Comparison of Cost-effective Distances for LFAC with HVAC and HVDC in Their Connections for Offshore and Remote Onshore Wind Energy

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Abstract—For a cost-effective connection of large-scale long-distance wind energy, a low frequency alternating current (LFAC) transmission scheme (16.7 Hz or 20 Hz) is proposed as an alternative to the conventional high voltage alternating current (HVAC) transmission scheme (50 Hz or 60 Hz) and the recently popular high voltage direct current (HVDC) transmission scheme (0 Hz). The technical feasibility of the LFAC system is demonstrated but the basis for identifying the distance ranges for which LFAC would be preferable to HVAC and HVDC are not established and the dependence of this range on factors, such as power transfer rating, voltage rating and cable/line type, is not investigated. This paper presents an in-depth analysis for the overall cost of LFAC system and then provides an extensive comparison with HVAC and HVDC, to explore the distance ranges over which LFAC is cost-effective over both HVAC and HVDC in connections of offshore and remote onshore wind energy. The results demonstrate that the LFAC system does possess ranges in the intermediate distance for which it is more cost-effective than both HVAC and HVDC, and its overall cost advantage is generally larger in the overhead line (OHL) connection of remote onshore wind energy than the cable connection of offshore wind energy.

Index Terms—Cost-effective ranges, LFAC, overall cost analysis, wind energy.

NOMENCLATURE

A. Acronyms

C Overall Cost.
CC Capital Cost.
CBC Cable Cost.
CPC Compensation Cost.
CSC Current Source Converter.
FFTS Fractional Frequency Transmission System.
HVAC High Voltage Alternating Current.
HVDC High Voltage Direct Current.
LC Power Losses Cost.
LFAC Low Frequency Alternating Current.
OHC Overhead Line Cost.
OHL Overhead Line.
RC Route Cost.
RCC Route Capital Cost.
RLC Route Power Losses Cost.
RMS Root Mean Square.
TC Terminal Cost.
TCC Terminal Capital Cost.
TLC Terminal Power Losses Cost.
VSC Voltage Source Converter.

B. Constants

$B_C$ Base cost for VSC–HVDC offshore platform and plant (25 M£).
$B_T$ Base cost for HVAC offshore platform and plant (5 M£).
$E$ Energy average price (50 £/MWh).
$F$ Power factor of HVAC system (1.0).
$f_{TC}$ Cost factor of transformer number or converter number per platform (0.2).
$Q_{C_{off}}$ Offshore compensation cost (0.025 M£/Mvar).
$Q_{C_{ons}}$ Onshore compensation cost (0.015 M£/Mvar).
$T_p$ Project time (15 years).
$V_C$ Variable cost for VSC–HVDC offshore platform and plant (0.109 M£/MVA).
$V_T$ Variable cost for HVAC offshore platform and plant (0.045 M£/MVA).
$\delta_{op}$ Operation factor (0.231).
$\delta_{offT}$ Offshore HVAC transformer plant efficiency (99.4%).
$\delta_{offC}$ Offshore VSC–HVDC converter plant (rectifier with transf.) efficiency (98.2%).
$\delta_{onsT}$ Onshore HVAC transformer plant efficiency (99.4%).
$\delta_{onsC}$ Onshore VSC–HVDC converter plant (inverter with transf.) efficiency (98.19%).
\( \theta_{\text{onCSC}} \) Onshore CSC–HVDC converter plant (inverter with transf.) efficiency (99.12%).

C. Variables

- \( C \): Subsea cable shunt capacitance per kilometer (F/km).
- \( c_c \): Subsea cable cost per set including supply and installation (k£/km).
- \( c_o \): Onshore OHL cost per set including supply and installation (k£/km).
- \( f_n \): Operation frequency (Hz).
- \( I_{ch} \): Capacitive charging current in subsea cable (ka).
- \( I_{cn} \): Subsea cable nominal current (ka).
- \( I_{on} \): Onshore OHL nominal current (ka).
- \( I_{Qoff} \): Offshore compensation current (ka).
- \( L \): Onshore OHL series inductance per kilometer (H/km).
- \( l_c \): Subsea cable length (km).
- \( l_o \): Onshore OHL length (km).
- \( n_C \): HVAC transformer number per platform.
- \( n_T \): VSC–HVAC converter number per platform.
- \( n_{cC} \): Number of subsea cable parallel circuits.
- \( n_{c_o} \): Number of Onshore OHL parallel circuits.
- \( P_c \): Active power transfer capability in subsea cable (MW).
- \( P_o \): Active power transfer capability in onshore OHL (MW).
- \( P_{sl} \): Stability limit in onshore OHL (MW).
- \( P_{th} \): Thermal limit in onshore OHL (MW).
- \( Q_c \): Reactive power produced by capacitive charging current (Mvar).
- \( Q_{off} \): Offshore compensation power (Mvar).
- \( Q_{ons} \): Onshore compensation power (Mvar).
- \( r_c \): Subsea cable resistance per kilometer (\( \Omega/km \)).
- \( r_o \): Onshore OHL resistance per kilometer (\( \Omega/km \)).
- \( S_C \): Apparent power in subsea cable (MVA).
- \( S_{TT} \): Power transfer rating (MVA).
- \( V_{cn} \): Subsea cable nominal voltage (kV).
- \( V_{on} \): Onshore OHL nominal voltage (kV).
- \( X_o \): Onshore OHL series reactance per kilometre (\( \Omega/km \)).

I. INTRODUCTION

Wind is regarded as one of the most important renewable energy resources throughout the world [1]–[3]. The total penetration of wind generation in some countries has already exceeded 20% of their total capacity [4]. It has also been determined that wind resources are often best installed in offshore or remote onshore areas [5], [6]. For instance, the offshore wind farm generation in Europe is approaching 25 GW as of 2020 and is planned to reach 70 GW by 2030 [7], and the largest wind farm station in the world, which is located in Jiuquan, China (remote onshore area), has already reached 10 GW capacity [8]. These large-scale wind farms are usually far away from the metropolitan load centers, and this fact has prompted a greater effort to advancing cost-effective long-distance transmission technologies in connection with wind energy [9], [10].

High voltage alternating current (HVAC) and high voltage direct current (HVDC) systems, illustrated in Fig. 1 and Fig. 2, have been commercialized for this use in both subsea cable form in connection with offshore wind energy and overhead line (OHL) form in connection with remote onshore wind energy [11]–[14]. The overall cost of a wind energy connection system is usually partitioned into the terminal cost and route cost for analysis and comparison [15]–[18]. A HVAC system has the advantage of relatively inexpensive terminal costs, whereas a HVDC system has an expensive power converter plant at each terminal. The route cost in a HVAC system rises much more sharply with distance than that in a HVDC system because of the different transmission capability limits in the AC and DC use of cables and OHL. Over short distances, a HVAC system is favored for its lower terminal costs but beyond some threshold distance, the advantages of lower route costs favors the HVDC system. The cross-over distance for the overall cost of HVAC and HVDC systems is reported to be in the region of 80 km [19]–[21] for a subsea cable system and 700 km for a remote onshore OHL system [22], [23].

However, the technology choice for HVAC or HVDC on a distance basis is not yet definitive. For example, the very recent practical wind farm projects of Hornsea [24], [25] and Dogger Bank [26], [27] made different choices (Hornsed chose HVAC while Dogger Bank chose HVDC) although they are located in the same area of the North Sea with almost the same power rating. This could raise a general equation whether there exists a third technology choice with cost advantages over both HVAC and HVDC for some distance ranges, which may further lower the wind energy price and increase wind energy penetration in the future.

The low frequency alternating current (LFAC) system [28]–[30], or alternatively, fractional frequency transmission system (FFTS) [31]–[34] was proposed in the 1990 s, and its structure for a wind energy connection is shown in Fig. 3. The operational frequency in a LFAC system is usually set at 16.7 Hz or 20 Hz, which is one third of the standard system frequency (50 Hz or 60 Hz) for HVAC. Because of the lower frequency, although the transformer volume tends to increase,
a LFAC system suffers less effects from cable shunt capacitive susceptance or OHL series inductive reactance than a standard HVAC system and so it makes for a more cost-effective use of the cable or OHL. In the case of a wind farms connection, only one AC-AC power converter plant is required as an interface between the LFAC system and the standard electrical network to realize frequency conversion. Therefore, the LFAC system could incur lower terminal costs compared to a HVDC system, and the maintenance costs would also be significantly reduced with the removal of an offshore converter station. Moreover, the voltage stability would be improved since the sensitivity of voltage on reactive power variations is diminished in a LFAC system [35]. Furthermore, a multi-terminal wind energy system could be built relying on LFAC since the protection scheme inherited from the HVAC system has been maturely designed, which is difficult to realize with a HVDC system due to the lack of cost-effective DC breakers. The technical feasibility of a LFAC system has been intensively studied [35]–[38] over the last decade and a laboratory prototype of a LFAC system has also been successfully demonstrated [39], [40]. Cost analysis and comparisons for a LFAC system also received some attention [41]–[43] in recent years but not to the degree needed to properly estimate its cost-effective distance ranges [44]–[46] in connection with wind energy.

