Development and Testing of Vascular Networks for Self-healing Cementitious Materials

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ABSTRACT

The success of self-healing cementitious materials relies on their ability to repeatedly heal over the lifetime of the material. Vascular networks have a distinct advantage over other self-healing techniques whereby the healing agent in the network can be routinely replenished. The aim of this study was to develop a multi-use vascular network that can be re-used over the lifetime of a structure, to enable repeated self-healing events in cementitious materials. The feasibility and self-healing efficacy of novel 2D vascular networks in concrete beams were tested on laboratory-scale specimens before being trialled in-situ on larger, structural-scale elements. The vascular networks were formed via linear interconnecting hollow channels filled with a healing agent which is delivered to zones of damage under an externally supplied pressure. This technique was reproducible at large scale and channels were re-filled over a test period of 6 months. Of the two healing agents used in this study, sodium silicate (SS) proved easier to handle and supply into the vascular network, but cyanoacrylate (CA) offered greater strength recovery (up to 90%) in a relatively short timescale. The presence of flow networks in the cover concrete tended to act as a crack initiator and this was particularly
evident in the larger scale specimens. Nevertheless, the potential to enhance and enable multi-scale healing in cementitious materials has been demonstrated.

**INTRODUCTION**

Our society is very much dependent on the security and durability of our civil engineering infrastructure, much of which is constructed from concrete. Indeed, concrete remains one of the most widely used construction materials in the world today. However, concrete degradation and concrete cracking is still considered a major problem (Gardner et al. 2018), the causes of which result from thermal effects, early age shrinkage, mechanical loading, deleterious chemical reactions or a combination of these actions on structures (Concrete Society 2010). These issues affect the durability of concrete structures and lead to a service life far shorter than that desired. The concept of a material with a self-repairing or self-healing capability has been identified as a potential solution to this problem. A state-of-the-art paper produced by the Self-healing as prevention repair of concrete structures (SARCOS) COST Action group describes the breadth of this novel research area and explores the latest innovations in the field of self-healing cementitious materials (De Belie et al. 2018).

The techniques used in self-healing concrete can be broadly classified into three groups (De Belie et al. 2018; Van Tittelboom and De Belie 2013): Autogenous and non-encapsulated autonomous self-healing (which include autogenous healing, stimulated autogenous healing with the use of mineral additions, crystalline admixtures, superabsorbent polymers and non-SAP polymer additions), self-healing bio-concrete, and encapsulated autonomous self-healing. Encapsulation techniques include the use of polymer and mineral-based healing agents, which are delivered into the cracked areas in concrete through micro-encapsulation (diameter capsules < 1 mm), macro-encapsulation or vascular network technologies embedded in the concrete (Sidiq et al. 2019; Xue et al. 2019).

The vascular network technique adopts a biomimetic approach to healing cracks by delivering healing agents to the damage location, in a similar manner to the human cardiovascular or plant vascular tissue systems. The vascular network has several advantages over closed systems, such as being able to supply different healing agents, over various time scales and at different rates to the...
damage location (Blaiszik et al. 2010) in order to treat a variety of damage scenarios.

The first use of capillary networks in cementitious materials was reported by Dry (1994). Originally, these networks comprised discrete capillary capsules embedded within the cementitious matrix (Van Tittelboom et al. 2011; Van Tittelboom and De Belie 2013), which were subsequently replaced by continuous glass capillaries extending throughout the specimen with external supply reservoirs (Mihashi et al. 2001; Joseph et al. 2010). Glass capillaries have been embedded into frame structures (Dry and McMillan 1996) and also cast into bridge decks for full-scale trials (Dry 1999; Dry 2001). However, due to the challenges associated with the use of these systems for in-situ concrete structures, in particular the increased time required to place the capillary tubes prior to casting (Van Tittelboom et al. 2016) and the fragility of the capillary tubes during casting, these systems have been predominantly limited to laboratory testing and evaluation. Moreover, Van Tittelboom et al. (2016) note that the positive self-healing efficiencies achieved through the careful placement of the capillary tubes within a mould at small-scale, may be diminished at large-scale, if methods employed for the ready inclusion of capillary tubes in a mix results in their random orientation within the section.

To overcome some of these challenges the glass capillaries have been replaced with channels formed through a variety of other methods: One early approach was the embedment of ethylene vinyl acetate polymer pipes containing conductive helical wire and healing agent in the cementitious matrix (Nishiwaki et al. 2010). Selective heating at the location of a crack released healing agent directly into the damage location. The second approach was the formation of hollow channels via the removal of smooth small diameter steel rods after 24 hours of concrete curing (Dry 1999; Pareek and Oohira 2011) and the third was the use of porous concrete cylinders surrounded by a standard concrete mix (Sangadji and Schlangen 2012). Nevertheless, the formation of these novel flow networks is not without difficulty since they rely on the timely and successful removal of channel forming elements in the former and require a two-stage construction process in the latter. Moreover, these techniques are currently limited to a two-dimensional format. Varying degrees of success have been reported on the performance of flow networks, such as an enhanced load carrying
capacity from beams healed with a 2-part epoxy (Dry et al. 2003) and greater post peak ductility for beams healed with cyanoacrylate (Joseph et al. 2010).

