented in Molpro. While density fitting greatly improves the efficiency of MP2, this is much less the case for canonical coupled-cluster methods. Therefore, DF is normally not recommended for conventional CCSD and its variants. However, highly efficient and accurate closed-shell and open-shell local CCSD(T) methods for large molecules are also available in Molpro, c.f. Section II D 3. These methods are entirely based on density fitting approximations and are recommended for calculations on molecules that are too large to be treated by conventional

CCSD(T).

3. Coupled-cluster methods for strong electron correlation

Although multireference methods are a preferred route to describing strong electron correlation, the difficulty of controlling both their cost scaling and accuracy for large systems means that single-reference methods are attractive whenever they can be used. However, it is well understood that standard truncated coupled-cluster methods, like CCSD and CCSD(T), result in significant errors when used to describe chemical systems with strong non-dynamic correlation.^{79,80} A number of alternative single reference (SR) methods that are able to model inherently MR systems have emerged in recent years.^{33,38,81–83} These include the quasi-variational coupled-cluster doubles (QVCCD) and the distinguishable cluster doubles (DCD) approaches.^{33–43} In essence, both of these methods attempt to improve upon CCD, either via the addition of higher order terms, as in QVCCD, or in the subtraction of specific quadratic terms, in the case of DCD. As a result, these methods can produce remarkable accuracy along dissociation paths, even though they are based on a single determinant reference.

QVCCD begins with an energy expression that takes the form of the CEPA(0), or linearised CCD, energy. However, the cluster amplitudes used in the energy expression are expressed as a linear combination of the true amplitudes that by construction yields an energy that is exact for 2 electrons, is extensive, and agrees with the series expansion of variational

coupled-cluster doubles (VCCD) up to third order in T . The transformation matrices that

T

satisfy these constraints are then defined as inverses and inverse square roots of reduced density matrices (RDMs) obtained from the CI wavefunction constructed from T .^{The}

T

use of matrix powers to achieve this leads to a closed-form expression for the energy and amplitude residual equations, introducing the implicit inclusion of an infinite sub-set of higher order terms based upon the third-order VCCD terms.³⁸

The further inclusion of the one- and three-body correlations can be obtained to produce a quantitatively correct QVCCD(T) method, that approaches chemical accuracy. The effects of the singles amplitudes are included via orbital optimisation or the use of Brueckner orbitals. Connected triple excitation effects can be effectively approximated by using the

standard perturbative (T) correction. However, this has been shown to overshoot for strongly correlated regimes,⁴¹ and instead a simple modification, effectively a renormalisation of the (T) denominator, should be used to produce accurate potential energy surfaces.⁴³

QVCCD is now implemented in Molpro within the Integrated Tensor Framework (ITF, cf. section II B 2), with similar computational scaling to CCSD but with a slightly larger prefactor because of the need to perform the extra linear algebra required in the QVCCD equations. This implementation has led to a significant speed up compared to the older implementation, meaning that this method can be routinely used in applications.

DCD amplitude equations can be obtained from the CCD equations by removing some inter-cluster exchange diagrams³³ or by accounting for all possible electron pair interactions with a RPA-screened Coulomb potential.³⁶ The orbital relaxation can be taken into account using Brueckner orbitals (BDCD), orbital-optimisation (ODCD), or single-excitation similarity transformation (DCSD), resulting in a size-extensive two-electron-exact method.³⁴

The distinguishable cluster methods work remarkably well for strongly and weakly correlated systems.^{33,35,37} They outperform the coupled-cluster doubles methods in virtually all situations, and are even on a par with CCSD(T) for the accuracy of optimized molecular geometries.³⁵ Strongly correlated molecular and model systems are treated qualitatively correct. In particular, Hubbard-type one-, two-, or three-dimensional equidistant hydrogen lattices are dissociated to the exact limit.³³

DCSD has been combined with the explicit correlation methods (DCSD-F12) and is available as a closed-shell (together with BDCD and ODCD) and an open-shell (RDCSD and UDCSD) implementation.³⁵ The orbital-optimized and Brueckner versions can be amended by a subsequent perturbative F12 correction.⁷⁷ Molecular properties and analytical nuclear gradients are implemented in Molpro for the closed-shell DCSD. Linear-scaling versions of DCSD are available in PAO and PNO implementations, cf. sections II D 2 and II D 3.

An extension of the distinguishable cluster approximation onto triple excitations (DC-CCSDT)⁸⁴ is available through a GeCCo interface (vide infra) and as an ITF implementation. First benchmarks demonstrate superior accuracy of the method compared to the parent CCSDT method.

4. EOM-CCSD, TD-CC2

The equation-of-motion (EOM) CCSD excitation energies for the singlet excited states from the RHF reference can be calculated along with the excited-state density matrices and transition density matrices, according to formulas described in Ref. 85, from which first-order properties and oscillator strengths are obtained. The population analysis of the singles part of the excitation operator can be performed as well. By default, only excitation energies are calculated by solving the right-hand-side similarity-transformed Schrödinger equation. The iterative solution follows the recipe of the generalization of Davidson procedure⁸⁶ to non-symmetric matrices.⁸⁷ The EOM-CCSD code is generally black-box and it does not require any extra settings apart from the required number of states of a given symmetry. The calculation of properties requires approximately twice as much time due to an additional effort for solving the analogous left-hand-side equation, and therefore it is performed on request only. The implementation of the EOM-CCSD method within the local approximation has been described in detail in Ref. 88. Ionization-potential (IP) and electron-attachment (EA) EOM-CCSD can be simulated by the EOM-CCSD code by introducing a diffuse orbital in the basis set, see e.g. Ref. 89. The one-electron densities for excited states can be computed and stored for subsequent analysis. For EOM-CCSD transition densities a Plasser-Lischka analysis in terms of charge-transfer numbers⁹⁰ has been implemented in Molpro.

The canonical TD-CC2, as well as the ADC(2), with a 'strict' treatment of transition moments (both independent from the TD-LCC2 and LADC(2) codes of Kats et al., cf. section II D 2) are also available within Molpro.⁹¹ Among application works utilizing the EOM-CCSD and ADC(2) codes one can name the calculation of accurate UV-Vis spectra of thiophene⁹² and furan.⁹³ The EOM-CCSD method has been used for molecules as large as magnesium-porphyrine.⁹⁴

5. Molecular properties from CC wavefunctions

Molecular properties in CC theory are usually derived as energy derivatives, which can conveniently be formulated through a Lagrangian formalism.⁹⁵⁻⁹⁷ First-order properties defined through this formalism are available in Molpro for CCSD,⁹⁸ QCISD,⁹⁹ and CCSD(T) the-

ories (in the two latter cases along with corresponding gradients, see section VI A). Since CC theory is nonvariational and therefore does not fulfill the Hellmann-Feynman theorem, the calculation of the expectation value of the corresponding perturbation operator gives a different alternative formalism for obtaining CC properties.¹⁰⁰ The development of this formalism was hampered for some time by the appearance of the deexcitation T^\dagger operators in the formula, and although some solutions to this problem were proposed, the most elegant solution is the expectation-value approach from Ref. 101, where an auxiliary excitation operator S , defined through the equation,

$$e^S \Phi_0 = \frac{e^{T^\dagger} e^T \Phi_0}{\Phi_0 | e^{T^\dagger} e^T \Phi_0}, \quad (1)$$

is utilized to get rid of the infinite summation problem. The resulting formula for the first-order property X is then given by the equation,

$$X = \Phi_0 | e^{S^\dagger} e^{-T^\dagger T - S^\dagger} X e^e \Phi_0. \quad (2)$$

For Eq. (2) one can use the BCH expansion and express it in terms of multiple commutators, which – given that both T and S operators are connected – shows that this formula is explicitly connected, and additionally allows for a truncation of this formula preserving this condition. The formula has been implemented for the CCSD case with some approximations in the S operators.¹⁰² Numerical tests show that most of these terms make negligible contributions to properties such as dipole moments, and that for practical calculations one can truncate at third order in T , which is the default option when requesting this property in Molpro.

An extension of this model to frequency-dependent second-order properties has been proposed by Moszynski et al.¹⁰³ for a general complex frequency ω and perturbation operators X and Y oscillating with ω ,

$$\begin{aligned} & \hat{X}; Y_{\omega} = \\ & = e^{S^\dagger} e^{-T^\dagger} Y e^{-T} e^S \Phi_0 | P(e^{T_X(\omega)} e^{-S^\dagger}) \Phi_0 + \text{g.c.c.}, \end{aligned} \quad (3)$$

where \hat{P} is a superoperator which projects onto the 1-, 2-, etc. excitation space, $T_X(\omega)$ is the first-order response of the CC amplitudes to the perturbation X , and where finally

the abbreviation g.c.c. stands for the operation of replacing the frequency ω by $-\omega^*$ and taking the complex conjugate of the result. Based on this formula and employing the truncations up to n-tuple commutators, the polarization propagator at the coupled cluster level limited to single and double excitations has been derived and implemented in Ref. 104. Among several truncation levels proposed in this reference, the CCSD(3) one seems to be the most suitable for routine applications. Its accuracy has been found to be at the same level as that of the CCSD Lagrangian formalism with unrelaxed orbitals, which can be easily deduced from the analysis of the leading order in terms of the fluctuation operator, which is the same in both cases.¹⁰⁵

Since the polarization propagators can be calculated for any frequency, it is also possible to obtain intermolecular dispersion coefficients, like C_6 and C_9 , at the CCSD level by calculating several electric-dipole polarizability tensors at imaginary frequencies and by performing the Gauss-Legendre numerical quadrature.¹⁰⁴

B. Multireference methods

1. MCSCF, CASSCF

The first second-order MCSCF methods in Molpro were developed by Werner and Meyer,¹⁰⁶ who also contributed the first quadratically convergent state-averaged MCSCF method.¹⁰⁷ A much improved implementation, which included an extension to CASSCF, was provided in 1985 by Werner and Knowles.^{108,109} Due to the inclusion of higher-order terms in the orbital optimization, which account approximately for the periodicity of the energy in the orbital rotation parameters, and the inclusion of the orbital-CI coupling in the optimization, the Werner, Meyer, Knowles (WMK) methods provide extremely fast and robust convergence. The CI optimization in the CASSCF methods are based on the efficient determinant-based full CI method of Knowles and Handy.¹¹⁰ Alternatively, spin-adapted configuration state functions (CSFs) can be used, in which case the coupling coefficients are computed on the fly by an efficient symmetric group technique.¹¹ This also makes it possible to choose the CSF basis manually, or to use restricted active space (RASSCF) wavefunctions. Recently, the convergence and reliability of the WMK method was further improved.⁶⁰

However, the computation time and memory requirements of second-order MCSCF methods grow strongly with the molecular size. This is due to the large number of two-electron integrals required for the orbital Hessian, namely $(rs|kl)$ and $(rk|ls)$, where k, l denote occupied orbitals and r, s any orbitals. The number of these integrals scales as $O(N^4)$ and the time for their evaluation as $O(N^5)$. To overcome this problem, a new MCSCF orbital optimization method has recently been proposed and implemented in Molpro,⁶¹ which combines a second-order optimization algorithm of the active orbitals with the first-order Super-CI (SCI) treatment of Roos et al.^{111,112} The active Hessian in this hybrid method (denoted as SO-SCI) can be built from the two-electron integrals $(rs|tu)$ and $(rt|us)$ with two active orbitals t, u . Hence, the number of integrals only scales as $O(N^2)$ and the computation time as $O(N^4)$ (if the number of active orbitals is considered as independent of the molecular size). The orbitals and the CI coefficients are optimized alternately, yielding only first-order convergence. However, the convergence is substantially improved using the Limited Memory Broyden-Fletcher-Goldfarb-Shanno (L-BFGS) quasi-Newton method.¹¹³

In all test calculations so far, the SO-SCI method showed faster convergence than the SCI method, and this overcompensates the small additional cost introduced by the two-electron integral computation. The robust convergence of the SO-SCI method allows to avoid a preceding Hartree-Fock calculation, if the character of the active orbitals is roughly known. Good starting guesses can be obtained by the “Automated Construction of Molecular Active Spaces from Atomic Valence Orbitals” (AVAS)¹¹⁴ with orbitals obtained from an atomic density guess.⁶⁴

Table I shows examples for CASSCF calculations with the new first-order program for three large transition-metal complexes.^{67,115} Additionally, results with our local PNO-CASPT2 program⁶² (cf. section II D 4) are presented. The structures of these complexes are depicted in Fig. 2. All CASSCF calculations were started with AVAS based on the Molpro atomic density guess orbitals. The largest CASSCF calculation included 5154 basis functions and took 12 hours on a single computer node. More details about these computations can be found in Ref. 61.

The SO-SCI method can also be used for the optimization of single-determinant ROHF wavefunctions. Due to the second-order optimization of the active orbitals, the SO-SCI method converges mostly faster and more robustly than the ROHF method, and we there-

TABLE I. CASSCF and PNO-CASPT2 vertical excitation energies of the large transition metal complexes shown in Fig. 2. All results are calculated with the def2-tzvpp basis set. The timings of the ground state (GS) and the excited state (ES) CASSCF calculations (run on 15 (Fe,Ni) and 20 (Co) CPU cores) are shown as well. CASSCF results are from Ref. 61.

Complex	Excitation	Active Space	N _{atoms}	Basis size	Time GS [h]	Time ES [h]	ΔE CASSCF	ΔE PNO-C
FeC ₇₂ N ₂ H ₁₀₀	⁵ A→ ³ A	CAS(6,10)	175	3785	5.6	3.4	1.972 eV	1.897 eV
CoON ₂ C ₄ H ₇₀	¹ A→ ³ A	CAS(14,14)	183	3937	8.2	8.3	0.009 eV	0.333 eV
[NiC ₉₀ N ₂₀ H ₁₂₀] ²⁺	³ A→ ¹ A	CAS(8,10)	231	5154	10.9	12.1	2.063 eV	1.819 eV

TABLE II. Open-shell single determinant calculations from Ref. 61 of the large transition metal complexes shown in Fig. 2. All calculations were done with the def2-tzvpp basis set and run on 15 CPU cores. Density fitting was used in all cases for integral evaluation and transformation.

Complex	Basis size	N _{occ}	State	ROHF			SCI		SO-SCI		Energy [Hartree]
				It.	Time [h]	It.	Time [h]	It.	Time [h]		
FeC ₇₂ N ₂ H ₁₀₀	3785	287	⁵ A _g	a)	91	15.4	27	4.3	-4156.211 440		
CoON ₂ C ₄ H ₇₀	3937	311	⁷ A	62	10.8	87	17.8	27	5.5	-5768.892 008	
[NiC ₉₀ N ₂₀ H ₁₂₀] ²⁺	5154	414	³ A	26	12.7	27	15.2	16	8.8	-6074.841 763	

a) No convergence after 100 iterations

fore recommend using the SO-SCI especially for large open-shell transition metal clusters where near degeneracies of several d-orbitals exist. Some examples for such calculations are presented in Table II.

The new CASSCF methods are well parallelized. An example for the speed-ups achieved with up to 100 cores in 5 computer nodes (connected by Infiniband) for the CASSCF calculation for the cobalt-complex is shown in Fig. 1.

2. Multireference configuration interaction

All multireference methods in Molpro are fully or partially internally contracted (IC). This means that the configuration space is created by applying excitation operators to the com-

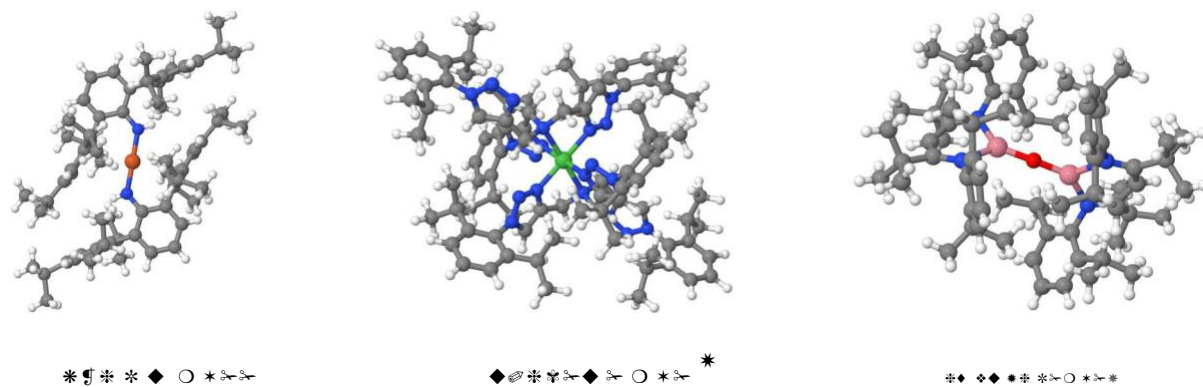


FIG. 2. Transition metal complexes^{67,115} used in the calculations shown in Table I and II.

plete fixed reference functions.^{116–118} The first fully contracted multireference configuration interaction (MRCI) program has been presented in 1981 by Werner and Reinsch.^{119,120} A much improved partially contracted MRCI method was implemented by Werner and Knowles (WK) in 1988.^{10,11} In this method only the excitations with 2 electrons in the external (virtual) space are internally contracted. Nonvariational approximately size consistent approximations such as the averaged coupled pair functional¹²¹ (ACPF), variational perturbation theory (VPT)¹²² [equivalent to CEPA(0)], or quasi-degenerate variational perturbation theory (QD-VPT),¹²³ are also available in Molpro's IC-MRCI program.¹² Somewhat later, the IC-MRCI method was extended to accurately treat electronically excited states.¹³ In order to avoid artifacts near avoided crossings and conical intersections, the internally contracted configuration space has to be made invariant with respect to unitary transformations among the reference states. This can be achieved by using the union of the internally contracted configurations (ICCs) obtained from all (or some) reference states. With this ansatz, even narrow avoided crossings and conical intersections can be accurately described. However, the computational effort scales almost cubically with the number of states. This problem can be avoided by using state-specific ICCs. To avoid root-flipping problems, a projection technique can be used.¹³ At the end, a small CI in the space of the (non-orthogonal) N_{state} wavefunctions $|\Psi_n$ is carried out, yielding finally orthogonal wavefunctions and variational energies for all included states. This works well unless the reference coefficients change strongly in the vicinity of narrow avoided crossings. In such cases, the contraction coefficients must be relaxed in order to obtain accurate potentials.

The WK ansatz described above avoids the computation and diagonalization of higher-order

RDMs, but has the disadvantage that the number of uncontracted CSFs increases strongly with the number of reference configurations. Furthermore, in cases with large active spaces, very many spin-couplings occur, many of which may have only a minor contribution since they do not belong to the first-order interacting space. In order to reduce these problems, Celani and Werner (CW) proposed to internally contract also parts of the internal and singly external configuration spaces.¹²⁴ In the CW ansatz, all spaces that have at most 2 active orbital labels are contracted, so that all required overlap matrices only depend on one- and two-electron RDMs. This greatly reduces the configuration space but has very little effect on the accuracy. In the original work of Celani and Werner,¹²⁴ the CW ansatz was used for an efficient CASPT2 implementation denoted in Molpro `RS2C`. Later on, a new IC-MRCI program (in Molpro called `CIC`) based on this ansatz has been developed by Shamasundar and Knizia.¹⁴ In both programs all contributions of inactive (doubly occupied) orbitals are treated explicitly, so that only the active-space RDMs are needed. This greatly improves the efficiency for larger molecules with many correlated inactive orbitals and eliminates a restriction to 32 correlated orbitals that is present in the original WK implementation. However, a huge number of terms in the amplitude equations occur. In the `RS2C` program these were still implemented manually, but for MRCI (or even MRCC) this is not feasible. Therefore a semi-automatic implementation based on the so-called Integrated Tensor Framework (ITF) developed by Knizia^{14,31} was used, which can efficiently execute long sequences of binary tensor contractions. The input is provided by a formula file, which can either be written manually or generated by a computer algebra program. The ITF program has been extended by Kats to support local domain and pair approximations^{62,125} (cf. section II D 4). It has also been used to implement the QVCCD methods of Knowles et al.^{42,43} (cf. section II A 3) as well as analytical MP2-F12 and CCSD(T)-F12 energy gradients,^{126,127} and it is currently used by Köhn and coworkers to implement a new efficient multireference coupled-cluster program.

Due to the high complexity, the `CIC` code currently only supports calculations with ICCs generated from a single-state reference wavefunction. However, we are actively working on multi-state extensions and hope that these can be made available to the community in the near future.