It is postulated that a LFAC system would have a lower cost than either HVAC or HVDC systems for some intermediate range of distances straddling the threshold distance between HVAC and HVDC. This is on the basis that a single power converter at one end will provide a lower terminal cost than an HVDC system (but higher than an HVAC system) and better cable or OHL use will give a lower route cost than an HVAC system (but higher than an HVDC system) [46]–[48]. Figure 4 illustrates the overall cost against distance for HVAC, HVDC and three possible cases of LFAC systems. Although all the LFAC cases have terminal costs and unit route costs between those of the HVAC and HVDC systems, whether the distance range that exists with the optimal choice of LFAC would also be affected by the power ratings and connection forms has not been determined. In cases 1 and 2, the overall cost of LFAC crosses the overall cost of HVAC before crossing the overall cost of HVDC and so the LFAC system has a cost-effective range over which it is cheapest. However, in case 3, the overall cost of LFAC first crosses the overall cost of HVDC and then there is no distance for which it is the preferred choice. Therefore, knowing that the terminal costs and unit route costs of the LFAC system lie between those of the HVAC and HVDC systems is not sufficient to establish whether a LFAC scheme has or has not the cost-effective range, let alone identifying the cost-effective distance range for different power ratings with different connection forms. A careful analysis of the overall cost of a LFAC system is required and a thorough comparison with HVAC and HVDC is also needed to bridge this knowledge gap, which can make a good contribution in the future choice of cost-effective technology in connection with large-scale offshore and remote onshore wind energy.

So far, few studies have illustrated the cost estimation for the LFAC based wind energy transmission system. In this paper, an in-depth analysis for the overall cost of a LFAC system is presented and an extensive comparison with HVAC and HVDC is further provided to allow estimation of the cost-effective distance ranges of LFAC over both HVAC and HVDC in connection with offshore and remote onshore wind energy. First, the overall cost of a LFAC system is decomposed
into constituent parts of terminal and route costs and further decomposed into capital and operational costs. Then, detailed analysis of each constituent cost follows with a derivation of equations specific to a LFAC system, and cost parameters are estimated from the most similar equipment used in HVDC and HVAC projects since there is an absence of commercial LFAC projects that can provide cost data. Lastly, the cost estimation process considers different choices of operating voltage and numbers of parallel conductors for each distance in order to meet the specified power transfer at minimum cost and finally provide a fair comparison for these three connection systems. The results demonstrate that a LFAC system does possess a cost-effective distance range over HVAC and HVDC systems in the intermediate distance for both connections of offshore and remote onshore wind energy, and its overall cost advantage is generally larger in the OHL connection of remote onshore wind energy than the cable connection of offshore wind energy.

II. DECOMPOSITION OF OVERALL COST

An all-inclusive analysis of overall cost for a large-scale and long-distance wind energy connection system is complex to conduct in analytical form since many detailed practical factors in the system would need to be taken into consideration and the analysis would become intractable [15], [21]. For a new technology choice, such as a LFAC system, this is complicated by the absence of full-scale demonstration projects which will have resolved some of the implementation details and established design limits. To make the overall cost analysis both feasible and widely applicable, some minor factors in the whole connection system have to be neglected [18], [49], [50] and the cost data of individual items needs to be estimated in broad terms from whatever real practical projects provide a reasonably close data point [51], [52].

It is common to separate out the terminal cost (TC) and route cost (RC) as the major factors in an estimation of the overall cost (C) for a wind energy connection system. The terminal cost is independent of distance while the route cost is a function of distance. Table I lists the cost of each constituent of HVAC, HVDC and LFAC systems under the headings of TC and RC with reference to Fig. 1–Fig. 3. The descriptions are for an offshore cable connection case with alternative descriptions for a remote onshore OHL connection case given in brackets. The overall cost (C) of a wind energy connection system can also be separated into capital cost (CC) and the capitalized cost of operational power losses (LC). The capital cost is relevantly independent of system operational years while power loss cost is a function of operational years. Thus, the overall cost could be further decomposed as terminal capital cost (TCC), terminal power loss cost (TLC), route capital cost (RCC) and route power loss cost (RLC). Fig. 5 shows these two decomposition directions and illustrates the relevant relationships between these constituent costs, and each constituent cost will be discussed and analyzed in detail in the next two sections.

III. ANALYSIS AND ESTIMATE OF THE COST-EFFECTIVE RANGE FOR OFFSHORE CABLE CONNECTIONS

By interpreting each constituent cost in Table I for offshore cable connections in terms of Fig. 5 reveals that TCC consists of the offshore platform and plant cost (TCC_{off}) and onshore plant cost (TCC_{ons}); TLC consists of offshore plant power loss cost (TLC_{off}) and onshore plant power loss cost (TLC_{ons}); RCC consists of the cable cost (CBC) and compensation cost (CPC), and RLC is the subsea cable power loss cost.

![Fig. 5. Decompositions and relationships between constituent costs.](image)

The cost analysis for each constituent in the two established technologies, HVAC and HVDC systems, can draw on the

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**TABLE I**

<table>
<thead>
<tr>
<th>System</th>
<th>Terminal Capital Cost (TCC)</th>
<th>Terminal Power Losses Cost (TLC)</th>
<th>Route Capital Cost (RCC)</th>
<th>Route Power Losses Cost (RLC)</th>
</tr>
</thead>
<tbody>
<tr>
<td>HVAC</td>
<td>Offshore (remote-end) step-up transformer plant and platform (compound). Onshore (load-end) step-down transformer plant and compensation.</td>
<td>Cables (or OHL) and compensation.</td>
<td>Offshore (remote-end) transformer plant power losses. Onshore (load-end) transformer plant power losses.</td>
<td>Cables (or OHL) power losses.</td>
</tr>
<tr>
<td>HVDC</td>
<td>Offshore (remote-end) converter plant and platform (compound) including valves, transformers and filters. Onshore (load-end) converter plant including valves, transformers and filters.</td>
<td>Cables (or OHL).</td>
<td>Offshore (remote-end) AC-DC converter plant power losses. Onshore (load-end) DC-AC converter plant power losses.</td>
<td>Cables (or OHL) power losses.</td>
</tr>
<tr>
<td>LFAC</td>
<td>Offshore (remote-end) LF step-up transformer plant and platform (compound). Onshore (load-end) AC-AC converter plant including valves, transformers and filters.</td>
<td>Cables (or OHL) and compensation.</td>
<td>Offshore (remote-end) LF transformer plant power losses. Onshore (load-end) AC-AC converter plant power losses.</td>
<td>Cables (or OHL) power losses.</td>
</tr>
</tbody>
</table>
published estimation methods and practical cost data. This also
serves as an important starting point for the analysis and es-
teration for the LFAC system. It should be noted that voltage-
source-converter HVDC (VSC–HVDC) is the preferred DC
option in connection with offshore wind energy so that an
isolated AC grid can be formed for the wind turbines.

A. Cost Analysis and Estimate in HVAC and VSC–HVDC
Systems

Examining cost data obtained from commercial projects
shows that the terminal capital cost for HVAC and VSC–
HVDC systems can be approximately estimated by the em-
pirical formula as in (1)–(4) [52]–[56]. For ease of reference, the
descriptions for all the variables and relatively assumed values in
this paper have been summarized in the Nomenclature
section and all the variables will also be described after the
specific equation for clarification.

\[ TCC_{\text{offHVAC}} = B_T + [1 + f_T \cdot (n_T - 2)] \cdot V_T \cdot S_{TT} \quad (1) \]
\[ TCC_{\text{onsHVAC}} = 0.02621 S_{TT}^{0.7513} \quad (2) \]
\[ TCC_{\text{offsVCHVDC}} = B_C + [1 + f_C \cdot (n_C - 2)] \cdot V_C \cdot S_{TT} \quad (3) \]
\[ TCC_{\text{onsVSHVDC}} = 0.08148 S_{TT} \quad (4) \]
where \( B_T \) and \( B_C \) are the base costs for HVAC and VSC–
HVDC offshore platform and plant, \( V_T \) and \( V_C \) are the variable
costs for HVAC and VSC–HVDC offshore platform and plant, \( n_T \) and \( n_C \) are the HVAC transformer number and VSC–
HVDC converter number per platform, \( f_T \) and \( f_C \) are the cost
costs for transformer number and converter number per
platform, \( S_{TT} \) is the terminal power rating.

The capitalized cost of power loss is an accumulated value
over an operational time and dependent on an energy price.
The power loss cost of the offshore plant and onshore plant
for HVAC and HVDC systems are calculated by (5)–(8)
respectively [57]–[61].

\[ TLC_{\text{offHVAC}} = S_{TT} \cdot F \cdot (1 - \vartheta_{\text{off}}) \cdot T_p \cdot \delta_{op} \cdot E \quad (5) \]
\[ TLC_{\text{onsHVAC}} = S_{TT} \cdot F \cdot (1 - \vartheta_{\text{ons}}) \cdot T_p \cdot \delta_{op} \cdot E \quad (6) \]
\[ TLC_{\text{offsVCHVDC}} = S_{TT} \cdot F \cdot (1 - \vartheta_{\text{offsVCHVDC}}) \cdot T_p \cdot \delta_{op} \cdot E \quad (7) \]
\[ TLC_{\text{onsVCHVDC}} = S_{TT} \cdot F \cdot (1 - \vartheta_{\text{onsVCHVDC}}) \cdot T_p \cdot \delta_{op} \cdot E \quad (8) \]
where \( F \) is the power factor for transmission, \( \vartheta_{\text{off}} \) and
\( \vartheta_{\text{ons}} \) are the efficiencies of an offshore and onshore HVAC
transformer plant, \( \vartheta_{\text{offsVCHVDC}} \) and \( \vartheta_{\text{onsVCHVDC}} \) are the efficiencies of an
offshore VSC–HVDC converter plant (rectifier with transformer)
and onshore VSC–HVDC converter plant (inverter with transformer), \( \vartheta_{\text{CHVAC}} \) and \( \vartheta_{\text{CVSHVDC}} \) are the efficiencies of HVAC and VSC–HVDC cables, \( T_p \) is the project time, \( \delta_{op} \)
is the operational factor and \( E \) is the energy average price.