Critical to the success of a vascular network is the correct selection of healing agent. The capillary flow of the healing agent is highly dependent on its flow properties, namely its viscosity, wettability and surface tension in a cementitious environment, whilst its healing ability will depend on its compatibility and reaction with the host matrix. The success or otherwise of a range of healing agents including sodium silicate (Formia et al. 2015; Kanellopoulos et al. 2015); polyurethane ((Gilabert et al. 2017; Belleghem et al. 2018); cyanoacrylates (Gardner et al. 2012; Gardner et al. 2014; Huang et al. 2014); and epoxies (Perez et al. 2015; Li et al. 2017) has been widely reported. The introduction of pressurised vascular networks, as trialled in self-healing polymer materials by Hamilton et al. (2011), greatly assists the extent of flow and infiltration of the healing agent into micro-cracked zones of damage and is worthy of further investigation in cementitious materials.

This paper describes a novel method for the formation of a two-dimensional vascular network for cementitious materials, including its deployment in slabs and structural scale elements. The design of the network facilitates repeated healing events over the lifetime of a cementitious structure. In addition, the first full account of the use of vascular networks in a site trial is reported herein. The paper is structured as follows:

- Section 2 provides an overview of a series of preliminary investigations concerning the manufacture of the vascular network, specifically the influence of channel diameter, joint/node design and network pressure.
- Section 3 presents the experimental details concerning the application of vascular networks in a range of structural elements, namely small beams, large beams, a slab and a wall panel. It also presents the selection and justification of the healing agent used in the study.
- Section 4 presents the experimental results and reports the healing efficiencies of structural elements with various network configurations.

**PRELIMINARY INVESTIGATIONS**
A series of preliminary investigations was conducted to establish a successful and repeatable method of forming vascular networks in cementitious materials. The criteria for their formation was: (i) to cause no damage to the cementitious matrix; (ii) to be capable of practical application to both laboratory and in-situ structural sized specimens and (iii) to allow the flow of liquid throughout the entire network in one and two dimensions. The most practical approach is to form a network during the concrete casting process, since this eliminates the potential for damage to the concrete in its hardened state. The novel method proposed in this paper employs the embedment of plastic tubing, which is extracted from hardened concrete to leave permanent one-dimensional and two-dimensional interconnecting channels. Both polyolefin (TE Connectivity CGPT clear heat shrink tubing) and polyurethane (SMC TU series) tubing proved successful candidates for this. In both instances, the tubes were placed through holes in the concrete specimen mould walls and held in place with small clamps on the outside of the moulds, as shown in Fig. 1a.

The polyolefin tubing had an outer diameter of 3.2 mm and a shrinkage ratio of 2:1 at 80 °C. This tubing was flexible and compressible and to prevent compression during placement of concrete the network required pressurisation with water. After casting, curing and de-moulding of the prism specimen, the polyolefin tubes were flushed with water at a temperature of 85 °C, which triggered tube shrinkage and thereby allowed them to be easily removed from the specimen.

The polyurethane tubing had an outer diameter of 4 mm and was selected for its smooth outer surface properties, relatively high stiffness and high tensile strength. The polyurethane tubes were robust enough to withstand the casting process without the need for pressurisation. After casting, curing and de-moulding, the polyurethane tubes were pulled out of the specimen. The radial contraction of the tube, when under tension, breaks the bond between the tube surface and the concrete, thus permitting the tubes to be removed with relative ease.

Neither tubing material required the application of a special coating. Preliminary experiments showed that the tubing placed as loops in small prismatic concrete beams could also be easily removed, therefore only requiring one accessible surface during casting. This would be advantageous.
for casting concrete foundations or other structural elements with limited accessible surfaces after casting. In subsequent studies with larger specimens, special coatings were applied to the tubes to guarantee their removal.

A plan 2-D network was created by taking advantage of the voids left by removal of the tubes and by the contact points between overlapping tubes, as illustrated by the schematic in Fig. 1b. The area of the contact points is maximised by using a weaving tube pattern shown in Fig. 1c. The voids left by the contact points are shown to be sufficiently large to allow the healing agent to flow. However, they depend on the tubes being tightly tensioned against each other and increase the complexity associated with the placement of the tubes in the mould. To overcome these challenges, a bespoke connection was designed and manufactured from Polylactic Acid (PLA) using a 3D printer (Ultimaker 2, Fused filament fabrication). This connection created a dedicated flow channel between the perpendicular voids, as shown in Fig. 1d, and had the added advantage of securing the tubing in position during the casting stage as evidenced in Fig. 1e. Fig. 1f shows the bespoke 2D PLA connection used for the larger panels, in which the angles between the tubes are set at 26.6°. The void shown is used to tie the connection to the reinforcement and when the tubing is removed from the concrete after casting, the PLA connections remain in situ.

Healing Agent Selection

It is widely regarded that the choice of healing agent is primarily governed by the self-healing application, with particular importance placed on the temporal and spatial nature of the damage/healing event (Maes et al. 2014; Van Tittelboom and De Belie 2013; Mostavi Ehsan et al. 2015). In this study, cyanoacrylate (CA) and sodium silicate (SS) were selected for use in the vascular networks.

