

Dust destruction and survival in the Cassiopeia A reverse shock

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ABSTRACT

Core-collapse supernovae (CCSNe) produce large ($\gtrsim 0.1 M_{\odot}$) masses of dust, and are potentially the primary source of dust in the Universe, but much of this dust may be destroyed before reaching the interstellar medium. Cassiopeia A (Cas A) is the only supernova remnant where an observational measurement of the dust destruction efficiency in the reverse shock is possible at present. We determine the pre- and post-shock dust masses in Cas A using a substantially improved dust emission model. In our preferred models, the unshocked ejecta contains $0.6\text{--}0.8 M_{\odot}$ of $0.1 \mu\text{m}$ silicate grains, while the post-shock ejecta has $0.02\text{--}0.09 M_{\odot}$ of $5\text{--}10 \text{ nm}$ grains in dense clumps, and $2 \times 10^{-3} M_{\odot}$ of $0.1 \mu\text{m}$ grains in the diffuse X-ray emitting shocked ejecta. The implied dust destruction efficiency is 74–94 per cent in the clumps and 92–98 per cent overall, giving Cas A a final dust yield of $0.05\text{--}0.30 M_{\odot}$. If the unshocked ejecta grains are larger than $0.1 \mu\text{m}$, the dust masses are higher, the destruction efficiencies are lower, and the final yield may exceed $0.5 M_{\odot}$. As Cas A has a dense circumstellar environment and thus a much stronger reverse shock than is typical, the average dust destruction efficiency across all CCSNe is likely to be lower, and the average dust yield higher. This supports a mostly stellar origin for the cosmic dust budget.

Key words: supernovae: individual: Cassiopeia A – dust, extinction – ISM: evolution – ISM: supernova remnants.

1 INTRODUCTION

The presence of large masses of interstellar dust in high-redshift galaxies (Bertoldi et al. 2003; Priddey et al. 2003; Watson et al. 2015), less than a Gyr after the big bang, requires a mechanism for rapid dust production. Core-collapse supernovae (CCSNe) have been suggested as potential sources of this dust, which would require an average dust yield of $\gtrsim 0.1 M_{\odot}$ per SN to explain the observationally derived dust masses (Morgan & Edmunds 2003; Dwek, Galliano & Jones 2007). Far-infrared (IR) observations of supernova remnants (SNRs) have detected quantities of cold ejecta dust comparable to this value (Matsuura et al. 2015; De Looze et al. 2017, 2019; Chawner et al. 2019, 2020), as have investigations of spectral line asymmetries (Bevan, Barlow & Milisavljevic 2017; Bevan et al. 2019, 2020), but the final dust yield enriching the interstellar medium (ISM) depends on how much of this newly formed dust can survive the reverse shock. With a reverse-shock dust destruction efficiency of $f_{\text{dest}} \lesssim 50$ per cent, De Looze et al. (2020) find that CCSNe are the dominant producers of dust over the history of the Universe, whereas Galliano et al. (2021), with a maximum SN dust yield of $\sim 0.03 M_{\odot}$ and best-fitting value of $7 \times 10^{-3} M_{\odot}$ (corresponding to $f_{\text{dest}} \gtrsim 90$ per cent for typically observed dust masses), find them to be unimportant except at very low metallicity. Both studies treat f_{dest} as a free parameter (implicitly, in the case of Galliano et al. 2021) when fitting chemical evolution models to observed galaxy

properties; an independent constraint on f_{dest} is necessary in order to break model degeneracies and further our understanding of cosmic dust evolution.

Simulations of dust destruction in SNR reverse shocks vary from almost complete destruction of the newly formed dust to almost complete survival; Kirchschlager et al. (2019) find reported values in the literature ranging from $f_{\text{dest}} \sim 1$ to 100 per cent, with their own values falling towards the higher end of this range. The results are highly sensitive to the choice of input physics, both relating to the large-scale hydrodynamics of the SNR, and the microphysics of the dust grains. While grains with radii of $a \gtrsim 0.1 \mu\text{m}$ were previously thought to be resistant to sputtering, and would thus mostly survive in the ISM (Nozawa et al. 2007), the inclusion of shattering in grain–grain collisions makes f_{dest} strongly (and non-linearly) dependent on the initial size distribution and grain composition (Kirchschlager et al. 2019). Additional complications, such as departures from spherical symmetry in the ejecta (Kirchschlager et al. 2019; Slavin et al. 2020) and a potentially non-uniform surrounding medium (Martínez-González et al. 2019), have only recently begun to be addressed, with no clear consensus on the value (or range of values) f_{dest} should take.

Cassiopeia A (Cas A) is one of few SNRs with a developed reverse shock, and is certainly the best studied of those. Barlow et al. (2010) found that the far-IR spectral energy distribution (SED) required the presence of $\gtrsim 0.1 M_{\odot}$ of dust in the SN ejecta. Using a more complex, spatially resolved dust model, accounting for unrelated foreground emission from the ISM and multiple SNR dust temperature components, De Looze et al. (2017) found

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Table 1. Adopted gas masses, electron and ionic densities, temperatures, and dominant ionic species for the three components in Cas A.

| Component | $M_{\text{gas}}(M_{\odot})$ | $n_i(\text{cm}^{-3})$ | $n_e(\text{cm}^{-3})$ | $T_i(\text{K})$ | $T_e(\text{K})$ | Ion | Ref. |
|-----------|-----------------------------|-----------------------|-----------------------|--------------------|--------------------|-----|-------------------|
| Pre-shock | 0.53 | 100 | 100 | 100 | 100 | O | (1), (2), and (3) |
| Clumped | 0.59 | 480 | 480 | 10^4 | 10^4 | O | (4) and (5) |
| Diffuse | 1.68 | 7.8 | 61 | 7.05×10^8 | 5.22×10^6 | O | (6) |

Note. References: (1) This work, (2) Smith et al. (2009), (3) Raymond et al. (2018), (4) Priestley et al. (2019), (5) Docenko & Sunyaev (2010), and (6) Willingale et al. (2003).

$\sim 0.6 M_{\odot}$ of cold (~ 30 K) silicate grains located within the radius of the reverse shock, in addition to a smaller mass ($\sim 0.01 M_{\odot}$) of warmer dust. In Priestley, Barlow & De Looze (2019), we used models of dust heating in the various ejecta components to fit the IR SED and determine the pre- and post-shock dust masses in Cas A. Combined with estimates of the corresponding gas masses, we found dust-to-gas (DTG) mass ratios of 0.2 and 0.1 in the pre- and post-shock ejecta clumps, respectively, providing an observational estimate of $f_{\text{dest}} \sim 50$ per cent for this object. However, several of the assumptions underlying this result have since been cast into some doubt, particularly regarding the grain size distribution (Priestley et al. 2020) and the gas mass in the unshocked ejecta (Laming & Temim 2020). In this paper, we revisit the Priestley et al. (2019) model of the Cas A dust emission, making numerous improvements to both the physics and the fitting procedure, in order to derive an updated observational estimate of f_{dest} for the only object for which this is presently feasible.