3. Multireference second-order perturbation theory

Second-order multireference perturbation theory (MRPT2 or CASPT2) differs from non-variational variants of MRCI by replacing the full Hamiltonian in the Hylleraas functional by an effective one-electron Hamiltonian that only depends on a Fock matrix. Third-order multireference perturbation theory (MRPT3, CASPT3) requires in addition effectively the computation of one MRCI residual. Thus, MRPT2 and MRPT3 programs can quite easily be obtained by modifying an MRCI program, skipping in the MRPT2 part all two-electron contributions and replacing the one-electron Hamiltonian by the effective Fock matrix. This has been done in the original `RS2` and `RS3` implementations in Molpro.¹²⁸ For the reasons outlined in section II B 2 these programs are less efficient than the more recent `RS2C` program of Celani,¹²⁴ but they support multi-state (MS) CASPT2 calculations using the same wavefunction ansatz as described in section II B 2 for the WK MRCI program. The proper treatment of conical intersections with MS-CASPT2 requires a configuration space that is invariant with respect to unitary transformations among the reference states. This has been realized in the extended multireference multi-state (MR-XMS-CASPT2) method,^{129,130} which is based on the work of Granovsky.¹³¹ Recently, an approximate form of the XMS-CASPT2 has also been implemented, in which state-specific ICCs are used for each state (SR-XMS-CASPT2). Despite the fact that in this case the configuration space is not unitarily invariant with respect to rotation of the reference vectors, this approximation works quite well to describe avoided crossings where the coupling between the states is weak (e.g. the avoided crossing in LiF). However, larger discrepancies have been observed for example in the treatment of valence-Rydberg mixings, and in this case the MR-XMS-CASPT2 method is more reliable. A thorough investigation of these effects is currently being carried out and will be published elsewhere.

4. Internally contracted multireference coupled-cluster

Transferring the accuracy and size-consistency of a coupled-cluster expansion of the wavefunction to the multireference domain has been one of the main challenges in electronic structure method development over the past decades; for reviews see Refs. 132–134. A

straightforward approach is to replace the reference determinant of conventional coupled-cluster theory by a multiconfigurational state,

$$|\Psi_n\rangle = e^{\hat{T}} |\Phi_R\rangle c_R^n, \quad (4)$$

where \hat{T} is the cluster operator that, in addition to the usual occupied to virtual excitations,

also involves excitations from the (doubly) occupied space into the active orbitals and from the active orbitals into the virtual space. As the ansatz generates internally contracted configurations, the notion internally contracted multireference coupled-cluster (icMRCC) theory has been established for this theory. Early work on this method was presented by Banerjee and Simons.^{135,136} The theory was recently revived^{137–140} and in particular extended by allowing for self-consistent relaxation of both, cluster amplitudes and reference coefficients c_R^n . Relaxing the reference coefficients is in fact one of the main reasons for the particular accuracy of the resulting method and it has been shown that it thus unifies state-specific and multistate coupled-cluster theories.¹⁴¹

The success of the method comes at a price of high complexity of the underlying equations, in particular due to the non-commutativity of the cluster operator manifold.¹³⁸ The current Molpro implementation still relies on a symbolic code (called GeCCo) that is generated by the automatized evaluation of the underlying second-quantized operator algebra. A more efficient implementation, based on the ITF and making use of Molpro features like avoidance of the full integral transformation, is currently under development. At present, a convenient interface to Molpro is provided, that allows the transfer of all important run state variables (e.g. wavefunction symmetry, core orbitals, etc.) and to use procedures like numerical geometry optimization. The methods icMRCCSD and icMRCCSD(T) can be selected directly from the Molpro input. A full integral transformation is performed, with the option to use density fitting, before the external program performing the icMRCC calculation is called.

Using this interface, a number of demonstrative applications have been carried out in the past, like a highly accurate reactive potential energy surface for [F,H,Cl]¹⁴² or a set of benchmark computations for diatomic transition metal compounds.¹⁴³ In order to address larger systems, an embedding scheme has been developed¹⁴⁴ that was inspired by the ‘region’ approximation originally developed for LCCSD(T).¹⁴⁵ Here, a mean-field computation is

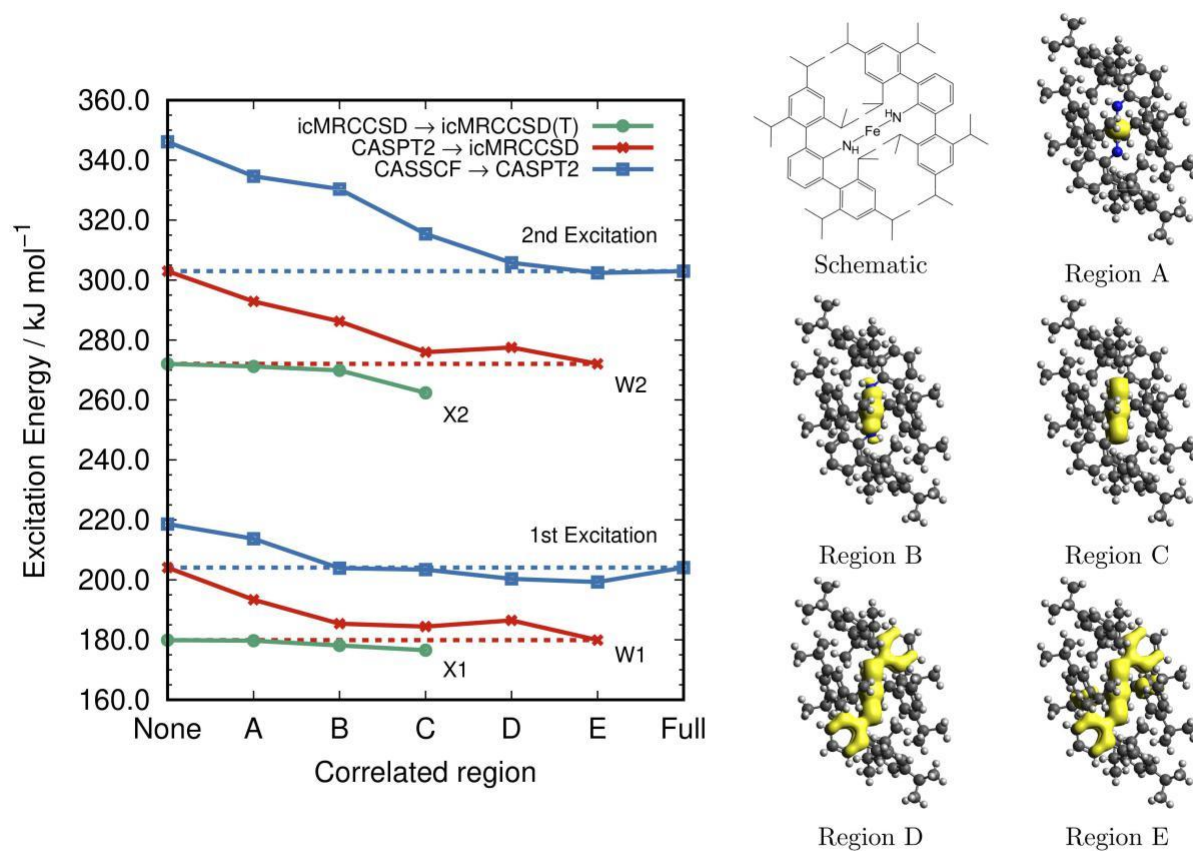


FIG. 3. Example of region-based embedding. Shown are the computed excitation energies (1st excitation: $1^5A \rightarrow 1^3A$, 2nd excitation: $1^5A \rightarrow 1^1A$) of an iron complex for different region sizes, as indicated in the right part of the figure. Reproduced with kind permission from Ref. 144. Copyright 2018 American Chemical Society.

carried out for the entire system, followed by localizing the orbitals using the intrinsic bond orbital (IBO) approach.¹⁴⁶ From the full system a local region is selected by both geometric and energy criteria, and the subsequent icMRCC computation is carried out for the subsystem only. Missing correlation contributions from the environment are added by a subtractive embedding approach, using the new PNO-CASPT2 program to treat the entire system. The approach is illustrated in Fig. 3.

Further work has been recently conducted in order to better understand the individual contributions to the icMRCCSD energy and to devise further approximations either based on perturbation theory¹⁴⁷ or linearization of the equations.¹⁴⁸ Excited states can also be targeted using icMRCC2 and linear response theory.¹⁴⁹ All these efforts have the goal of providing a more efficient access to size-consistent multireference theories in future versions of Molpro.

5. Uncontracted multireference and higher-order coupled cluster methods (MRCC)

Molpro provides also an interface to the uncontracted MRCC program of M. Kállay et al.¹⁵⁰ As the icMRCC program this can be invoked using commands and options in the Molpro input. The program can also be used to carry out higher-order coupled-cluster calculations (including perturbative corrections and excitation energies).

C. Explicitly correlated methods

Explicitly correlated (F12) methods are available in Molpro for MP2,^{16,17} coupled cluster methods [CCSD(T)-F12x, x={a,b,c} and DCSD-F12],^{18–20,35} as well as CASPT2²¹ and MRCI.^{22–24} These methods greatly reduce the basis set incompleteness errors and are therefore strongly recommended for most calculations. When using F12 it is important to include diffuse functions in the basis set, and we recommend using the cc-pVXZ-F12 sets,^{151–154} which have been especially designed for F12 calculations. Such sets are also available for heavier elements with pseudopotentials.¹⁵⁴ The application of F12 methods is very useful for highly accurate thermochemistry,^{19,35,155–157} including core-valence correlation effects,^{20,30,152} transition metal compounds,^{153,158} and intermolecular interactions.^{26,27,159} In the latter case, it is recommended to use the recently added augmented aug-cc-pVXZ-F12 basis sets.¹⁶⁰

In the F12 methods, all integrals that involve the F12 correlation factor are computed using density fitting approximations. Furthermore, resolution of the identity (RI) approximations are necessary to approximate 3-electron and 4-electron integrals. Thus, apart from the orbital basis, also density fitting and RI auxiliary basis sets are necessary in F12 calculations.

For most elements, these basis sets are chosen automatically. More details about these basis sets and the Molpro basis set library are given in section VIII B.

In order to obtain highly accurate results with F12 methods, it is important to apply the complementary auxiliary basis set (CABS) singles correction¹⁸ in order to minimize errors of the Hartree-Fock energy contribution. This correction is applied automatically in all canonical F12 calculations. For explicitly correlated local correlation methods (cf. section II D), the correction can either be computed separately or automatically. The default is to compute it separately, since it does not include local approximations. Furthermore, local calculations are often repeated with different threshold in order to study the convergence with respect to the local approximations, and since the CABS correction is additive it is not necessary to recompute it each time.

D. Local correlation methods

1. Orbital localization

The occupied orbitals can be localized using the Foster-Boys,¹⁶¹ Pipek-Mezey,¹⁶² or IBO¹⁶³ methods. The localization can be restricted to groups, as for example closed-shell and active orbitals. The performance of local correlation methods as described below does not strongly depend on the choice of the localization procedure. A comparison can be found in Ref. 51.

2. PAO based CC methods

In order to reduce the steep scaling of coupled cluster methods with system size, local correlation methods have been implemented in Molpro. The first generation of linear scaling methods in Molpro^{164–180} used domains of projected atomic orbitals (PAOs) to span the local virtual orbital space for each electron pair. With these methods energy calculations are possible up to the LCCSD(T)-F12 level, and analytical energy gradients are available for LMP2.^{175,181,182} Excited state calculations for large systems, including calculation of molecular properties and analytical nuclear gradients, can be done with local CC2 and ADC(2) methods.^{70–74,183,184} A problem of these approaches is that very large PAO domains

are needed to approach the canonical limit closely, and it is difficult to obtain accurate and balanced results if the electronic structure of a system changes strongly during a reaction. This problem is much alleviated in the explicitly correlated variants, since the explicitly correlated terms not only reduce basis set incompleteness errors, but also strongly reduce the domain errors.^{44–47} Since 2012, a new generation of local coupled cluster methods has been developed,^{48–58} which are based on domains of pair natural orbitals (PNOs). These methods, which are much more accurate and efficient than PAO methods, are described in section II D 3. At an intermediate stage, these methods also use orbital specific virtual orbitals (OSVs).^{185–187}

3. Explicitly correlated local coupled-cluster methods using pair natural orbitals PNO-LCCSD(T)-F12

Over the past few years a new generation of local correlation methods using pair natural orbitals (PNOs) has been developed in Molpro, which brings roughly an order of magnitude reduction in local errors over the previous methods described in Sec. II D 2 at even lower costs. In Molpro2019, PNO-LMP2-F12^{49,50} and PNO-LCCSD(T)-F12^{53–55} methods are available for closed-shell molecules. A review of these methods and extensive benchmark results can be found in Ref. 56. A new revision of the methods that supports both closed-shell and open-shell molecules, namely PNO-RMP2-F12,⁵⁷ PNO-RCCSD(T)-F12, and PNO-UCCSD(T)-F12⁵⁸ is featured in Molpro 2020 (the prefix “L” in the names of the methods is omitted for simplicity). Explicitly correlated distinguishable cluster methods (see Sec. II A 3) PNO-RDCSD-F12 and PNO-UDCSD-F12 will also be available.

The local correlation methods are based on two distinct approximations: “domain approximations”, which limit the correlation space for each electron pair to a domain of PAOs or PNOs, and “pair approximations”. The latter simplify the amplitude equations for weak and distant pairs, which are very numerous but each of them contributes only a very small amount to the total correlation energy. For example, distant pair energies can be approximated using multipole approximations, and the treatment of weak pairs can be simplified by linearizing the amplitude equations, neglecting small couplings between pairs, or neglecting terms in the amplitude equations that cancel at long range.

The major improvements over the PAO-based local methods include: (1) The use of PNOs on top of PAO domains leads to significantly more compact wave functions, and therefore makes possible calculations on larger molecules with less aggressive local approximations. Using PNOs also allows the iterative solution of the local (T) equations at a reasonable cost.⁵⁵ (2) Improved pair approximations in the LCCSD equations,^{53,188} together with more accurate multipole approximations for distant pair energies⁵² are adopted. These techniques reduce the pair-approximation errors in relative energies to below 0.1 kcal mol⁻¹ in nearly all systems we tested. (3) Near-linear scaling F12 treatment has been implemented.^{50,54} The F12 terms add only a small fraction to the computational cost, yet significantly reduce the basis-set incompleteness and superposition errors, as well as local domain approximation errors. (4) Refined parameters for local approximations have been established based on systematic benchmark tests⁵⁶ so that the methods can be used in a black-box manner. (5) Advanced parallelization techniques using both the GlobalArrays toolkit¹⁸⁹ and MPI (Message Passing Interface) point-to-point communication have been implemented to allow efficient cross-node parallelization on small computer clusters with fast network connection (e.g. InfiniBand), and hence a shorter time-to-solution.

As an illustration of the performance of the methods, we present some PNO-LCCSD(T)-F12 results in Tables III and IV. Calculations on systems involving open-shell molecules were computed with a development version of the PNO-RCCSD(T)-F12 program. Table III shows the errors of the local calculations against the canonical ones for several benchmark sets on small to medium sized molecules. The errors from the local approximations are only a small fraction of 1 kcal mol⁻¹ for these systems using the default settings, and the errors can be further reduced by using large PAO and PNO domains. The pair approximations show little effect on the results. Table IV shows the results for some large and difficult test systems. It can be seen that the domain errors should be at the 1 kcal mol⁻¹ scale, estimated from the difference between standard and large-domain calculations. All these large calculations can be done in hours of elapsed time on a small computer cluster. The largest PNO-LCCSD(T)-F12 calculation we have performed so far has more than 10000 basis functions (using augmented triple- ζ basis sets).

Table V presents some computed excitation energies for the Fe-complex in Fig. 2 using different methods and basis sets. For comparison, also the results from Table I are included.

TABLE III. Root-mean-square errors of PNO-LCCSD(T)-F12 relative energies against canonical CCSD(T)-F12 results in kcal mol⁻¹ using various program settings. Unless otherwise stated, the same F12 ANSATZ and basis sets were used in local and canonical calculations.

benchmark set	default	large domains	tight pair options
organic chemical reactions ^a	0.18	0.10	0.18
noncovalent interactions ^b	0.10	0.02	0.10
radical stability energies ^c	0.05	0.01	0.05
ionization potentials ^d	0.13	0.06	0.13

^aA benchmark set of 51 reactions described in Ref. 190; cc-pVTZ-F12 basis.

^bS66 benchmark set, using the aug-cc-pVTZ-F12 basis and F12 scaled triples. Errors are against the “silver” CCSD(T)/CBS estimates in Ref. 191.

^cRadical stability energies of 30 radicals described in Ref. 192; aug-cc-pV(T+d)Z basis.

^dVertical ionization potentials of 30 ions described in Ref. 192; aug-cc-pVTZ basis.

It is found that CASPT2, RMP2, and RCCSD yield very similar results, and also basis set effects are small. However, the inclusion of connected triple excitations lowers the excitation energies significantly.

4. PNO-CASPT2

The computational cost of the conventional CASPT2 method (cf. II B 3) scales as $O(N^5)$ with the molecular size. However, the scaling can be reduced to linear by applying local correlation techniques, similar to the linear-scaling single-reference methods (cf. II D 2 and II D 3).

The PNO-CASPT2 method⁶² is based on the internally contracted formalism and therefore the interacting configuration space can be divided into eight mutually orthogonal subspaces, coupled through generalized Fock matrices. These subspaces differ in the number of electrons in the closed-shell, active, and virtual orbital subspaces. Some of them are expanded in PNO bases, and others (involving single excitations) in the PAO basis. Due to the local restrictions

TABLE IV. PNO-LCCSD(T)-F12 reaction energies (in kcal mol⁻¹) and computational cost of some reactions involving large molecules. The molecular size and computational time shown are for the most expensive single-point PNO-LCCSD(T)-F12 calculation in the reaction.

reaction	basis	molecular formula	largest calculation		reaction energy cost (default settings)			
			NAO ^a	NeI ^b	default ^c	tight ^d	No. CPU cores	elapsed time / h
ISOL24-4 ^e	cc-pVTZ-F12	$\begin{matrix} \text{C} & \text{H} & \text{O} \\ 30 & 50 & \end{matrix}$	2543	176	67.5	68.0	80	3.6
AuAmin ^f	cc-pVTZ-F12	AuN ₄ PC ₄₁ H ₄₅	3345	244	47.3	47.7	120	6.4
WCCR10-4 ^g	cc-pVTZ-F12	RuCl ₂ P ₃ C ₆₂ H ₁₀₆	5168	390	51.5	53.0	150	10.6
Fe(tacn) ₂ cplx. ^h	aug-cc-pVTZ ⁱ	FeC ₁₂ N ₆ H ₃₀	1645	122	0.8	1.3	60	4.5
FeC ₇₂ N ₂ H ₁₀₀ cplx. ^j	aug-cc-pVDZ	$\begin{matrix} \text{FeC} & \text{N} & \text{H} \\ 72 & 2 & 100 \end{matrix}$	2939	406	39.0	38.3	64	13.3

^aNumber of AO basis functions.

^bNumber of correlated electrons.

^cUsing default settings.

^dUsing tight domain settings denoted as “domopt=tight” in Ref. 56. The local errors are almost exclusively from domain errors and results using other settings are not shown here.

^eReaction 4 from the ISOL24 set of isomerization reactions from Ref. 193.

^fDissociation energy of a gold(I)-aminonitrene complex from Ref. 194, using re-optimized geometries from Ref. 49.

^gDissociation energy of Complex 4 in the WCCR10 benchmark set from Ref. 195, using re-optimized geometries from Ref. 56.

^h¹A → ⁵B spin-state energy of [Fe(tacn)₂]²⁺, geometries from Ref. 196.

ⁱaug-cc-pwCVTZ basis for Fe. 3s and 3p orbitals of Fe are correlated.

^j⁵A → ³A spin-state energy difference of an iron complex, geometries from Ref. 115.

only the residual calculations for one of the eight subspaces scale linearly with the molecular size, all other residuals can be obtained in nearly constant time, cf. Figure 4. It should be noted, however, that this applies to a linear chain system, for which the asymptotic region is quickly reached. For 3-dimensional systems the linear scaling region is much more difficult to reach. Nevertheless, very large systems can be treated in quite short times.