Combining (1), (2), (5), (6) and (3), (4), (7), (8) with the
assumption values listed in the Nomenclature, the terminal cost
of the HVAC and VSC–HVDC systems are estimated as (9)
and (10) respectively.

\[ TC_{\text{HVAC}} = TCC_{\text{HVAC}} + TLC_{\text{HVAC}} = TCC_{\text{offHVAC}} + TCC_{\text{onsHVAC}} + TLC_{\text{offHVAC}} + TLC_{\text{onsHVAC}} \]
\[ = 5 + 0.045 S_{TT} + 0.02621 S_{TT}^{0.7513} + 0.00911 S_{TT} + 0.00906 S_{TT} \cdot \vartheta_{\text{CHVAC}} \quad (9) \]
\[ TC_{\text{VSHVDC}} = TCC_{\text{VSHVDC}} + TLC_{\text{VSHVDC}} = TCC_{\text{offsVCHVDC}} + TCC_{\text{onsVSHVDC}} + TLC_{\text{offsVCHVDC}} + TLC_{\text{onsVSHVDC}} \]
\[ = 25 + 0.11 S_{TT} + 0.08148 S_{TT} + 0.02610 S_{TT} + 0.02701 S_{TT} \cdot \vartheta_{\text{CVSHVDC}} \quad (10) \]

To estimate the cable cost and compensation cost in a stan-
dard HVAC system, the cable transmission capability needs
to first be analyzed. Shunt capacitive susceptance is the key
parameter limiting active power transfer in a subsea cable, and
the reactive power produced by capacitive charging current is
expressed as (11).

\[ Q_c = 3 \left( \frac{V_{cn}}{\sqrt{3}} \right)^2 \cdot 2 \pi f_n \cdot C \cdot l_c = V_{cn}^2 \cdot 2 \pi f_n \cdot C \cdot l_c \quad (11) \]
where \( Q_c \) is the reactive power, \( V_{cn} \) is the subsea cable nominal
voltage, \( f_n \) is the operational frequency, \( C \) is the subsea cable
shunt capacitance per kilometre and \( l_c \) is the subsea cable
length.

Splitting the reactive power compensation evenly between
the two ends of the subsea cable makes available most of the
capacity for active power use [21], [51], [60], [63]. On this
basis, the cable transmission capability is given by (12),
and the compensation cost in the HVAC system can be
estimated by (13). With the distance increasing, the cable transmis-
sion capability in the HVAC system will decrease and the required
compensation power and compensation cost will increase.

\[ P_c = \sqrt{S_c^2 - Q_{\text{off}}^2} = \sqrt{S_c^2 - \left( \frac{Q_{\text{off}}}{2} \right)^2} \]
\[ = \left( \sqrt{3} V_{cn} I_{cn} \right)^2 \cdot \frac{1}{4} (V_{cn}^2 \cdot 2 \pi f_n \cdot C \cdot l_c)^2 \quad (12) \]
\[ CPC_{\text{HVAC}} = QC_{\text{off}} \cdot Q_{\text{offHVAC}} + QC_{\text{ons}} \cdot Q_{\text{onsHVAC}} \]
\[ = QC_{\text{off}} \cdot \frac{Q_{\text{CHVAC}}}{2} + QC_{\text{ons}} \cdot \frac{Q_{\text{CHVAC}}}{2} \]
\[ = \frac{QC_{\text{off}} + QC_{\text{ons}}}{2} \cdot V_{cn}^2 \cdot 2 \pi f_n \cdot C \cdot l_c \quad (13) \]
where \( P_c \) is the active power transfer capability in the subsea
cable, \( S_c \) is the apparent power in the subsea cable, \( Q_{\text{off}} \) is the
offshore compensation power, \( l_{cm} \) is the subsea cable nominal
length.

The parameters of the common cables for a HVAC system
are listed in Appendix Table I. The capital costs and power
loss costs of HVAC cables are calculated by (14) and (15)
respectively, and its efficiency in transmission is expressed in
(16).

\[ CBC_{\text{HVAC}} = c_c \cdot l_c \cdot n_{c_c} \quad (14) \]
\[ RLC_{\text{HVAC}} = 3 \left( \frac{S_{TT} \cdot F \cdot \vartheta_{\text{off}}}{n_{c_c} \cdot \frac{3 L_c}{\sqrt{3}}} \right)^2 \cdot r_c \cdot l_c \cdot n_{c_c} \cdot T_p \delta_{op} E \]
\[ = \left( \frac{S_{TT} \cdot F \cdot \vartheta_{\text{off}}}{V_{cn}} \right)^2 \cdot r_c \cdot l_c \cdot n_{c_c} \cdot T_p \delta_{op} E \quad (15) \]
\[ \vartheta_{\text{HVAC}} = \frac{S_{\text{TT}} \cdot F \cdot \vartheta_{\text{offTT}}}{V_{\text{cn}}^2} - \frac{(S_{TT} \cdot F \cdot \vartheta_{\text{offTT}})^2}{V_{\text{cn}}^2} \cdot \frac{r_c \cdot l_c}{n_c} \]

\[ = 1 - \frac{S_{\text{TT}} \cdot F \cdot \vartheta_{\text{offTT}}}{V_{\text{cn}}^2} \cdot \frac{r_c \cdot l_c}{n_c} \]

(16)

where \( c_c \) is the subsea cable cost per set including supply and installation, \( n_{cc} \) is the number of subsea cable parallel circuits, \( r_c \) is the subsea cable resistance per kilometer.

A VSC–HVDC system has an advantage in active power transfer over HVAC since a DC system can utilize the peak value of voltage continuously whereas the root-mean-square (RMS) value of voltage that sets the AC power is a factor of \( \sqrt{2} \) less than the peak value. Moreover, there is no capacitive shunt current in the DC cable transmission, which enlarges the advantages in active power transfer for smaller cable cost and also avoids the compensation cost.

The parameters of the common VSC–HVDC cables are listed in Appendix Table II, and (14) can also be used to calculate the cable capital cost. The power loss cost of VSC–HVDC cables and its efficiency in transmission are given in (17) and (18).

\[ RLC_{\text{VSC HVDC}} = 2 \left( \frac{S_{\text{TT}} \cdot F \cdot \vartheta_{\text{offTT}}}{n_c \cdot 2 V_{\text{cn}}} \right)^2 \cdot \frac{r_c \cdot l_c \cdot n_c}{2 n_c} \cdot T_p \cdot \delta_{\text{op}} \cdot E \]

\[ = \left( \frac{S_{\text{TT}} \cdot F \cdot \vartheta_{\text{offTT}}}{V_{\text{cn}}} \right)^2 \cdot \frac{r_c \cdot l_c}{2 n_c} \cdot T_p \cdot \delta_{\text{op}} \cdot E \]

(17)

\[ \vartheta_{\text{VSC HVDC}} = \frac{S_{\text{TT}} \cdot F \cdot \vartheta_{\text{offTT}}}{V_{\text{cn}}^2} - \frac{(S_{TT} \cdot F \cdot \vartheta_{\text{offTT}})^2}{V_{\text{cn}}^2} \cdot \frac{r_c \cdot l_c}{n_c} \]

\[ = 1 - \frac{S_{\text{TT}} \cdot F \cdot \vartheta_{\text{offTT}}}{V_{\text{cn}}^2} \cdot \frac{r_c \cdot l_c}{n_c} \]

(18)

Combining (14)–(16) and (17), (18) with the assumption values in the Nomenclature, the route costs of HVAC and VSC–HVDC systems are estimated as shown in (19) and (20) respectively.

\[ RC_{\text{HVAC}} = RCC_{\text{HVAC}} + RLC_{\text{HVAC}} \]

\[ = CBC_{\text{HVAC}} + CPC_{\text{HVAC}} + RLC_{\text{HVAC}} \]

\[ = c_c \cdot l_c \cdot n_c + 0.02 V_{\text{cn}}^2 \cdot 2 \pi f_n \cdot C \cdot l_c + 1.51767 \cdot \left( \frac{0.994 S_{\text{TT}}}{V_{\text{cn}}} \right)^2 \cdot \frac{r_c \cdot l_c}{n_c} \]

(19)

\[ RC_{\text{VSC HVDC}} = RCC_{\text{VSC HVDC}} + RLC_{\text{VSC HVDC}} \]

\[ = CBC_{\text{VSC HVDC}} + RLC_{\text{VSC HVDC}} \]

\[ = c_c \cdot l_c \cdot n_c + 0.75884 \cdot \left( \frac{0.983 S_{\text{TT}}}{V_{\text{cn}}} \right)^2 \cdot \frac{r_c \cdot l_c}{n_c} \]

(20)

With (9), (10) and (19), (20), the estimations of the overall costs for HVAC and VSC–HVDC systems are obtained as shown in (21) and (22).

\[ C_{\text{HVAC}} = TC_{\text{HVAC}} + RC_{\text{HVAC}} = 5 + 0.04 S_{\text{TT}} \cdot 0.02621 S_{\text{TT}} \cdot 0.00911 I_{\text{TT}} + \]

\[ 0.00906 \cdot \left( \frac{S_{\text{TT}} - 0.994 S_{\text{TT}}^2}{V_{\text{cn}}} \right) + c_c \cdot l_c \cdot n_c + 0.02 V_{\text{cn}}^2 \cdot 2 \pi f_n \cdot C \cdot l_c + \]

\[ 1.51767 \cdot \left( \frac{0.994 S_{\text{TT}}}{V_{\text{cn}}} \right)^2 \cdot \frac{r_c \cdot l_c}{n_c} \]

(21)

\[ C_{\text{VSC HVDC}} = TC_{\text{VSC HVDC}} + RC_{\text{VSC HVDC}} = 25 + 0.11 S_{\text{TT}} + 0.08148 S_{\text{TT}} + 0.02610 I_{\text{TT}} + \]

\[ 0.02701 \cdot \left( \frac{S_{\text{TT}} - 0.492 S_{\text{TT}}^2}{V_{\text{cn}}} \right) + c_c \cdot l_c \cdot n_c + 0.75884 \cdot \left( \frac{0.983 S_{\text{TT}}}{V_{\text{cn}}} \right)^2 \cdot \frac{r_c \cdot l_c}{n_c} \]

(22)

B. Cost Analysis and Estimate in a LFAC System

Because there have been no commercial LFAC example to date in connection with wind energy, the capital cost of a LFAC system needs to be analyzed and estimated from the equipment in practical HVAC and VSC–HVDC projects that most closely correspond to the LFAC case.