2 METHOD

2.1 Physical conditions in Cas A

In Priestley et al. (2019), we divided the Cas A SNR into four physical components: the unshocked ejecta (‘pre-shock’), the clumped ejecta that has passed through the reverse shock (‘clumped’), the lower-density, X-ray emitting shocked ejecta (‘diffuse’), and the circumstellar material (CSM) heated by the forward shock (‘blastwave’). The diffuse and blastwave components produced very similar dust SEDs peaking in the mid-IR, which the available data in this region cannot reliably distinguish. In the updated analysis, we assume the CSM contains no dust, and therefore ignore the blastwave component. Dust is far more likely to be present in the highly metal-enriched ejecta than in the mostly hydrogen CSM, and pre-existing CSM grains may well have been sublimated by radiation from the SN itself. If we make the opposite assumption (i.e. include a blastwave component at the expense of the diffuse one), our main results are virtually unchanged, due to the low dust mass required to fit the mid-IR SED in either case. We use the gas properties (density, temperature, and composition) from Priestley et al. (2019), and the same gas masses for all but the pre-shock component, which we discuss below; these are listed in Table 1. We assume a distance to the SNR of 3.4 kpc (Reed et al. 1995).

The pre-shock gas mass of $3 M_{\odot}$ used in Priestley et al. (2019) was taken from the radio self-absorption study by Arias et al. (2018). It has since come to our attention that this value was dominated by a few degenerate pixels that contributed disproportionately to the mass estimate. We have redone the analysis using the complete LOFAR Cas A LBA data set presented in de Gasperin et al. (2020), with twice the observing time and five times the bandwidth of the original study, and using a more stringent mask of degenerate pixels. As intermediate products for the broad-band imaging, de Gasperin et al. (2020) produced 61 narrow-band images of Cas A in the frequency

range of 30–77 MHz. We followed the same method presented in section 3 of Arias et al. (2018) and fitted for deviation from power-law behaviour (assuming $\alpha = 0.77$ for Cas A), coming to the results in Fig. 1.

Going from the best-fitting value of the emission measure, 4.2 pc cm^{-6} , to an estimate of the unshocked mass inside of Cas A’s reverse shock depends on the temperature, ionisation, and geometry of the absorbing material. In Arias et al. (2018), it was assumed that the absorbing material has a temperature of 100 K, an average ionisation state $Z = 3$, and that the unshocked ejecta are mostly composed of oxygen, with a mass number A of 16. Using these values, we arrive at the following mass estimate:

$$M = 0.53 \pm 0.10 M_{\odot} \left(\frac{A}{16} \right) \left(\frac{l}{0.16 \text{ pc}} \right)^{-3/2} \left(\frac{Z}{3} \right)^{-3/2} \times \left(\frac{T}{100 \text{ K}} \right)^{3/4} \sqrt{\frac{g_{\text{ff}}(T = 100 \text{ K}, Z = 3)}{g_{\text{ff}}(T, Z)}}, \quad (1)$$

here, g_{ff} is a Gaunt factor given in equation (2) of Arias et al. (2018). The corresponding electron density is $n_e = 5.12 \left(\frac{l}{0.16 \text{ pc}} \right)^{-1/2} \text{ cm}^{-3}$. The choice of temperature, ionisation state, and geometry follow the assumptions made in DeLaney et al. (2014). The $T = 100$ K assumption was later confirmed by Raymond et al. (2018). Moreover, we assume that the unshocked ejecta is composed mostly of three-times ionised oxygen ([O IV], as observed by Isensee et al. (2010) among others), whereas we know that there are low ionisation, heavier species, such as [Si II] and [S III] (Smith et al. 2009; Isensee et al. 2010; Milisavljevic & Fesen 2015), and possibly also Fe. There is also neutral material inside the reverse shock (Koo et al. 2018) that does not contribute to the ionisation, and therefore is not included in this estimate. Perhaps more importantly, we assume that the unshocked ejecta are confined to a disc of thickness $l = 0.16$ pc. Milisavljevic & Fesen (2015) found in fact that the internal ejecta are bubble-like, formed by cavities and ejecta walls that separate them. Finally, as discussed in Arias et al. (2018), we do not know how clumped the ejecta are. These factors can significantly increase (or, in the case of high clumping, decrease) the mass estimate as derived from radio free-free absorption. As our value agrees with the recent independent estimate of $0.49^{+0.47}_{-0.24} M_{\odot}$ from Laming & Temim (2020), we use it throughout the rest of this paper, but note that it remains a significant source of systematic uncertainty in the estimate of f_{dest} .

In Priestley et al. (2019), the assumed shape of the radiation field responsible for dust heating was taken from Wang & Li (2016). This fit to the radio and X-ray observations included no data at the optical/ultraviolet (UV) wavelengths, which typically dominate dust heating. To better constrain the radiation field, we instead use the SED of the 1000 km s $^{-1}$ V_n10_b0.001 model from the Allen et al. (2008) collection of radiative shock models, which produces post-shock properties best matching those of the blastwave from Willingale et al. (2003). We scale this to match the total X-ray luminosity