TABLE V. Energy differences (in eV) between the triplet first excited state and the quintet ground state of the complex $\text{FeC}_{72}\text{N}_2\text{H}_{100}$. Basis aVTZ: aug-cc-pVTZ, H=cc-pVTZ.

method	energy difference
HF/def2-TZVP	2.496
HF/aVTZ	2.484
CASSCF/def2-TZVPP	1.972
PNO-CASPT2/def2-TZVPP	1.897
PNO-RMP2/aVTZ	1.888
PNO-RMP2-F12/aVTZ	1.778
PNO-RCCSD-F12/aVTZ	1.806
PNO-RCCSD(T)-F12/aVTZ	1.688

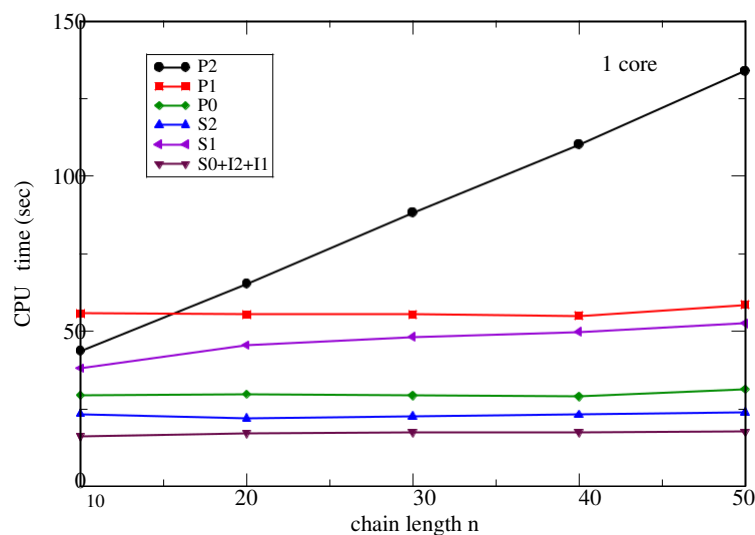


FIG. 4. Timings of individual contributions to the PNO-CASPT2 residuals for the 1A ground states of $[(\text{C}_4\text{SH}_3)\text{-}[\text{CH}_2]_n\text{-}(\text{C}_4\text{SH}_3)]^{2+}$ using a (10,10) active space. Reproduced from Ref. 62, with the permission of AIP Publishing.

The amplitude equations have been implemented using the local ITF framework, which can efficiently handle various local restrictions.^{62,125,197,198} A PNO-CASPT2 calculation of the iron-complex in Figure 2 takes around 30 minutes using four compute cores.

Multiple states in the same space/spin symmetry can be obtained using state-averaged CASSCF, and the dynamical correlation can be added using the state-specific PNO-CASPT2

method. However, it is more efficient to use the multi-state PNO-CASPT2 method (PNO-MS-CASPT2),⁶³ which additionally approximately accounts for couplings of the states. A PNO-MS-CASPT2 calculation for 45 states for the same iron-complex takes about 12.5 hours using four compute cores. Additional approximations are possible, which neglect couplings between some of the configuration subspaces.⁶³ Then the amplitudes which describe the correlation of the electrons in inactive orbitals (P2 space in Figure 4) are identical for all states and need to be computed only once. Thus, the additional effort for computing the excited state energies is small and nearly independent of the molecular size. Using such approximations, the time for the above-mentioned calculation with 45 states can be reduced to 7.2 hours, with a maximum additional error of 11 meV in the excitation energies.

III. DENSITY FUNCTIONAL METHODS

Molpro implements Kohn-Sham theory in its most commonly-used forms, including (a) pure density functionals that are integrals of general functions of the spin-density, its scalar gradient, and the kinetic energy density; (b) hybrid functionals that include also a fraction of the exact exchange energy; (c) additional empirical dispersion corrections including the D3¹⁹⁹ and D4²⁰⁰ models and the nonlocal DFT (NLDF) functional,^{201,202} (d) range-separated hybrids, with wavefunction methods for long-range correlation; (e) exact exchange (EXX) density functionals based on the local Hartree-Fock (LHF) method²⁰³ and the optimised effective potential (OEP) method.²⁰⁴

Kohn-Sham theory in a finite basis requires evaluation of the exchange-correlation functional and its derivative with respect to elements of the one-particle density matrix. Numerical quadrature is implemented through a newly-written library that generates grids for a pseudo-adaptive quadrature specified through a target accuracy and some other parameters. The usual fuzzy Voronoi partitioning^{205,206} with a spherical-polar atomic coordinate system is used, and the library implements most of the available radial and angular quadrature schemes. A fixed-size radial quadrature is chosen, and then at each radial grid point, experiments are carried out with different angular grids in order to achieve the target accuracy for a simple model energy density function with minimum effort. This scheme automatically ensures the avoidance of unnecessarily large grid densities close to nuclei (where a low-order

spherical-harmonic expansion describes the density well) and distant (where electron density and/or Voronoi switch functions mean the integrand is small).

Density functionals are specified through a library in which the exchange-correlation energy density is defined using one or more Maple symbolic-algebra expressions. This library is then compiled into Fortran code using the `dfauto`²⁰⁷ utility, which also generates documentation.

A. Dispersion corrections

Common DFT methods need to be corrected by additional dispersion interaction energy contributions in order to describe noncovalent interactions between two separate molecules or to describe the intramolecular interactions of large molecular complexes.²⁰⁸ In addition to the standard D3 and D4 dispersion corrections by Grimme,^{199,200} Molpro contains an implementation of the NLDFT (nonlocal DFT) method that is based on a double-Hirshfeld partitioning of the correlation energy density.^{201,202} Due to this, the influence of the hybridisation states of the interacting atoms on the long-range interaction is implicitly described, requiring no additional informations of the atom bond partners like in the D3 model.¹⁹⁹ Moreover, the NLDFT method is a consistent Kohn-Sham method because the long-range correction also describes a modified xc potential through the functional derivative of the NLDFT correlation functional. It was shown that the NLDFT method outperforms many dispersion corrected GGA and meta-GGA functionals for a large number of thermodynamic properties from the GMTKN30 data base and it delivers mean absolute errors in the range of 0.2 kcal/mol only for the S22 and S66 benchmark databases.^{201,209,210} The accuracy of the method was also tested for describing the interaction energy of H₂O with graphene,²⁰¹ for the description of the interactions of large supramolecular complexes²¹¹ and for the description of conformer geometries of a range of peptide molecules.²⁰²

B. Exact exchange Kohn-Sham methods

Unlike in common hybrid Kohn-Sham (KS) DFT methods, in exact exchange (EXX) KS methods the functional derivative with respect to the exact exchange energy is taken with

respect to the electron density^{212,213}:

$$v_x(\mathbf{r}) = \frac{\delta E_x[\rho]}{\delta \rho(\mathbf{r})} \quad (5)$$

yielding a local exchange potential. Due to this, EXX methods have a number of advantages as compared to the Hartree-Fock method, e.g., orbital energy differences computed from EXX orbital energies are suitable first approximations to valence excitation energies, see, e.g. Ref. 214. Molpro contains various EXX implementations based on the optimised effective potential (OEP) method^{204,215–218} and the common energy denominator approximation (LHF and CEDA methods).^{203,219,220} Orbitals from EXX or hybrid-EXX (mixing the EXX functional with standard GGA exchange and correlation functionals) calculations are also suitable for use in DFT-SAPT calculations (see section VII B 1) because the local exact exchange potential $v_x(\mathbf{r})$ possesses the correct asymptotic behaviour and thus yields an improved description of the electronic density in the asymptotic range.²²¹

C. Time-dependent density functional theory

A basic implementation of time-dependent density functional theory (TDDFT)²²² is available in Molpro that can be used to calculate excitation energies and linear response properties within the standard GGA approximation. While having a number of limitations regarding choices for the exchange-correlation functional and kernel, the program is capable to treat large systems through the employment of density-fitting techniques for computing the Hessian-times-vector products.

Exact-exchange TDDFT (TDEXX) calculations^{214,223–225} can currently be done within the adiabatic approximation to the TDEXX kernel. This feature may be used in conjunction with EXX ground-state calculations, see section III B.

The response module of the TDDFT program can be used both for computing static and frequency-dependent linear response properties for arbitrary one-electron operators available in Molpro, as well as for computing the coupled Kohn-Sham response matrix of the molecule at a given (imaginary) frequency. These quantities can be used to calculate two-body and three-body dispersion interaction energies between two/three noncovalently bonded sub-systems. The former is required, e.g., to calculate the coupled and uncoupled dispersion

energies in MP2C calculations, see section [VII A 2](#).

IV. MULTISCALE MODELLING

A. Quantum mechanics/molecular mechanics

Combined quantum mechanics/molecular mechanics (QM/MM) calculations are possible using practically any electronic structure method in Molpro for the QM region. The key elements of the interface are the `lattice` and `force` commands, respectively allowing an array of point charges to be specified, and forces on the QM atoms to be computed. The charges are specified in a simple file format in which each row specifies the Cartesian coordinates of the charge (in Å), the charge itself, and a flag to indicate whether the gradient with respect to the coordinates of this charge should be computed. Interfacing to MM molecular dynamics packages can be hand-rolled using these tools, or there is also an existing Molpro interface in the Tcl-ChemShell package.²²⁶

For QM/MM calculations with large MM regions, the interaction contribution can become a bottleneck. In Molpro, extremely rapid evaluation of these contributions is achieved by unpublished early-summation techniques (inspired by analogous approaches for the Coulomb operator^{227,228}). For the energy, the Boys function can be contracted immediately with the fixed point charges, so that the recurrence relations that build and transfer angular momentum, and the contraction steps, are performed only once, not once per point charge. Similarly in the gradient, early contraction with the density (as is commonly done) prevents the need to compute individual gradient integrals.

The density-fitted local correlation methods and QM/MM functionality in Molpro have been combined in numerous studies in enzymology.^{229–232} More recently, and as described in the next section, three-layer combinations of wavefunction-based methods, density functional theory, and MM have proved a powerful addition to the suite of tools available in Molpro for the treatment of complex, multiscale chemical problems.

B. Projection-based wavefunction-in-DFT embedding

Despite dramatic improvements in algorithms and efficiency, it is often the case that the sheer complexity of the chemical problem precludes direct application of coupled-cluster or multi-reference methods. For such problems DFT plays a key role, but selection of the exchange-correlation functional can be difficult; and systematic deficiencies across large classes of functionals can lead to errors that are hard to eliminate.

Molpro provides a suite of tools that allow for multiscale combinations of highly accurate wavefunction-based methods with DFT. This allows high-accuracy treatment of a small, chemically relevant part, with a more approximate description of a complex chemical environment. Wavefunction-in-DFT (WF-in-DFT) embedding in Molpro is based on the use of projection operators to maintain orthogonal subsets of orbitals describing the two subsystems.⁵⁹ This simple approach is robust and efficient, leading to a total computational cost equivalent to DFT on the whole system, plus the high-level calculation on the small, active subsystem. The coupling between subsystems is entirely captured through a modified core-Hamiltonian in the high-level subsystem, so that almost any electronic structure method in Molpro can be used. The implementation in Molpro has been tested and applied in a range of application areas,^{233–240} demonstrating the robustness and utility of the approach.

The method was used in combination with experiment in a detailed study of a new class of cobalt-based hydrogen-evolution catalysts.²³⁵ A small subsystem, containing the transition metal and its first coordination sphere, was treated using OSV-LCCSD(T),^{186,187} with the surrounding environment described using DFT with the BP86 functional. This combination provided close agreement with LCCSD(T) on the whole complex, while the restriction of the coupled-cluster treatment to a small, electronically complex region reduced the computational cost of each energy evaluation by a factor of around 20.

DFT — often in combination with QM/MM — is a standard workhorse for computational enzymology. Elucidation of reaction mechanisms requires reliable prediction of barrier heights across competing chemical processes, and conclusions from DFT are often sensitive on the choice of the exchange-correlation functional. Projection-based embedding combining CCSD(T) on a small, active subsystem with DFT on the surrounding chemical environment

all but eliminates dependence on the choice of functional.^{236,239}

New features that greatly improve the range of applicability of projection-based embedding include efficient truncation of the atomic-orbital basis set for the high-level calculation,²⁴¹ and development of analytic gradients for CCSD(T)-in-DFT.²⁴² Robustness of calculations can further be improved using the even-handed approach for partitioning the system into high- and low-level subsystems.²³⁸ Together these provide a powerful tool for studying reactivity in complex chemical environments.

V. RELATIVISTIC EFFECTS

A. All-electron effective Hamiltonians

For all-electron calculations, Molpro allows the use of the Douglas-Kroll-Hess (DKH)^{243–245} and eXact-2-Component (X2C) scalar relativistic Hamiltonians.^{246,247} In both cases only the 1-electron integrals are modified. In the case of the DKH Hamiltonian, the default order of the associated unitary transformation is 2, but arbitrarily higher orders can be selected.²⁴⁸ Because scalar relativistic effects change, in particular, the radial extent of inner-core orbitals, it is important to use orbital basis sets that are optimized using the relativistic Hamiltonian; as described in Section VIII B, these are available for most of the periodic table. Related to the use of these all-electron relativistic Hamiltonians, Molpro now also allows the use of a Gaussian finite nuclear model²⁴⁹ instead of the default point-charge nucleus.

B. Pseudopotentials

Effective core potentials (ECPs) or pseudopotentials (PPs) can be an effective and convenient way to include relativistic effects, both scalar and spin-orbit. Of course in many cases the use of PPs can also lead to significant computational cost savings due to the reduced number of electrons and basis functions included in the calculation. This becomes less of a factor, however, when highly correlated methods such as coupled cluster or MRCI are used. The implementation of a given pseudopotential V_{pp} in Molpro is based on the following general form involving a maximum of 4 terms²⁵⁰

$$V_{PP} = -\frac{Z - n_{\text{core}}}{r} + V_{\ell_{\text{MAX}}} + \sum_{\ell=0}^{\ell_{\text{MAX}}-1} (V_{\ell} - V_{\ell_{\text{MAX}}}) P_{\ell} + \sum_{\ell=1}^{\ell_{\text{MAX}}} \Delta V_{\ell} P_{\ell} \cdot \mathbf{s} P_{\ell} \quad (6)$$

corresponding to (i) the monopole potential with core charge $Q = Z - n_{\text{core}}$, where n_{core} is the number of core electrons replaced by the PP, (ii) a local term, (iii) a semi-local term for scalar relativity, and (iv) a semi-local term for the radial potentials of the spin-orbit (SO) part. The semi-local terms involve angular momentum projectors P_{ℓ} , and the terms involving $V_{\ell_{\text{MAX}}}$, $V_{\ell} - V_{\ell_{\text{MAX}}}$, and ΔV_{ℓ} are defined by expansions over terms $c_j r^{m_j} e^{-\gamma_j r^2}$ with tabulated parameters c_j , m_j , and γ_j . The 1-electron SO term, if defined, can be used in the state-interacting approach as described above.

A large number of PP families are available from the Molpro basis set library. These include the LANL ECPs,^{251,252} the SBKJ series,^{253,254} the Casino ECPs,^{255,256} and the energy-consistent PPs from the Stuttgart/Köln groups.^{257,258} Other PPs can easily be entered directly into the input as long as they adhere to the general form above. An ECP for a given element generally has one or more Gaussian basis sets associated with it - often just of double-zeta quality - but in the cases of many of the Stuttgart/Köln PPs, the latter are accompanied by full sequences of correlation consistent basis sets, e.g., cc-pVnZ-PP (n=D, T, Q, 5). See, for instance, reference 259. It is important to note that the resulting accuracy of a particular choice of ECP, as compared to an analogous scalar relativistic all-electron calculation for example, is not only dependent on the underlying adjustment method used to define the ECP and the number of core electrons it replaces, but also on the basis set used to represent the remaining valence electrons. In general a given basis set is also not transferable between different ECPs.

C. Spin-orbit coupling

The calculation of spin-orbit coupling is implemented for MRCI wavefunctions using the Breit-Pauli operator. For any atoms described with a PP, the one-electron spin-orbit part of PP replaces the bare-nucleus operator. Matrix elements of the operator between MRCI

wavefunctions are evaluated for a single choice of \hat{S}_z eigenvalue, and then the complete effective Hamiltonian matrix is constructed using the Wigner-Eckart theorem. Diagonalization of this Hamiltonian yields new states, for which properties such as dipole matrix elements are transformed. To make calculations more efficient without significant sacrifice of accuracy, an effective Fock matrix technique is used for the external parts of the MRCI wave function, but retaining the full two-electron operator for the dominant part of the wavefunction with configurations that occupy only internal orbitals.^{260,261}

For larger systems, different approximate schemes are implemented. These include the use of effective Fock matrix for internal parts as well (then spin-orbit becomes one-electron effective operator), and the use of one-center approximation. In these cases, the integral-direct calculations can strongly speed up the computation.

VI. MOLECULAR PROPERTIES AND WAVEFUNCTION ANALYSIS

A. Energy gradients, geometry optimization, and harmonic vibrational frequencies

Analytical gradients are implemented for Hartree-Fock (spin restricted and unrestricted), DFT, and most single reference methods. This includes closed-shell MP2,^{175,181,182} CCSD, DCSD, QCISD(T),⁹⁹ and CCSD(T) as well as for the corresponding F12 methods.^{126,127} Particularly accurate geometries are obtained with DCSD-F12 gradients,³⁵ which avoids the expensive inclusion of triple excitations.

Analytical MCSCF and CASPT2 gradients^{129,262,263} are available for the methods based on the WK contraction (cf. sections II B 2, II B 3), including MS-CASPT2 and XMS-CASPT2.^{129,263} For most methods the gradients are implemented with and without density fitting approximations. The latter are highly efficient and preferable for most applications. Gradients are also available for local MP2,^{175,181,182} using either Pipek-Mezey localization¹⁶² or intrinsic bond orbitals (IBOs).¹⁴⁶

Geometry optimizations^{264,265} and harmonic frequency calculations use the analytical gradients whenever available. Otherwise, the gradients or Hessians are computed automatically using finite difference methods. In such numerical derivative calculations the energies or

gradients for different displacements can be computed in parallel. The program automatically switches from its normal mode (parallel execution of a single workflow) to devolve the displaced-geometry energies to each MPI process as a serial task; this embarrassingly-parallel strategy leads to very good parallel scaling of the overall derivative computation.

B. Anharmonic vibrational spectra

Besides the multitude of electronic structure methods, Molpro offers a variety of programs for solving the nuclear Schrödinger equation, all of them being based on the Watson Hamiltonian.²⁶⁶ This allows for the very accurate simulation of vibrational and vibronic spectra as well as many vibrationally averaged properties.

The first step within these calculations is the generation of a multidimensional potential energy surface (PES), which can be obtained in a fully automated manner using any of the implemented electronic structure methods.^{267,268} Likewise, dipole moment and polarizability tensor surfaces as needed for infrared and Raman intensities can be generated for those methods, for which analytical gradients are available.²⁶⁹ Usually, these surfaces are represented in an n-mode expansion of a user-defined order.²⁷⁰ Alternatively, one may use quartic or sextic force fields. The PES generator can handle any molecular point group and can exploit molecular point group symmetry and permutational symmetry in dependence on the chosen coordinate system, which is currently restricted to canonical or localized normal coordinates.^{268,271} Multi-level schemes,^{272,273} interpolation and prescreening techniques²⁷¹ in combination with an embarrassingly parallel implementation allow for the very efficient calculation of PESs of local minima or degenerate double-well potentials.²⁷⁴ In particular the modeling of high-order terms of the PES expansion leads to substantial accelerations.^{275,276} These potentials can be dumped as ASCII files to be used in any other program. In a subsequent transformation program the grid representation of the PES can be transformed to an analytical sum-of-products representation of multivariate polynomials, B-splines or distributed Gaussians.²⁷⁷ This transformation is based on highly efficient Kronecker product fitting.

Once the PES has been generated it can be used for determining wavefunctions from conventional vibrational self-consistent field theory (VSCF), configuration-averaged VSCF theory (CA-VSCF)²⁷⁸ or multiconfigurational self-consistent field theory (VMCSCF).^{279–281} Grid-based and finite basis variants of these programs are available. One-mode wavefunctions (modals) are expanded in terms of harmonic oscillator functions or mode-specific, local distributed Gaussians. Vibrational angular momentum terms are added a posteriori to the state energies.²⁸² In order to account for vibration correlation effects, programs for 2nd order vibrational Møller-Plesset perturbation theory (VMP2), vibrational configuration interaction (VCI) calculations or vibrational multireference configuration interaction theory (VMRCI) have been implemented.^{283–285} These programs can handle up to 9-tuple excitations and provide a variety of options to tailor the configuration space. Vibrational ground-state and state-specific calculations are offered, which fully exploit molecular symmetry, even for non-Abelian point groups. By default, the VCI program uses a highly efficient configuration selection scheme, which allows for calculations of up to 10^{10} initial configurations.^{283,286} Sparse matrix techniques and a newly developed eigenvalue solver are used to limit memory demands and to speed up the calculations.²⁸⁷ Once the PES has been determined from explicitly correlated coupled-cluster calculations and the n-mode expansion of the PES has been converged, typical mean absolute deviations are in the range of $1\text{--}5\text{ cm}^{-1}$ for fundamental transitions and slightly larger values for overtones and combination bands.²⁸⁸ For example, Table VI shows the mean absolute and maximum deviations of computed VCI fundamentals from experimental gas phase or matrix isolation data for a small set of molecules. Molecular properties as for example intensities, vibrationally averaged rotational constants, molecular geometries and dipole moments, etc. can be obtained from these VCI calculations.²⁸⁹ These programs have been applied to a multitude of molecules and molecular clusters of up to 20 atoms.²⁸⁶ Besides these variational methods, a program based on 2nd order vibrational perturbation theory (VPT2) is available, which relies on the polynomial coefficients determined in the PES transformation program.^{277,290}

Photoelectron or photoionization spectra can be computed in two different ways. This first one being offered by Molpro relies on a selection of Franck-Condon factors at the VSCF level within a sum-over-states approach.²⁹¹ In order to match the normal coordinates of the two

TABLE VI. Mean absolute (MAD) and maximum deviations (MAX) of VCI calculations based on explicitly correlated coupled-cluster calculations from experimental data for the fundamental modes of a small set of molecules (in cm^{-1}).