CA has been used in many self-healing applications (Li et al. 1998; Dry 2000; Joseph et al. 2010), and is employed here due to its low viscosity, rapid curing time and strong potential to achieve repeated healing events within a short timescale. The ethyl-2-cyanoacrylate resin polymerises rapidly in small crack widths (<0.5 mm) in the presence of hydroxide ions, which are available from moisture within the crack plane, or calcium hydroxide present in the cement matrix. CA

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has been shown to offer advanced healing from its ability to infiltrate not only the macro-cracks but also the micro-cracked area of the fracture process zone (Joseph et al. 2010). Nevertheless, the use of CA also attracts a significant number of challenges namely: difficulty in handling due to its rapid bonding ability and high toxicity, its relatively short shelf-life (approx. 6 months) and uncertainty regarding its long-term compatibility with the cementitious matrix. Some of the difficulties encountered with the use of CA in these experiments are described in Section 4.

Sodium silicate was chosen for its ability to react chemically with the cementitious matrix and its documented success as an encapsulated healing agent in previous studies (Huang and Ye 2011; Pelletier et al. 2011; Gilford III et al. 2013; Kanellopoulos et al. 2015). Its slower reaction rate and higher viscosity makes it more suitable for site application than the rapidly curing CA. In the presence of water, SS reacts with excess calcium hydroxide, a by-product of clinker hydration, available in the cement matrix to form additional calcium-silicate-hydrate (CSH) gel. The chemical reaction is shown in Eq. 1. It is this additional CSH gel which forms and fills in the crack and leads to the recovery in mechanical and durability-based material properties.

\[ Na_2O \cdot SiO_2 + Ca(OH)_2 \rightarrow CaO \cdot SiO_2 \cdot H_2O + Na_2O \]  

Parametric study on capillary rise and surface coverage of healing agent

Healing agents may be delivered by capillary flow alone, but it has been found that the supply of agents may be improved by pressurising the healing agent fluid (Hamilton et al. 2011). Even a small additional pressure of 0.01 bar allows the healing agent to flow more effectively along the supply channels and into the macro-cracks using the capillary rise mechanism (Gardner et al. 2012; Gardner et al. 2014). The degree of saturation of the crack faces has also been reported to influence the rate and degree of capillary rise of a healing agent (Gardner et al. 2012), whilst the crack width is one of the primary governing factors affecting the final healing agent capillary rise height.

In order to examine the above parameters, a series of tests were performed on 75 mm x 75 mm x 255 mm concrete beams cast with two 4 mm flow channels, formed using the polyurethane tubing detailed in Section 2. The details of the test series are summarised in Table 1. All of the
beams were cured in water (apart from beams in series 3). The beams were tested in a 3-point bending arrangement, as shown in Fig. 2, using a controlled crack mouth opening displacement (CMOD) rate of 0.0001 m/s. The healing agent employed was a SS solution of molar ratio 1:1.5 (water : sodium silicate). The SS solution was supplied from an open reservoir on one side, the height of which was adjustable, whilst the other side was left open to atmospheric pressure. Once the CMOD had reached the desired value, SS was released into each of the network channels from the required pressure head. The beams were then unloaded and left in-situ for between 60 and 300 seconds, after which time the healing agent was flushed out of the channels using pressurised air and the beams broken in half with a hammer. The extent of the spread of the SS on the crack face was then recorded.

The effect of a change in healing agent exposure time (as per series 2) can be seen in Fig. 3. The black marker outline shows the extent of the healing agent spread on the crack face, which is termed the crack coverage. This healing agent crack coverage is expressed as a percentage of the crack plane cross-section.

Fig. 4 shows the effect of the various parameters on the healing agent crack coverage. In particular, Fig. 4a shows how increasing the pressure of the healing agent increases its coverage on the crack face (Series 1). Fig. 4b and Fig. 4c consider the effect of the curing regime and age of the specimen on crack coverage respectively. The drier beams (i.e. those cured under ambient room conditions) have lower crack coverages, which may result from a concrete matrix with higher porosity and hence greater absorption of the healing agent into the crack faces, effectively reducing the capillary driving force. The older specimens also show a lower healing agent coverage than the younger specimen. The authors have previously demonstrated that the capillary rise response in older specimens is slower than that in younger specimens (Gardner et al. 2012), and this is thought to be related to the effect of the time dependent development of the mortar microstructure on the dynamic resistive forces acting during capillary flow. The results from the present study suggest that the crack coverage associated with older specimens has yet to reach its optimum level given the chosen exposure times. As shown in Fig. 4d, the crack coverage reduces as the cover to the
flow channels increases. This reduction may be due to a smaller crack area above the flow channel, since the residual crack opening at the height of the network is smaller.

This short parametric study has shown that there are a number of factors that can affect the initial delivery of the healing agent to the crack surface. A relatively small pressure of 0.001 N/mm$^2$ can provide 80% coverage at a 0.2 mm crack width. The cover to the flow network ranges between 20 mm and 44 mm from the underside of the beam, which is consistent with placing the flow networks in a typical concrete cover zone. The curing regime and age of specimen do have an impact on the extent of coverage of the healing agent on the crack surface but are not considered critical to the performance of the system.

**MAIN EXPERIMENTAL PROGRAMME**

Programme of Study and Experimental Procedure

The main experimental programme of study presented in this paper comprises 6 sets of experiments, summarised in Table 2 and the different forms are showing in Fig. 5. Sets 1 to 3 demonstrate the performance of vascular networks in a range of prismatic beam specimens, whilst sets 4, 5 and 6 explore the application of the flow network in different structural elements (a 0.6 m x 0.6 m slab, a 1 m x 1 m wall panel and 1.8 m x 1 m site trial panel). The purpose of the second group of tests (sets 4 to 6) is to prove the scalability of the technique for industrial applications.

