

# Imperfect integration: congruency between multiple sensory sources modulates decision-making processes

## Supplementary Material

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### Supplementary methods

#### The neural-mass model of perceptual decision

We used the two-state neural-mass model (Wong and Wang, 2006) in the following form:

$$\frac{dS_i}{dt} = -\frac{S_i}{\tau_S} + (1 - S_i)\gamma r(I_{\text{syn},i}) , \quad (1)$$

$$r(I_{\text{syn},i}) = \frac{aI_{\text{syn},i} - b}{1 - \exp(-d(aI_{\text{syn},i} - b))} , \quad (2)$$

$$\begin{cases} I_{\text{syn},L} = J_{L,L}S_L + J_{L,R}S_R + I_{in,L} + I_{\eta,L} \\ I_{\text{syn},R} = J_{R,R}S_R + J_{R,L}S_L + I_{in,R} + I_{\eta,R} , \end{cases} \quad (3)$$

$$\tau_{\eta} \frac{dI_{\eta,i}}{dt} = -I_{\eta,i} + \eta_t \sqrt{\tau_{\eta}} \sigma_{\eta} , \quad (4)$$

where the index  $i = L, R$  refers to two neural populations selective for leftwards and rightwards choices. The state variable  $S$  describes the NMDA gating variable (fraction of open gates). It can be shown that  $S$  has a bijection mapping on pre-synaptic firing rates (Wong and Wang, 2006).  $r$  describes the population firing rate function that depends on the synaptic input current  $I_{\text{syn},i}$ . The following values of the parameters were used:  $a = 270(\text{VnC})^{-1}$ ,

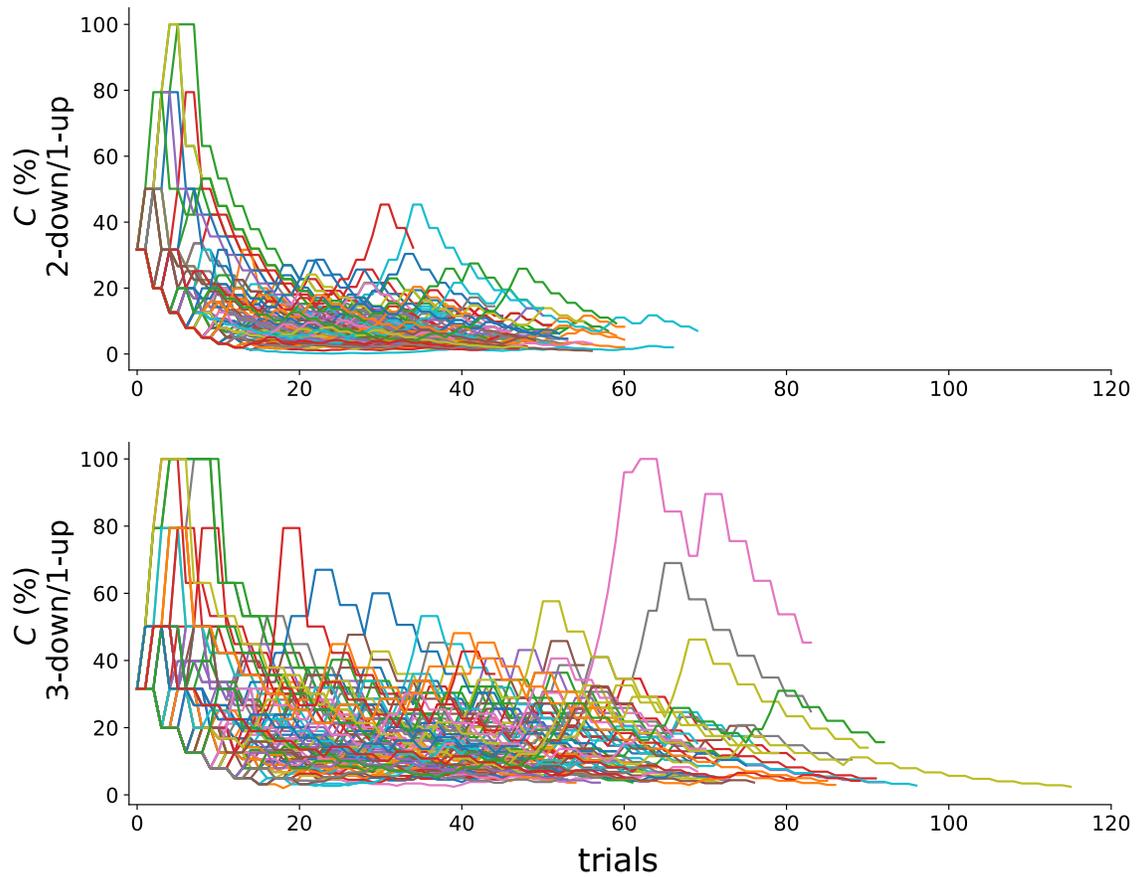
$b = 108 \text{ Hz}$ ,  $d = 0.154 \text{ s}$ ,  $\gamma = 0.641 \cdot 10^{-3}$ ,  $\tau_S = 100 \text{ ms}$ .