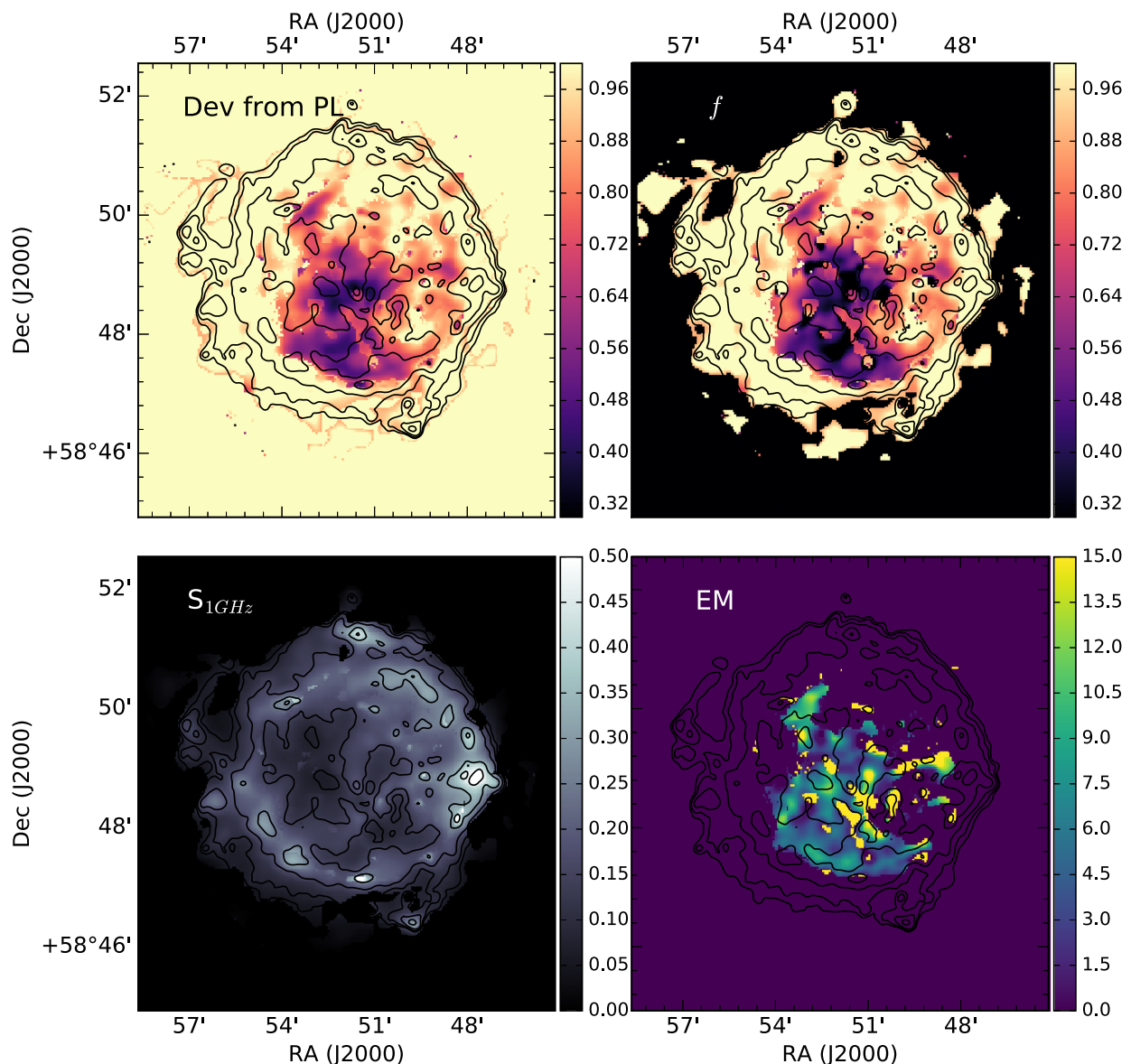


Figure 1. Results of fitting the Cas A narrow-band images from de Gasperin et al. (2020) to equations 5–7 in Arias et al. (2018). $S_{1\text{GHz}}$ is the best-fitting flux density at 1 GHz in Jy, and Dev from PL is the best-fitting deviation from a power-law spectrum, with $S_\nu \propto S_{1\text{GHz}}(\frac{\nu}{1\text{GHz}})^{-0.77}$. EM is the emission measure from the absorbing material given in pc cm^{-6} , and f is the fraction of material lying in front of the absorbing material (and that is therefore not subject to free-free absorption).

of $4 \times 10^{37} \text{ erg s}^{-1}$ (Laming & Temim 2020), approximating the emitting surface area as a shell of radius 1.7 pc (Reed et al. 1995). By symmetry, the flux at any point inside a spherical shell of emitting material is identical; we can thus use the radiation field at the centre, and ignore the fact that the dust grains will in fact be located at a range of radii.

2.2 Dust SED models

We model the emission from dust grains using DINAMO (Priestley et al. 2019), a dust heating and emission code accounting for stochastic heating effects on small grains, under the conditions of the three SNR components described above. Rather than assuming a Mathis, Rumpl & Nordsieck (1977) ISM grain size distribution for each component, as in Priestley et al. (2019), we calculate single-

grain SEDs for a range of grain sizes. There is strong observational evidence that dust grains formed in CCSNe are large ($a \gtrsim 0.1 \mu\text{m}$; Gall et al. 2014; Wesson et al. 2015; Bevan & Barlow 2016; Priestley et al. 2020), and that the size distributions are much more top-heavy than those found by Mathis et al. (1977) (Owen & Barlow 2015; Wesson et al. 2015; Priestley et al. 2020), but processing by the reverse shock can significantly alter the original distribution (Kirchschlager et al. 2019). The available IR data are insufficient to constrain the size distribution in each component, so we assume a single grain size for each.

De Looze et al. (2017) and Priestley et al. (2019) both find that the dust must be mostly comprised of silicates. While the exact composition is unknown, the differences in dust masses for different silicate optical properties are relatively minor with the exception of the $\text{Mg}_{0.7}\text{SiO}_{2.7}$ grains from Jäger et al. (2003), which require

Table 2. Cas A SNR dust IR fluxes for the $G = 0.6$ ISM dust model of De Looze et al. (2017), and those from an annulus with inner/outer radii of 140/165 arcsec. Effective wavelengths for each filter are given in μm .

| Filter | F_ν (Jy) | $F_\nu(> 140 \text{ arcsec})$ (Jy) |
|-----------|------------------|------------------------------------|
| IRAC 8 | 0.2 ± 0.1 | <0.4 |
| WISE 12 | 3.4 ± 0.3 | <0.3 |
| IRS 17 | 63.3 ± 6.0 | 10.6 ± 2.3 |
| WISE 22 | 202.0 ± 19.3 | 27.7 ± 2.6 |
| MIPS 24 | 154.4 ± 15.0 | 22.0 ± 1.7 |
| IRS 32 | 168.5 ± 17.3 | 25.3 ± 5.0 |
| PACS 70 | 149.5 ± 20.1 | 19.3 ± 3.0 |
| PACS 100 | 125.8 ± 19.9 | 14.6 ± 5.0 |
| PACS 160 | 69.9 ± 12.0 | 1.1 ± 6.9 |
| SPIRE 250 | 27.3 ± 4.8 | <3.8 |
| SPIRE 350 | 10.9 ± 1.9 | <2.5 |
| SPIRE 500 | 2.6 ± 0.5 | <1.5 |
| SCUBA 850 | 0.4 ± 0.1 | - |

unrealistically large masses, so we use the values for MgSiO_3 grains from Dorschner et al. (1995), extended to UV and X-ray wavelengths with data from Laor & Draine (1993). For consistency with previous work, we assume a bulk grain density of 2.5 g cm^{-3} .

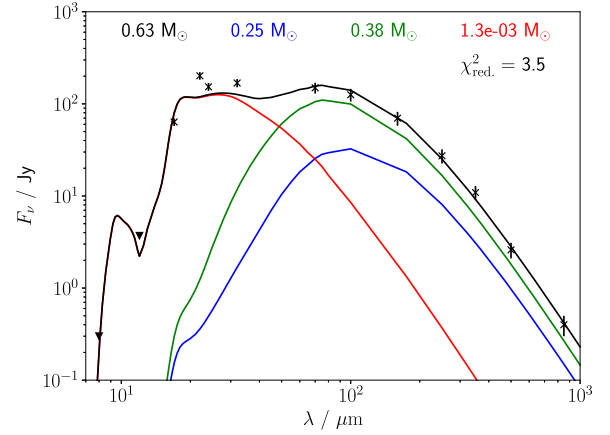
We fit the $G = 0.6$ Cas A SN dust SED from De Looze et al. (2017), given in Table 2, with the number (and, equivalently, mass) of grains in each ejecta component as our three free parameters, treating the 8 and $12 \mu\text{m}$ fluxes as upper limits due to the highly uncertain contribution from ISM dust at these wavelengths. Rather than performing a grid search for the minimum χ^2_{red} , as in Priestley et al. (2019), we fit the SED using *emcee* (Foreman-Mackey et al. 2013), a Monte Carlo Markov chain (MCMC code, which allows us to more accurately determine the best-fitting dust masses while also accounting for any model degeneracies and the observational uncertainties. We use 500 walkers with 5000 steps per walker and 500 burn-in steps, which we have confirmed is sufficient for the models to converge. We additionally consider an SED extracted in the same way as the De Looze et al. (2017) dust SED, but from an annulus with inner and outer radii of 140 and 165 arcsec, representing a ‘post-shock’ SED with minimal contribution from the central, unshocked ejecta dust, also given in Table 2.