The experimental programme also included a set of self-healing site trials on the A465 Heads of the Valleys (HoV), Section 2, highway project near Abergavenny in South Wales. These site trials considered a number of healing systems, including the vascular networks being considered in the present paper. All of the moulds/shutters for the concrete specimens were made from timber. These wooden moulds were prepared by drilling 5 mm diameter holes in the desired position and then threading through the 4 mm (external) diameter polyurethane tubes (see Fig. 1a, 1c, 1e). These tubes were straightened by hand tensioning and fixed in position with small clamps on the outside of the mould. Sets 4 to 6 employed the connectors described in Section 2. The channels typically had 20 mm concrete cover. Release oil (and petroleum jelly for Sets 5 and 6) were applied to the tubes before casting the concrete to guarantee their easy removal from the specimens. A standard
concrete mix (see Table 3) was used for all lab specimens, with a slight amendment made to the mix for the site trial. The standard C40/50 concrete was designed to achieve consistency class S3 (BS EN 12350-2 2019) with an average compressive strength of 53 MPa.

All concrete samples were demoulded after 24 hours and the polyurethane tubes removed immediately after demoulding leaving behind hollow channels and the bespoke 3D printed connectors. The chosen concrete curing regime was dependent on the selected self-healing agent. CA polymerises rapidly with water and as such, the specimens were cured at ambient conditions and dried thoroughly before the healing agent was introduced into the flow network. For SS, the specimens were cured in water at 20 °C and surface dried before testing.

**Testing Procedure Sets 1-3**

The three-point flexural bending test set-up, shown in Fig. 6, was used for Sets 1 to 3. In these specimens, the healing agent was supplied to the channels using polyurethane supply tubes of external diameter 6 mm and internal diameter 4 mm (See Fig. 6). The supply channel was glued in place using CA. This provided a vascular network of constant diameter from the supply tube throughout the specimen. The healing agent was introduced into the vascular network using a syringe. For Sets 1 to 4 the healing agent was supplied into the vascular network before testing began, whilst in the other sets it was introduced at a later stage. The system was pressurised with air via this supply tube, see Fig. 7a. The pressure in the flow network was controlled and monitored using a regulator and inline digital gauges respectively, as can be seen in Fig. 7b. The pressurised system was closed, in order to maintain a constant pressure in the network before load was applied to the specimen. The pressurised system was also used to flush out the remaining healing agent from the main channels by leaving one outlet open to the atmosphere. This flushing allows repeated healing to take place with a re-supply of healing agent. The loading was controlled via a crack mouth opening displacement (CMOD) feedback loop at a rate of 0.0001 mm/s using an Avery Denison 7152 hydraulic loading machine. For Set 1, the beams were loaded until a CMOD of 0.3 mm was recorded, at which point the beams were unloaded and the healing agents (CA and SS) were flushed out of the networks using pressurised air. The beams with CA were reloaded after
For Sets 2 and 3, the specimens were loaded until a CMOD of 0.5 mm was recorded. At this point the networks in the Set 2 beams were flushed out and the beams left in-situ for 24 hours to allow further curing of the CA before being retested. Similarly the networks in the Set 3 beams were also flushed out, but the beams were then placed in a water tank for 28 days to promote the reaction of SS, after which time the beams were reloaded.

**Testing Procedure Set 4**

Fig. 8 shows two configurations of flow networks in a 600 mm square slab mould before casting. In the first configuration (Fig. 8a, specimen 1) the channels were placed at an angle of 45° to the line of the supports (and to the steel reinforcement) whilst in the second configuration (Fig. 8b, specimen 2) the channels were placed perpendicular to the supports. In both cases, the channels were located below the reinforcement and had a cover of 20 mm to the base of the slab. One control slab was also cast which included reinforcement only. Eight 8 mm diameter bars were used in each slab, four in each direction at equal spacing.

A loading frame, fabricated from 50 mm square hollow steel sections, provided simple supports on all 4 sides of the slab. The central patch load was applied at a controlled displacement rate of 0.005 mm/s through a 100 mm square 25 mm thick steel plate and 8 mm thick fibreboard. The displacement was monitored at the centre on the underside of the slab and at the mid-span of one support. The loading setup can be seen in Fig. 8c. The slab was supplied with healing agent and then loaded to 100 kN, unloaded and cured under moist hessian sacks for 28 days before re-loading for a second time.

The set-up used to supply healing agent to the specimens was the same as that employed for sets 1 to 3 (Section 3.2). Initially, all supply channels were clamped at their ends. One by one, each supply channel was opened to the atmosphere and the healing agent introduced via a syringe, ensuring that the whole network was filled in a controlled manner. In lieu of a closed pressure system, the network was filled to give 50 mm of head (0.005 bar) above the network level (Fig. 8c).
Testing Procedure Set 5

The configuration of the flow channels for the 1 m x 1 m x 0.15 m demonstration panel in the laboratory is shown in Fig. 9a. This reinforcement arrangement was chosen to replicate the starter bar reinforcement in the trial wall panels (which are discussed in Section 3). Five 10 mm diameter 500 mm long reinforcement bars at 200 mm spacing were fixed vertically in the bottom of the mould, in addition, an A252 mesh (i.e. 8 mm bars @ 200 mm c/c) was placed adjacent to the front and rear faces of the wall over the entire area. A cover of 30 mm was provided to the outermost reinforcement. The flow network was formed by ten sets of 4 mm diameter polyurethane tubes which were placed within the wall panels at an angle of 26.6° to the horizontal, with a vertical spacing of 100 mm and a cover of 20 mm. Ten injection points, as shown in Fig. 9b, were fitted each side of the panel on the vascular network outlets. The 100 mm long packers, of 10 mm external and 2.7 mm internal diameter, were fitted with a locking tap which allowed each channel to be independently opened and closed as required.