First, on a basic view of flux and current densities, the core cross-sectional area of low frequency (LF) step-up transformers is expected to be three times larger than that of a HVAC system. However, consideration of the thermal design and insulation/bushing requirement leads instead to the view that an LF transformer could be only about \( \sqrt{3} \) times of the size and weight of the standard frequency transformer in an HVAC system [30], [43], [64]. Here, the base and variable costs of the offshore platform and plant for a LFAC system are assumed to be \( \sqrt{3} \) times of those for a HVAC system and the capital cost of the LFAC offshore terminal is estimated by (23).

\[ TCC_{\text{offLFAC}} = \sqrt{3} B_T + \left[ 1 + f_T \cdot (n_T - 2) \right] \cdot \sqrt{3} V_T \cdot S_{\text{TT}} \]

(23)

Second, there are several possible technology options for the onshore AC-AC converter plant for a LFAC system [65], [66], such as cycloconverter [67]–[70], back-to-back modular multilevel converter [71]–[73] and modular multilevel matrix converter [74]–[77], but the choice for most cost-effective technology would be the thyristor-based cycloconverter. The circuit topology, power device number and passive component value of these AC-AC converters are a reasonably close match to the thyristor-based DC-AC converter from a CSC–HVDC (current source converter HVDC) system. The onshore plant cost in a LFAC system should be comparable to that of a CSC–HVDC onshore station and an empirical formula of which could be used for the estimation for LFAC onshore plant cost [15], [59], [78] is suggested in (24).

\[ TCC_{\text{onLFAC}} \approx TCC_{\text{onCSC HVDC}} = 0.05926 S_{\text{TT}} \]

(24)

For the capitalized cost of power losses in a LFAC system, it can still use (5) and (6) to analyze and estimate the offshore power loss cost and onshore power loss cost respectively with the corresponding efficiency adjustments for offshore a LF transformer and onshore AC-AC converter.

The LF transformer volume is about \( \sqrt{3} \) times the volume of a standard frequency transformer but the core losses per unit volume would be reduced at low frequency operations. Based on the theoretical analysis and simulation results in [43], [64], the efficiency of a LF transformer would be very close to a
standard transformer efficiency. For the efficiency of the onshore AC-AC converter, practical efficiency data of a thyristor-based DC-AC converter in a CSC–HVDC system [59], [79] could be used based on the same analysis for (24).

With these assumptions and relative efficiency data given in the Nomenclature, the terminal cost estimation for a LFAC system is presented in (25).

\[
TC_{LFAC} = TCC_{LFAC} + TLC_{LFAC} \\
= TCC_{offLFAC} + TCC_{onsLFAC} + TLC_{offLFAC} + TLC_{onsLFAC} \\
= 5\sqrt{3} + 0.045\sqrt{3}S_{TT} + 0.05926S_{TT} + 0.00911S_{TT} + 0.01303S_{TT} \cdot \theta_{CLFAC}
\]

(25)

For the compensation cost in a LFAC system, it can be seen in (11) that the reactive power produced by charging current is proportional to the operational frequency and so the required compensation power and compensation cost in a LFAC system will be theoretically one third of that in a HVAC system based on the analysis in (13).

The unit price of the subsea cable for a LFAC system is assumed to be the same as the same physical cable for a HVAC system but because of the reduced charging current and skin effect in the cable, it will have a larger transmission capability in a LFAC system than in a HVAC system. The results of a simulation and experiment [36], [80]–[82] on subsea cables identified parameters for a LFAC system are presented in Appendix Table III. The cable capital cost, power loss cost and cable efficiency calculation can follow the formulas in (14)–(16) with the corresponding parameter adjustments for a LFAC system, and its route cost estimation is given as (26).

\[
RC_{LFAC} = RCC_{LFAC} + RLC_{LFAC} \\
= CCLFAC + CPCR_{LFAC} + RLC_{LFAC} \\
= c_c \cdot l_c \cdot nc_c + 0.02 V_{cn}^2 \cdot 2\pi f_n \cdot C \cdot l_c + 1.51767 \cdot \left( \frac{0.994S_{TT}}{V_{cn}} \right)^2 \cdot \frac{r_c \cdot l_c}{nc_c}
\]

(26)

With (25) and (26), the estimation of the overall cost for LFAC system is obtained in (27).

\[
CLFAC = TCF_{LFAC} + RCF_{LFAC} \\
= 5\sqrt{3} + 0.045\sqrt{3}S_{TT} + 0.00911S_{TT} + 0.01303\left( S_{TT} - \frac{0.994S_{TT}^2}{V_{cn}} \cdot \frac{r_c \cdot l_c}{nc_c} \right) + c_c \cdot l_c \cdot nc_c + 0.02 V_{cn}^2 \cdot 2\pi f_n \cdot C \cdot l_c + 1.51767 \cdot \left( \frac{0.994S_{TT}}{V_{cn}} \right)^2 \cdot \frac{r_c \cdot l_c}{nc_c}
\]

(27)

\[C_{LFAC} = TCF_{LFAC} + RCF_{LFAC}\]

C. Case Study for Lower Power Rating Connection

This first case study will examine a relatively low power connection case of 0.6 GW. For AC schemes (both HVAC and LFAC), it is necessary that at each distance the choice of voltage rating and cable current capacity (including use of parallel circuits) is re-examined and a minimum-cost choice made from the options available. In this study, the available cables are described in Appendix Table I for a HVAC system and Appendix Table III for a LFAC system. The analysis in (6) shows that the transmission capability of a HVAC or a LFAC cable system will fall off with the increasing distance. This is illustrated in Fig. 6 with the cable parameters in Appendix Table I and Appendix Table III. It can be seen in Fig. 6 that a LFAC system has a significant advantage over a HVAC system in terms of usable distance of a given cable based on the reduction in charging current and skin effect. For a HVDC scheme where charging current and reactive power do not apply, the cable transmission capability would not decrease with the increasing distance and so a given cable can be used over any distance for its rated transfer power.

Table II records the minimum-cost choices of cable made for distances up to 240 km, which is taken as the likely upper limit on offshore wind farm connections [83]–[87]. Different cable selections are made for a HVAC system to achieve the minimum cost for each distance. It is worth noting that the minimum cost selection yields the same cable for a LFAC system for all distances up to 240 km in this lower power connection case, but different cable selections will appear when power rating increases, which will be presented in the next sub-section.

The analysis in (19) and the cable choices in Table II were used to estimate the overall cost of a 0.6 GW HVAC offshore cable connection and the results are plotted in Fig. 7 for the distance ranges 0–240 km. The terminal cost is 46.1 M£, and the route cost per unit rises rapidly with the increasing distance from 1.78 M£/km to 3.76 M£/km. The breakdown of terminal capital cost (TCC), route capital cost (RCC) terminal power loss cost (TLC) and route power loss cost (RLC) are provided in Fig. 8, and the detailed data for these constituent costs are given in Appendix Table IV. To validate the estimated costs in Fig. 7, the overall costs of two comparable connections that have been realized in practice, the 0.3 GW Capri–Torre Annunziata Interconnector in Italy and the 0.4 GW Kriegers Flak Combined Grid Interconnector between Denmark and Germany, were obtained from [88]–[91] and plotted as points P1 and P2 respectively, which, while not strictly validating the results, give reassurances that the overall cost estimation for the HVAC system are reasonable.
TABLE II

<table>
<thead>
<tr>
<th>System</th>
<th>Distance (km)</th>
<th>Voltage (kV)</th>
<th>Size (mm$^2$)</th>
<th>Capability per circuit (GW)</th>
<th>Number of circuits ($n_c$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>HVAC</td>
<td>0–65</td>
<td>400</td>
<td>1000</td>
<td>0.646–0.604</td>
<td>1</td>
</tr>
<tr>
<td></td>
<td>65–80</td>
<td>400</td>
<td>1400</td>
<td>0.639–0.603</td>
<td>1</td>
</tr>
<tr>
<td></td>
<td>80–120</td>
<td>220</td>
<td>800</td>
<td>0.320–0.300</td>
<td>2</td>
</tr>
<tr>
<td></td>
<td>120–150</td>
<td>220</td>
<td>1000</td>
<td>0.321–0.299</td>
<td>2</td>
</tr>
<tr>
<td></td>
<td>150–200</td>
<td>220</td>
<td>630</td>
<td>0.255–0.205</td>
<td>3</td>
</tr>
<tr>
<td></td>
<td>200–215</td>
<td>220</td>
<td>800</td>
<td>0.225–0.203</td>
<td>3</td>
</tr>
<tr>
<td></td>
<td>215–230</td>
<td>132</td>
<td>800</td>
<td>0.158–0.150</td>
<td>4</td>
</tr>
<tr>
<td></td>
<td>230–240</td>
<td>132</td>
<td>1000</td>
<td>0.157–0.151</td>
<td>4</td>
</tr>
<tr>
<td>LFAC</td>
<td>0–240</td>
<td>400</td>
<td>800</td>
<td>0.733–0.685</td>
<td>1</td>
</tr>
<tr>
<td>VSC-HVDC</td>
<td>0–240</td>
<td>± 300</td>
<td>800</td>
<td>0.986</td>
<td>1</td>
</tr>
</tbody>
</table>

Fig. 7. Overall cost estimate of a 0.6 GW HVAC system (P1: 0.3 GW Capri–Torre Annunziata Interconnector in Italy; P2: 0.4 GW Kriegers Flak Combined Grid Interconnector between Denmark and Germany).