Molecule	MAD	MAX
CH ₂ F ₂	1.6	4.3
C ₂ H ₄	2.7	5.9
CH ₃ OPO	4.4	8.2
C ₂ H ₆	1.5	3.6
CH ₃ CH ₂ F	2.1	7.4

potential energy surfaces, a Duschinsky transformation is provided, which can also be used to alter the normal coordinates of a PES in order to compute vibrational spectra for any isotopologues without recomputing the PES.²⁹² Once the list of significant Franck-Condon factors has been generated, the corresponding vibrational states can be computed at the VCI level, which will be used for the calculation of Franck-Condon factors at the correlated level. Note that this approach is only meaningful once the vibrational states retain their state identity within the VCI calculations, otherwise the sum of the Franck-Condon factors will not add up to 1.0. This approach has been applied to a variety of small molecules, e.g. ketene.²⁹³ In cases of high density of states or the loss of the state identity in general, the time-independent Raman wavefunction approach (RWF)²⁹⁴ can be used instead, which avoids the explicit calculation of vibrational eigenstates altogether, but determines the orientationally averaged absorption cross section at relevant spectral points. This leads to an iterative solution of the inhomogeneous Schrödinger equation, for which several techniques have been developed. This method was found to be very robust, even for very high state densities, see for example the spectrum of CH₂F₂.²⁹⁵ Quite recently, this approach has been extended for the calculation of Herzberg-Teller terms.

C. One electron properties and transition moments

Normally, the expectation values and transition moments of standard one-electron properties are computed automatically where possible. By default, only dipole moments are evaluated, but other properties can be requested, including multipole moments, electric field and its gradient, angular momentum, diamagnetic shielding tensor, and velocity. Transition properties can be calculated for state-averaged CASSCF calculations, or for MRCI wavefunctions. For MRCI wavefunctions, it is also possible to evaluate properties in the case when bra- and ket- molecular orbitals are different, via a transformation to bi-orthogonal orbitals.²⁹⁶ Calculation of overlaps, one-electron transition properties and Hamiltonian operators is possible, including the overlap between MRCI wave functions obtained at different molecular geometries. These can be used, by applying numerical differentiation, to obtain non-adiabatic first- and second-order corrections.

D. Population analysis, IBO, NBO

Mulliken population analysis and distributed multipole analysis²⁹⁷ as well as intrinsic bond orbital (IBO) analysis¹⁴⁶ are available in Molpro. The latter is based on Pipek-Mezey localized orbitals in a polarized minimal basis of atomic orbitals that spans the Hartree-Fock wavefunction exactly. The results of this method are particularly independent of the basis set and give a picture that corresponds closely to chemical intuition. Some applications can be found in Refs. [298–302](#). Molpro also provides an interface to the NBO6 program.³⁰³

VII. INTERMOLECULAR INTERACTIONS

A. Supermolecular calculations

Intermolecular interaction energies can be computed either using supermolecular calculations or by symmetry adapted perturbation theory (SAPT). The former has the advantage that any electronic structure method can be used, and the current gold standard for such calculations is CCSD(T) or, even better, CCSD(T)-F12.¹⁹¹ On the other hand, SAPT calcu-

lations make it possible to analyze the interaction energies and to determine various physical meaningful contributions. Larger systems, for which canonical CCSD(T) calculations are too expensive, can be treated very accurately using the new PNO-CCSD(T)-F12 program in Molpro. For recent benchmarks and references to previous work see Ref. 159.

1. Counterpoise corrections

Supermolecular calculations of interaction energies require counter-poise (CP) corrections³⁰⁴ to compensate the basis set superposition errors (BSSE). This is even recommended with explicitly correlated methods which yields results close to the complete basis set (CBS) limit already with triple- ζ basis sets. Counterpoise calculations can be straightforwardly done by specifying “dummy” atoms, which carry a basis set but no nuclear charge and no electrons. It is also possible to remove the basis set from the dummy atoms for convenient computation of the monomer energies at formally infinite separation.

2. Dispersion corrections to MP2

The standard second-order Møller-Plesset perturbation theory (MP2) method fails to describe long-range correlation energies accurately. The reason for this stems from the fact that the MP2 method does not take into account intramolecular correlation effects of two interacting monomers, i.e., describes dispersion interactions on an uncoupled Hartree-Fock level.^{305,306} To remedy this, the supermolecular MP2 interaction energy can be corrected in a hybrid supermolecular-perturbation theory approach by subtracting the uncoupled HF (UCHF) dispersion energy and adding the dispersion energy from a more accurate response theory method instead.^{306,307} In the MP2C (MP2 coupled) method, the latter is computed using the time-dependent density-functional theory (TDDFT) approach, employing static response functions from the EXX method (see section III B) and coupled response functions computed by using the ALDA exchange kernel:^{307,308}

$$\Delta E_{\text{int}}^{\text{MP2C}} = \Delta E_{\text{int}}^{\text{MP2}} - E_{\text{disp}}^{(20)}[\text{UCHF}] + E_{\text{disp}}^{(2)}[\text{TDDFT}] \quad (7)$$

In Molpro, MP2C calculations can be performed with the aid of the TDDFT module that computes frequency-dependent coupled or uncoupled response functions. Exact-exchange

KS calculations required to compute $E_{\text{disp}}^{(2)}$ [TDDFT] can be performed using the EXX methods described in section III B. A remarkable feature of the MP2C approach of Eq. (7) is that it delivers far more accurate interaction energies than the MP2 method for dispersion energy dominated systems, while in case of hydrogen-bonded systems the overall well performance of MP2 is conserved.^{306,307} In a thorough study of Burns et al. of a large number of different spin-component-scaled (SCS), explicitly correlated (F12) and specialised wavefunction approaches using four different benchmark data bases with 94 dimers and 345 geometry configurations in total, the MP2C method was appointed to bronze standard for describing noncovalent interactions, as it yields very accurate energies at a moderate computational cost as compared to the other methods studied.³⁰⁹ Binding energies of large supramolecular complexes were found to be very similar to results from DFT-SAPT (section VII B 1) or the NLDF method (section III A).

B. Symmetry adapted perturbation theory (SAPT)

1. Symmetry-adapted perturbation theory based on Kohn-Sham description of monomers

Intermolecular interaction energies between two noncovalently bonded molecules (denoted as monomers) can be calculated by perturbation theory approaches using the product of the monomer wave functions as the zeroth order approximation to the dimer wave function. In order to enforce the proper antisymmetry of the dimer wave function, various weak to strong symmetry forcing procedures can be employed,³¹⁰ which are generally known under the name symmetry-adapted perturbation theory (SAPT).^{310–312} Among these methods the symmetrized Rayleigh-Schrödinger theory (SRS), which belongs to the weak symmetry-forcing group, turned out to be the best practical choice, as it yields very accurate intermolecular interaction energies at equilibrium and even in the short distance range.^{310,313} The SAPT interaction energy is typically expanded up to second order in terms of the intermolecular interaction operator (defined as a difference between the total electronic Hamiltonian

of the dimer and the sum of monomer Hamiltonians), leading to the terms

$$\Delta E_{\text{SAPT}} = E_{\text{int}}^{(1)} + E_{\text{pol}}^{(1)} + E_{\text{exch}}^{(1)} + E_{\text{ind}}^{(2)} + E_{\text{exch-ind}}^{(2)} + E_{\text{disp}}^{(2)} + E_{\text{exch-disp}}^{(2)} + \Delta^{3-\infty} \quad (8)$$

with $E_{\text{pol}}^{(1)}$: electrostatic energy, $E_{\text{ind}}^{(2)}$: induction energy, $E_{\text{disp}}^{(2)}$: dispersion energy and $E_{\text{exch}}^{(1)}$, $E_{\text{exch}}^{(2)}_{\text{-ind}}$, $E_{\text{exch}}^{(2)}_{\text{-disp}}$ are the corresponding exchange interaction counterparts that stem from a tunneling of the electrons among the monomers and which vanish at large distances between monomers. The term $\Delta^{3-\infty}$ defines an approximation to the higher order interaction energy terms and can be estimated using the supermolecular Hartree-Fock method³¹⁴. As compared to the supermolecular method, the SAPT method has a number of advantageous features. Namely, it is free from any basis set superposition error (BSSE) and it yields a deeper physical insight into the nature of the interaction through the energy decomposition of Eq. (8).

In order to obtain accurate interaction energies from Eq. (8), intramolecular correlation effects need to be taken into account. The most efficient approach is to describe the monomers in terms of densities, density matrices and response properties obtained by density functional theory methods and the corresponding SAPT variant is termed as DFT-SAPT.³¹⁵⁻³²² The DFT-SAPT method was shown to yield very accurate intermolecular interaction energies for small^{221,318,321,323} and large^{324,325} dimer systems. The DFT-SAPT method implemented in the Molpro program can be used with a large variety of different settings in the monomer and the perturbation theory calculations. It should be noted that further approximations are usually employed for exchange contributions: namely, the so-called S^2 or single-exchange simplified variants of these energies are used, where double and higher simultaneous exchanges of electrons between the monomers are neglected. This approximation works well for the minimum region and for larger distances. However, it can become inaccurate in the valence wall region. Errors in the short-range regions of the intermolecular potential,

originating from the common single-exchange approximation to the $E_{\text{exch}}^{(1)}$, $E_{\text{exch}}^{(2)}_{\text{-ind}}$ and terms can be overcome using the infinite-exchange expansion approach derived by Schäffer and Jansen.^{326, 327}

Charge-transfer interactions, which are a contribution to the sum of $E_{\text{ind}}^{(2)} + E_{\text{exch}}^{(2)}_{\text{-ind}}$, can be calculated by the regularised SAPT method of Misquitta.³²⁸ This variant of the SAPT method can also be employed in cases where the standard pertur-

bative approach breaks down, e.g., in the calculation of heavy metal interactions³²⁹ or for describing the σ -hole bond in complexes containing halogen electron donors.³³⁰

As an alternative to the commonly employed generalised gradient approximations (GGA) to the exchange-correlation (xc) potential and kernel in DFT-SAPT calculations, it is also possible to use orbital-dependent exact exchange functionals (see section III B) and kernels,³³¹ using Molpro. It was recently shown that DFT-SAPT methods which employ the exact nonadiabatic Kohn-Sham exchange kernel (TDEXX) and accurate long-range corrected exchange-correlation potentials in the monomer calculations clearly outperform a large number of empirical and nonempirical quantum chemistry approaches for the popular S22 and S66 dimer benchmark sets of Hobza et al.^{209,210,332}

All contributions in Eq. (8) can be computed using density-fitting techniques in the DFT-SAPT program, leading to remarkable speed-ups in the calculations already for medium sized dimers like benzene-benzene.²²¹ The DFT-SAPT method implemented in the Molpro program was also tested on the S12L set of large supramolecular complexes of Grimme et al.^{333,334} containing dimers with more than 800 electrons.²¹¹ The interaction energy of the bucky catcher complex (system C4b in the S12L data base) can be calculated within 6 days using the DFT-SAPT program on a 16 core Sandybridge computer clocked at 2 Mhz. Here, almost two thirds of the CPU time were spent in the calculation of the exchange-dispersion energy $E_{\text{exch}}^{(2)}\text{-disp}$ that possesses a scaling of N^5 with respect to the system size N .²¹¹ Other interesting applications of this code include endohedral complexes of fullerenes, like e.g. hydrogen molecule(s) inside C₆₀ and C₇₀³³⁵ or CHFCIBr inside chiral isomers of C₈₂.³³⁶

2. Symmetry-adapted perturbation theory based on Coupled-Cluster monomer wave functions

The SAPT with monomers described at the CCSD level has been implemented for all SAPT components of the first and second order with respect to the intermolecular interaction operator (see also Eq. (8)) as described in a number of papers for individual SAPT components.^{102,337-341} It should be noted that dispersion and exchange-dispersion components are calculated from a numerical integration over several imaginary frequencies, where the integrand contains full frequency-dependent polarization propagators at the

CCSD level.¹⁰⁴ Since the calculation of such propagators requires N^2 responses (for each \hat{r} operator), and each of these responses is as expensive as a single CCSD calculation, E_s the cost for full CCSD propagators scales with the 8th power of molecular size N . This scaling can be reduced by one order of N if density fitting is applied to the electron-density operator entering into the definition of the polarization propagator.^{340,341} Nevertheless, the SAPT(CCSD) method is primarily devoted to produce high-quality benchmarks for small noncovalent complexes and to compare them with less accurate methods. For instance, in Ref. 342 the SAPT(CCSD) and supermolecular CCSD(T) results were compared to a number of SAPT(DFT) approaches with different functionals. The SAPT(CCSD) code is also available in the monomer-centered basis set (MCBS) or various other subsets of the full dimer-centered basis set, thus making use of the SAPT independence on BSSE. It should be noted, however, that the saturation of orbital basis sets for most expensive SAPT components (dispersion and exchange-dispersion) is very slow, which makes the use of the MCBS inefficient in most cases.

VIII. USER INTERFACES

A. Input Structure

Molpro input is provided in an ASCII file. It contains of commands (calling programs as e.g. HF, CCSD(T) etc) with associated options, and directives which provide additional information such as occupations, symmetry, spin state etc. Geometries can be given in xyz or z-matrix form. Any number of commands can follow each other. Also branching and looping over parts of the input is possible. In the beginning of a calculation, the input is pre-checked to detect typos or invalid input specifications at the earliest possible stage. There are facilities to tabulate, plot, or export results, and marked-up xml output is generated as well. Despite the flexibility to generate rather complicated program-like inputs, the input for standard calculations is very simple. Some typical inputs for DFT and coupled-cluster calculations are shown in Table VII.

TABLE VII. Input examples for a DFT, CCSD(T) and PNO-LCCSD(T) calculation. The auxiliary basis density fitting and RI basis sets are determined automatically.

```

geometry=mygeom.xyz
basis=vtz          ! basis set cc-pVTZ
uks,pbe0+d3       ! unrestricted Kohn-Sham with D3 dispersion correction
optg              ! geometry optimization
frequencies       ! harmonic vibrational frequencies

```

```

geometry=mygeom.xyz
basis=vtz          ! basis set cc-pVTZ
hf                ! Hartree-Fock with density fitting
ccsd(t)           ! conventional coupled-cluster
extrapolate,vtz:vtz:v5z ! automatic basis set extrapolation

```

```

geometry=mygeom.xyz
basis=vtz-f12     ! basis set cc-pVTZ-F12
df-hf             ! Hartree-Fock with density fitting
pno-lccsd(t)-f12 ! explicitly correlated local coupled-cluster

```

B. Basis set library

An extensive basis set library is included in the Molpro program. This includes not only a large variety of orbital basis sets, but also a large number of auxiliary basis sets, i.e., basis sets for density fitting in HF, DFT, and correlated methods, as well as sets for approximate identity resolution for explicitly correlated calculations. In addition, a large library of effective core potentials (ECPs) is also maintained that include those from the Los Alamos group,^{251,252} the Stuttgart/Köln group,^{257,258} and others. In particular, the library of orbital basis sets includes all currently available correlation consistent basis sets³⁴³ across the entire periodic table (see: <http://www.grant-hill.group.shef.ac.uk/ccrepo/bib.html>). These include relatively new basis sets optimized for scalar relativistic Douglas-Kroll-Hess and X2C Hamiltonians, as well as those matched to Stuttgart/Köln small-core relativistic pseudopotentials, all of which extend the range of this basis set family down to Z=103 (Lr).^{259,344,345} Recent correlation consistent basis

sets optimized for explicitly correlated F12 approaches are also included.^{346–350} Finally, of course nearly all other commonly used basis sets appearing in the literature (obtained predominately from the Basis Set Exchange at <https://www.basissetexchange.org>) are also available, including the Karlsruhe def2 sets,^{351,352} Roos ANO sets,^{353,354} etc. Commonly used auxiliary sets include the JKFIT sets of Weigend and co-workers,³⁵⁵ the MP2FIT series of sets,^{356–358} and the OptRI sets for resolution of the identity in explicitly correlated F12 calculations.^{359–361} The Molpro basis set library can be conveniently browsed via the web interface at <https://www.molpro.net/info/basis.php>.

While the user has complete control over the choices of orbital and auxiliary basis set for each atom in a given calculation, including any sort of augmentations that might be desired, the program automatically selects appropriate defaults for all required auxiliary basis sets if an orbital basis set from either the correlation consistent or def2 family of basis sets is chosen. This is particularly useful in F12 calculations where 3 different auxiliary basis sets are required.

In the case of correlation consistent basis sets, Molpro provides a convenient mechanism to perform complete basis set extrapolations. After first specifying the type of energy calculation, the user specifies a range of basis sets, e.g., cc-pVTZ and cc-pVQZ, and then the required calculations are automatically carried out (cf. Table VII). The user can choose between a large number of common extrapolation formulas, which can be applied separately to reference energies, e.g. HF, and correlation energies. For example the user can extrapolate the HF energies with an exponential function (requiring 3 energies) and then the correlation energies with the default n^{-3} formula (n is the cardinal number of the basis set, e.g., 2 for VDZ, 3 for VTZ etc). The latter can be carried out with just the two largest basis sets or as a least squares fit to all 3 basis sets. The results of the extrapolation are automatically saved to variables that can be used in both geometry optimizations and harmonic frequency calculations, as well as output in Molpro's table command.

C. Graphical User Interface: gmolpro

`gmolpro` is a GTK-based graphical interface to Molpro that runs on Linux and macOS workstations. It supports the preparation of inputs through an expert system that interacts

with Molpro's registry of commands, methods and basis sets, guiding the user towards feasible combinations of calculation types (single point, optimisation etc), methods, basis sets and options. Checks are implemented so that the geometry, charge and spin are consistent, and only appropriate methods are selected. Reasonable default settings are provided so that an input can be quickly set up. It also provides a plain-text editor to allow further editing of existing job inputs.

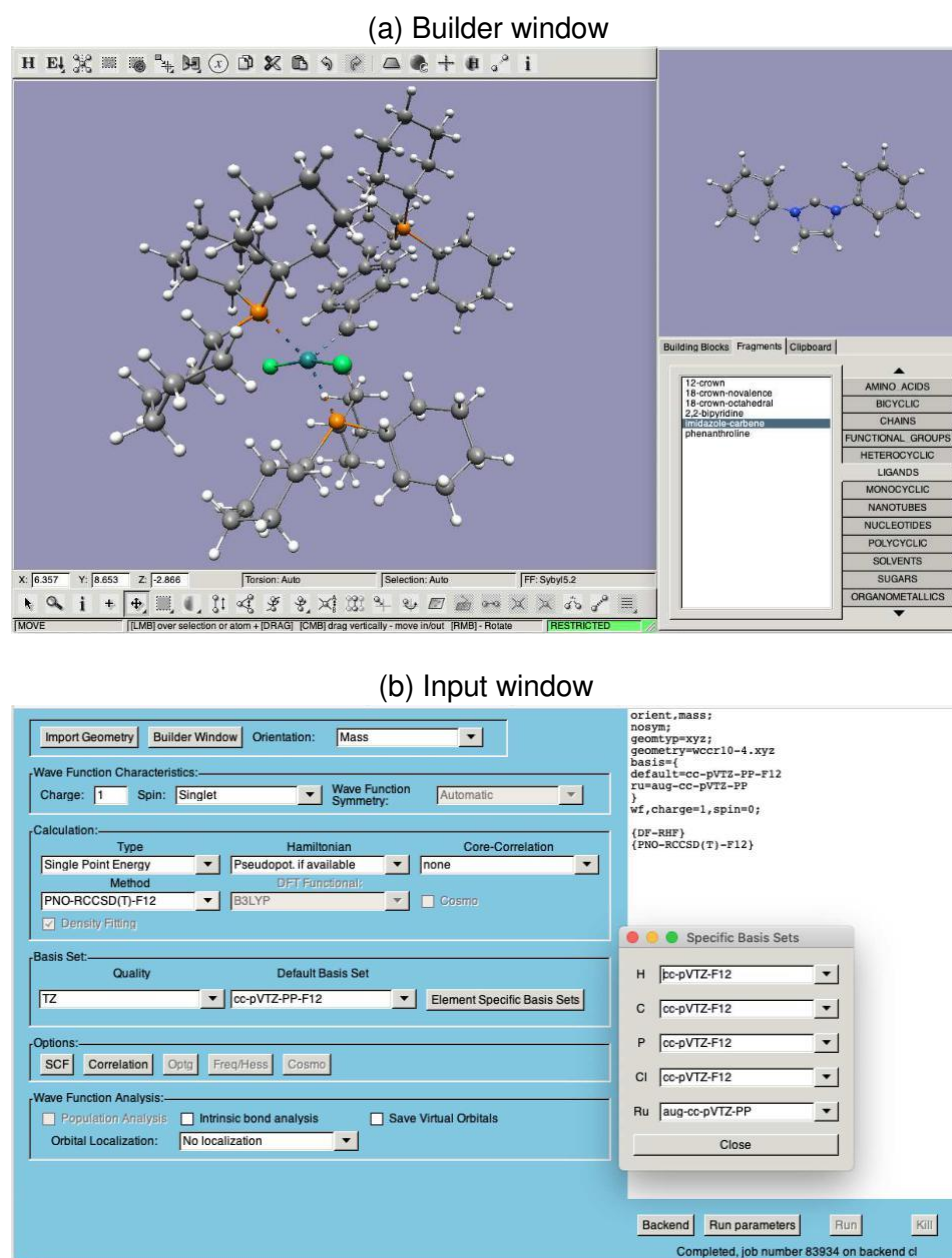
Molecular structures can be constructed and edited using an integrated builder derived from the PQSMol³⁶² interface to the PQS^{363,364} package. It incorporates fragment libraries, force fields, and an optimisation based on force fields. Jobs can then be submitted and managed on the local computer or a remote machine (see section VIII D for details). Results may be visualised via the viewer component of PQSMol, including an interactive display of structures, orbitals, property maps and vibrational modes. Figure 5 shows the PQSMol builder window (upper part) and the gmolpro input window (lower part) for a PNO-LCCSD(T)-F12 calculation on a large transition metal complex.