The demonstration panel was loaded in the laboratory to induce cracking in the panel. During loading, the wall panel was supported along on two parallel edges (i.e. the top and bottom edges in Fig. 9a) and a horizontal crack was induced via the application of load through a partial width spreader beam at a distance of 500 mm from the base of the wall panel (Fig. 9c). The panel was loaded to 100 kN, at which point a crack was visible on the surface, although the crack opening was not measured during testing. Once the panel had been loaded and a crack became visible, the panel was unloaded and returned to the upright position. Water was pumped into the flow network through the lowest injection valve at the base of the wall, using a pedal controlled reciprocating pump (DESOI PED-3D). Once the water was seen to flow out of a valve, the valve was closed, forcing the network to fill vertically upwards and expel air through the open valves towards the top of the wall. Once the water reached the topmost valve, the valve was closed. The channels in the flow network had the ability to be emptied and refilled, which supports the potential for repeated damage and healing events.
The full site trial programme (See Davies et al. 2018) examined the performance of a range of self-healing systems and included five separate wall panels. The present paper considers the behaviour of one of these panels that contained a vascular network, which was denoted Panel E. The arrangement of Panel E (1.8 m x 1.0 m x 0.15 m) is shown in Fig. 10a, in which the five pairs of evenly spaced 16 mm starter bars (which projected 500 mm from the base of the wall), A393 (10 mm bars @ 200 mm c/c) front and A142 (6 mm bars @200 mm c/c) rear steel reinforcing mesh and timber shutters can be seen. The tubes that formed the flow network were placed in an identical manner to that of Set 5 (i.e. the tubes were at angle of 26.6° to the horizontal and spaced at 100 mm), as illustrated in Fig. 10a. These tubes were placed with a cover of 20 mm. The bespoke 3D-printed PLA connections, shown in Fig. 1f, were used at every intersection of the flow network and tied to the steel reinforcement. After casting, the 4 mm diameter polyurethane tubes were removed by hand with relative ease.

The 1800 mm tall panel was loaded 300 mm below its upper edge, which meant the panel acted as a vertical cantilever that as illustrated in Fig. 10c. The load was applied through a 100 mm square 10 mm thick section steel wailing spreader beam using a hollow jack ram system that was anchored to the rear of the reaction wall. When the load reached a certain level (20 kN) a horizontal crack became visible on front surface of the panel, approximately 500 mm above the base of the wall, denoted on figures as crack on section (CoS). As with the laboratory trial panel (Section 3) injection point valves were fitted to each location where the network exited the wall panel. The final as-built wall panel is shown in Fig. 10c, in which the painted speckle pattern for the digital image correlation monitoring system can be seen on the surface of the concrete.

RESULTS AND DISCUSSION

The results of each test set are discussed in this section. The degree of mechanical healing is expressed in terms of two parameters: (i) a strength recovery index ($H_P$), calculated according to Eq. 2 (Homma et al. 2009; Davies and Jefferson 2017) and (ii) a stiffness recovery index ($H_K$) shown in Eq. 3, both recovery indexes are illustrated in Fig. 11:
in which $P_1$ represents the initial peak load (kN); $P_0$ the load at unloading at a predetermined CMOD (kN); and $P_2$ the peak load upon reloading (kN). Similarly, for the stiffness recovery index $H_K$:

$$H_K = \frac{K_2 - K_0}{K_1 - K_0} \cdot 100.$$  \hspace{1cm} (3)$$

$K_1$ represents the initial stiffness of the beam (N/mm$^2$); $K_0$ the stiffness during unloading (N/mm$^2$); and $K_2$ the stiffness upon reloading (N/mm$^2$). The terms in Eq. 2 and 3 are clearly defined when cracking and healing are separated in time, as in Fig. 11, but the indices are less distinct when these processes overlap. In the latter case, it is necessary to use the results of the control specimen to compute the unhealed response values that appear in the indices. However, due to the natural variation of response in these materials the response of the control specimen of a test series may deviate from the response that the healed specimen would have undergone without healing. The indices for such cases are therefore given with a degree of caution and this degree of uncertainty is marked by adding a $^*$ superscript to the indices (i.e. $H_{P}^*$ and $H_{K}^*$).

**Sets 1 to 3 - Twin 1D Channel Beam Specimens**

A typical load versus CMOD response for one CA, one SS and one control beam from Set 1 is given in Fig. 12. The control beam was loaded until a CMOD of 0.3 mm was reached, at which point the beam was unloaded and then immediately reloaded until failure.