3 RESULTS

3.1 Dust masses and grain sizes

Fig. 2 shows the best-fitting model assuming a Mathis et al. (1977) size distribution for each component, as in Priestley et al. (2019). The model fails to reproduce the observed mid-IR fluxes as the high-temperature small grains that make up most of the distribution emit too strongly at $\sim 10 \mu\text{m}$, exceeding the observational upper limits.¹ It is thus necessary to consider the grain size in each component individually.

Fig. 3 shows best-fitting models for grain sizes of either $1 \mu\text{m}$ (model A) or 10 nm (model B) in all three components; median dust masses with uncertainties are given in Table 3. Both models fail to fit the mid-IR SED, with grain temperatures being too low or too high for models A and B, respectively. The observed SED shape

**Figure 2.** Cas A dust SED (black crosses) and best-fitting model SEDs for pre-shock (blue), clumped (green), and diffuse (red) components using a Mathis et al. (1977) grain size distribution as in Priestley et al. (2019), with the total model SED shown in black.

in the mid-IR requires grains with a size $\sim 0.1 \mu\text{m}$ in the diffuse component. Fig. 4 shows the best-fitting model for $0.1 \mu\text{m}$ grains in all three components (model C), with $0.72 M_\odot$ of post-shock clumped dust, $2.5 \times 10^{-3} M_\odot$ in the diffuse phase, and a negligible quantity of unshocked dust. While model C is a good fit to the data, it is physically problematic, as it would imply formation, rather than destruction, of dust in the reverse shock.² The majority of the dust is observed to lie within the reverse-shock radius (De Looze et al. 2017), and extinction-based measurements also require a significant mass of unshocked ejecta dust (Bevan et al. 2017; Niculescu-Duvaz et al. 2021). A clumped dust grain size of $0.1 \mu\text{m}$ is also in conflict with the post-shock SED, as shown in Fig. 5, which clearly requires smaller, higher-temperature grains in this phase.

To maintain physical consistency, we require that both the DTG ratios and the grain sizes in the two post-shock components be smaller than those in the pre-shock component, thereby assuming that accretion onto grains or grain coagulation cannot exceed grain destruction in the reverse shock. Fig. 6 shows the results for models with $0.1 \mu\text{m}$ grains in both the pre-shock and diffuse components, and either 10 nm (model D) or 5 nm (model E) clumped grain sizes. Models D and E both fit the observed $70 \mu\text{m}$ flux better than the all $0.1 \mu\text{m}$ model C, requiring $0.63\text{--}0.68 M_\odot$ of pre-shock dust, $0.05\text{--}0.07 M_\odot$ of dust in the post-shock clumps, and $2.4 \times 10^{-3} M_\odot$ of dust in the diffuse material. This is in much better agreement with the inferred spatial distribution of the dust mass in the SNR. The smaller grain size in the post-shock clumps is a natural result of shattering via grain–grain collisions (Kirchschlager et al. 2019). The grain size in the diffuse phase, which is strongly constrained to be $\sim 0.1 \mu\text{m}$ (Fig. 3), could be due to smaller grains being rapidly destroyed via sputtering in the high-temperature gas, or their being more strongly coupled to the gas and thus unable to escape from the clumps.

While we argue that the pre-shock grain size cannot be smaller than the $\sim 0.1 \mu\text{m}$ in the diffuse component, it could be larger. This would be in better agreement with observations of other SNRs, which are often found to require micron-sized grains (e.g. Priestley et al. 2020). Fig. 7 shows best-fitting models for a $1 \mu\text{m}$ pre-shock grain

¹The 8/12 μm fluxes were not included in the fitting procedure in Priestley et al. (2019). It can be seen in that paper that the predicted model fluxes do, in fact, exceed these values in all cases.

²While there are some observational (Matsuura et al. 2019) and theoretical (Kirchschlager, Barlow & Schmidt 2020) justifications for post-shock dust reformation, these are to a far lesser extent than implied by the best-fitting model.

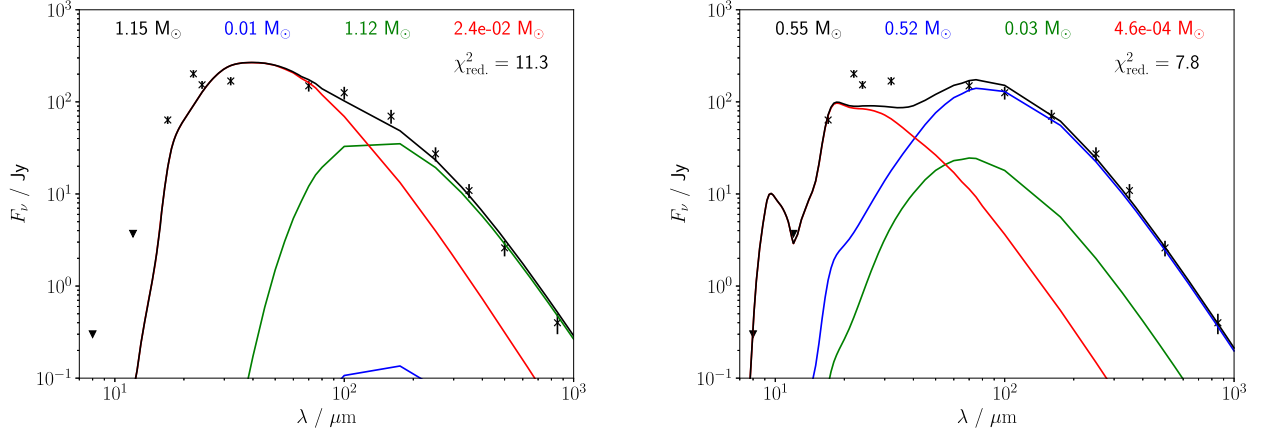


Figure 3. Cas A dust SED (black crosses) and best-fitting model SEDs for pre-shock (blue), clumped (green) and diffuse (red) grains of radius 1 μm (left-hand panel, model A) or 10 nm (right-hand panel, model B), with the total model SEDs shown in black.

Table 3. Median dust masses for each component and the best-fitting χ^2_{red} values for different combinations of grain size, listed as $a_{\text{pre-shock}}/a_{\text{clumped}}/a_{\text{diffuse}}$. The uncertainties give the 16th and 84th percentiles from the MCMC.