The synaptic input current  $I_{syn,i}$  combines recurrent inputs, mutual inputs, external inputs that relate to sensory information ( $I_{in,i}$ , Equation 1 in the main text) and the noise current  $I_{\eta,i}$ . The following symmetric synaptic coupling parameters were used:  $J_{A,A} = J_{B,B} = 0.2601 \text{ nA}$  and  $J_{A,B} = J_{B,A} = 0.0497 \text{ nA}$ ,  $J_{ext} = 5.2 \cdot 10^{-4} \text{ nA}\cdot\text{Hz}^{-1}$ .

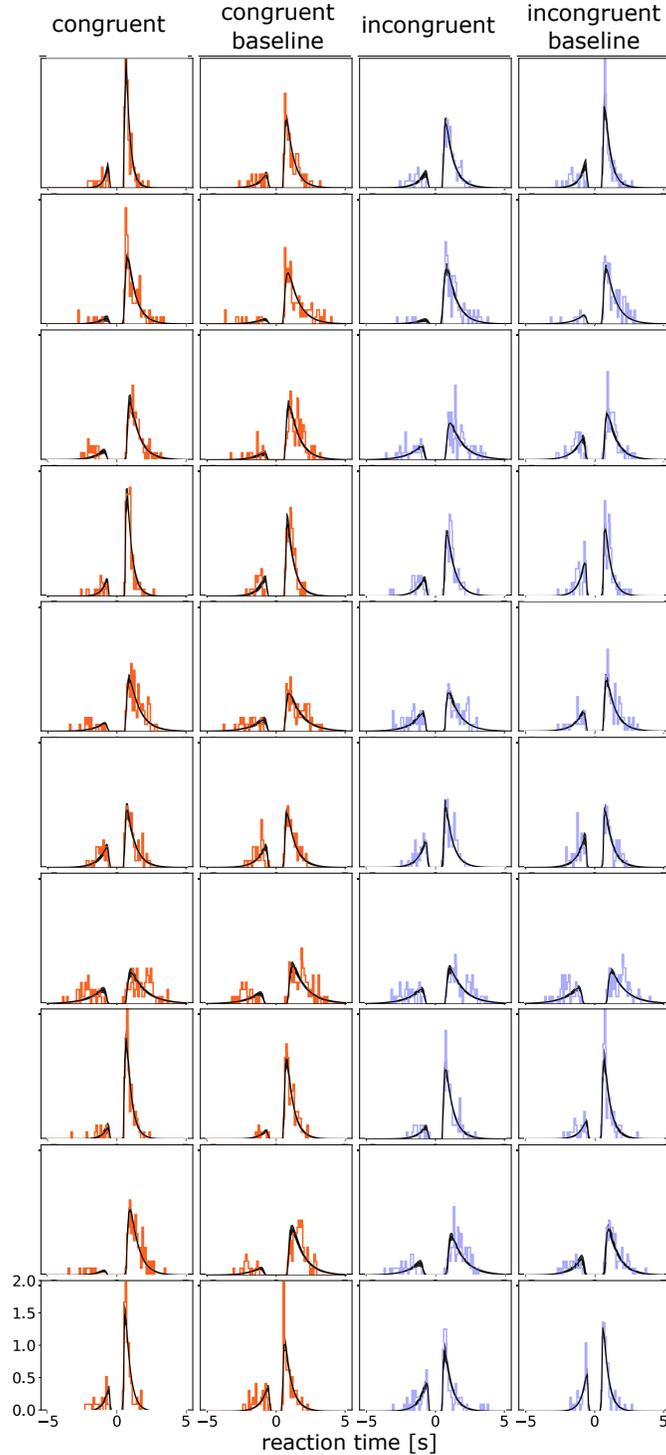
The noise current  $I_{\eta,i}$  is integrated with  $\tau_\eta = 2 \text{ ms}$  (time decay of AMPA receptor activation) and random variable sample from Normal distribution  $\eta$ . The variance of the noise factor is kept constant  $\sigma_\eta = 0.01972$ .