D. Job submission and analysis tools

A new framework for managing individual Molpro runs, collections of calculations, and relationships between them has been developed. The central concept is a project, which is a filesystem-resident object, implemented as a directory containing all necessary files, holding everything that belongs to a single run of Molpro. This includes not only the input and output files, but also a dictionary of properties which are simple key-value pairs of strings. Some of the property names have special meaning for the operation of the project, but otherwise anything can be stored in the dictionary. `gmolpro` makes use of these projects in managing the entire set of data associated with a Molpro calculation, but is not the only context in which they can be useful.

The Simple Job Execution Framework (SJEF)³⁶⁵ defines a C++ class that provides an interface to these objects; there is also a C binding and command-line utility, as well a Python library `pysjef` that includes a binding to SJEF. Although intended for use with Molpro, SJEF has been written in a generic way so that it could be used with any other program. As well as providing utilities to manipulate projects and their contents, SJEF

FIG. 5. (a) gmolpro builder and (b) input and job submission windows. The builder window, based on PQSMol,³⁶² shows in its left pane the structure of the reactant molecule of system 4 in the WCCR10 benchmark.¹⁹⁵ PNO-LCCSD(T)-F12 results for this benchmark can be found in Ref. 56.



supports the launching and monitoring of Molpro runs on either the local computer or a different system. Jobs are placed through the definition of one or more backends that are defined in per-user and per-system configuration files. A cache copy of the project bundle is maintained on the remote host, and synchronization in both directions is carried out as

needed. The backend specification contains the command needed to launch a Molpro job, either directly or via a batch system, together with further specifications of batch systems that facilitate the monitoring and abortion of jobs. SJEF is then able to provide information about the status of the job, as well as serving its output after performing any necessary synchronisation.

The primary output from a Molpro job consists of a plain-text transcript of the progress of the calculation, together with a more detailed log file containing further information about, for example, individual steps in a geometry optimization. In addition, a marked-up version of the output is generated within the `molpro-output` XML schema³⁶⁶ to support automated post-processing of results such as energies, geometries, vibrations, basis sets and orbitals in `pysjef`, `gmolpro` and elsewhere.

`pysjef`³⁶⁷ is a Python module that supports the manipulation of collections of projects. As well as containing a full Python binding of SJEF, it implements a search for results in output files. Projects, output files, and individual elements in the XML tree of the output file are all represented as instances of a `Node` class, that is linked to other nodes in a tree. Because nodes can be constructed as containers for other nodes, hierarchies of individual projects can be brought together in a single tree. As well as parent and children, each node contains a number of attributes, which are typically the actual data from the calculation. `pysjef` then supports selection of nodes from the tree or a list of trees satisfying given conditions, with the possibility of returning attributes by value instead of nodes. A group of nodes or sub-trees can also be used to build slices of a full tree. This highly flexible structure allows construction of complicated workflows with uniform interface to the output, project, or any other custom node. Similar to SJEF, `pysjef` does not have any Molpro specific code and works with any program satisfying SJEF's criteria. We have also developed `pysjef molpro`³⁶⁸ which is extended with utility functions and nodes specialized for Molpro. Figure 6 shows a simple example of a `pysjef` script in a Jupyter notebook,³⁶⁹ in which a potential energy surface scan is carried out. Although this simple example could also be expedited through the use of loops within the input of a single Molpro job, the Python-driven approach gives the possibility of independent jobs being executed in parallel, and localises the entire scientific project to a single shareable file. The intention is to give support to more complex workflows involving many different molecules and methods. The Python program can be executed repeatedly


```

from pysjef import Project, DirectoryNode, all_completed
from pysjef_molpro import no_errors
import numpy

```

```

root = DirectoryNode('dihedral_scan')

```

```

grid = numpy.linspace(0, 90, 18, endpoint=False)
for i, D in enumerate(grid):
    p = root.add_child(f'd{i}', suffix='molpro')
    p.write_input(
        f"""geometry={{
            H1
            C1 H1 rch
            C2 C1 rcc H1 A
            H2 C2 rch C1 A H1 D
            H3 C2 rch C1 A H2 180
            H4 C1 rch C2 A H1 180}}
            rch = 2.05; rcc = 2.65; A = 121.5; D = {D}+.01;
            basis = cc-pVTZ
            rhf
            set, mcoocc=[3,2,2,2], mcclosed=[3,1,1,2], mcsym=1
            casscf,so_sci
            {{optg; inactive, D}}
            set,mcsym=[1,4]
            casscf,so_sci
            {{mrci; wf, sym=1;}}
            {{mrci; wf, sym=4;}}""")

```

```

from multiprocessing.dummy import Pool
from operator import methodcaller
with Pool(processes=8) as pool:
    pool.map(methodcaller('run', backend='local', wait=True),
            root.children, 1)
print('all completed', all_completed(root.children))
print('without errors', no_errors(root.children))

```

```

all completed True
without errors True

```

```

import matplotlib.pyplot as plt
%matplotlib notebook
energies = root.select(
    '//jobstep[command=MRCI]/property[name=Energy].value')
e1, e2 = energies[:,2], energies[:,1]
cc = root.select('//variable[name=rcc]/value..')
plt.plot(grid, e1, grid, e2)
plt.legend([r'$X^1A_1$', r'$V^1B_1$'])
plt.xlabel('HCCH dihedral angle (degrees)')
plt.ylabel(r'Energy $(E_h)$')
plt.show()

```

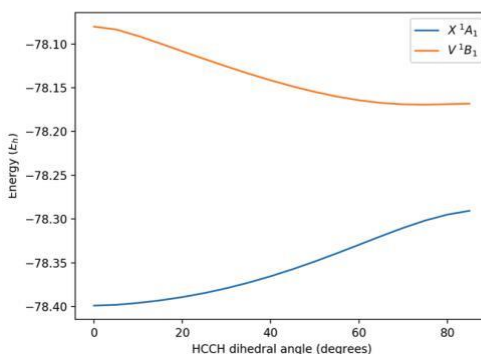


FIG. 6. Example of pysjef workflow showing calculation of potential energy curves (PEC) for ground and first excited states of C_2H_4 along its dihedral angle. The first input cell imports `pysjef` and `pysjef molpro`. The second input cell creates root of the project tree, using a node that maps to a directory. The third input cell adds projects to the root using a suffix to specify that they are Molpro jobs. In the fourth cell all jobs are executed in parallel independently on 8 processors, and checked for completion and errors. In the last cell, the whole tree is searched to select energies and C-C bond lengths, and PECs are plotted.

- for example whilst experimenting with plotting parameters - and, provided the Molpro inputs do not change, the Molpro calculations will not be re-executed.

IX. DEVELOPMENT TOOLS

A. FCIdump and other interfaces

Molpro connects to a number of other programs by providing the Hamiltonian operator expressed in molecular orbital basis, together, in some cases, with management of input options. The `FCIdump`^{370,371} format is used to specify the Hamiltonian structure and matrix elements, whilst the `molpro-plugin` library³⁷² is used to launch, and communicate with, the guest program. `molpro-plugin` works by using the standard process-spawning mechanism of MPI, and its installation in the guest is achieved through a simple library call that has no effect when not launched from Molpro. Programs using this mechanism include MRCC¹⁵⁰ and NECI,³⁷³ and in both those cases, the options for the guest code can be specified in Molpro input.

Conversely, `FCIdump` files can be read in by Molpro facilitating calculations on model Hamiltonians and frozen virtual approximations, using all available integral-non-direct methods.

B. Development environment, cmake etc

Molpro is written in a mixture of Fortran, C and C++, and depends on a number of external libraries. In order to manage the complexity of compilation portably, it employs the `cmake` build system generator. This enables, in particular, the easy incorporation of libraries that themselves have `cmake` support, and the use of an integrated development environment. Most external libraries are specified by reference; if not found locally by `cmake`, they are fetched and incorporated into the overall build process.

Molpro has a rich interface for basic objects such as orbitals, basis sets and integral generators, and can be effectively used as a development platform for new quantum-chemical methods.

X. OUTLOOK AND SUMMARY

We have described the principal and recent features of the Molpro program package; further details of well-established features can be found in Ref. 31. Many current developments are in progress, including in particular a strong focus on multireference methodology for large molecules. The package is used by a large community of users, and continues to make a distinctive strong contribution to the capability of predicting chemical structure and activity for molecules that are large and that have strongly correlated electronic structure.

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Molpro has been written by a large community of developers over many years; see <https://www.molpro.net/> for a full list. Their work has been made possible by numerous public funders, including the Deutsche Forschungsgemeinschaft (DFG), the European Research Council (ERC Advanced Grant 320723, ASES), and the Engineering and Physical Sciences Research Council (EP-SRC), as well as Technologie-Transfer-Initiative GmbH an der Universität Stuttgart (TTI GmbH), the current owner of Molpro.³²

AIP PUBLISHING DATA SHARING POLICY

The data that support the findings of this study are available within the article.

REFERENCES

- ¹W. Meyer, *Int. J. Quantum Chem.* **5**, 341 (1971).
- ²W. Meyer, *J. Chem. Phys.* **58**, 1017 (1973).
- ³P. Pulay, *Mol. Phys.* **17**, 197 (1969) .
- ⁴W. Meyer, *Theoretica Chimica Acta* **35**, 277 (1974).

- ⁵W. Meyer and P. Rosmus, *J. Chem. Phys.* **63**, 2356 (1975).
- ⁶H.-J. Werner and W. Meyer, *Mol. Phys.* **31**, 855 (1976).
- ⁷E.-A. Reinsch and W. Meyer, *Physical Review A* **14**, 915 (1976).
- ⁸P. Rosmus and W. Meyer, *J. Chem. Phys.* **66**, 13 (1977).
- ⁹P. Rosmus and W. Meyer, *J. Chem. Phys.* **69**, 2745 (1978).
- ¹⁰H.-J. Werner and P. J. Knowles, *J. Chem. Phys.* **89**, 5803 (1988).
- ¹¹P. J. Knowles and H.-J. Werner, *Chem. Phys. Letters* **145**, 514 (1988).
- ¹²H.-J. Werner and P. J. Knowles, *Theor. Chim. Acta* **78**, 175 (1990).
- ¹³P. J. Knowles and H.-J. Werner, *Theor. Chim. Acta* **84**, 95 (1992).
- ¹⁴K. R. Shamasundar, G. Knizia, and H.-J. Werner, *J. Chem. Phys.* **135**, 054101 (2011).
- ¹⁵A. Berning, M. Schweizer, H.-J. Werner, P. J. Knowles, and P. Palmieri, *Molecular Physics* **98**, 1823 (2010).
- ¹⁶H.-J. Werner, T. B. Adler, and F. R. Manby, *J. Chem. Phys.* **126**, 164102 (2007).
- ¹⁷G. Knizia and H.-J. Werner, *J. Chem. Phys.* **128**, 154103 (2008).
- ¹⁸T. B. Adler, G. Knizia, and H.-J. Werner, *J. Chem. Phys.* **127**, 221106 (2007).
- ¹⁹G. Knizia, T. B. Adler, and H.-J. Werner, *J. Chem. Phys.* **130**, 054104 (2009).
- ²⁰H.-J. Werner, G. Knizia, and F. R. Manby, *Mol. Phys* **109**, 407 (2011).
- ²¹T. Shiozaki and H.-J. Werner, *J. Chem. Phys.* **133**, 141103 (2010).
- ²²T. Shiozaki, G. Knizia, and H.-J. Werner, *J. Chem. Phys.* **134**, 034113 (2011).
- ²³T. Shiozaki and H.-J. Werner, *J. Chem. Phys.* **134**, 184104 (2011).
- ²⁴T. Shiozaki and H.-J. Werner, *Mol. Phys.* **111**, 607 (2013).
- ²⁵D. P. Tew, W. Klopper, C. Neiss, and C. Hättig, *Phys. Chem. Chem. Phys.* **9**, 1921 (2007).
- ²⁶O. Marchetti and H.-J. Werner, *Phys. Chem. Chem. Phys.* **10**, 3400 (2008).
- ²⁷O. Marchetti and H.-J. Werner, *J. Phys. Chem. A* **113**, 11580 (2009).
- ²⁸H.-J. Werner, T. B. Adler, G. Knizia, and F. R. Manby, in *Recent Progress in Coupled Cluster Methods*, edited by P. Čársky, J. Paldus, and J. Pittner (Springer, Dordrecht, Heidelberg, London, New York, 2010) pp. 573–619.
- ²⁹D. P. Tew, C. Hättig, R. A. Bächorz, and W. Klopper, in *Recent Progress in Coupled Cluster Methods*, edited by P. Čársky, J. Paldus, and J. Pittner (Springer, Dordrecht, Heidelberg, London, New York, 2010) pp. 535–572.

- ³⁰K. A. Peterson, C. Krause, H. Stoll, J. G. Hill, and H.-J. Werner, *Mol. Phys.* **109**, 2607 (2011).
- ³¹H.-J. Werner, P. J. Knowles, G. Knizia, F. R. Manby, and M. Schütz, *WIREs Comput Mol Sci* **2**, 242 (2012).
- ³²H.-J. Werner, P. J. Knowles, G. Knizia, F. R. Manby, M. Schütz, P. Celani, K. Doll, W. Győrffy, A. Hesselmann, D. Kats, T. Korona, D. Kreplin, R. Lindh, Q. Ma, A. J. May, A. Mitrushenkov, K. A. Peterson, G. Rauhut, K. R. Shamasundar, T. B. Adler, R. D. Amos, S. J. Bennie, A. Bernhardsson, A. Berning, D. L. Cooper, M. J. O. Deegan, A. J. Dobbyn, F. Eckert, E. Goll, C. Hampel, G. Hetzer, T. Hrenar, G. Jansen, C. Köppl, S. J. R. Lee, Y. Liu, A. W. Lloyd, R. A. Mata, S. J. McNicholas, F. Menezes, W. Meyer, T. F. Miller III, M. E. Mura, A. Nicklass, D. P. O'Neill, P. Palmieri, D. Peng, K. Pflüger, R. Pitzer, M. Reiher, M. Schwilk, T. Shiozaki, H. Stoll, A. J. Stone, R. Tarroni, T. Thorsteinsson, D. Usvyat, M. Wang, and M. Welborn, "Molpro, version 2020.0, a package of ab initio programs," (2020), see <https://www.molpro.net>.
- ³³D. Kats and F. R. Manby, *J. Chem. Phys.* **139**, 021102 (2013).
- ³⁴D. Kats, *J. Chem. Phys.* **141**, 061101 (2014).
- ³⁵D. Kats, D. Kreplin, H.-J. Werner, and F. R. Manby, *J. Chem. Phys.* **142**, 064111 (2015).
- ³⁶D. Kats, *J. Chem. Phys.* **144**, 044102 (2016).
- ³⁷D. Kats, *Mol. Phys.* **116**, 1435 (2018).
- ³⁸J. B. Robinson and P. J. Knowles, *J. Chem. Phys.* **136**, 054114 (2012).
- ³⁹J. B. Robinson and P. J. Knowles, *Phys. Chem. Chem. Phys.* **14**, 6729 (2012).
- ⁴⁰J. B. Robinson and P. J. Knowles, *J. Chem. Phys.* **137**, 054301 (2012).
- ⁴¹J. B. Robinson and P. J. Knowles, *J. Chem. Phys.* **138** (2013).
- ⁴²J. A. Black and P. J. Knowles, *Mol. Phys.* **116**, 1421 (2017).
- ⁴³J. A. Black and P. J. Knowles, *J. Chem. Phys.* **148** (2018).
- ⁴⁴H.-J. Werner, *J. Chem. Phys.* **129**, 101103 (2008).
- ⁴⁵T. B. Adler and H.-J. Werner, *J. Chem. Phys.* **130**, 241101 (2009).
- ⁴⁶T. B. Adler, H.-J. Werner, and F. R. Manby, *J. Chem. Phys.* **130**, 054106 (2009).
- ⁴⁷T. B. Adler and H.-J. Werner, *J. Chem. Phys.* **135**, 144117 (2011).
- ⁴⁸C. Krause and H.-J. Werner, *Phys. Chem. Chem. Phys.* **14**, 7591 (2012).
- ⁴⁹H.-J. Werner, G. Knizia, C. Krause, M. Schwilk, and M. Dornbach, *J. Chem. Theory Comput.* **11**, 484 (2015).

- ⁵⁰Q. Ma and H.-J. Werner, *J. Chem. Theory Comput.* **11**, 5291 (2015).
- ⁵¹H.-J. Werner, C. Köppl, Q. Ma, and M. Schwilk, in *Fragmentation: Towards Accurate Calculations on Complex Molecular Systems*, edited by M. S. Gordon (Wiley, Chichester, UK, 2017) pp. 1–89, this article is freely available under <https://www.wiley.com>.
- ⁵²H.-J. Werner, *J. Chem. Phys.* **145**, 201101 (2016).
- ⁵³M. Schwilk, Q. Ma, C. Köppl, and H.-J. Werner, *J. Chem. Theory Comput.* **13**, 3650 (2017).
- ⁵⁴Q. Ma, M. Schwilk, C. Köppl, and H.-J. Werner, *J. Chem. Theory Comput.* **13**, 4871 (2017).
- ⁵⁵Q. Ma and H.-J. Werner, *J. Chem. Theory Comput.* **14**, 198 (2017).
- ⁵⁶Q. Ma and H.-J. Werner, *WIREs Comput. Mol. Sci.*, e1371 (2018).
- ⁵⁷C. Krause and H.-J. Werner, *J. Chem. Theory Comput.* **15**, 987 (2019).
- ⁵⁸Q. Ma and H.-J. Werner, TBD (2019).
- ⁵⁹F. R. Manby, M. Stella, J. D. Goodpaster, and T. F. Miller III, *Journal of Chemical Theory and Computation* **8**, 2564 (2012).
- ⁶⁰D. A. Kreplin, P. J. Knowles, and H.-J. Werner, *J. Chem. Phys.* **150**, 194106 (2019).
- ⁶¹D. A. Kreplin, P. J. Knowles, and H.-J. Werner, *J. Chem. Phys.* **152**, 074102 (2020).
- ⁶²F. Menezes, D. Kats, and H.-J. Werner, *J. Chem. Phys.* **145**, 124115 (2016).
- ⁶³D. Kats and H.-J. Werner, *J. Chem. Phys.* **150**, 214107 (2019).
- ⁶⁴C. Köppl and H.-J. Werner, *J. Chem. Theory Comput.* **12**, 3122 (2016).
- ⁶⁵P. P. Hallmen, C. Köppl, G. Rauhut, H. Stoll, and J. van Slageren, *J. Chem. Phys.* **147**, 164101 (2017).
- ⁶⁶P. P. Hallmen, H.-J. Werner, D. Kats, S. Lenz, G. Rauhut, H. Stoll, and J. van Slageren, *Phys. Chem. Chem. Phys.* **21**, 9769 (2019).
- ⁶⁷L. Roy, M. H. Al-Afyouni, D. E. DeRosha, B. Mondal, I. M. DiMucci, K. M. Lancaster, J. Shearer, E. Bill, W. W. Brennessel, F. Neese, S. Ye, and P. L. Holland, *Chem. Sci.* **10**, 918 (2019).
- ⁶⁸C. Hampel, K. A. Peterson, and H.-J. Werner, *Chem. Phys. Lett.* **190**, 1 (1992).
- ⁶⁹O. Christiansen, H. Koch, and P. Jørgensen, *Chem. Phys. Lett.* **243**, 409 (1995).
- ⁷⁰D. Kats, T. Korona, and M. Schütz, *J. Chem. Phys.* **125**, 104106 (2006).
- ⁷¹D. Kats, T. Korona, and M. Schütz, *J. Chem. Phys.* **127**, 064107 (2007).
- ⁷²D. Kats and M. Schütz, *J. Chem. Phys.* **131**, 124117 (2009).