| Model | Grain size (μm) | Dust mass (M_\odot) | | | Total | χ^2_{red} |
|----------------|------------------------------|-------------------------|---------------------------|------------------------------------|------------------------|-----------------------|
| | | Pre-shock | Clumped | Diffuse | | |
| A | 1.0/1.0/1.0 | $0.10^{+0.72}_{-0.08}$ | $1.00^{+0.14}_{-0.61}$ | $2.4^{+0.1}_{-0.1} \times 10^{-2}$ | $1.17^{+0.10}_{-0.09}$ | 11.3 |
| B | 0.01/0.01/0.01 | $0.57^{+0.04}_{-0.56}$ | $0.00^{+0.21}_{-0.00}$ | $4.6^{+0.2}_{-0.2} \times 10^{-4}$ | $0.57^{+0.03}_{-0.32}$ | 7.8 |
| C | 0.1/0.1/0.1 | $0.00^{+0.26}_{-0.00}$ | $0.70^{+0.05}_{-0.22}$ | $2.5^{+0.1}_{-0.1} \times 10^{-3}$ | $0.73^{+0.06}_{-0.04}$ | 1.4 |
| D | 0.1/0.01/0.1 | $0.65^{+0.11}_{-0.09}$ | $0.069^{+0.023}_{-0.027}$ | $2.5^{+0.1}_{-0.1} \times 10^{-3}$ | $0.72^{+0.08}_{-0.08}$ | 1.2 |
| E | 0.1/0.005/0.1 | $0.70^{+0.11}_{-0.09}$ | $0.046^{+0.016}_{-0.024}$ | $2.4^{+0.1}_{-0.1} \times 10^{-3}$ | $0.74^{+0.08}_{-0.07}$ | 1.2 |
| F | 1.0/0.01/0.1 | $0.91^{+0.15}_{-0.12}$ | $0.13^{+0.01}_{-0.02}$ | $2.4^{+0.1}_{-0.1} \times 10^{-3}$ | $1.05^{+0.14}_{-0.11}$ | 1.4 |
| G | 1.0/0.005/0.1 | $1.04^{+0.17}_{-0.12}$ | $0.094^{+0.011}_{-0.016}$ | $2.3^{+0.1}_{-0.1} \times 10^{-3}$ | $1.13^{+0.16}_{-0.11}$ | 1.6 |
| H ^a | 0.1/0.005/0.1 | $0.74^{+0.12}_{-0.09}$ | $0.051^{+0.016}_{-0.023}$ | $2.3^{+0.1}_{-0.1} \times 10^{-3}$ | $0.79^{+0.09}_{-0.08}$ | 0.7 |
| I ^b | 0.1/0.005/0.1 | $0.13^{+0.03}_{-0.03}$ | $0.069^{+0.009}_{-0.010}$ | $1.9^{+0.1}_{-0.1} \times 10^{-3}$ | $0.20^{+0.03}_{-0.03}$ | 2.1 |

^a With $\text{Mg}_{2.4}\text{SiO}_{4.4}$ optical properties. ^b With a 50:50 MgSiO_3 :amorphous carbon mixture.

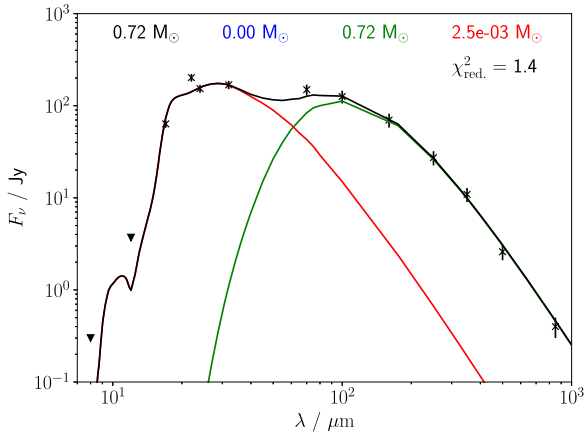


Figure 4. Cas A dust SED (black crosses) and the best-fitting model SED for pre-shock (blue), clumped (green) and diffuse (red) grains of radius 0.1 μm (model C), with the total model SEDs shown in black.

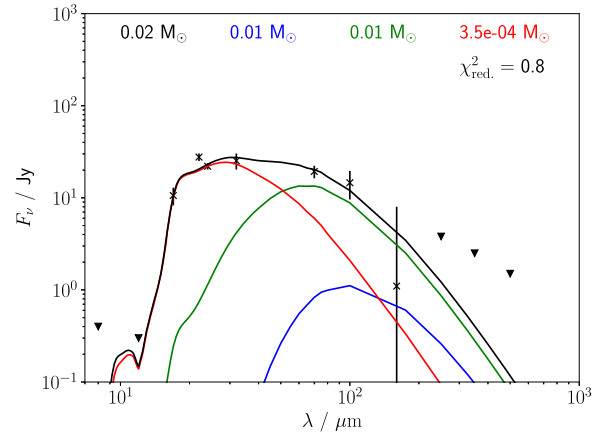


Figure 5. Cas A post-shock dust SED (black crosses) and best-fitting model SEDs for clumped 0.1 μm (blue), clumped 5 nm (green), and diffuse 0.1 μm (red) grains, with the total model SED shown in black.

size, with either a 10 nm (model F) or 5 nm (model G) clumped grain size. These models require larger dust masses in both the pre-shock and clumped components, with a slightly worse χ^2_{red} compared to models D and E with 0.1 μm pre-shock grains. Niculescu-Duvaz et al.

(2021) find that micron-sized grains produce unphysically large dust masses if responsible for the measured optical extinction in Cas A, and it is unclear whether shattering is efficient enough to completely reprocess a population of 1 μm grains into the 0.1 μm required in the

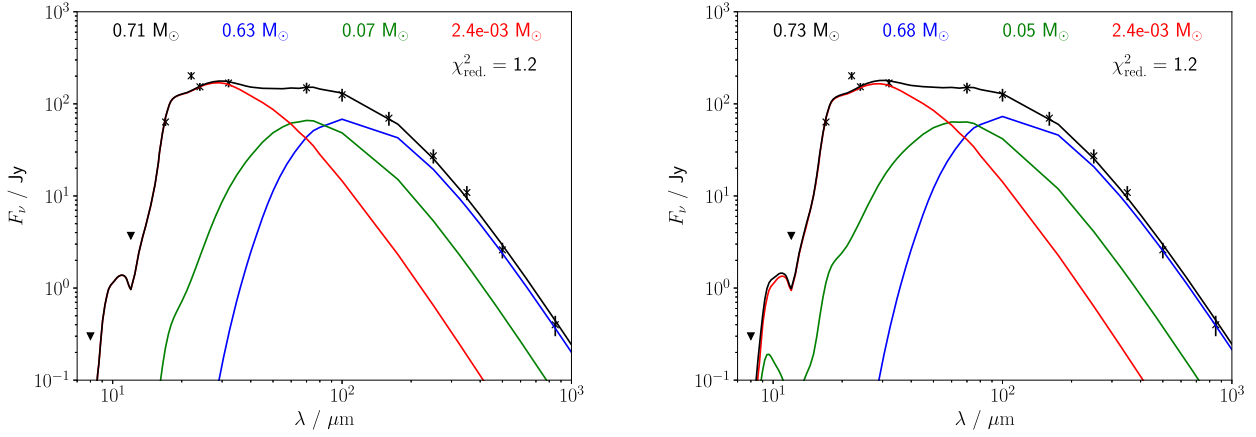


Figure 6. Cas A dust SED (black crosses) and best-fitting model SEDs for pre-shock 0.1 μm (blue) and diffuse 0.1 μm (red) grains, with a clumped grain size of 10 nm (green, left-hand panel; model D) or 5 nm (green, right-hand panel; model E) with the total model SED shown in black.