Fig. 8. Constituent costs of a 0.6 GW HVAC system.

Cost estimation for 0.6 GW VSC–HVDC offshore cable connection were produced from (20) and plotted in Fig. 9. The terminal cost is 171.8 M£, and the route cost per unit distance maintains the same value at 0.92 M£/km for all distances up to 240 km. The detailed constituent costs are recorded in Fig. 10 and Appendix Table V. Cost data for three commercial and comparable connections, the 1.0 GW ElecLink Interconnector between UK and France, the 0.7 GW Kontek2 Interconnector between Denmark and Germany and the 0.6 GW ELMED Interconnector between Italy and Tunisia were obtained [92]–[95] and plotted as P1, P2 and P3 respectively in Fig. 9, which provides reassurance for the overall cost estimation of a VSC–HVDC system.

The cost estimation for a LFAC system based on (25) are presented in Fig. 11, Fig. 12 and Appendix Table VI. The terminal cost is 104.2 M£, and the route cost per unit distance is maintained at 1.51 M£/km for all distances up to 240 km. There are no practically realized LFAC offshore connections to use for validation. However, the costs of individual items were estimated from similar HVAC and HVDC items and these were partially validated in the comparisons of Fig. 7 and Fig. 9.

Comparison results of these three technologies are provided in Fig. 13(a) for the distance ranges 0–240 km, and a detailed view of the ranges 65–125 km given in Fig. 13(b). It can
be seen that the overall cost of a LFAC system crosses the overall cost of a HVAC system at 80 km before crossing the overall cost of HVDC at 115 km, giving a range of 35 km over which LFAC is the least-cost solution and the percentage of overall cost advantage over both HVAC and HVDC is about 10% in this case. The terminal cost of a LFAC system is approximately halfway between that of the HVAC and HVDC systems. The route cost per unit distance of a HVAC system changes several times as the cable choice changes but beyond 65 km the route of a LFAC system lies closer to a HVDC system than to a HVAC system and this condition corresponds to the cases 1 and 2 in Fig. 4. The cross-over point of HVAC and VSC–HVDC costs is at 87 km, which is close to the value expected given the commercial project data available [19]–[21] and gives reassurance that the cost curves are realistic.

D. Case Study for Higher Power Rating Connection

A wind power connection of 1.4 GW was chosen for the higher power rating case study. The minimum-cost choices of cable for each of the three schemes are recorded in Table III. The estimated overall cost and their constituent costs of each connection technology are plotted in Fig. 14–Fig. 19, and the

<table>
<thead>
<tr>
<th>System</th>
<th>Distance (km)</th>
<th>Voltage (kV)</th>
<th>Size (mm²)</th>
<th>Capability per circuit (GW)</th>
<th>Number of circuits (n_c)</th>
</tr>
</thead>
<tbody>
<tr>
<td>HVAC</td>
<td>0–30</td>
<td>400</td>
<td>1600</td>
<td>0.718–0.703</td>
<td>2</td>
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<tr>
<td></td>
<td>50–115</td>
<td>400</td>
<td>800</td>
<td>0.580–0.471</td>
<td>3</td>
</tr>
<tr>
<td></td>
<td>115–130</td>
<td>400</td>
<td>1000</td>
<td>0.503–0.458</td>
<td>3</td>
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<td>800</td>
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<td>5</td>
</tr>
<tr>
<td></td>
<td>150–170</td>
<td>220</td>
<td>800</td>
<td>0.297–0.279</td>
<td>5</td>
</tr>
<tr>
<td></td>
<td>170–195</td>
<td>220</td>
<td>800</td>
<td>0.260–0.232</td>
<td>6</td>
</tr>
<tr>
<td></td>
<td>195–215</td>
<td>220</td>
<td>800</td>
<td>0.230–0.203</td>
<td>7</td>
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<tr>
<td></td>
<td>215–230</td>
<td>220</td>
<td>800</td>
<td>0.203–0.176</td>
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<td>132</td>
<td>800</td>
<td>0.150–0.145</td>
<td>10</td>
</tr>
<tr>
<td>LFAC</td>
<td>0–200</td>
<td>400</td>
<td>800</td>
<td>0.733–0.685</td>
<td>2</td>
</tr>
<tr>
<td></td>
<td>200–240</td>
<td>400</td>
<td>1000</td>
<td>0.749–0.733</td>
<td>2</td>
</tr>
<tr>
<td>VSC-HVDC</td>
<td>0–240</td>
<td>±300</td>
<td>2000</td>
<td>1.444</td>
<td>1</td>
</tr>
</tbody>
</table>
detailed cost data are given in Appendix Table VII–Appendix Table X.

![Fig. 14. Overall cost estimate of a 1.4 GW HVAC system.](image)

![Fig. 15. Constituent costs of a 1.4 GW HVAC system.](image)

![Fig. 16. Overall cost estimate of a 1.4 GW VSC–HVDC system.](image)

![Fig. 17. Constituent costs of a 1.4 GW VSC–HVDC system.](image)

![Fig. 18. Cost analysis of a 1.4 GW LFAC system.](image)

![Fig. 19. Constituent costs of a 1.4 GW LFAC system.](image)

The comparison result for the three technologies is provided in Fig. 20(a) over distances from 0–240 km and are shown in detail over 65–89 km in Fig. 20(b). The cross-over points of a LFAC system with HVAC and VSC–HVDC are 67 km and 79 km respectively which straddle the cross-over point of HVAC and VSC–HVDC costs at 73 km for this higher power rating comparison. It is clear that the cost-effective range and overall cost advantage in the intermediate distance for a LFAC system is narrower at 1.4 GW than it was at 0.6 GW in Fig. 13. The terminal cost of a LFAC system is closer to that of a HVDC than HVAC system and its route cost per unit distance lies above halfway between HVDC than HVAC in the intermediate range from 50 km to 115 km. With reference to Fig. 4, at this higher power rating case study, the overall cost of LFAC starts to move from the cases 1 and 2 toward case 3.
The analysis of costs for a remote onshore OHL connection will also follow the decomposition shown in Fig. 5. TCC comprises the remote-end plant cost ($TCC_{rem}$), for instance at a wind farm site, and the load-end plant cost ($TCC_{loa}$). TLC consists of cost of power losses in the remote-end plant ($TLC_{rem}$) and load-end plant ($TLC_{loa}$). RCC is made up of the OHL cost ($OHC$) and compensation cost ($CPC$). RLC is the cost of power loss in the OHL.

**A. Cost Analysis and Estimate in HVAC and CSC–HVDC Systems**

The calculation and estimation for the terminal cost of HVAC and HVDC systems are based on the analysis used in the previous section. A CSC–HVDC system is selected for analysis since it is more likely to be used in the OHL connection of remote onshore wind energy than the voltage sourced alternative.

The structure of the remote-end plant and load-end plant in an OHL-based remote onshore HVAC system are similar to the onshore plant in the offshore connection case, and for which the terminal capital costs and terminal power loss costs were analyzed in (2) and (6) respectively. For a CSC–HVDC system, the estimation for its terminal capital cost and terminal power loss cost can build on (24) and (8) respectively with corresponding parameter adjustments. Thus, the calculation for the terminal cost of OHL-based HVAC and CSC–HVDC systems are provided in (28) and (29).

$$T_{C_{HVAC}} = TCC_{HVAC} + TLC_{HVAC}$$

$$= TCC_{remHVAC} + TCC_{loaHVAC} + TLC_{remHVAC} + TLC_{loaHVAC}$$

$$= 2 \cdot 0.02621 S_{TT}^{0.7513} + 0.00911 S_{TT}^{0.7513} + 0.00906 \cdot \left( S_{TT} - \frac{0.994 S_{TT}^{2}}{V_{on}^{2}} \cdot \frac{r_{o} \cdot l_{o}}{n_{c_{o}}} \right)$$

(28)

$$T_{C_{CSCHVDC}} = TCC_{CSCHVDC} + TLC_{CSCHVDC}$$

$$= TCC_{remCSCHVDC} + TCC_{loaCSCHVDC} + TLC_{remCSCHVDC} + TLC_{loaCSCHVDC}$$

$$= 2 \cdot 0.05926 S_{TT}^{0.7513} + 0.01331 S_{TT}^{0.7513} + 0.01319 \cdot \left( S_{TT} - \frac{0.496 S_{TT}^{2}}{V_{on}^{2}} \cdot \frac{r_{o} \cdot l_{o}}{n_{c_{o}}} \right)$$

(29)

The main differences in analysis between the remote onshore OHL case and offshore cable case lies in the route cost. The analysis of transmission capability for a HVAC system is different because for the subsea cable, the effects of the shunt capacitive susceptance dominate, whereas for OHL the effects of the series inductive reactance dominate. The thermal limit described in (30) and the stability limit in (31) are the key determinants of the active power transfer capability for a given OHL-based HVAC system [39], [96]. The thermal limit applies over short distances and the stability limit for longer distances.

$$P_{thl} = 3 \frac{V_{on}}{\sqrt{3}} I_{on} = \sqrt{3} V_{on} I_{on}$$

(30)

$$P_{stl} = 3 \left( \frac{V_{on}}{\sqrt{3}} \right)^{2} \cdot \frac{1}{X_{o}} = \frac{V_{on}^{2}}{2 \pi f_{a} \cdot L \cdot l_{o}}$$

(31)

where $P_{thl}$ and $P_{stl}$ are the thermal limit and stability limit in OHL transmission, $V_{on}$ and $I_{on}$ are the OHL nominal voltage and current, $X_{o}$ is the series reactance per kilometre, $L$ is the OHL inductance per kilometer and $l_{o}$ is the OHL length.