- ⁷³K. Freundorfer, D. Kats, T. Korona, and M. Schütz, *J. Chem. Phys.* **133**, 244110 (2010).
- ⁷⁴T. Korona and H.-J. Werner, *J. Chem. Phys.* **118**, 3006 (2003).
- ⁷⁵S. Grimme, *J. Chem. Phys.* **118**, 9095 (2003).
- ⁷⁶P. J. Knowles, C. Hampel, and H.-J. Werner, *J. Chem. Phys.* **99**, 5219 (1993).
- ⁷⁷D. Kats and D. P. Tew, *J. Chem. Theory Comput.* **15**, 13 (2019).
- ⁷⁸M. Schütz, R. Lindh, and H.-J. Werner, *Mol. Phys.* **96**, 719 (1999).
- ⁷⁹B. Cooper and P. J. Knowles, *J. Chem. Phys.* **133**, 234102 (2010).
- ⁸⁰P. Piecuch, S. A. Kucharski, and K. Kowalski, *Chem. Phys. Lett.* **344**, 176 (2001).
- ⁸¹T. Van Voorhis and M. Head-Gordon, *J. Chem. Phys.* **113**, 8873 (2000).
- ⁸²P. Piecuch and M. Wloch, *J. Chem. Phys.* **123**, 224105 (2005).
- ⁸³A. I. Krylov, L. V. Slipchenko, and S. V. Levchenko, in *ACS Symp. Ser. Vol. 958* (American Chemical Society, 2007) pp. 89–102.
- ⁸⁴D. Kats and A. Köhn, *J. Chem. Phys.* **150**, 151101 (2019).
- ⁸⁵J. F. Stanton and R. J. Bartlett, *The Journal of Chemical Physics* **98**, 7029 (1993).
- ⁸⁶E. R. Davidson, *Journal of Computational Physics* **17**, 87 (1975).
- ⁸⁷K. Hirao and H. Nakatsuji, *Journal of Computational Physics* **45**, 246 (1982).
- ⁸⁸T. Korona and H.-J. Werner, *Journal of Chemical Physics* **118** (2003), 10.1063/1.1537718.
- ⁸⁹T. Korona, *Molecular Physics* **110**, 199 (2012).
- ⁹⁰F. Plasser and H. Lischka, *J. Chem. Theory Comput.* **8**, 2777 (2012).
- ⁹¹G. Walz, D. Kats, D. Usvyat, T. Korona, and M. Schütz, *Phys. Rev. A* **86**, 052519 (2012).
- ⁹²D. M. P. Holland, A. B. Trofimov, E. A. Seddon, E. V. Gromov, T. Korona, N. de Oliveira, L. E. Archer, D. Joyeux, and L. Nahon, *Phys. Chem. Chem. Phys.* **16**, 21629 (2014).
- ⁹³D. M. P. Holland, E. A. Seddon, A. B. Trofimov, E. V. Gromov, M. Wormit, A. Dreuw, T. Korona, N. De Oliveira, L. E. Archer, and D. Joyeux, *Journal of Molecular Spectroscopy* **315**, 184 (2015).
- ⁹⁴D. Rutkowska-Zbik and T. Korona, *Journal of Chemical Theory and Computation* **8**, 2972 (2012).
- ⁹⁵A. C. Scheiner, G. E. Scuseria, J. E. Rice, T. J. Lee, and H. F. Schaefer, *The Journal of Chemical Physics* **87**, 5361 (1987), <https://doi.org/10.1063/1.453655>.
- ⁹⁶P. Jørgensen and T. Helgaker, *The Journal of Chemical Physics* **89**, 1560 (1988), <https://doi.org/10.1063/1.455152>.

- ⁹⁷H. Koch, H. J. A. Jensen, P. Jørgensen, T. Helgaker, G. E. Scuseria, and H. F. Schaefer, *The Journal of Chemical Physics* **92**, 4924 (1990), <https://doi.org/10.1063/1.457710>.
- ⁹⁸T. Korona, B. Jeziorski, and R. Moszynski, *Molecular Physics* **100**, 1723 (2002).
- ⁹⁹G. Rauhut and H. J. Werner, *Phys. Chem. Chem. Phys.* **3**, 4853 (2001).
- ¹⁰⁰R. J. Bartlett and J. Noga, *Chemical Physics Letters* **150**, 29 (1988).
- ¹⁰¹B. Jeziorski and R. Moszynski, *International Journal of Quantum Chemistry* **48**, 161 (1993), <https://onlinelibrary.wiley.com/doi/pdf/10.1002/qua.560480303>.
- ¹⁰²T. Korona, *Journal of Chemical Physics* **128**, 224104 (2008).
- ¹⁰³R. Moszynski, P. S. Zuchowski, and B. Jeziorski, *Collect. Czech. Chem. Commun.* **70**, 1109 (2005).
- ¹⁰⁴T. Korona, M. Przybytek, and B. Jeziorski, *Molecular Physics* **104**, 2303 (2006).
- ¹⁰⁵T. Korona, *Molecular Physics* **108**, 343 (2010).
- ¹⁰⁶H.-J. Werner and W. Meyer, *J. Chem. Phys.* **73**, 2342 (1980).
- ¹⁰⁷H.-J. Werner and W. Meyer, *J. Chem. Phys.* **74**, 5794 (1981).
- ¹⁰⁸H.-J. Werner and P. J. Knowles, *J. Chem. Phys.* **82**, 5053 (1985).
- ¹⁰⁹P. J. Knowles and H.-J. Werner, *Chem. Phys. Letters* **115**, 259 (1985).
- ¹¹⁰P. J. Knowles and N. C. Handy, *Chem. Phys. Letters* **111**, 315 (1984).
- ¹¹¹P. A. Malmqvist, A. Rendell, and B. O. Roos, *J. Phys. Chem.* **94**, 5477 (1990).
- ¹¹²B. O. Roos, *Int. J. Quantum Chem.* **18**, 175 (1980).
- ¹¹³J. Nocedal, *Math. Comput.* **35**, 773 (1980).
- ¹¹⁴E. R. Sayfutyarova, Q. Sun, G. K.-L. Chan, and G. Knizia, *J. Chem. Theory Comput.* **13**, 4063 (2017).
- ¹¹⁵Y. Guo, K. Sivalingam, E. F. Valeev, and F. Neese, *J. Chem. Phys.* **144**, 094111 (2016).
- ¹¹⁶W. Meyer, "Modern theoretical chemistry vol. 3," (Plenum, New York, 1977) Chap. Configuration Expansion by Means of Pseudonatural Orbitals.
- ¹¹⁷P. E. M. Siegbahn, *Int. J. Quantum Chem.* **18**, 1229 (1980).
- ¹¹⁸P. E. M. Siegbahn and M. Svensson, *Int. J. Quantum Chem.* **41**, 153 (1992).
- ¹¹⁹H.-J. Werner and E.-A. Reinsch, in Proceedings of the fifth seminar on computational methods in quantum chemistry (Max-Planck-Institut für Physik und Astrophysik, München, Groningen, Netherlands, 1981).
- ¹²⁰H.-J. Werner and E. Reinsch, *J. Chem. Phys.* **76**, 3144 (1982).
- ¹²¹R. J. Gdanitz and R. Ahlrichs, *Chem. Phys. Lett.* **143**, 413 (1988).

- ¹²²R. J. Cave and E. R. Davidson, *J. Chem. Phys.* **88**, 5770 (1988).
- ¹²³R. J. Cave and E. R. Davidson, *J. Chem. Phys.* **89**, 6798 (1988).
- ¹²⁴P. Celani and H.-J. Werner, *J. Chem. Phys.* **112**, 5546 (2000).
- ¹²⁵D. Kats and F. R. Manby, *J. Chem. Phys.* **138**, 144101 (2013).
- ¹²⁶W. Győrffy, G. Knizia, and H.-J. Werner, *J. Chem. Phys.* **147**, 214101 (2017).
- ¹²⁷W. Győrffy and H.-J. Werner, *J. Chem. Phys.* **148**, 114104 (2018).
- ¹²⁸H.-J. Werner, *Mol. Phys.* **89**, 645 (1996).
- ¹²⁹T. Shiozaki, W. Győrffy, P. Celani, and H.-J. Werner, *J. Chem. Phys.* **135**, 081106 (2011).
- ¹³⁰T. Shiozaki, C. Woywod, and H.-J. Werner, *Phys. Chem. Chem. Phys.* **15**, 262 (2013).
- ¹³¹A. A. Granovsky, *J. Chem. Phys.* **134**, 214113 (2011).
- ¹³²D. I. Lyakh, M. Musial, V. F. Lotrich, and R. J. Bartlett, *Chem. Rev.* **112**, 182 (2012).
- ¹³³A. Köhn, M. Hanauer, L. A. Müuck, T.-C. Jagau, and J. Gauss, *WIREs Comput. Mol. Sci.* **3**, 176 (2013).
- ¹³⁴ F. A. Evangelista, *J. Chem. Phys.* **149**, 030901 (2018).
- ¹³⁵A. Banerjee and J. Simons, *Int. J. Quantum Chem.* **19**, 207 (1981).
- ¹³⁶A. Banerjee and J. Simons, *J. Chem. Phys.* **76**, 4548 (1982).
- ¹³⁷ F. A. Evangelista and J. Gauss, *J. Chem. Phys.* **134**, 114102 (2011).
- ¹³⁸M. Hanauer and A. Köhn, *J. Chem. Phys.* **134**, 204111 (2011).
- ¹³⁹M. Hanauer and A. Köhn, *J. Chem. Phys.* **136**, 204107 (2012).
- ¹⁴⁰M. Hanauer and A. Köhn, *J. Chem. Phys.* **137**, 131103 (2012).
- ¹⁴¹Y. A. Aoto and A. Köhn, *J. Chem. Phys.* **144**, 074103 (2016).
- ¹⁴²Y. A. Aoto and A. Köhn, *Phys. Chem. Chem. Phys.* **18**, 30241 (2016).
- ¹⁴³Y. A. Aoto, A. P. de Lima Batista, A. Köhn, and A. G. S. de Oliveira-Filho, *J. Chem. Theory Comput.* **13**, 5291 (2017).
- ¹⁴⁴D. J. Coughtrie, R. Giereth, D. Kats, H.-J. Werner, and A. Köhn, *J. Chem. Theory Comput.* **14**, 693 (2018).
- ¹⁴⁵R. A. Mata, H.-J. Werner, and M. Schütz, *J. Chem. Phys.* **128**, 144106 (2008).
- ¹⁴⁶G. Knizia, *J. Chem. Theory Comput.* **9**, 4834 (2013).
- ¹⁴⁷Y. A. Aoto, A. Bargholz, D. Kats, H.-J. Werner, and A. Köhn, *J. Chem. Theory Comput.* **15**, 2291 (2019).
- ¹⁴⁸ J. A. Black and A. Köhn, *J. Chem. Phys.* **150**, 194107 (2019).
- ¹⁴⁹A. Köhn and A. Bargholz, *J. Chem. Phys.* **151**, 041106 (2019).

- ¹⁵⁰“MRCC, a quantum chemical program suite written by M. Kállay, P. R. Nagy, Z. Rolik, D. Mester, G. Samu, J. Csontos, J. Csóka, B. P. Szabó, L. Gyevi-Nagy, I. Ladjánszki, L. Szegedy, B. Ladóczki, K. Petrov, M. Farkas, P. D. Mezei, and B. Hégyel. See also Z. Rolik, L. Szegedy, I. Ladjánszki, B. Ladóczki, and M. Kállay, *J. Chem. Phys.* **139**, 094105 (2013), as well as: www.mrcc.hu.” (2013).
- ¹⁵¹K. A. Peterson, T. B. Adler, and H.-J. Werner, *J. Chem. Phys.* **128**, 084102 (2008).
- ¹⁵²J. G. Hill, S. Mazumder, and K. A. Peterson, *J. Chem. Phys.* **132**, 054108 (2010).
- ¹⁵³D. H. Bross, J. G. Hill, H. J. Werner, and K. A. Peterson, *J. Chem. Phys.* **139**, 094302 (2013).
- ¹⁵⁴J. G. Hill and K. A. Peterson, *J. Chem. Phys.* **141**, 094106 (2014).
- ¹⁵⁵H.-J. Werner, G. Knizia, T. B. Adler, and O. Marchetti, *Z. Phys. Chem.* **224**, 493 (2010).
- ¹⁵⁶D. Feller, K. A. Peterson, and J. G. Hill, *J. Chem. Phys.* **133**, 184102 (2010).
- ¹⁵⁷J. G. Hill, K. A. Peterson, G. Knizia, and H.-J. Werner, *J. Chem. Phys.* **131**, 194105 (2009).
- ¹⁵⁸J. G. Hill and K. A. Peterson, ACS Publications (2012).
- ¹⁵⁹Q. Ma and H.-J. Werner, *Journal Of Chemical Theory And Computation* **15**, 1044 (2019).
- ¹⁶⁰N. Sylvetsky, M. K. Kesharwani, and J. M. L. Martin, *J. Chem. Phys.* **147**, 134106 (2017).
- ¹⁶¹J. M. Foster and S. F. Boys, *Reviews of Modern Physics* **32**, 300 (1960).
- ¹⁶²J. Pipek and P. G. Mezey, *The Journal of Chemical Physics* **90**, 4916 (1989).
- ¹⁶³G. Knizia, *Journal of Chemical Theory and Computation* **9**, 4834 (2013).
- ¹⁶⁴C. Hampel and H.-J. Werner, *J. Chem. Phys.* **104**, 6286 (1996).
- ¹⁶⁵G. Hetzer, P. Pulay, and H.-J. Werner, *Chem. Phys. Lett.* **290**, 143 (1998).
- ¹⁶⁶M. Schütz, G. Hetzer, and H.-J. Werner, *J. Chem. Phys.* **111**, 5691 (1999).
- ¹⁶⁷G. Hetzer, M. Schütz, H. Stoll, and H.-J. Werner, *J. Chem. Phys.* **113**, 9443 (2000).
- ¹⁶⁸J. Gauss and H.-J. Werner, *Phys. Chem. Chem. Phys.* **2**, 2083 (2000).
- ¹⁶⁹M. Schütz and H.-J. Werner, *Chem. Phys. Lett.* **318**, 370 (2000).
- ¹⁷⁰M. Schütz, *J. Chem. Phys.* **113**, 9986 (2000).
- ¹⁷¹M. Schütz and H.-J. Werner, *J. Chem. Phys.* **114**, 661 (2001).
- ¹⁷²M. Schütz, *J. Chem. Phys.* **116**, 8772 (2002).
- ¹⁷³M. Schütz, *Phys. Chem. Chem. Phys.* **4**, 3941 (2002).
- ¹⁷⁴H.-J. Werner, F. R. Manby, and P. Knowles, *J. Chem. Phys.* **118**, 8149 (2003).

- ¹⁷⁵M. Schütz, H.-J. Werner, R. Lindh, and F. R. Manby, *J. Chem. Phys.* **121**, 737 (2004).
- ¹⁷⁶R. Mata and H.-J. Werner, *J. Chem. Phys.* **125**, 184110 (2006).
- ¹⁷⁷H.-J. Werner and K. Pflüger, *Ann. Rep. Comput. Chem.* **2**, 53 (2006).
- ¹⁷⁸R. Mata and H.-J. Werner, *Mol. Phys.* **105**, 2753 (2007).
- ¹⁷⁹R. Mata, H.-J. Werner, and M. Schütz, *J. Chem. Phys.* **128**, 144106 (2008).
- ¹⁸⁰H.-J. Werner and M. Schütz, *J. Chem. Phys.* **135**, 144116 (2011).
- ¹⁸¹A. ElAzhary, G. Rauhut, P. Pulay, and H.-J. Werner, *J. Chem. Phys.* **108**, 5185 (1998).
- ¹⁸²M. Dornbach and H.-J. Werner, *Mol. Phys.* **117**, 1252 (2018).
- ¹⁸³K. Ledermüller, D. Kats, and M. Schütz, *J. Chem. Phys.* **139**, 084111 (2013).
- ¹⁸⁴K. Ledermüller and M. Schütz, *J. Chem. Phys.* **140**, 164113 (2014).
- ¹⁸⁵J. Yang, Y. Kurashige, and F. R. Manby, *J. Chem. Phys.* **134**, 044123 (2011).
- ¹⁸⁶J. Yang, G. K.-L. Chan, F. R. Manby, M. Schütz, and H.-J. Werner, *J. Chem. Phys.* **136**, 144105 (2012).
- ¹⁸⁷M. Schütz, J. Yang, G. K.-L. Chan, F. R. Manby, and H.-J. Werner, *J. Chem. Phys.* **138**, 054109 (2013).
- ¹⁸⁸M. Schwilk, D. Usvyat, and H.-J. Werner, *J. Chem. Phys.* **142**, 121102 (2015).
- ¹⁸⁹J. Nieplocha, B. Palmer, V. Tipparaju, M. Krishnan, H. Trease, and E. Apr`a, *Int. J. High Perform C.* **20**, 203 (2006).
- ¹⁹⁰J. Friedrich and J. H`anchen, *J. Chem. Theory Comput.* **9**, 5381 (2013).
- ¹⁹¹M. K. Kesharwani, A. Karton, N. Sylvetsky, and J. M. L. Martin, *Aust. J. Chem.* **71**, 238 (2018).
- ¹⁹²Y. Liu, Linear scaling high-spin open-shell local correlation methods, *Ph.D. thesis*, Uni-versity of Stuttgart (2011).
- ¹⁹³S. Luo, Y. Zhao, and D. G. Truhlar, *Phys. Chem. Chem. Phys.* **13**, 13683 (2011).
- ¹⁹⁴A. Fedorov, L. Batiste, E. P. A. Couzijn, and P. Chen, *ChemPhysChem* **11**, 1002 (2010).
- ¹⁹⁵T. Weymuth, E. P. A. Couzijn, P. Chen, and M. Reiher, *J. Chem. Theory Comput.* **10**, 3092 (2014).
- ¹⁹⁶M. Rado´n, *Phys. Chem. Chem. Phys.* **21**, 4854 (2019).
- ¹⁹⁷D. Kats, *J. Chem. Phys.* **141**, 244101 (2014).
- ¹⁹⁸D. Kats, *J. Chem. Phys.* **145**, 014103 (2016).
- ¹⁹⁹S. Grimme, J. Antony, S. Ehrlich, and H. Krieg, *J. Chem. Phys.* **132**, 154104 (2010).
- ²⁰⁰E. Caldeweyher, C. Bannwarth, and S. Grimme, *J. Chem. Phys.* **147**, 034112 (2017).

- ²⁰¹A. Heßelmann, *J. Chem. Theory Comput.* **9**, 273 (2013).
- ²⁰²A. Heßelmann, *J. Chem. Phys.* **149**, 044103 (2018).
- ²⁰³F. Della Sala and A. Görling, *J. Chem. Phys.* **115**, 5718 (2001).
- ²⁰⁴A. Heßelmann, A. W. Götz, F. Della Sala, and A. Görling, *J. Chem. Phys.* **127**, 054102 (2007).
- ²⁰⁵A. D. Becke, *J. Chem. Phys.* **88**, 2547 (1988).
- ²⁰⁶C. W. Murray, N. C. Handy, and G. J. Laming, *Mol. Phys.* **78**, 997 (1993).
- ²⁰⁷R. Strange, F. R. Manby, and P. J. Knowles, *Comput. Phys. Commun.* **136**, 310 (2001).
- ²⁰⁸S. Grimme, A. Hansen, G. B. J., and C. Bannwarth, *Chem. Rev.* **116**, 5105 (2016).
- ²⁰⁹P. Jurecka, J. Sponer, J. Cerny, and P. Hobza, *Phys. Chem. Chem. Phys.* **8**, 1985 (2006).
- ²¹⁰J. Rezac, K. E. Riley, and P. Hobza, *J. Chem. Theory Comput.* **10**, 1359 (2014).
- ²¹¹A. Heßelmann and T. Korona, *J. Chem. Phys.* **141**, 094107 (2014).
- ²¹²A. Holas and M. Cinal, *Phys. Rev. A* **72**, 032504 (2005).
- ²¹³A. Görling, *J. Chem. Phys.* **123**, 062203 (2005).
- ²¹⁴A. Heßelmann and A. Görling, *J. Chem. Phys.* **134**, 034120 (2011).
- ²¹⁵R. T. Sharp and G. K. Horton, *Phys. Rev.* **90**, 317 (1953).
- ²¹⁶J. D. Talman and W. F. Shadwick, *Phys. Rev. A* **14**, 36 (1976).
- ²¹⁷A. Görling, *Phys. Rev. Lett.* **83**, 5459 (1999).
- ²¹⁸S. Hamel, M. E. Casida, and D. R. Salahub, *J. Chem. Phys.* **116**, 8276 (2002).
- ²¹⁹M. Grüning, O. V. Gritsenko, and E. J. Baerends, *J. Chem. Phys.* **116**, 6435 (2002).
- ²²⁰V. N. Staroverov, G. E. Scuseria, and E. R. Davidson, *J. Chem. Phys.* **125**, 081104 (2006).
- ²²¹A. Heßelmann, G. Jansen, and M. Schütz, *J. Chem. Phys.* **122**, 014103 (2005).
- ²²²M. A. L. Marques, C. A. Ullrich, F. Nogueira, A. Rubio, K. Burke, and E. K. U. Gross, eds., *Time-Dependent Density Functional Theory, Lecture Notes in Physics, Vol. 706* (Springer, Heidelberg, 2006).
- ²²³A. Heßelmann, A. Ipatov, and A. Görling, *Phys. Rev. A* **80**, 012507 (2009).
- ²²⁴A. Görling, A. Ipatov, A. W. Götz, and A. Heßelmann, *Z. Phys. Chem.* **224**, 325 (2010).
- ²²⁵A. Ipatov, A. Heßelmann, and A. Görling, *Int. J. Quantum Chem.* **110**, 2202 (2010).
- ²²⁶P. Sherwood, A. H. de Vries, M. F. Guest, G. Schreckenbach, C. R. A. Catlow, S. A. French, A. A. Sokol, S. T. Bromley, W. Thiel, A. J. Turner, et al., *J. Mol. Struct.: THEOCHEM* **632**, 1 (2003).