The beam containing CA was pressurised to 0.2 bar before the load was applied. The first loading cycle resulted in the formation of a central discrete crack. A drop in pressure in the system was recorded at the time this crack first became visible, which is assumed to coincide with the time at which the CA first entered the crack. This resulted in two primary healing responses, characterised by an increase in the load between a CMOD of 0.1 mm and 0.15 mm and also between 0.25 mm and 0.3 mm. These primary healing responses can be attributed to the short-term curing of the CA.
It is interesting to note that two healing peaks occurred in the first loading cycle, which points to multiple damage-healing events. Similar primary healing responses have been observed by Joseph et al. (2010) using comparable healing agents and experimental arrangements. For the CA beams, the unloading response, which is considerably stiffer than that of the control beams, confirms that significant healing has taken place in the first loading cycle. During the second loading cycle an increase in load over and above that recorded upon unloading can be seen.

In a similar manner, the SS beams were also pressurised to 0.2 bar and showed evidence of a pressure drop upon crack formation. However, due to the longer chemical reaction time of the SS, there was no indication of primary healing. The beam was unloaded at a CMOD of 0.3 mm and a similar unloading response to the control beam was observed. The peak load upon reloading was higher than the load at unloading and the response showed a recovery in stiffness greater than that of the control beam and comparable to the CA beam.

Table 4 shows the strength recovery (HP) and stiffness recovery indices (HK) for set 1 for a typical beam for each healing agent, as presented in Fig. 12. It is clear from Table 4 that CA results in much greater healing in terms of strength recovery (79%) compared to SS (17%). The CA results show more variability with a coefficient of variation (CoV) of 15.5% for the HP compared with 3.5% for the SS. This increased variability for CA is almost certainly influenced by the complexity of the damage-healing process in the first loading cycle, which means that there would not have been an even distribution of CA available to cure during the fixed crack healing period. There is clear evidence of two primary healing events in the first loading cycle for cyanoacrylate, a phenomenon observed by other researchers working with similar self-healing systems (Joseph et al. 2010).

A typical healing response for Set 2 is presented in Fig. 13. As with set 1, a softening curve is observed following the initial peak load, and at a CMOD of 0.2 mm there is a distinctive rise in load carrying capacity (a primary healing response), which coincided with a drop in network pressure. The average strength recovery (HP*) index for set 2 was 39% with a CoV of 6.7% and the average stiffness recovery index (HK*) was 1.3% with a CoV of 35.9%. In load cycle 2, there is evidence of healing, characterised by a regain in stiffness upon reloading and partial recovery of
the initial peak load (P1). The average strength recovery (HP) of the specimens in set 2 was 59.7% with a coefficient of variation of 33.7% and the average stiffness recovery (HK) of 81.6% with a coefficient of variation of 20.9%. The relatively high CoV for the results are linked to the significant difficulties in setting up the experimental arrangement (system pressurisation and premature curing of the CA prior to testing), this level of variability confirms the challenges associated with the use of CA as a healing agent.

The results from a typical load versus CMOD response for Set 3 beams is presented in Fig. 14, with particular attention to the unload/reload portion of the response given in Fig. 15. The same trends, as observed in Sets 1 and 2, are also seen in Set 3 with the exception that the drop in pressure at crack formation is less pronounced in this case, which almost certainly is due to the fact that SS has a higher viscosity than the CA. For comparison purposes, Fig. 14 and 15 include a control beam response which was subjected to the same conditions. The average strength recovery (HP) of the set was 5.3% with a coefficient of variation of 34%. The stiffness of the SS beam upon reloading is much greater than the control beam as shown by the stiffness healing index of the SS beam being 4.9% with a coefficient of variation of 60%. The significant difference between the recovery index of SS and CA can be attributed to the crack opening, and the ability of the different healing agents to bridge the crack opening during the healing period. The primary healing action of SS is assumed to be its reaction with surplus calcium hydroxide in the cementitious matrix to form further calcium-silicate-hydrate gel. Natural autogenic healing processes yield the most promising results at crack widths of 0.15 mm or less and at larger crack widths, the potential for autogenic healing diminishes. This suggests that SS would work best in systems that employ other mechanisms to limit crack widths. Moreover, the mechanical healing recovery may be low due to the limited availability of calcium hydroxide in the crack plane, especially since hardened cement paste comprises only 15% calcium hydroxide by volume. Nevertheless, SS remains one of the preferred healing agents due to its long-term compatibility with the host matrix.
Fig. 16 shows the load versus CMOD response of the control and vascular network slabs. Cracking became visible when the central displacement reached approximately 1.5 mm, after which cracks continued to develop and propagate until the central displacement reached 6 mm (point 2 on the graph), at which point the slab was unloaded. The crack pattern at point (2) is shown in Fig. 17a and, as may be seen in the photograph, significant leakage of the healing agent from the underside of the slab could be observed at this displacement level. Fig. 17b shows the condition of the underside of the slab after unloading (i.e. at point (3)) and this shows the extent of the healing agent migration from the network to the underside of the slabs radial cracks. During the re-loading phase, the effect of healing on the stiffness is evident, in that the initial gradient of the re-load curve in the healed slab is significantly steeper than the control slab. The stiffness healing index \( H_K \) for the control slab is 46.3% whereas the SS healed slab is 100.2%. The peak load in the second cycle of the self-healing slab is only 2% above that of the control specimen but the response is noticeably more ductile. This limited increase in peak load is strongly influenced by the presence of reinforcement, which tends to mask the healing response, and affected by the fact that the residual crack openings were relatively large during healing (See Fig. 17b), even though the slab was unloaded during healing period. No additional leakage of healing agent was seen (Fig. 17c) indicating that the initial supply of healing agent was exhausted over the month long healing period. Nevertheless, it is proposed that replenishment of the healing between loading cycles may have allowed further cycles of healing to take place.