The parameters of a typical OHL in a HVAC system are listed in Appendix Table X. Their capital costs and operational power loss costs follow (14) and (15) respectively and the calculation for the route cost of an OHL-based HVAC system is given in (32).

$$R_{C_{HVAC}} = R_{C_{CSCHVDC}} + R_{C_{HVDC}} = c_{o} \cdot l_{o} \cdot n_{c_{o}} + 1.51767 \cdot \left( \frac{0.994 S_{TT}}{V_{on}^{2}} \right)^{2} \cdot \frac{r_{o} \cdot l_{o}}{n_{c_{o}}}$$

(32)

where $c_{o}$ is the OHL cost per set including supply and installation, $n_{c_{o}}$ is the number of OHL parallel circuits and $r_{o}$ is the OHL resistance per kilometer. The stability limit imposed by the inductive reactance in HVAC has no relevance to the HVDC case. A thermal limit does still apply but here HVDC has an advantage because the line can be used consistently at its peak voltage and does not suffer an effective/peak ratio underutilization. The parameters of the typical CSC–HVDC OHL are listed in
Appendix Table XI, and the route cost for an OHL-based CSC–HVDC system is given by (33) based on (14) and (17).

\[ RC_{CSCHVDC} = R_{CC_{CSCHVDC}} + R_{LC_{CSCHVDC}} = c_o \cdot l_o \cdot n_{c_o} + 0.75884 \cdot \left( \frac{0.991 S_{TT}}{V_{on}} \right)^2 \frac{r_o \cdot l_o}{n_{c_o}} \]  

(33)

Summing the terminal costs and route costs yields the estimates of overall costs. Adding (28) and (32) gives (34) for a HVAC system and adding (29) and (33) gives (35) for a CSC–HVDC system.

\[ C_{HVAC} = TC_{HVAC} + RC_{HVAC} = 2 \cdot 0.02621 S_{TT}^{0.7513} + 0.00911 S_{TT} + 0.00906 \cdot \left( S_{TT} - \frac{0.994 S_{TT}^2}{V_{on}^2} \frac{r_o \cdot l_o}{n_{c_o}} \right) + c_o \cdot l_o \cdot n_{c_o} + 1.51767 \cdot \left( \frac{0.994 S_{TT}}{V_{on}} \right)^2 \frac{r_o \cdot l_o}{n_{c_o}} \]  

(34)

\[ C_{CSCHVDC} = TC_{CSCHVDC} + RC_{CSCHVDC} = 2 \cdot 0.05926 S_{TT} + 0.01331 S_{TT} + 0.01319 \cdot \left( S_{TT} - \frac{0.996 S_{TT}^2}{V_{on}^2} \frac{r_o \cdot l_o}{n_{c_o}} \right) + c_o \cdot l_o \cdot n_{c_o} + 0.75884 \cdot \left( \frac{0.991 S_{TT}}{V_{on}} \right)^2 \frac{r_o \cdot l_o}{n_{c_o}} \]  

(35)

B. Cost Analysis and Estimate in a LFAC System

Building on the analysis in (28) and (29) for HVAC and CSC–HVDC systems, the terminal cost for a LFAC system can be estimated by (36).

\[ TC_{LFAC} = TCC_{LFAC} + TLC_{LFAC} = TCC_{remLFAC} + TCC_{loadLFAC} + TLC_{remLFAC} + TLC_{loadLFAC} = 0.02621 \sqrt{3} S_{TT}^{0.7513} + 0.05926 S_{TT} + 0.00911 S_{TT} + 0.01323 \cdot \left( S_{TT} - \frac{0.994 S_{TT}^2}{V_{on}^2} \frac{r_o \cdot l_o}{n_{c_o}} \right) \]  

(36)

For the route cost of LFAC, the price per unit distance of the OHL is assumed to be the same as for HVAC but, as (31) suggests, the stability limit in LFAC is expected to be at a distance three times that of HVAC assuming a frequency reduction to one third. The parameters of onshore OHL LFAC can be taken from the simulation and experimental results [39], [42], [97], and are presented in Appendix Table XII, and the route cost for an OHL-based LFAC system is provided in (37).

\[ RC_{LFAC} = R_{CC_{LFAC}} + R_{LC_{LFAC}} = c_o \cdot l_o \cdot n_{c_o} + 1.51767 \cdot \left( \frac{0.994 S_{TT}}{V_{on}} \right)^2 \frac{r_o \cdot l_o}{n_{c_o}} \]  

(37)

Adding the terminal cost and route cost of (36) and (37), yields the overall cost for a LFAC system as given in (38).

\[ C_{LFAC} = TC_{LFAC} + RC_{LFAC} = 0.02621 \sqrt{3} S_{TT}^{0.7513} + 0.05926 S_{TT} + 0.00911 S_{TT} + 0.01323 \cdot \left( S_{TT} - \frac{0.994 S_{TT}^2}{V_{on}^2} \frac{r_o \cdot l_o}{n_{c_o}} \right) + c_o \cdot l_o \cdot n_{c_o} + 1.51767 \cdot \left( \frac{0.994 S_{TT}}{V_{on}} \right)^2 \frac{r_o \cdot l_o}{n_{c_o}} \]  

(38)

C. Case Study for Lower Power Rating Connection

A wind power connection of 3.0 GW was selected as an example of a relatively lower power rating case study. Following Sections III-C and III-D, the choice of voltage rating and OHL current capacity should be re-examined at each distance for AC schemes and a minimum-cost choice can be made from the options available. In this study, the available OHL are given in Appendix Table X for a HVAC system and Appendix Table XII for a LFAC system. According to the analysis in (30) and (31), it is the thermal limit that is relevant for HVAC and LFAC systems applied over short distances, and beyond this, the stability limit is the constraining factor. The change-over distance between the limitations is greater for LFAC than HVAC, and this is clear from the results in Fig. 21 and with the parameters in Appendix Table X and Appendix Table XII. It can be seen that a LFAC system has a clear advantage over a HVAC system due to the reduced impact of skin effect for the thermal limit and the one-third series reactance which extends the stability limit. It also illustrates that since the thermal limit is irrelevant to the transmission distance while the reliability limit is relevant, the constant transmission capacity over shorter distances and the declining capacity over longer distances can be observed for OHL-based AC schemes. For a DC scheme, a CSC–HVDC system does not suffer from effects of the series inductive reactance and the transmission capability is set by the thermal limit at all distances.

Fig. 21. Transmission capability of some typical OHL in HVAC and LFAC.
TABLE IV

<table>
<thead>
<tr>
<th>System</th>
<th>Distance (km)</th>
<th>Voltage (kV)</th>
<th>Capability per circuit (GW)</th>
<th>Number of circuits ($n_c$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>HVAC</td>
<td>0–645</td>
<td>750</td>
<td>5.090–3.007</td>
<td>1</td>
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<tr>
<td></td>
<td>645–1290</td>
<td>750</td>
<td>3.007–1.504</td>
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<td></td>
<td>1290–1500</td>
<td>750</td>
<td>1.504–1.293</td>
<td>3</td>
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<td>LFAC</td>
<td>0–1500</td>
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<td>6.819–3.879</td>
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<td>CSC-HVDC</td>
<td>0–1500</td>
<td>±600</td>
<td>6.564</td>
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in Fig. 22–Fig. 27 and further details are provided in Appendix Table XIII–Appendix Table XV.

Fig. 22. Overall cost estimate of a 3.0 GW HVAC system.

Fig. 23. Constituent costs of a 3.0 GW HVAC system.

Fig. 24. Overall cost estimate of a 3.0 GW CSC–HVDC system.

Fig. 25. Constituent costs of a 3.0 GW HVDC system.

Fig. 26. Overall cost estimate of a 3.0 GW LFAC system.

The comparison result is given in Fig. 28(a) for the distance from 0–1500 km, and a detailed view of 600-1000 km is provided in Fig. 28(b). The cross-over points of a LFAC system with HVAC and CSC–HVDC are 650 km and 960 km respectively, giving a cost-effective range of 310 km in the intermediate distance and the overall cost advantage over both HVAC and HVDC is close to 15% in this case study. It can be seen that the terminal cost of a LFAC system is approximately midway between that of the HVAC and HVDC systems. The route cost is a relatively complex picture because the unit cost of AC increases with distance as the stability limit grows in significance and this happens more so in standard frequency than low frequency. For distances below 650 km, the route cost per unit distance of LFAC and HVAC are similar but beyond that the route cost of HVAC rises rapidly as parallel circuits are required whereas a single circuit suffices for LFAC all the way to 1500 km and so the route cost of LFAC lies closer to HVDC than to HVAC after 650 km. The overall cost of a LFAC system in this OHL-based lower power connection belongs to a situation between case 1 and case 2 as shown in Fig. 4. The break-even point of HVAC and CSC–HVDC is 700 km, which reaches good agreement with the practical result in the commercial OHL-based remote onshore connection projects [22], [23].
Fig. 27. Constituent costs of a 3.0 GW LFAC system.

Fig. 28. 3.0 GW overall cost comparison among HVAC, CSC–HVDC and LFAC systems. (a) Full distance comparison. (b) Detailed view for the cross-over and break-even points.

D. Case Study for Higher Power Rating Connection

A power connection of 5.0 GW was chosen for the higher power rating case study. The minimum-cost choices of OHL for each of the three technologies over 0–1500 km are presented in Table V.

The estimated overall costs of each technology choice at 5.0 GW connection are plotted in Fig. 29–Fig. 34 and the details of the constituent costs are given in Appendix Table XVIII.