- ²²⁷G. R. Ahmadi and J. Almlöf, *Chem. Phys. Lett.* **246**, 364 (1995).
- ²²⁸C. A. White and M. Head-Gordon, *J. Chem. Phys.* **104**, 2620 (1996).
- ²²⁹F. Claeysens, J. N. Harvey, F. R. Manby, R. A. Mata, A. J. Mulholland, K. E. Ranaghan, M. Schütz, S. Thiel, W. Thiel, and H.-J. Werner, *Angew. Chemie Int. Ed.* **45**, 6856 (2006).
- ²³⁰R. A. Mata, H.-J. Werner, S. Thiel, and W. Thiel, *J. Chem. Phys.* **128**, 01B610 (2008).
- ²³¹M. W. van der Kamp, J. Zurek, F. R. Manby, J. N. Harvey, and A. J. Mulholland, *J. Phys. Chem. B* **114**, 11303 (2010).
- ²³²N. Lawan, K. E. Ranaghan, F. R. Manby, and A. J. Mulholland, *Chem. Phys. Lett.* **608**, 380 (2014).
- ²³³M. Stella, S. J. Bennie, and F. R. Manby, *Molecular Physics* **113**, 1858 (2015).
- ²³⁴T. A. Barnes, J. W. Kaminski, O. Borodin, and T. F. Miller III, *The Journal of Physical Chemistry C* **119**, 3865 (2015).
- ²³⁵P. Huo, C. Uyeda, J. D. Goodpaster, J. C. Peters, and T. F. Miller III, *ACS Catalysis* **6**, 6114 (2016).
- ²³⁶S. J. Bennie, M. W. van der Kamp, R. C. R. Pennifold, M. Stella, F. R. Manby, and A. J. Mulholland, *Journal of Chemical Theory and Computation* **12**, 2689 (2016).
- ²³⁷S. J. Bennie, B. F. E. Curchod, F. R. Manby, and D. R. Glowacki, *The Journal of Physical Chemistry Letters* **8**, 5559 (2017).
- ²³⁸M. Welborn, F. R. Manby, and T. F. Miller III, *The Journal of Chemical Physics* **149**, 144101 (2018).
- ²³⁹X. Zhang, S. J. Bennie, M. W. van der Kamp, D. R. Glowacki, F. R. Manby, and A. J. Mulholland, *Royal Society Open Science* **5**, 171390 (2018).
- ²⁴⁰A. Chapovetsky, M. Welborn, J. M. Luna, R. Haiges, T. F. Miller III, and S. C. Marinescu, *ACS Central Science* **4**, 397 (2018).
- ²⁴¹S. J. Bennie, M. Stella, T. F. Miller III, and F. R. Manby, *The Journal of Chemical Physics* **143**, 024105 (2015).
- ²⁴²S. J. R. Lee, F. Ding, F. R. Manby, and T. F. Miller III, *J. Chem. Phys.* **151**, 064112 (2019).
- ²⁴³M. Douglas and N. Kroll, *Ann. Phys. (N.Y.)* **82**, 89 (1974).
- ²⁴⁴B. Hess, *Phys. Rev. A* **33**, 3742 (1986).
- ²⁴⁵G. Jansen and B. Hess, *Phys. Rev. A* **39**, 6016 (1989).
- ²⁴⁶M. Iliaš and T. Saue, *The Journal of Chemical Physics* **126**, 4102 (2007).

- ²⁴⁷D. Peng and M. Reiher, *Theoretical Chemistry Accounts: Theory, Computation, and Modeling (Theoretica Chimica Acta)* **131**, 1081 (2012).
- ²⁴⁸M. Reiher and A. Wolf, *Journal of Chemical Physics* **121**, 10945 (2004).
- ²⁴⁹L. Visscher and K. G. Dyall, *Atomic Data and Nuclear Data Tables* **67**, 207 (1997).
- ²⁵⁰M. Dolg and X. Cao, *Chemical Reviews* **112**, 403 (2012).
- ²⁵¹W. R. Wadt and P. J. Hay, *The Journal of Chemical Physics* **82**, 284 (1985).
- ²⁵²P. J. Hay and W. R. Wadt, *The Journal of Chemical Physics* **82**, 270 (1985).
- ²⁵³W. J. Stevens, H. Basch, and M. Krauss, *The Journal of Chemical Physics* **81**, 6026 (1984).
- ²⁵⁴W. Stevens, M. Krauss, H. Basch, and P. Jasien, *Canadian Journal Of Chemistry- Revue Canadienne De Chimie* **70**, 612 (1992).
- ²⁵⁵J. R. Trail and R. J. Needs, *The Journal of Chemical Physics* **122**, 174109 (2005).
- ²⁵⁶J. R. Trail and R. J. Needs, *The Journal of Chemical Physics* **142**, 064110 (2015).
- ²⁵⁷H. Stoll, B. Metz, and M. Dolg, *Journal Of Computational Chemistry* **23**, 767 (2002).
- ²⁵⁸A. Weigand, X. Cao, T. Hangele, and M. Dolg, *The Journal of Physical Chemistry A* **118**, 2519 (2014).
- ²⁵⁹D. Figgen, K. A. Peterson, M. Dolg, and H. Stoll, *Journal of Chemical Physics* **130**, 164108 (2009).
- ²⁶⁰B. A. Heß, C. M. Marian, U. Wahlgren, and O. Gropen, [Chemical Physics Letters](#) **251**, 365 (1996).
- ²⁶¹A. Berning, M. Schweizer, H.-J. Werner, P. J. Knowles, and P. Palmieri, [Molecular Physics](#) **98**, 1823 (2000), <https://doi.org/10.1080/00268970009483386>.
- ²⁶²P. Celani and H.-J. Werner, *J. Chem. Phys.* **119**, 5044 (2003).
- ²⁶³W. Gy"orffy, T. Shiozaki, G. Knizia, and H.-J. Werner, [J. Chem. Phys.](#) **138**, 104104 (2013).
- ²⁶⁴F. Eckert, P. Pulay, and H. J. Werner, *J. Comput. Chem.* **18**, 1473 (1997).
- ²⁶⁵F. Eckert and H. J. Werner, *Theor. Chem. Acc.* **100**, 21 (1998).
- ²⁶⁶J. K. G. Watson, *Mol. Phys.* **15**, 479 (1968).
- ²⁶⁷G. Rauhut, *J. Chem. Phys.* **121**, 9313 (2004).
- ²⁶⁸B. Ziegler and G. Rauhut, *J. Chem. Phys.* **149**, 164110 (2018).
- ²⁶⁹D. Oschetzki, M. Neff, P. Meier, F. Pfeiffer, and G. Rauhut, *Croat. Chem. Acta* **85**, 379 (2012).

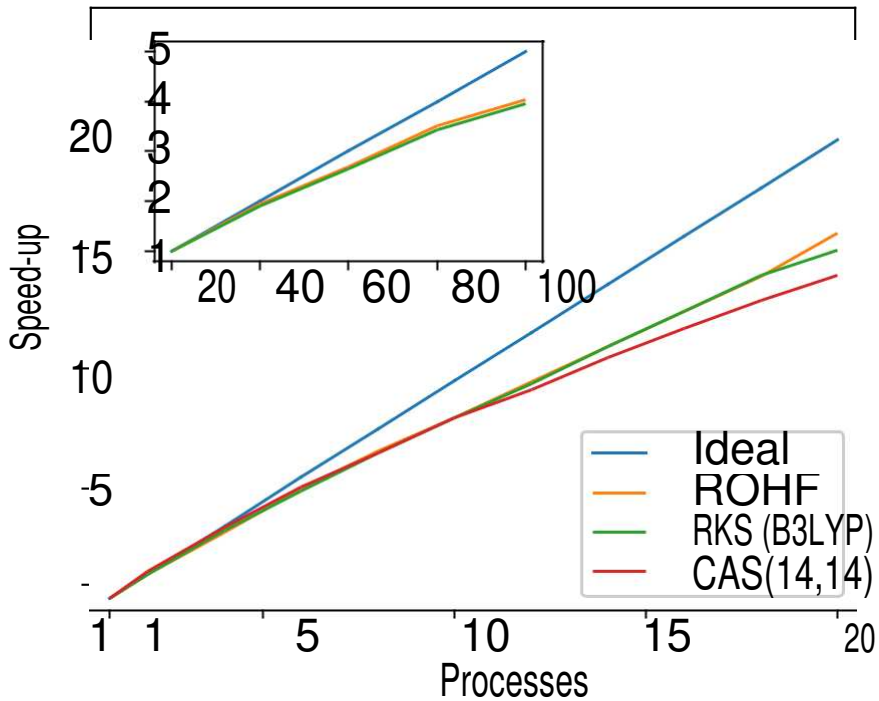
- ²⁷⁰J. M. Bowman, T. Carrington Jr., and H. D. Meyer, *Mol. Phys.* **106**, 2145 (2008).
- ²⁷¹B. Ziegler and G. Rauhut, *J. Chem. Theory Comput.* **15**, 4187 (2019).
- ²⁷²K. Pflüger, M. Paulus, S. Jagiella, T. Burkert, and G. Rauhut, *Theor. Chem. Acc.* **114**, 327 (2005).
- ²⁷³K. Yagi, S. Hirata, and K. Hirao, *Theor. Chem. Acc.* **118**, 681 (2007).
- ²⁷⁴M. Neff and G. Rauhut, *Spectrochim. Acta A* **119**, 100 (2014).
- ²⁷⁵G. Rauhut and B. Hartke, *J. Chem. Phys.* **131**, 014108 (2009).
- ²⁷⁶P. Meier, G. Bellchambers, J. Klepp, F. Manby, and G. Rauhut, *Phys. Chem. Chem. Phys.* **15**, 10233 (2013).
- ²⁷⁷B. Ziegler and G. Rauhut, *J. Chem. Phys.* **144**, 114114 (2016).
- ²⁷⁸J. Meisner, P. P. Hallmen, J. Kästner, and G. Rauhut, *J. Chem. Phys.* **150**, 084306 (2019).
- ²⁷⁹S. Heislbetz and G. Rauhut, *J. Chem. Phys.* **132**, 124102 (2010).
- ²⁸⁰S. Heislbetz, F. Pfeiffer, and G. Rauhut, *J. Chem. Phys.* **134**, 204108 (2011).
- ²⁸¹F. Pfeiffer and G. Rauhut, *J. Phys. Chem. A* **115**, 11050 (2011).
- ²⁸²M. Neff, T. Hrenar, D. Oschetzki, and G. Rauhut, *J. Chem. Phys.* **134**, 064105 (2011).
- ²⁸³M. Neff and G. Rauhut, *J. Chem. Phys.* **131**, 124129 (2009).
- ²⁸⁴Pfeiffer and G. Rauhut, *J. Chem. Phys.* **140**, 064110 (2014).
- ²⁸⁵P. Meier, D. Oschetzki, F. Pfeiffer, and G. Rauhut, *J. Chem. Phys.* **143**, 244111 (2015).
- ²⁸⁶D. Oschetzki and G. Rauhut, *Phys. Chem. Chem. Phys.* **16**, 16426 (2014).
- ²⁸⁷T. Petrenko and G. Rauhut, *J. Chem. Phys.* **146**, 124101 (2017).
- ²⁸⁸X. Zhao, X. Chu, G. Rauhut, C. Chen, C. Song, B. Lu, and X. Zeng, *Angew. Chem. Int. Ed.* **58**, 12164 (2019).
- ²⁸⁹B. Ziegler and G. Rauhut, *Mol. Phys.* **117**, 1741 (2019).
- ²⁹⁰R. Ramakrishnan and G. Rauhut, *J. Chem. Phys.* **142**, 154118 (2015).
- ²⁹¹P. Meier and G. Rauhut, *Mol. Phys.* **13**, 3859 (2015).
- ²⁹²P. Meier, D. Oschetzki, R. Berger, and G. Rauhut, *J. Chem. Phys.* **140**, 184111 (2014).
- ²⁹³G. Rauhut, *J. Phys. Chem. A* **119**, 10264 (2015).
- ²⁹⁴T. Petrenko and G. Rauhut, *J. Chem. Phys.* **143**, 234106 (2015).
- ²⁹⁵T. Petrenko and G. Rauhut, *J. Chem. Theory Comput.* **13**, 5515 (2017).
- ²⁹⁶A. Mitrushchenkov and H.-J. Werner, *Molecular Physics* **105**, 1239 (2007), <https://doi.org/10.1080/00268970701326978>.

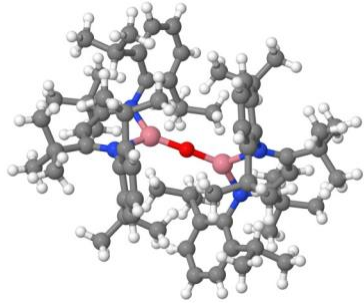
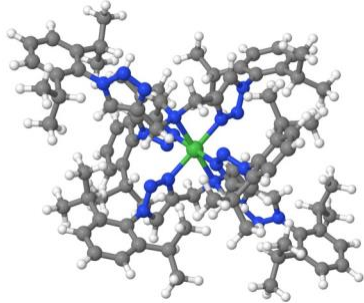
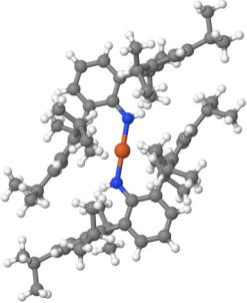
- ²⁹⁷A. J. Stone, *Chem. Phys. Lett.* **83**, 233 (1981).
- ²⁹⁸J. E. M. N. Klein, G. Knizia, B. Miehlich, J. K̄astner, and B. Plietker, *Chemistry-A European Journal* **20**, 7254 (2014).
- ²⁹⁹G. Knizia and J. E. M. N. Klein, *Angewandte Chemie-International Edition* **54**, 5518 (2015).
- ³⁰⁰L. N. dos Santos Comprido, J. E. M. N. Klein, G. Knizia, J. K̄astner, and A. S. Hashmi, *Angew. Chem. Int. Ed.* **54**, 10336 (2015).
- ³⁰¹J. E. M. N. Klein, G. Knizia, L. Nunes Dos Santos Comprido, J. K̄astner, and A. S. K. Hashmi, *Chemistry-A European Journal* **23**, 16097 (2017).
- ³⁰²J. S. Steen, G. Knizia, and J. E. M. N. Klein, *Angewandte Chemie* **131**, 13267 (2019).
- ³⁰³E. D. Glendening, C. R. Landis, and F. Weinhold, *J. Comput. Chem.* **34**, 1429 (2013).
- ³⁰⁴S. F. Boys and F. Bernardi, *Mol. Phys.* **19**, 553 (1970).
- ³⁰⁵S. M. Cybulski, G. Chalasinski, and R. Moszynski, *J. Chem. Phys.* **92**, 4357 (1990).
- ³⁰⁶S. M. Cybulski and M. L. Lytle, *J. Chem. Phys.* **127**, 141102 (2007).
- ³⁰⁷A. Heßelmann, *J. Chem. Phys.* **128**, 144112 (2008).
- ³⁰⁸M. Pitonak and A. Heßelmann, *J. Chem. Theory Comput.* **6**, 168 (2010).
- ³⁰⁹L. A. Burns, M. S. Marshall, and C. D. Sherrill, *J. Chem. Phys.* **141**, 234111 (2014).
- ³¹⁰B. Jeziorski, R. Moszynski, and K. Szalewicz, *Chem. Rev.* **94**, 1887 (1994).
- ³¹¹K. Szalewicz, K. Patkowski, and B. Jeziorski, *Structure and Bonding* **116**, 43 (2005).
- ³¹²K. Szalewicz, *WIREs Comput. Mol. Sci.* **2**, 254 (2012).
- ³¹³K. Patkowski, B. Jeziorski, T. Korona, and K. Szalewicz, *J. Chem. Phys.* **117**, 5124 (2002).
- ³¹⁴M. Jeziorska, B. Jeziorski, and J. Cizek, *Int. J. Quant. Chem.* **32**, 149 (1987).
- ³¹⁵A. Heßelmann and G. Jansen, *Chem. Phys. Lett.* **357**, 464 (2002).
- ³¹⁶A. Heßelmann and G. Jansen, *Chem. Phys. Lett.* **362**, 325 (2002).
- ³¹⁷A. Heßelmann and G. Jansen, *Chem. Phys. Lett.* **367**, 778 (2003).
- ³¹⁸A. Heßelmann and G. Jansen, *Phys. Chem. Chem. Phys.* **5**, 5010 (2003).
- ³¹⁹A. Misquitta and K. Szalewicz, *Chem. Phys. Lett.* **357**, 301 (2002).
- ³²⁰A. Misquitta, B. Jeziorski, and K. Szalewicz, *Phys. Rev. Lett.* **91**, 033201 (2003).
- ³²¹A. J. Misquitta, R. Podeszwa, B. Jeziorski, and K. Szalewicz, *J. Chem. Phys.* **123**, 214103 (2005).
- ³²²G. Jansen, *WIREs Comput. Mol. Sci.* **4**, 127 (2013).

- ³²³R. Podeszwa, R. Bukowski, and K. Szalewicz, *J. Phys. Chem. A* **110**, 10345 (2006).
- ³²⁴A. Heßelmann, “Springer series in topics in current chemistry (density functionals: thermochemistry,” (Springer, Heidelberg, 2014) Chap. The ring and exchange-ring approximations based on Kohn–Sham reference states.
- ³²⁵R. Podeszwa, *J. Chem. Phys.* **132**, 044704 (2010).
- ³²⁶R. Schäffer and G. Jansen, *Theo. Chem. Acc.* **131**, 1235 (2012).
- ³²⁷R. Schäffer and G. Jansen, *Mol. Phys.* **111**, 2570 (2013).
- ³²⁸A. J. Misquitta, *J. Chem. Theory Comput.* **9**, 5313 (2013).
- ³²⁹R.-F. Liu, C. A. Franzese, R. Malek, P. S. Zuchowski, J. G. Angyan, M. M. Szczesniak, and G. Chalasiński, *J. Chem. Theory Comput.* **7**, 2399 (2011).
- ³³⁰T. Clark and A. Heßelmann, *Phys. Chem. Chem. Phys.* **20**, 22849 (2018).
- ³³¹A. Görling, *Int. J. Quantum Chem.* **69**, 265 (1998).
- ³³²A. Heßelmann, *J. Chem. Theory Comput.* **14**, 1943 (2018).
- ³³³S. Grimme, *Chem. Eur. J.* **18**, 9955 (2012).
- ³³⁴T. Risthaus and S. Grimme, *J. Chem. Theory Comput.* **9**, 1580 (2013).
- ³³⁵T. Korona, A. Heßelmann, and H. Dodziuk, *J. Chem. Theory Comput.* **5**, 1585 (2009).
- ³³⁶H. Dodziuk, K. Ruud, T. Korona, and T. B. Demissie, *Phys. Chem. Chem. Phys.* **18**, 26057 (2016).
- ³³⁷T. Korona and B. Jeziorski, *Journal of Chemical Physics* **125**, 184109 (2006).
- ³³⁸T. Korona, *Physical Chemistry Chemical Physics* **10**, 6509 (2008).
- ³³⁹T. Korona, *Physical Chemistry Chemical Physics* **10**, 5698 (2008).
- ³⁴⁰T. Korona and B. Jeziorski, *Journal of Chemical Physics* **128**, 144107 (2008).
- ³⁴¹T. Korona, *Journal of Chemical Theory and Computation* **5**, 2663 (2009).
- ³⁴²T. Korona, *Molecular Physics* **111**, 3705 (2013).
- ³⁴³T. H. Dunning Jr, *The Journal of Chemical Physics* **90**, 1007 (1989).
- ³⁴⁴R. Feng and K. A. Peterson, *Journal of Chemical Physics* **147**, 084108 (2017).
- ³⁴⁵J. G. Hill and K. A. Peterson, *Journal of Chemical Physics* **147**, 244106 (2017).
- ³⁴⁶K. A. Peterson, T. B. Adler, and H.-J. Werner, *Journal of Chemical Physics* **128**, 084102 (2008).
- ³⁴⁷J. G. Hill, S. Mazumder, and K. A. Peterson, *Journal of Chemical Physics* **132**, 054108 (2010).
- ³⁴⁸J. G. Hill and K. A. Peterson, *Physical Chemistry Chemical Physics* **12**, 10460 (2010).