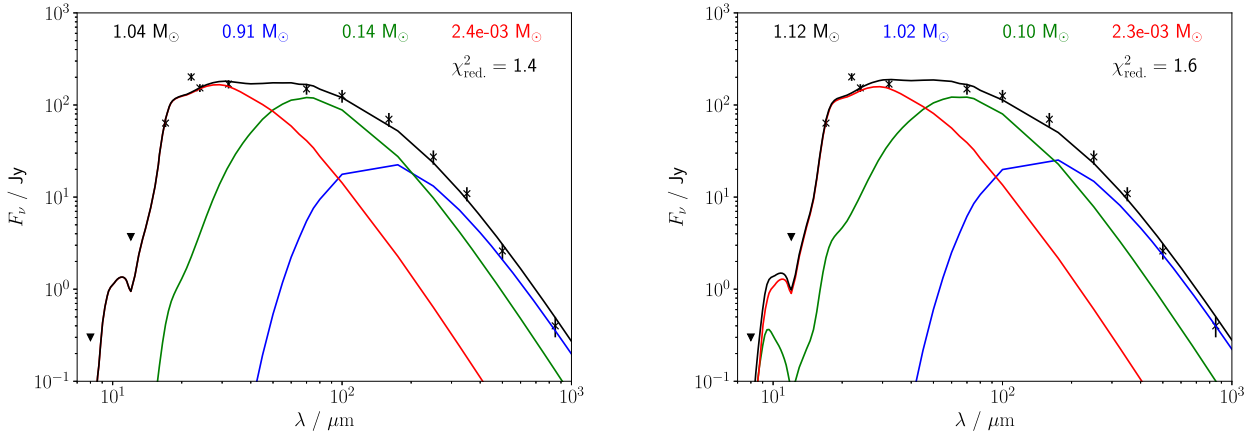


Figure 7. Cas A dust SED (black crosses) and best-fitting model SEDs for pre-shock 1 μm (blue) and diffuse 0.1 μm (red) grains, with a clumped grain size of 10 nm (green, left; model F) or 5 nm (green, right; model G) with the total model SED shown in black.

diffuse component.³ We therefore consider models D and E as more plausible, although we cannot rule out the larger grain sizes.

We note that no model correctly reproduces the SED peak at 21 μm . This is an issue of dust composition in the diffuse component, which we discuss briefly in Appendix A. As this component makes up a negligible fraction of the total dust mass, its importance for the derived destruction efficiency is limited. The assumed silicate composition in the pre-shock and clumped components also has little effect on our results. Using optical properties from the $\text{Mg}_{2.4}\text{SiO}_{4.4}$ sample in Jäger et al. (2003) (model H), rather than the MgSiO_3 grains from Dorschner et al. (1995), and the same grain sizes as model E, we find statistically indistinguishable dust masses, as shown in Fig. 8.

If we assume a 50:50 mixture by mass of MgSiO_3 silicate and carbon grains using ACAR amorphous carbon properties from Zubko et al. (1996), and a bulk density of 1.6 g cm^{-3} (model I), we find a total dust mass a factor of ~ 4 lower than for pure-silicate models, and lower than the values reported by De Looze et al. (2017) and Bevan et al. (2017) for the same mixture by a similar factor. This is due to most of the far-IR flux coming from post-shock carbon grains in our best-fitting model, which are warmer (and thus more emissive) than

the pre-shock silicates that provide nearly all the far-IR flux in the other models (a similar effect occurred in the carbon grain models from Priestley et al. 2019). Model I is a worse fit to the data than our preferred silicate-only models, particularly in the mid-IR, where it exceeds both the 8 and 12 μm upper limits on the flux. Cas A is also an oxygen-rich SNR (Docenko & Sunyaev 2010), which suggests that silicate grains should be predominant, so we consider model I to be less plausible than the silicate-only models. In any case, the final dust yield for model I obtained below is comparable to those from the silicate-only models (Table 4).

3.2 Destruction efficiencies

Combining the dust masses in Table 3 of models D–I, which are both good fits to the data and physically plausible, with the corresponding gas masses from Table 1, we calculate the DTG ratio for each ejecta component, listed in Table 4. We find pre-shock DTG ratios greater than unity, clumped DTG ratios of ~ 0.1 and diffuse DTG ratios of $\sim 10^{-3}$. If the clumped and diffuse ejecta initially had the same DTG ratios as the pre-shock component, this suggests significant and almost total dust destruction in the other two components, respectively.

The destruction efficiency, $f_{\text{dest}} = 1 - M_f/M_i$, where the subscripts refer to the initial and final dust masses, can be expressed in terms

³Grains this large are almost completely unaffected by sputtering (Nozawa et al. 2007).

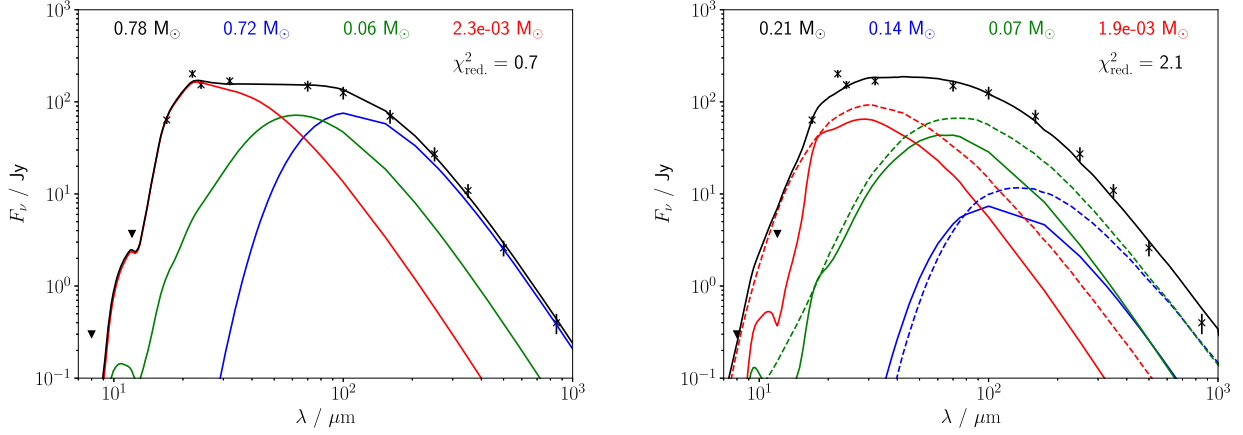


Figure 8. Cas A dust SED (black crosses) and best-fitting model SEDs for pre-shock $0.1 \mu\text{m}$ (blue), clumped 5 nm (green), and diffuse $0.1 \mu\text{m}$ (red) grains, with the total model SED shown in black. The left-hand panel uses $\text{Mg}_{2.4}\text{SiO}_{4.4}$ optical properties (model H), the right-hand panel a 50:50 mixture of MgSiO_3 (solid lines) and amorphous carbon (dashed lines) grains (model I).