The comparison results are provided in Fig. 35(a) over the whole distance with details over 750–1000 km in Fig. 35(b). It shows the cross-over points of the LFAC overall cost with HVAC and CSC–HVDC are 775 km and 965 km respectively which straddle the cross-over point of HVAC and CSC–HVDC overall costs at 790 km. The cost-effective range for LFAC is narrowed to 190 km at this 5.0 GW comparison whereas it was 310 km at 3.0 GW comparison, and the percentage of overall cost advances is also reduced in this case study. In this higher power connection case, the terminal cost of a LFAC system is between that of HVAC and HVDC but becomes closer to HVDC. The unit route cost per unit distance of LFAC is higher than the midpoint of the HVAC and CSC–HVDC systems in the intermediate range and shows one increase at
1164 km because of a need to move to two parallel circuits. This comparison results belong to a situation between the case 2 and case 3 of Fig. 4.

V. DISCUSSION OF COST-EFFECTIVE DISTANCE

The cross-over points of overall costs between HVAC, HVDC and LFAC in the four case studies of wind energy connections (lower power rating and higher power rating, offshore cable connection and remote onshore OHL connection) are summarized in Table VI. The range of cost-effective distance for the LFAC system is also recorded.

First, it can be seen that there is indeed a cost-effective range for the LFAC system over both HVAC and HVDC technologies in the intermediate distance for all the four cases of wind energy connection.

Second, it can be determined that the cost-effective range narrows with increasing power rating for both offshore cable connections and remote onshore OHL connections. The narrowing of the cost-effective range with an increasing power rating can be explained by reference to the detailed constituent
TABLE VI
SUMMARY OF CROSS-OVER POINTS AND LFAC COST-EFFECTIVE RANGES

<table>
<thead>
<tr>
<th>Case study</th>
<th>Cross-over points of overall costs</th>
<th>LFAC cost-effective ranges</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cable 0.6 GW</td>
<td>80 km 87 km 115 km</td>
<td>35 km (14.5% of full length)</td>
</tr>
<tr>
<td>Cable 1.4 GW</td>
<td>67 km 73 km 79 km</td>
<td>12 km (5.0% of full length)</td>
</tr>
<tr>
<td>OHL 3.0 GW</td>
<td>650 km 700 km 960 km</td>
<td>310 km (20.7% of full length)</td>
</tr>
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<td>OHL 5.0 GW</td>
<td>775 km 790 km 965 km</td>
<td>190 km (12.7% of full length)</td>
</tr>
</tbody>
</table>

cost in Appendix Table VII to Appendix Table IX and Appendix Table XVI to Appendix Table XVIII. This reveals that the LFAC terminal cost approaches that of HVDC rather than HVAC at higher power case because of the expense of the AC-AC converter and LF transformer. Also, at higher power rating, the advantages of DC operations, rather than AC (standard frequency and low frequency) of both cable and OHL are greater in terms of both transmission capability and route cost.

Third, it can also be observed that the overall costs of the LFAC system are more competitive in the remote onshore OHL cases than the offshore cable cases and this is for both lower and higher power rating connections. The cost-effective ranges are larger for OHL cases than for cable cases both in absolute terms and relative to the longest distances that might be built. These differences can be explained by the different mechanisms that limit transmission capability of LFAC in cables and OHL. This will be analyzed further in the next section.

VI. TRANSMISSION CAPABILITY OF THE LFAC SYSTEM

For offshore cable case, the transmission capability is dependent on the analysis of (12). The ratio of active power transfer capability of the LFAC system to HVAC system can be expressed as (39). Taking skin effect into consideration, the rated current of a given cable under the LFAC system would be about 1.2 greater than under the HVAC system [43], [80]. In this manner, (39) can be simplified as (40) and this difference can be observed by the starting points in Fig. 6.

\[
P_{c-LFAC} = \frac{1}{\sqrt{\left(\frac{\sqrt{3} V_{cn-LFAC}}{I_{ch-LFAC}}\right)^2 - \frac{1}{4} \left[V_{cn-LFAC} \cdot 2\pi f_{n-LFAC} \cdot C \cdot l_{c}\right]^2}}
\]

\[
P_{c-LFAC} = \frac{\sqrt{3} I_{ch-LFAC}}{4} \left[\frac{V_{cn-LFAC} \cdot 2\pi f_{n-LFAC} \cdot C \cdot l_{c}}{4} \right]^2 - \frac{1}{4} \left[V_{cn-LFAC} \cdot 2\pi f_{n-LFAC} \cdot C \cdot l_{c}\right]^2}
\]

From (40), this ratio has a minimum value of 1.2 if no compensation current is needed and the ratio will increase with the compensation current. In short distance transmission, the compensation current would not normally exceed the active power current [21], [57], [63] which yields a maximum ratio of 1.7 as given by (41), so the ratio of active power transfer capability of the LFAC system to HVAC system would be between 1.2 and 1.7.

\[
P_{c-LFAC} = \frac{4.32 I_{ch-LFAC} \cdot V_{cn-LFAC}^2 - \frac{1}{36} \left(\sqrt{3} I_{ch-LFAC}\right)^2}{3 I_{cn-LFAC} - \frac{1}{4} \left(\sqrt{3} I_{ch-LFAC}\right)^2}
\]

\[
P_{c-HVAC} = \frac{4.32 I_{ch-HVAC} \cdot V_{cn-HVAC}^2 - \frac{1}{36} \left(2\sqrt{3} I_{off-HVAC}\right)^2}{3 I_{cn-HVAC} - \frac{1}{4} \left(2\sqrt{3} I_{off-HVAC}\right)^2}
\]

\[
P_{n-LFAC} = \frac{4.32 I_{ch-LFAC} \cdot V_{cn-LFAC}^2 - \frac{1}{36} \left(\sqrt{3} I_{ch-LFAC}\right)^2}{3 I_{cn-LFAC} - \frac{1}{4} \left(\sqrt{3} I_{ch-LFAC}\right)^2}
\]

\[
P_{n-HVAC} = \frac{4.32 I_{ch-HVAC} \cdot V_{cn-HVAC}^2 - \frac{1}{36} \left(2\sqrt{3} I_{off-HVAC}\right)^2}{3 I_{cn-HVAC} - \frac{1}{4} \left(2\sqrt{3} I_{off-HVAC}\right)^2}
\]

where \(I_{ch}\) is the capacitive charging current in the subsea cable and \(I_{off}\) is the offshore compensation current.

For the remote onshore OHL case, the same assumption for skin effect is made for direct comparison with the cable case. In short distances, the OHL transmission capability is thermally limited and the ratio between the LFAC to HVAC system is 1.2 as the starting points shown in Fig. 21. When the distance increases beyond some critical point, the OHL transmission capability is governed by the stability limit which is the curved section of Fig. 21 based on the analysis in (31), and the ratio between the LFAC to HVAC system becomes 3 as shown in (42).

\[
P_{n-LFAC} \leq \frac{V_{on}^2}{2\pi f_{n-LFAC} \cdot L \cdot I_{o}} = \frac{V_{on}^2}{2\pi f_{n-HVAC} \cdot L \cdot I_{o}} = 3
\]

Comparing the offshore cable and remote onshore OHL cases, the LFAC system could give a greater transmission capability enhancement in OHL than that in cables, and as a result, the benefit-cost ratio will be better for the OHL system than cable system, which may imply that LFAC would find more potential in remote onshore OHL applications than offshore cable applications.

VII. CONCLUSION

This paper presented an in-depth analysis for the overall cost of a LFAC system and then gave an extensive comparison with HVAC and HVDC to explore the distances range of over which LFAC is more cost-effective over both HVAC and HVDC in connections of offshore and remote onshore wind energy.

First, the overall cost of a LFAC system was decomposed into constituent costs of terminal and route costs and further decomposed into capital and operational costs. Then, equations for evaluating these constituent costs were elaborated. Given the absence of commercial LFAC projects that might yield cost data, parameters for the cost equations for the LFAC system were estimated with reference to similar equipment used in HVDC and HVAC practices. Lastly, the cost estimation algorithm compared different choices of operating voltage, conductor size and number of circuits in order to identify the lowest cost combination at each distance for the specified
power transfer and provide a fair comparison for these three technology choices.

Graphs of costs against distance for offshore cable and remote onshore OHL cases have been created. The results have demonstrated that the LFAC system does possess distance ranges over which it is expected to be more cost-effective than both HVAC and HVDC systems. The overall cost advantage of LFAC is generally larger in the OHL connection of remote onshore wind energy than the cable connection of offshore wind energy, and it is more competitive for a lower power rating connection than higher power rating connection in both the cable and OHL cases.

