# Deep neural network based framework for in-vivo axonal permeability estimation

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# Synopsis

This study introduces a novel framework for estimating permeability from diffusion-weighted MRI data using deep learning. Recent work introduced a random forest (RF) regressor model that outperforms approximate mathematical models (Kärger model). Motivated by recent developments in machine learning, we propose a deep neural network (NN) approach to estimate the permeability associated with the water residence time. We show in simulations and in in-vivo mouse brain data that the NN outperforms the RF method. We further show that the performance of either ML method is unaffected by the choice of training data, i.e. raw diffusion signals or signal-derived features yield the same results.

#### Introduction

This work investigates the potential of novel deep learning techniques for diffusion-weighted (DW) MRI microstructure imaging. We focus here on estimating the permeability of the axonal membrane, a potentially important biomarker for conditions affecting the myelin sheath<sup>1</sup> such as Multiple Sclerosis. Recent work introduced for the first time a machine-learning (ML) approach<sup>2</sup> based on a random Forest (RF) regressor to estimate the intra-axonal residence time  $\tau_i$  (used as a measure of permeability) and showed that it outperforms approximate mathematical models (e.g. Kärger<sup>3</sup>).

Here we implement a novel ML framework based on deep neural networks (NN), which have been shown in other applications to outperform RF<sup>4</sup>. Furthermore, we investigate whether the raw DW-MRI signals (DW-signals) can provide better training than the signal-derived features (DW-features) used in Nedjati et al<sup>2</sup>.

# Methods

We trained and tested the NN by constructing a mapping between DW-MRI data and ground truth microstructure parameters (intra-axonal volume fraction  $f_{i,}$  intrinsic diffusivity d and  $\tau_i$ ). We then compared it with the RF approach both in simulations and in in-vivo mouse brain data.

<u>Synthetic Data:</u> The training database is constructed from 11,000 synthetic DW-MRI signals simulated using Camino<sup>5</sup>, each corresponding to a unique substrate mimicking the in-vivo mouse data (Fig.1).

In-vivo Data: We use a healthy C57BL6J mouse scanned on a BrukerBioSpec 11.7T scanner using diffusion-weighted Pulsed-Gradients-Spin-Echo (DW-PGSE) sequence (protocol in Fig 1).

<u>RF Regressor</u>: We implemented an RF regressor with 100 trees and 20 maximum depth (Fig.2) using the scikitlearn Python toolkit<sup>6</sup> and the default values for the other parameters. The regressor learns by implementing a greedy linear splitting process of the signal space guided by its associated tissue parameters provided as labels.

<u>Deep NN</u>: For this model (Fig.2) we use the open-source Keras<sup>7</sup> library. The feed-forward NN is formed of an input layer that takes as an input the DW-signals/DW-features, two fully-connected hidden layers with 300 units and dropout and a final output layer for regression.

<u>Training</u>: We use separately DW-signals and DW-features for training and compare the performance of the two approaches for both RF and NN. The features, orientationally-invariant DTI parameters and spherical harmonics, were extracted as in Nedjati-Gilani et al<sup>2</sup>.

### Results

We observed very strong correlations between the predictions and the ground truth for all parameters on the noise free data (Fig.3). The NN outperforms the RF for both DW-signals and DW-features when predicting  $\tau_i$  (R<sub>R</sub><sup>2</sup>=0.74/0.71 versus R<sub>NN</sub><sup>2</sup>=0.90/0.90), providing a superior benchmark for the novel NN approach.

In the case of SNR=40, the NN continues to outperform the RF (Fig.4). All correlation coefficients are affected by noise; however, the parameters maintain a consistent, positive correlation. While the correlation coefficients for *f* and *d* remain high, that of  $\tau_i$  drops to 0.60 for NN and 0.54 for RF, due to a loss of sensitivity caused by experimental noise. As the RF performs slightly better when fitted to DW-signals, we applied this approach to the manually segmented corpus callosum (CC) of the mouse brain (Fig 5).