Table 4. Median DTG ratios for the three ejecta components and the inferred destruction efficiencies in the two post-shock components separately and in combination. The uncertainties give the 16th and 84th percentiles from the MCMC. See Table 3 for model details.

| Model | Pre-shock | DTG ratio Clumped | Diffuse | Clumped | f_{dest} Diffuse | Total |
|-------|------------------------|------------------------|------------------------------------|------------------------|------------------------------|------------------------|
| D | $1.22^{+0.20}_{-0.18}$ | $0.12^{+0.04}_{-0.05}$ | $1.5^{+0.1}_{-0.1} \times 10^{-3}$ | $0.81^{+0.08}_{-0.07}$ | $0.9973^{+0.0002}_{-0.0002}$ | $0.94^{+0.02}_{-0.02}$ |
| E | $1.31^{+0.20}_{-0.16}$ | $0.08^{+0.03}_{-0.04}$ | $1.4^{+0.1}_{-0.1} \times 10^{-3}$ | $0.87^{+0.07}_{-0.05}$ | $0.9975^{+0.0001}_{-0.0002}$ | $0.96^{+0.02}_{-0.01}$ |
| F | $1.72^{+0.28}_{-0.23}$ | $0.23^{+0.03}_{-0.03}$ | $1.4^{+0.1}_{-0.1} \times 10^{-3}$ | $0.71^{+0.04}_{-0.04}$ | $0.9977^{+0.0001}_{-0.0001}$ | $0.91^{+0.01}_{-0.01}$ |
| G | $1.96^{+0.23}_{-0.31}$ | $0.16^{+0.02}_{-0.03}$ | $1.4^{+0.1}_{-0.1} \times 10^{-3}$ | $0.79^{+0.04}_{-0.03}$ | $0.9979^{+0.0001}_{-0.0001}$ | $0.94^{+0.01}_{-0.01}$ |
| H | $1.40^{+0.17}_{-0.22}$ | $0.08^{+0.04}_{-0.03}$ | $1.4^{+0.1}_{-0.1} \times 10^{-3}$ | $0.86^{+0.05}_{-0.06}$ | $0.9976^{+0.0002}_{-0.0001}$ | $0.96^{+0.01}_{-0.02}$ |
| I | $0.25^{+0.07}_{-0.06}$ | $0.12^{+0.02}_{-0.02}$ | $1.1^{+0.1}_{-0.1} \times 10^{-3}$ | $0.48^{+0.14}_{-0.20}$ | $0.9945^{+0.0009}_{-0.0014}$ | $0.85^{+0.04}_{-0.06}$ |

of the DTG ratios⁴ as

$$f_{\text{dest}} = 1 - \frac{\text{DTG}_f}{\text{DTG}_i} \frac{1 + \text{DTG}_i}{1 + \text{DTG}_f}. \quad (2)$$

Assuming the initial DTG ratio is identical to the pre-shock component, for our preferred models with a $0.1 \mu\text{m}$ pre-shock grain size (D, E, and H), this suggests $f_{\text{dest}} = 74\text{--}94$ per cent in the clumped ejecta and > 99 per cent in the diffuse component. The inferred total destruction efficiency, accounting for the relative mass of each post-shock component, is $92\text{--}98$ per cent. Applying the f_{dest} value for the clumped ejecta to the current (presumably clumped) unshocked dust mass suggests that $0.03\text{--}0.21 M_{\odot}$ should survive the reverse shock. If no further destruction occurs, then combined with the current post-shock dust mass, this gives a total dust yield ($M_{\text{diffuse}} + M_{\text{clump}} + (1 - f_{\text{dest}})M_{\text{pre-shock}}$) for Cas A of $0.05\text{--}0.30 M_{\odot}$. If we assume that the diffuse ejecta represents material stripped from clumps during the passage of the reverse shock, then the appropriate value is the total f_{dest} , and the resulting dust yield is $0.03\text{--}0.15 M_{\odot}$.

If the pre-shock grain size is $1 \mu\text{m}$ (models F and G), then f_{dest} is lower and both pre- and post-shock dust masses are higher, leading to dust yields approaching $0.5 M_{\odot}$. For model I, with a 50:50 carbon-to-silicate grain ratio, the minimum dust yield is still $\sim 0.12 M_{\odot}$, despite the total (current) dust mass being significantly lower than the all silicate models – the proportion of shocked to unshocked dust mass is much larger than in the silicate models, leading to a low inferred f_{dest} and a higher relative final yield.

4 DISCUSSION

4.1 Comparison with theory

Our values of f_{dest} for the clumped ejecta in models D and E are somewhat lower than those from dust destruction models including grain–grain collisions (Kirchschlager et al. 2019), although there is overlap between the ranges. We note that the model clumps in Kirchschlager et al. (2019) are mostly dispersed into what would be termed ‘diffuse’ ejecta by our definition, and the total f_{dest} values accounting for this component are in closer agreement with the theoretical prediction. While Slavin et al. (2020) find $f_{\text{dest}} \sim 80\text{--}90$ per cent for silicate grains in clumps, close to that observed, this includes significant additional destruction in the ISM after grains have escaped the SNR. The immediate post-shock value of f_{dest} from Slavin et al. (2020) appears to be substantially lower than those in Table 4, likely due to their model not accounting for grain–grain collisions (Kirchschlager et al. 2019). We note that De Looze et al. (2017) estimated $f_{\text{dest}} \sim 70$ per cent from the spatial distribution of the dust mass and the radius of the reverse shock, consistent with our models D and E and in good agreement with models F and G.

4.2 Implications

Although our estimated dust yield for Cas A has a fairly large uncertainty, the $\sim 0.1 M_{\odot}$ per CCSNe value required to explain high-redshift observations (Dwek et al. 2007) is well within reach.

⁴A derivation is given in Appendix B.

We note that Cas A is an exceptionally strongly interacting SNR, and thus presumably has a much higher f_{dest} and lower dust yield than less extreme objects. This suggests that CCSNe may be major dust producers even up to the present day. De Looze et al. (2020) find that this is the case for $f_{\text{dest}} \lesssim 50$ per cent, not far from our lower limit, which is again for a very strong reverse shock. Galliano et al. (2021) find a maximum possible dust yield of $0.03 M_{\odot}$ per CCSNe; even our lower limit exceeds this, and for our best-fitting models, a larger dust mass has already survived passing through the reverse shock. The Galliano et al. (2021) CCSNe yields are primarily constrained by observations of the dust mass in low-metallicity galaxies. If our results are correct, and applicable beyond Cas A, this suggests that extending dust evolution models towards low-metallicity environments requires a better understanding of how SN dust yields, gaseous inflows/outflows (Nanni et al. 2020), and ISM dust destruction efficiencies (Priestley, De Looze & Barlow 2022) vary with metallicity, rather than assuming that these remain fixed.

4.3 High dust-to-gas ratios

Laming & Temim (2020) suggest that, due to the pre-shock gas mass of $\sim 0.6 M_{\odot}$, it is implausible that there is also $0.6 M_{\odot}$ of dust in the unshocked ejecta, as this implies a DTG ratio of around unity. We disagree with this argument. The ejecta of Cas A is almost entirely made up of elements that form dust (Docenko & Sunyaev 2010), and such high condensation efficiencies are also seen in other objects; the Crab Nebula contains $\sim 0.2 M_{\odot}$ of metals (Owen & Barlow 2015) and $0.02\text{--}0.08 M_{\odot}$ of dust (De Looze et al. 2019; Priestley et al. 2020), while born-again planetary nebulae, which also feature dust formation in explosively ejected, heavily fusion-processed ejecta, can reach DTG ratios of ~ 1 (e.g. Toalá et al. 2021). As mentioned previously, two independent studies based on optical line extinction (Bevan et al. 2017; Niculescu-Duvaz et al. 2021) have found Cas A dust masses even larger than the $\sim 0.6 M_{\odot}$ in this and previous IR-based works, so we consider the Laming & Temim (2020) value for the pre-shock gas mass as possible evidence of highly efficient dust formation in Cas A, rather than as indicating an error in the determination of the dust mass.