The crack pattern for a flow network arrangement aligned with the steel reinforcement, as shown in Fig. 17b, was very similar to the crack pattern exhibited by the control slab. This can be seen in Fig. 17a, b and c. However, in the slab in which the vascular network was aligned at 45° to steel to the steel reinforcement, shown in Fig. 8a, the crack patterns replicated the channel configuration (see Fig. 17d), suggesting that the channels act as crack inducers.
Set 5 - 2D Channels in a Demonstration Panel

Following the testing of the set 4 slabs, and with insight thereby gained of the influence of the network configuration on the resulting crack pattern, a 1 m x 1 m demonstration panel was cast as a preparatory stage to the full site-trial tests. This demonstration panel employed water rather than a healing agent. The results presented in this section are descriptive and qualitative in nature and serve to highlight the changes required in the channel filling techniques and testing procedures in readiness for site-trial applications. Following the loading of the panel and the introduction of the water into the network, a small amount of pressure remained in the system (less than 0.5 bar) and this resulted in water leaking out of the crack, as seen in Fig 18b and 18c. Fig 18d shows the concrete panel after testing and partial drying, where the horizontal and diagonal cracking on the face are visible. The diagonal cracks are concurrent with the flow network, again showing the crack initiation action of the flow channels. There is evidence that the supply mechanism was effective, with the filling technique clearly allowing water to fill the entire vascular network, despite the presence of cracks during the filling stage. The injection valves were capable of not only sealing the network but also retaining a small level of pressure (0.5 bar) within it for time enough to allow sufficient water to pass through the cracks onto the surface of the panel. The network supplied water to the full crack network and this is a positive indication of its ability to deliver healing agents of similar flow characteristics as water, to zones of damage.

Set 6 - Vascular Networks in a Site Trial Wall Panel

The panel was first loaded and unloaded at 36 days after casting. The SS was pumped through the network after a further 111 days which showed that the system was still intact and operable. The healing agent was pumped into the panel using the procedure presented in section 4, as depicted in Fig. 19a, The healing agent flowed out of the cracks, assisted by a pressure of 0.2 bar, as evidenced in Fig. 19b. As soon as the SS became visible on the surface of the panel, the system was drained and each channel flushed with water under gravity. The water flushing technique did not result in additional leakage from the panels front face. Furthermore, it is believed that the flushing process did not remover the SS from the cracks. This is because sodium silicate solution has a high viscosity,
when compared to water, and a low water flushing pressure was employed to empty the channels.

A digital image correlation (DIC) technique was used to monitor the strains on the front face of the panel. The results, shown in Fig. 19c, give the strain plot for Panel E. The crack pattern observed on Panel E at a load of 20 kN supports previous observations that the network channels act as crack inducers, with the diagonal crack pattern reflecting the form of the vascular network (Fig. 19a and 19b).

The panel was reloaded to the original load at 231 days after casting and the load versus displacement results compared pre-and post-healing (see Fig. 20). The presence of substantial steel reinforcement in the panel, masks the influence of healing on the load-displacement response, which made it difficult to quantify the mechanical strength recovery which could be directly attributed to the vascular network. Despite the clear site-trial evidence of healing agent flow into the cracks (surface leakage), there was only minimal evidence of healing using visual assessment techniques. It is suggested that a range of non-destructive techniques such as in-situ permeability testing, ultrasonic techniques and microscopy be employed in future tests to help identify the recovery of mechanical and durability-based properties.

The work reported earlier suggested that SS is most effective when healing cracks that are 0.3 mm wide or less but in the present case the cracks were wider than this, which may have reduced the healing potential of the system. It is concluded that it would be better to use either a healing agent with a higher viscosity or a different reaction mechanism when a vascular network is required to heal larger cracks (i.e. cracks >0.3 mm in width).

The site trials showed that vascular networks can be used at large scale and it has been shown that and the presence of the vascular networks cause the cracks to form in a similar pattern to the vascular network beneath the surface, giving direct access to the healing agent supply. The construction of the vascular networks on site undoubtedly demands additional labour but despite this shortcoming, it is concluded that vascular networks have the potential to heal repeated occurrences of damage.

CONCLUSIONS

A novel technique for creating a vascular network characterised by a series of 2D interconnected
hollow channels has been presented. The deployment of this network in both small laboratory and larger structural sized elements has proved successful and has highlighted the potential for its in-situ application to provide a healing mechanism for repeated damage events.

A series of preliminary investigations demonstrated the development and refinement of the design of the connectors, whilst the influence of specimen age, flow network location, healing time and curing condition were examined. The preliminary results showed that a small pressure head of 0.02 bar was sufficient to ensure that healing agent reached the majority of a crack surface (>90%) within 3 minutes. The greatest coverage of the healing agent on the crack face was achieved when specimens were 14 days old, cured in water, and tested at a CMOD of 0.3 mm.

With regards to the healing agents tested it was apparent that although SS was easier to handle and supply into the vascular network, CA offered greater strength recovery (up to 90%) in a significantly shorter time than the SS. This may suggest that CA is the preferred healing agent in applications where rapid healing of damage is required. On the other hand, SS may offer slower healing times and lower levels of healing which may be more suited to low levels of damage in early age structures where there is an abundance of calcium hydroxide in the matrix to facilitate healing. Nevertheless, as with the majority of the tests conducted using autonomic healing agents, there remains considerable uncertainty over the agents suitability for long term encapsulation and its compatibility with the cementitious matrix.