### APPENDIX

#### Appendix TABLE I
PARAMETERS OF THE COMMON CABLES IN A HVAC SYSTEM

<table>
<thead>
<tr>
<th>Nominal Voltage $V_n$ (kV)</th>
<th>Cable size (mm²)</th>
<th>Resistance $r_c$ (mΩ/km)</th>
<th>Capacitance $C$ (nF/km)</th>
<th>Nominal Current $I_n$ (A)</th>
<th>Cables cost $c_c$ (k£/km)</th>
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<tr>
<td>132</td>
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#### Appendix TABLE II
PARAMETERS OF THE COMMON CABLES IN A VSC–HVDC SYSTEM

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<th>Nominal Voltage $V_n$ (kV)</th>
<th>Cable size (mm²)</th>
<th>Resistance $r_c$ (mΩ/km)</th>
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<th>Nominal Current $I_n$ (A)</th>
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#### Appendix TABLE III
PARAMETERS OF THE COMMON CABLES IN A LFAC SYSTEM

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<th>Nominal Voltage $V_n$ (kV)</th>
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#### Appendix TABLE IV
DETAILED CONSTITUENT COST DATA FOR A 0.6 GW HVAC SYSTEM

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#### Appendix TABLE V
DETAILED CONSTITUENT COST DATA FOR A 0.6 GW VSC–HVDC SYSTEM

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#### Appendix TABLE VI
DETAILED CONSTITUENT COST DATA FOR A 0.6 GW LFAC SYSTEM

<table>
<thead>
<tr>
<th>LFAAC</th>
<th>Transmission Distance / (km)</th>
</tr>
</thead>
<tbody>
<tr>
<td>TCC</td>
<td>0.0</td>
</tr>
<tr>
<td></td>
<td>20.0</td>
</tr>
<tr>
<td></td>
<td>40.0</td>
</tr>
<tr>
<td></td>
<td>60.0</td>
</tr>
<tr>
<td></td>
<td>80.0</td>
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</tbody>
</table>
### Appendix TABLE VII
**Detailed Constituent Cost Data for a 1.4 GW HVAC System**

<table>
<thead>
<tr>
<th>HVAC</th>
<th>Transmission Distance / (km)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>0</td>
</tr>
<tr>
<td>Cost (ME)</td>
<td></td>
</tr>
<tr>
<td>TCC</td>
<td>73.9</td>
</tr>
<tr>
<td>TLC</td>
<td>24.4</td>
</tr>
<tr>
<td>RCC</td>
<td>0</td>
</tr>
<tr>
<td>RLC</td>
<td>0</td>
</tr>
<tr>
<td>C</td>
<td>99.5</td>
</tr>
</tbody>
</table>

### Appendix TABLE VIII
**Detailed Constituent Cost Data for a 1.4 GW VSC–HVDC System**

<table>
<thead>
<tr>
<th>HVDC</th>
<th>Transmission Distance / (km)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>0</td>
</tr>
<tr>
<td>Cost (ME)</td>
<td></td>
</tr>
<tr>
<td>TLC</td>
<td>74.4</td>
</tr>
<tr>
<td>RCC</td>
<td>0</td>
</tr>
<tr>
<td>C</td>
<td>366.4</td>
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</tbody>
</table>

### Appendix TABLE IX
**Detailed Constituent Cost Data for a 1.4 GW LFAC System**

<table>
<thead>
<tr>
<th>LFAC</th>
<th>Transmission Distance / (km)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>0</td>
</tr>
<tr>
<td>Cost (ME)</td>
<td></td>
</tr>
<tr>
<td>TCC</td>
<td>201.4</td>
</tr>
<tr>
<td>TLC</td>
<td>33.3</td>
</tr>
<tr>
<td>RCC</td>
<td>0</td>
</tr>
<tr>
<td>RLC</td>
<td>0</td>
</tr>
<tr>
<td>C</td>
<td>231.7</td>
</tr>
</tbody>
</table>

### Appendix TABLE X
**Parameters of the Typical OHL in a HVAC System**

<table>
<thead>
<tr>
<th>OHL type</th>
<th>Nominal Voltage $V_n$ (kV)</th>
<th>Aluminium area (mm$^2$)</th>
<th>Nominal current $I_n$ (A)</th>
<th>Resistance $r_o$ (Ω/km)</th>
<th>Reactance $X_o$ (Ω/km)</th>
<th>OHL cost per circuit $c_o$ (£/km)</th>
</tr>
</thead>
<tbody>
<tr>
<td>562-AL1/49-ST1A</td>
<td>380</td>
<td>2 x 562</td>
<td>2100</td>
<td>0.029</td>
<td>0.33</td>
<td>165</td>
</tr>
<tr>
<td>494-AL1/34-ST1A</td>
<td>500</td>
<td>3 x 494</td>
<td>2850</td>
<td>0.022</td>
<td>0.30</td>
<td>245</td>
</tr>
<tr>
<td>653-AL1/45-ST1A</td>
<td>750</td>
<td>4 x 563</td>
<td>4380</td>
<td>0.012</td>
<td>0.29</td>
<td>370</td>
</tr>
</tbody>
</table>

### Appendix TABLE XI
**Parameters of the Typical OHL in a CSC–HVDC System**

<table>
<thead>
<tr>
<th>OHL type</th>
<th>Nominal Voltage $V_n$ (kV)</th>
<th>Aluminium area (mm$^2$)</th>
<th>Nominal current $I_n$ (A)</th>
<th>Resistance $r_o$ (Ω/km)</th>
<th>Reactance $X_o$ (Ω/km)</th>
<th>OHL cost per circuit $c_o$ (£/km)</th>
</tr>
</thead>
<tbody>
<tr>
<td>562-AL1/49-ST1A</td>
<td>±300</td>
<td>2 x 562</td>
<td>2620</td>
<td>0.019</td>
<td>0.11</td>
<td>165</td>
</tr>
<tr>
<td>494-AL1/34-ST1A</td>
<td>±400</td>
<td>3 x 494</td>
<td>3560</td>
<td>0.015</td>
<td>0.10</td>
<td>245</td>
</tr>
<tr>
<td>653-AL1/45-ST1A</td>
<td>±600</td>
<td>4 x 563</td>
<td>5470</td>
<td>0.0079</td>
<td>0.097</td>
<td>370</td>
</tr>
</tbody>
</table>

### Appendix TABLE XII
**Parameters of the Typical OHL in a LFAC System**

<table>
<thead>
<tr>
<th>OHL type</th>
<th>Nominal Voltage $V_n$ (kV)</th>
<th>Aluminium area (mm$^2$)</th>
<th>Nominal current $I_n$ (A)</th>
<th>Resistance $r_o$ (Ω/km)</th>
<th>Reactance $X_o$ (Ω/km)</th>
<th>OHL cost per circuit $c_o$ (£/km)</th>
</tr>
</thead>
<tbody>
<tr>
<td>562-AL1/49-ST1A</td>
<td>380</td>
<td>2 x 562</td>
<td>2520</td>
<td>0.019</td>
<td>0.11</td>
<td>165</td>
</tr>
<tr>
<td>494-AL1/34-ST1A</td>
<td>500</td>
<td>3 x 494</td>
<td>3420</td>
<td>0.015</td>
<td>0.10</td>
<td>245</td>
</tr>
<tr>
<td>653-AL1/45-ST1A</td>
<td>750</td>
<td>4 x 563</td>
<td>5470</td>
<td>0.0079</td>
<td>0.097</td>
<td>370</td>
</tr>
</tbody>
</table>

### Appendix TABLE XIII
**Detailed Constituent Cost Data for a 3.0 GW HVAC System**

<table>
<thead>
<tr>
<th>HVAC</th>
<th>Transmission Distance / (km)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>0</td>
</tr>
<tr>
<td>Cost (ME)</td>
<td></td>
</tr>
<tr>
<td>TLC</td>
<td>55.5</td>
</tr>
<tr>
<td>RCC</td>
<td>0</td>
</tr>
<tr>
<td>RLC</td>
<td>0</td>
</tr>
<tr>
<td>C</td>
<td>92.6</td>
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</tbody>
</table>
Appendix TABLE XIV
DETAILED CONSTITUENT COST DATA FOR A 3.0 GW CSC–HVDC SYSTEM

<table>
<thead>
<tr>
<th>HVDC</th>
<th>Transmission Distance (km)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>0</td>
</tr>
<tr>
<td>TCC</td>
<td>354</td>
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<tr>
<td>TLC</td>
<td>37.4</td>
</tr>
<tr>
<td>RCC</td>
<td>0</td>
</tr>
<tr>
<td>C</td>
<td>0</td>
</tr>
</tbody>
</table>

Appendix TABLE XV
DETAILED CONSTITUENT COST DATA FOR A 3.0 GW LFAC SYSTEM

<table>
<thead>
<tr>
<th>LFAC</th>
<th>Transmission Distance (km)</th>
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</thead>
<tbody>
<tr>
<td></td>
<td>0</td>
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<tr>
<td>TCC</td>
<td>209.0</td>
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<tr>
<td>TLC</td>
<td>65.0</td>
</tr>
<tr>
<td>RCC</td>
<td>0</td>
</tr>
<tr>
<td>C</td>
<td>321</td>
</tr>
</tbody>
</table>

Appendix TABLE XVI
DETAILED CONSTITUENT COST DATA FOR A 5.0 GW HVAC SYSTEM

<table>
<thead>
<tr>
<th>HVAC</th>
<th>Transmission Distance (km)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>0</td>
</tr>
<tr>
<td>TCC</td>
<td>55.7</td>
</tr>
<tr>
<td>TLC</td>
<td>88.8</td>
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<tr>
<td>RCC</td>
<td>0</td>
</tr>
<tr>
<td>C</td>
<td>146.7</td>
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</tbody>
</table>

Appendix TABLE XVII
DETAILED CONSTITUENT COST DATA FOR A 5.0 GW CSC–HVDC SYSTEM

<table>
<thead>
<tr>
<th>HVDC</th>
<th>Transmission Distance (km)</th>
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</thead>
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<td></td>
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</tr>
<tr>
<td>TCC</td>
<td>590</td>
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<tr>
<td>TLC</td>
<td>132.4</td>
</tr>
<tr>
<td>RCC</td>
<td>0</td>
</tr>
<tr>
<td>C</td>
<td>722.4</td>
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</table>

Appendix TABLE XVIII
DETAILED CONSTITUENT COST DATA FOR A 5.0 GW LFAC SYSTEM

<table>
<thead>
<tr>
<th>LFAC</th>
<th>Transmission Distance (km)</th>
</tr>
</thead>
<tbody>
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<td></td>
<td>0</td>
</tr>
<tr>
<td>TCC</td>
<td>246.7</td>
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<tr>
<td>TLC</td>
<td>115.7</td>
</tr>
<tr>
<td>RCC</td>
<td>0</td>
</tr>
<tr>
<td>C</td>
<td>455.1</td>
</tr>
</tbody>
</table>

REFERENCES


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