4.4 Caveats

The distribution of dust mass between the various ejecta components appears to be fairly robust, as our results here do not greatly differ from those in Priestley et al. (2019) despite the different methodologies. The gas masses represent a potentially much larger source of uncertainty not captured by the errors in Table 4. More recent estimates of the mass of X-ray emitting material are comparable with the value from Willingale et al. (2003) that we use (e.g. Hwang & Laming 2012), but the unshocked gas masses from Laming & Temim (2020) and this work, despite agreeing within the errors, are based on conflicting assumptions. Laming & Temim (2020) assume the unshocked ejecta has a density $\sim 10 \text{ cm}^{-3}$ and a temperature $\sim 8000 \text{ K}$, whereas in equation (1) we used $T = 100 \text{ K}$ as found by Raymond et al. (2018), and the density of the post-shock clumps suggests a pre-shock density of $\sim 100 \text{ cm}^{-3}$ (Docenko & Sunyaev 2010). In Priestley et al. (2019), we also found an average ionisation state of $Z = 1$ for the clumped gas, lower than the $Z = 3$ assumed for the unshocked ejecta in equation (1). The lower value gives a pre-shock gas mass of $2.5 M_{\odot}$, which then results in $f_{\text{dest}} \sim 50$ per cent for models D/E and a correspondingly enhanced dust yield of $\sim 0.5 M_{\odot}$. Observations of atomic line emission by the *James Webb Space Telescope*, combined with a model accounting

for all ejecta components, would be extremely useful in resolving this uncertainty.

5 CONCLUSIONS

We have reanalysed the IR SED of Cas A with a substantially improved dust emission model, finding dust masses of $0.6\text{--}0.8 M_{\odot}$ in the unshocked material, $0.02\text{--}0.09 M_{\odot}$ in the post-shock clumps, and $2.3\text{--}2.5 \times 10^{-3} M_{\odot}$ in the X-ray emitting diffuse gas for our preferred pre-shock grain size of $0.1 \mu\text{m}$. Combined with updated gas mass estimates, these give DTG ratios of $1.0\text{--}1.5$ in the unshocked gas, $0.04\text{--}0.16$ in the shocked clumps, and 0.001 in the X-ray emitting gas. The implied dust destruction efficiency of the reverse shock is $74\text{--}94$ per cent in the clumped material and $92\text{--}98$ per cent overall, with a final dust yield for Cas A of $0.05\text{--}0.30 M_{\odot}$ that is sufficient to explain the observed dust masses in high-redshift galaxies. For a pre-shock grain size of $1 \mu\text{m}$, the final dust yield may exceed $0.5 M_{\odot}$. As Cas A is one of the most strongly interacting SNRs known, the large dust yield even for this object suggests that CCSNe, in general, are efficient dust producers, and contribute significantly to the overall cosmic dust budget.

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DATA AVAILABILITY

The data underlying this article will be made available on request to the corresponding author.

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APPENDIX A: THE 21 μm EXCESS

While grains with MgSiO_3 optical properties result in a good fit to nearly all of the IR SED, there is a notable excess at 21 μm which is not well reproduced. This is even more apparent in the *Spitzer* IRS spectrum (Rho et al. 2008), and can be fit with a variety of other dust compositions, including SiO_2 and FeO . A similar excess is also seen in G54.1 + 0.3 (Rho et al. 2018). The optical properties of $\text{Mg}_{0.7}\text{SiO}_{2.7}$ from Jäger et al. (2003) can reproduce this peak reasonably well, and also do so for G54.1 + 0.3 (Priestley et al. 2020), but the sharply declining opacity beyond 21 μm is in conflict with the data at these wavelengths (Fig. A1). Most other proposed carriers of the feature also display this behaviour, suggesting that at least two dust species are present in the diffuse component. This behaviour results in implausibly high dust masses if the same species

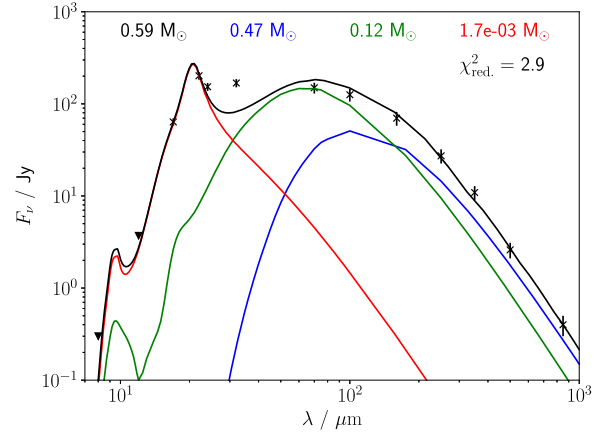


Figure A1. Cas A dust SED (black crosses) and best-fitting SEDs for pre-shock 0.1 μm (blue), clumped 5 nm (green), and diffuse 0.1 μm (red) grains, with the total model SED shown in black. The pre-shock and clumped dust has MgSiO_3 optical properties from Dorschner et al. (1995), the diffuse dust has $\text{Mg}_{0.7}\text{SiO}_{2.7}$ from Jäger et al. (2003).

is used to fit the far-IR SED, which implies that the 21 μm carrier is either not present in the colder gas components, or makes up only a small fraction of the total dust mass. We are unable to satisfactorily fit the mid-IR SED using a combination of different silicate grains in the diffuse component; given the uncertainties regarding both dust and gas properties, it is almost certainly possible to achieve this while remaining physically consistent with other observations, but as the dust masses are a small proportion of the total, we do not consider it necessary for the objectives of this paper.

APPENDIX B: f_{DEST} IN TERMS OF DTG RATIOS

The dust destruction efficiency, $f_{\text{dest}} = 1 - M_{f,d}/M_{i,d}$, can be expressed in terms of the pre- and post-shock DTG ratios as follows. We multiply the numerator and denominator of the dust mass ratio by $M_{\text{tot}} = M_d + M_g$ ($M_{f,d} + M_{f,g} = M_{i,d} + M_{i,g}$, as mass is only transferred between the gas/dust phases, not lost) to obtain

$$f_{\text{dest}} = 1 - \frac{M_{f,d}}{M_{f,d} + M_{f,g}} \frac{M_{i,d} + M_{i,g}}{M_{i,d}}, \quad (\text{B1})$$

and divide the numerator and denominator of each ratio in equation (B1) by the respective value of M_g , to get

$$f_{\text{dest}} = 1 - \frac{M_{f,d}/M_{f,g}}{1 + M_{f,d}/M_{f,g}} \frac{1 + M_{i,d}/M_{i,g}}{M_{i,d}/M_{i,g}} \quad (\text{B2})$$

$$= 1 - \frac{\text{DTG}_f}{1 + \text{DTG}_f} \frac{1 + \text{DTG}_i}{\text{DTG}_i} \quad (\text{B3})$$

$$= 1 - \frac{\text{DTG}_f}{\text{DTG}_i} \frac{1 + \text{DTG}_i}{1 + \text{DTG}_f}, \quad (\text{B4})$$

as in equation (2). Note that in Priestley et al. (2019), we assumed $f_{\text{dest}} = 1 - \text{DTG}_f/\text{DTG}_i$. While this is a reasonable approximation when the DTG ratio is $\ll 1$, as the pre-shock dust and gas masses in Cas A are comparable this will give erroneous results. For these values, a significant fraction of the current post-shock gas mass was initially locked up in dust grains, so the second term, $(1 + \text{DTG}_i)/(1 + \text{DTG}_f)$, cannot be neglected.

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