Not only do vascular networks provide multiple opportunities to supply a wide range of healing agents but such agents can also be replenished over the lifetime of a structure provided that the channels are emptied at the end of each healing event. With further research, into more efficient methods of forming these networks on site and the identification of compatible healing agents for a range of physical and chemical damage events, vascular networks could provide a viable and efficient healing system in structural elements formed from cementitious materials.

Data Availability Statement

All data created during this research are openly available from the Cardiff University data archive at http://doi.org/10.17035/d.2020.0107901898.
Acknowledgments

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<td>Age (days)</td>
<td>Crack width (mm)</td>
</tr>
<tr>
<td>-------------</td>
<td>------------</td>
<td>------------------</td>
</tr>
<tr>
<td>Series 1</td>
<td>14 †</td>
<td>0.2</td>
</tr>
<tr>
<td>Series 2</td>
<td>14 w, 140 w</td>
<td>0.1, 0.2, 0.3, 0.4</td>
</tr>
<tr>
<td>Series 3</td>
<td>14 †</td>
<td>0.2</td>
</tr>
<tr>
<td>Series 4</td>
<td>7 w</td>
<td>0.1, 0.2, 0.3, 0.4</td>
</tr>
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Note. ★ above the underside of the beam, † cured in ambient room conditions, w cured in water
### TABLE 2. Summary of vascular network experimental programme.

<table>
<thead>
<tr>
<th></th>
<th>Set 1</th>
<th>Set 2</th>
<th>Set 3</th>
<th>Set 4</th>
<th>Set 5</th>
<th>Set 6</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>No. of specimens</strong></td>
<td>8</td>
<td>6</td>
<td>6</td>
<td>3</td>
<td>1</td>
<td>2</td>
</tr>
<tr>
<td><strong>Specimen dimensions</strong></td>
<td>255x75</td>
<td>x100</td>
<td>500x100</td>
<td>500x100</td>
<td>600x600</td>
<td>1000x100</td>
</tr>
<tr>
<td>(l x b x d) (mm³)</td>
<td>x75</td>
<td>x100</td>
<td>x100</td>
<td>x100</td>
<td>x150</td>
<td>x150</td>
</tr>
<tr>
<td><strong>Age at 1st test (days)</strong></td>
<td>100</td>
<td>7</td>
<td>7</td>
<td>28</td>
<td>28</td>
<td>36</td>
</tr>
<tr>
<td><strong>Age at 2nd test (days)</strong></td>
<td>100</td>
<td>8</td>
<td>35</td>
<td>56</td>
<td>-</td>
<td>231</td>
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<tr>
<td><strong>Healing agent</strong></td>
<td>CA and SS</td>
<td>CA</td>
<td>SS</td>
<td>SS</td>
<td>Water</td>
<td>SS</td>
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<tr>
<td><strong>Notch depth (mm)</strong></td>
<td>5</td>
<td>5</td>
<td>5</td>
<td>None</td>
<td>None</td>
<td>None</td>
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<tr>
<td><strong>Pressure (bar)</strong></td>
<td>0.2</td>
<td>0.2</td>
<td>0.2</td>
<td>0.005</td>
<td>up to 0.5</td>
<td>up to 0.05</td>
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<tr>
<td><strong>Reinforcement (mm)</strong></td>
<td>None</td>
<td>None</td>
<td>None</td>
<td>8</td>
<td>8</td>
<td>10</td>
</tr>
<tr>
<td><strong>Curing regime</strong></td>
<td>Ambient</td>
<td>Ambient</td>
<td>Water (20 °C)</td>
<td>Hessian sack</td>
<td>Ambient</td>
<td>Outdoors</td>
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<td></td>
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<td>Cement (400 (CEM II/B-V 32.5R))</td>
<td>400</td>
</tr>
<tr>
<td>Coarse aggregate (4-10 mm crushed limestone)</td>
<td>990</td>
</tr>
<tr>
<td>Limestone fines (0-2 mm)</td>
<td>162</td>
</tr>
<tr>
<td>Sand (0-4 mm marine sand)</td>
<td>648</td>
</tr>
<tr>
<td>Water</td>
<td>200</td>
</tr>
<tr>
<td>w/c ratio</td>
<td>0.5</td>
</tr>
<tr>
<td>VS100 (SIKA) plasticiser l/100 kg cement</td>
<td>0.3</td>
</tr>
<tr>
<td>SIKATARD R retarder l/100 kg cement</td>
<td>-</td>
</tr>
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<th>Stiffness Recovery</th>
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<td>CA Load Cycle 2 Healing</td>
<td>78.6</td>
<td>69.7</td>
</tr>
<tr>
<td>SS Load Cycle 2 Healing</td>
<td>17.2</td>
<td>60.5</td>
</tr>
<tr>
<td>CA Load Cycle 1 Primary Healing 1</td>
<td>23.4*</td>
<td>1.9*</td>
</tr>
<tr>
<td>CA Load Cycle 1 Primary Healing 2</td>
<td>45.1*</td>
<td>14.5*</td>
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Note. * uncertainty due to variations in control response.
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