The mouse CC parametric maps in Fig.5 show estimates within the physiologically plausible ranges for all three parameters. The in-vivo results are inherently difficult to validate, nevertheless, studies<sup>8,9</sup> suggest values between 0.3s and 0.6s, consistent with our predictions. The mean predictions for  $\tau_i$  and *d* across the CC are consistent between the RF and the NN. There is less variability in the NN estimations for  $\tau_i$ , potentially attributable to the higher correlation coefficient seen in simulations. For *f*, the RF predictions are approximately 10% lower, an underestimation bias already observed by Nedjati et al<sup>2</sup>.

#### Discussion

The numerical simulations show that the NN framework outperforms RF. Although the presence of noise affects the performance of both approaches, NN continues to outperform RF also in realistic experimental conditions (SNR=40). Application to in-vivo data showed that both NN and RF provide histologically plausible parameters maps for mouse CC. NN predictions of  $\tau_i$  have a narrower variability compared to RF which is potentially indicative of a higher robustness to noise of the NN approach. We additionally showed that the raw DW-signals are not performing better but are equally informative as the DW-features introduced by Nedjati et al<sup>2</sup>. Future work will optimise the NN architecture, improve sequences for sensitivity to permeability and conduct further validation.

#### Conclusion

This work introduces a novel deep NN framework for the DW-MRI based estimation of permeability, representing a step forward in the construction of increasingly robust and reliable ML-based approaches for tissue microstructure estimation. The framework proposed here can be extended to other more complex biophysical models improving the estimation of microstructure parameters.

Substrate Parameters		
mean radius - $\mu_R$	[0.1,1.0] μm	
radius standard deviation - $\sigma_R$	[min(0.1,μR/5), μR/2] μm	
intra-axonal volume fraction - $f_i$	[0.40, 0.75]	
water residence time - $\tau_i$	[0.02,1.00] s	
intrinsic diffusivity - d	[0.8,2.2] µm <sup>2</sup> /ms	

PGSE EPI Sequence Parameters	
Diffusion gradient duration	5 ms
Diffusion gradient separation	10.8, 13.1, 15.4, 17.7, 20.0 ms
Diffusion gradient strength	50, 100, 150, 200, 300, 400, 500 mT/m
No. of diffusion gradient directions	16, 16, 16, 16, 8, 11, 13
TE	33.6 ms
TR	2000 ms
FOV	16x16 mm
Matrix size	160x160
Number of slices	5
Slice thickness	0.5 mm

*Figure 1*: Tissue substrate parameter ranges for the Monte Carlo Camino simulations. Each substrate is modelled as a collection of parallel non-abutting cylinders with gamma distributed radii. The parameter ranges have been chosen to mimic the structure of in-vivo mouse brain white matter. Each substrate is generated by randomly sampling each parameter from the ranges above.



*Figure 2*: The schematic architecture of the two machine learning models. The RF (left) is formed of a collection of 100 decision trees with a maximum depth of 20. The prediction of the RF is calculated as the average prediction of the decision trees. The deep NN (right) has two fully connected hidden layers, each with 300 hidden units with ReLU activation functions. The NN uses a Stochastic Gradient Descent optimiser.



*Figure 3*: Correlation-accuracy plots comparing the predicted values and the ground truth parameters for the RF (first row) and NN (second row) for the noise free condition. The test set represents previously unseen randomly selected substrates accounting for 15% of the simulated database. The data plots are colour coded according to the percentage difference between actual and estimated values as shown in the colour bar.



**Figure 4**: Correlation-accuracy plots comparing the predicted values and the ground truth parameters for the RF (first row) and NN (second row) for synthetic signals with SNR=40. Areas where  $\tau_i$ >0.5s are shaded since the signal is not sensitive to  $\tau_i$  for this protocol and SNR=40 as estimated by a sensitivity analysis fully described in another abstract submitted to this symposium. The correlation coefficients displayed are calculated in the non-shaded areas. The data plots are colour coded according to the percentage difference between actual and estimated values as shown in the colour bar.



*Figure 5*: Parametric maps showing the volume fraction, water residence time and diffusivity for one mouse CC estimated with the RF approach (first row) and the NN approach (second row). The bottom line shows the probability distributions of the predicted values for each parameter across the CC for RF (blue) and NN (brown).

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