For simulations, we use standard Euler's integration method with a time step of 1 ms.

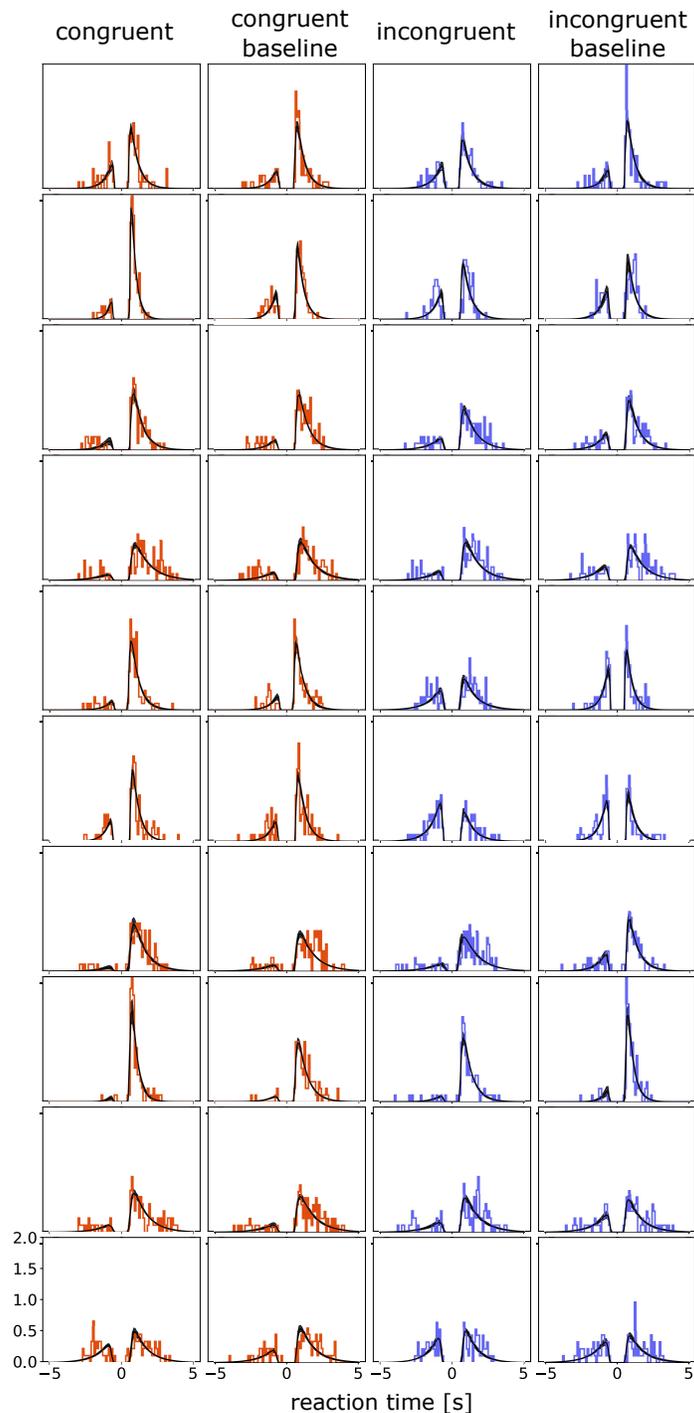
## Supplementary figures



**Supplementary Figure 1:** Steps of the staircase procedure for the two staircase rules (top: two-up/one-down rule; bottom: three-up/one-down rule). Each line represents one participant.



**Supplementary Figure 2:** Posterior predictive data distributions of 10 participants in Group 1 ( $\theta = \pm 20^\circ$ ). Each row shows data distributions (histograms) as well as Posterior model predictions (black lines) from the best fitted model from one of ten representative participants. The distributions along the positive x-axis indicate normalised correct response times, and the distributions along the negative x-axis indicate normalised error response times. Model predictions was generated in the same procedure as in Figure 6.



**Supplementary Figure 3:** Posterior predictive data distributions of 10 participants in Group 2 ( $\theta = \pm 45^\circ$ ). Each row shows data distributions (histograms) as well as Posterior model predictions (black lines) from the best fitted model from one of ten representative participants. The distributions along the positive x-axis indicate normalised correct response times, and the distributions along the negative x-axis indicate normalised error response times. Model predictions was generated in the same procedure as in Figure 6.

## References

Wong KF and Wang XJ (2006). A recurrent network mechanism of time integration in perceptual decisions. *Journal of Neuroscience*, 26(4):1314–1328.