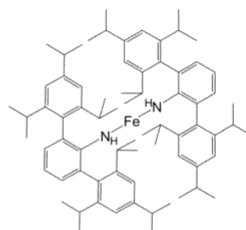
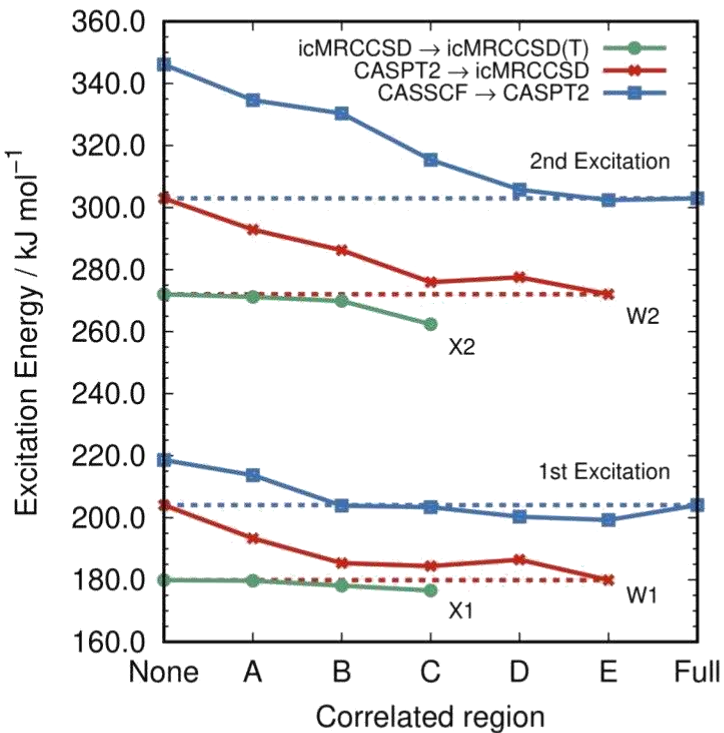
- ³⁴⁹J. G. Hill and K. A. Peterson, *The Journal of Chemical Physics* **141**, 094106 (2014).
- ³⁵⁰K. A. Peterson, M. K. Kesharwani, and J. M. L. Martin, *Molecular Physics* **113**, 1551 (2015).
- ³⁵¹F. Weigend and R. Ahlrichs, *Physical Chemistry Chemical Physics* **7**, 3297 (2005).
- ³⁵²R. Gulde, P. Pollak, and F. Weigend, *Journal Of Chemical Theory And Computation* **8**, 4062 (2013).
- ³⁵³P. O. Widmark, P. A. Malmqvist, and B. O. Roos, *Theoretica Chimica Acta* **77**, 291 (1990).
- ³⁵⁴B. O. Roos, R. Lindh, P.-A. Malmqvist, V. Veryazov, P.-O. Widmark, and A. C. Borin, *The Journal of Physical Chemistry A* **112**, 11431 (2008).
- ³⁵⁵F. Weigend, *Journal Of Computational Chemistry* **29**, 167 (2008).
- ³⁵⁶F. Weigend, M. Häser, H. Patzelt, and R. Ahlrichs, *Chemical Physics Letters* **294**, 143 (1998).
- ³⁵⁷C. Hättig, *Physical Chemistry Chemical Physics* **7**, 59 (2005).
- ³⁵⁸S. Kritikou and J. G. Hill, *Journal Of Chemical Theory And Computation* **11**, 5269 (2015).
- ³⁵⁹K. E. Yousaf and K. A. Peterson, *Journal of Chemical Physics* **129**, 184108 (2008).
- ³⁶⁰K. E. Yousaf and K. A. Peterson, *Chemical Physics Letters* **476**, 303 (2009).
- ³⁶¹R. A. Shaw and J. G. Hill, *Journal Of Chemical Theory And Computation* **13**, 1691 (2017).
- ³⁶²["http://www.pqs-chem.com/software.php,"](http://www.pqs-chem.com/software.php) (2019), accessed 2019-12-20.
- ³⁶³J. Baker, K. Wolinski, M. Malagoli, D. Kinghorn, P. Wolinski, G. Magyarfalvi, S. Saebo, T. Janowski, and P. Pulay, *Journal of Computational Chemistry* **30**, 317–335 (2009), <https://onlinelibrary.wiley.com/doi/pdf/10.1002/jcc.21052>.
- ³⁶⁴J. Baker, T. Janowski, K. Wolinski, and P. Pulay, *WIREs Computational Molecular Science* **2**, 63–72 (2012), <https://onlinelibrary.wiley.com/doi/pdf/10.1002/wcms.80>.
- ³⁶⁵["https://gitlab.com/molpro/sjef,"](https://gitlab.com/molpro/sjef) (2020), accessed 2020-01-10.
- ³⁶⁶["http://www.molpro.net/schema/molpro-output,"](http://www.molpro.net/schema/molpro-output) (2019), accessed 2019-12-20.
- ³⁶⁷M. Sibae, "Python simple job execution framework," <https://molpro.gitlab.io/pysjef/> (2020) .

- ³⁶⁸M. Sibaev, “pysjef extension for molpro,” https://gitlab.com/molpro/pysjef_molpro (2020).
- ³⁶⁹T. Kluyver, B. Ragan-Kelley, F. Pérez, B. Granger, M. Bussonnier, J. Frederic, K. Kelley, J. Hamrick, J. Grout, S. Corlay, P. Ivanov, D. Avila, S. Abdalla, and C. Willing, in [Positioning and Power in Academic Publishing: Players, Agents and Agendas](#), edited by F. Loizides and B. Schmidt (IOS Press, 2016) pp. 87 – 90.
- 370 P. J. Knowles and N. C. Handy, *Comput. Phys. Commun.* **54**, 75 (1989).
- ³⁷¹<https://gitlab.com/molpro/fcidump>, (2019), accessed 2019-12-20.
- 372 <https://gitlab.com/molpro/molpro-plugin>, (2019), accessed 2019-12-20.
- ³⁷³G. H. Booth, S. D. Smart, and A. Alavi, *Mol. Phys.* **112**, 1855 (2014), [arXiv:1305.6981](#).

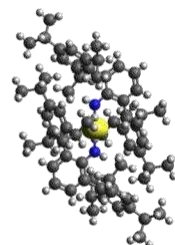




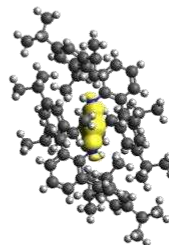
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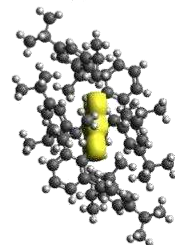
Schematic



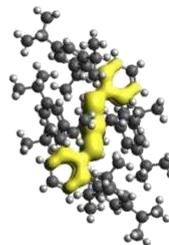
Region A



Region B



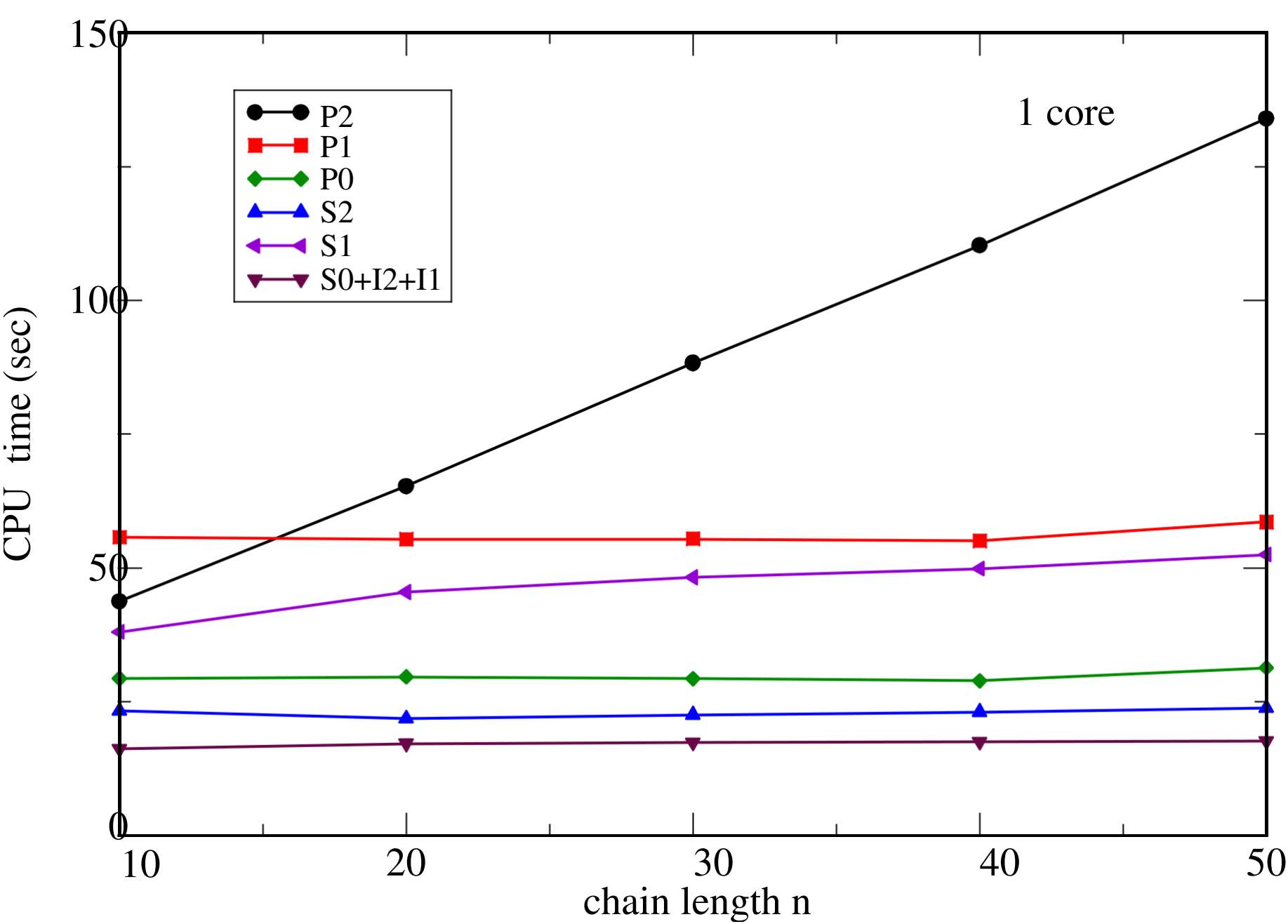
Region C

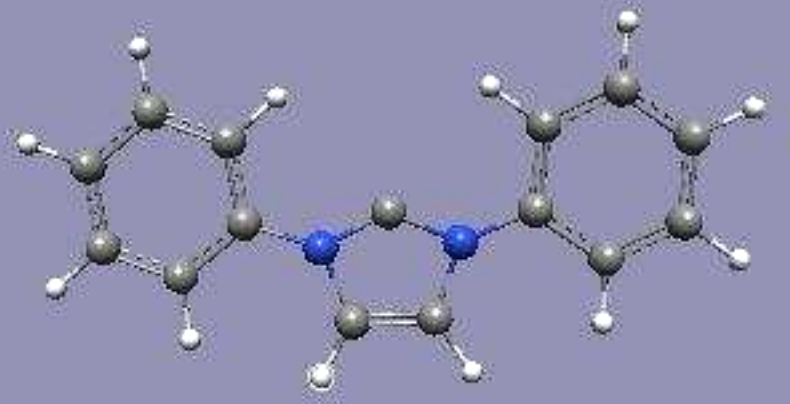
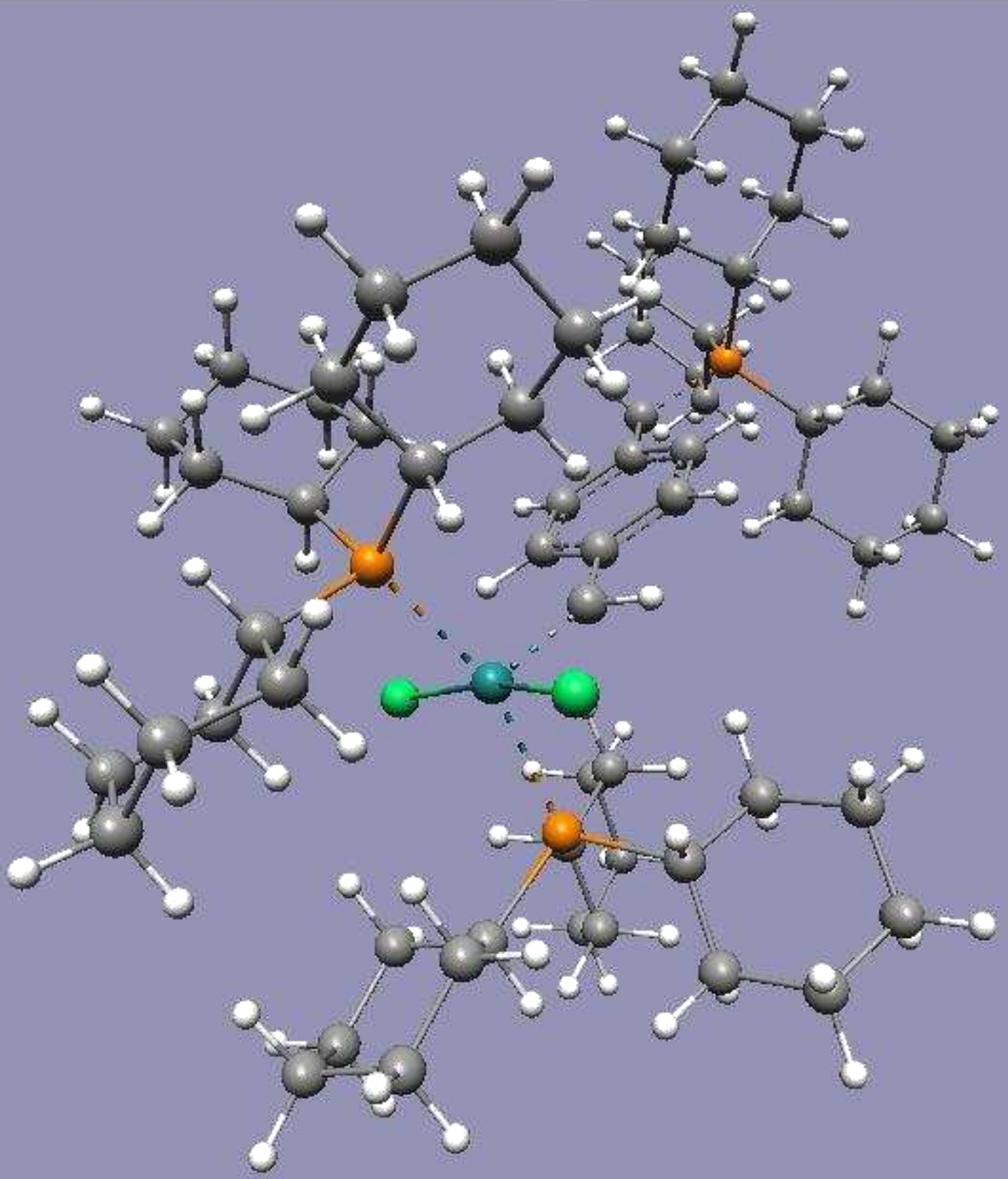


Region D



Region E



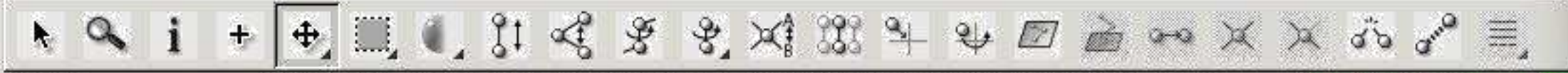


Building Blocks Fragments Clipboard

- 12-crown
- 18-crown-novalence
- 18-crown-octahedral
- 2,2-bipyridine
- imidazole-carbene**
- phenanthroline

- AMINO ACIDS
- BICYCLIC
- CHAINS
- FUNCTIONAL GROUPS
- HETEROCYCLIC
- LIGANDS
- MONOCYCLIC
- NANOTUBES
- NUCLEOTIDES
- POLYCYCLIC
- SOLVENTS
- SUGARS
- ORGANOMETALLICS

X: 6.357 Y: 8.653 Z: -2.866 Torsion: Auto Selection: Auto FF: Sybyl5.2



MOVE [LMB] over selection or atom + [DRAG] [CMB] drag vertically - move in/out [RMB] - Rotate RESTRICTED

Import Geometry

Builder Window

Orientation:

Mass

Wave Function Characteristics:

Charge: 1

Spin: Singlet

Wave Function Symmetry:

Automatic

Calculation:

Type

Hamiltonian

Core-Correlation

Single Point Energy

Pseudopot. if available

none

Method

DFT Functional:

PNO-RCCSD(T)-F12

B3LYP

Cosmo

Density Fitting

Basis Set:

Quality

Default Basis Set

TZ

cc-pVTZ-PP-F12

Element Specific Basis Sets

Options:

SCF

Correlation

Optg

Freq/Hess

Cosmo

Wave Function Analysis:

Population Analysis

Intrinsic bond analysis

Save Virtual Orbitals

Orbital Localization:

No localization

```
orient,mass;
```

```
nosym;
```

```
geomtyp=xyz;
```

```
geometry=wccr10-4.xyz
```

```
basis={
```

```
default=cc-pVTZ-PP-F12
```

```
ru=aug-cc-pVTZ-PP
```

```
}
```

```
wf,charge=1,spin=0;
```

```
{DF-RHF}
```

```
{PNO-RCCSD(T)-F12}
```

Specific Basis Sets

H cc-pVTZ-F12

C cc-pVTZ-F12

P cc-pVTZ-F12

Cl cc-pVTZ-F12

Ru aug-cc-pVTZ-PP

Close

Backend

Run parameters

Run

Kill

Completed, job number 83934 on backend cl

```
from pysjef import Project, DirectoryNode, all_completed
from pysjef_molpro import no_errors
import numpy
```

```
root = DirectoryNode('dihedral_scan')
```

```
grid = numpy.linspace(0, 90, 18, endpoint=False)
for i, D in enumerate(grid):
    p = root.add_child(f'd{i}', suffix='molpro')
    p.write_input(
        f"""geometry={{
            H1
            C1 H1 rch
            C2 C1 rcc H1 A
            H2 C2 rch C1 A H1 D
            H3 C2 rch C1 A H2 180
            H4 C1 rch C2 A H1 180}}
        rch = 2.05; rcc = 2.65; A = 121.5; D = {D}+.01;
        basis = cc-pVTZ
        rhf
        set, mcooc=[3,2,2,2], mcclosed=[3,1,1,2], mcsym=1
        casscf,so_sci
        {{optg; inactive, D}}
        set,mcsym=[1,4]
        casscf,so_sci
        {{mrci; wf, sym=1;}}
        {{mrci; wf, sym=4;}}""")
```

```
from multiprocessing.dummy import Pool
from operator import methodcaller
with Pool(processes=8) as pool:
    pool.map(methodcaller('run', backend='local', wait=True),
            root.children, 1)
print('all completed', all_completed(root.children))
print('without errors', no_errors(root.children))
```

```
all completed True
without errors True
```

```
import matplotlib.pyplot as plt
%matplotlib notebook
energies = root.select(
    '//jobstep[command=MRCI]/property[name=Energy].value')
e1, e2 = energies[::2], energies[1::2]
cc = root.select('//variable[name=rcc]/value..')
plt.plot(grid, e1, grid, e2)
plt.legend([r'$X\;{}^1A_1$', r'$V\;{}^1B_1$'])
plt.xlabel('HCCH dihedral angle (degrees)')
plt.ylabel(r'Energy $(E_h)$')
plt.show()
```

