Electron density analysis of metal–metal bonding in a Ni$_4$ cluster featuring ferromagnetic exchange

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Abstract

We present a combined experimental and theoretical study of the nature of the proposed metal–metal bonding in the tetranuclear cluster Ni₄(NP'Bu₃)₄, which features four nickel(I) centers engaged in strong ferromagnetic coupling. High-resolution single crystal synchrotron X-ray diffraction data collected at 25 K provide an accurate geometrical structure and a multipole-model electron density description. Topological analysis of the electron density in the Ni₄N₄ core using the quantum theory of atoms in molecules clearly identifies the bonding as an eight-membered ring of type [Ni–N–]₄ without direct Ni–Ni bonding, and this result is generally corroborated by an analysis of the energy density distribution. In contrast, the calculated bond delocalization index of ~0.6 between neighboring Ni atoms is larger than what has been found for other bridged metal-metal bonds, and implies direct Ni-Ni bonding. Similar support for the presence of direct Ni–Ni bonding is found in the interacting quantum atom approach, an energy decomposition scheme, which suggests the presence of stabilizing Ni–Ni bonding interactions with an exchange-correlation energy contribution approximately 50% of that of the Ni–N interactions. Altogether, while the direct interactions between neighboring Ni centers are too weak and sterically constrained to bear the signature of a topological bond critical point, other continuous measures clearly indicate significant Ni-Ni bonding. These metal–metal bonding interactions likely mediate direct ferromagnetic exchange, giving rise to the high-spin ground state of the molecule.
Introduction

The topic of chemical bonding is of integral importance for understanding the magnetic properties of molecular and extended solids.¹ Metal–metal bonding in particular underpins the properties of lanthanide-based permanent magnets and has recently been exploited in molecular lanthanide compounds to achieve record coercivities.² In certain multinuclear transition metal complexes, direct metal–metal orbital overlap has also been shown to give rise to strong ferromagnetic coupling and thermally isolated large spin ground states, as well as single-molecule magnetism due to the suppression of quantum tunneling of magnetization.³⁻⁶ Among these compounds, the tetranuclear species M₄(NPᵗBu₃)₄⁺⁻₀ (M = Co, Ni, Cu; 'Bu = tert-butyl)⁷ represent an interesting case study.⁸⁻⁹ The coordination geometry of the metal ions in these complexes is rather unusual: each metal is coordinated to two nitrogen atoms in a nearly linear fashion, creating an eight-membered (MN−)₄ ring, with all four metal atoms residing in a plane dictated by a crystallographic two-fold rotation axis and nitrogen atoms alternating above and below this plane. In the case of the neutral compound Ni₄(NPᵗBu₃)₄, computational analysis indicated a partial, direct metal–metal bonding interaction that leads to an isolated ground state molecular spin of S = 2.⁸ Density functional theory (DFT) calculations predicted four unpaired electrons residing in the metal–ligand antibonding orbitals with partial metal–metal antibonding character. If these four orbitals (4b₁*, 2a₂* and 6e*) are considered metal-metal antibonding and the three remaining metal-ligand antibonding orbitals (5e* and 3a₁*) are considered metal-metal bonding, a total metal-metal bond order of two is obtained for 1.

In contrast to a molecular orbital picture of bonding, wherein the contribution of each molecular orbital to the chemical bonding is assessed individually, the quantum theory of atoms in molecules (QTAIM)¹⁰ operates exclusively on the total electron density distribution.
Partitioning the molecule into individual Bader atomic basins allows for an unbiased analysis of interatomic interactions. This topological analysis yields so-called critical points that are classified by two numbers: the number of non-zero Hessian eigenvalues (the rank, $m$), and the algebraic sum of the signs of the Hessian eigenvalues (the signature, $n$). For example, a $(3,-1)$ bond critical point is a minimum in electron density along the bonding direction but a maximum in the two remaining directions, corresponding to one positive and two negative eigenvalues of the Hessian matrix, yielding a signature of $-1$. The QTAIM is rooted in quantum mechanics and has been used to study metal–metal bonding in a variety of molecular and extended solids.\textsuperscript{11-28} A landmark study summarizing the strengths of this approach was published by Macchi et al.,\textsuperscript{28} wherein the authors compared the molecular graphs for various cobalt cluster complexes with and without bridging ligands. It was shown that the direct metal–metal bond path disappeared and nearly straight metal–ligand bond paths emerged when a bridging ligand was introduced.

Herein, we present the results of a detailed study of chemical bonding in the central Ni$_4$N$_4$ moiety of Ni$_4$(NP$i^3$Bu$_3$)$_4$ (I). We begin by deriving a multipole model for the experimental electron density of I based on high-resolution single-crystal synchrotron X-ray diffraction data obtained at low temperature (Figure 1). We experimentally evaluate the chemical bonding based on the quantum theory of atoms in molecules via inclusion of a topological analysis of both the electron density and the total energy density. As previously established, I exhibits an $S = 2$ molecular ground state, and complete active space self-consistent field (CASSCF) analysis indicated that the four Ni sites are ferromagnetically coupled, with a computed electron-transfer energy of 6.1 eV between the adjacent Ni ions being the dominant exchange pathway.\textsuperscript{8} A major goal of the current study was to investigate whether the experimental electron density is able to detect such highly
delocalized bonding. We additionally present results from delocalization indices and an Interacting Quantum Atoms energy-partitioning as derived from computations.

**Experimental Section**

**Synthesis and Single-Crystal X-ray Diffraction Analysis**

The compound Ni₄(NP'Bu₃)₄ (1) was synthesized and crystallized using a previously published procedure.⁷ One molecule of hexane co-crystallizes with each tetranuclear cluster in the solid-state structure. Single-crystal X-ray diffraction data were collected at the BL02B1 beamline at SPring-8 in Japan. The crystal was cooled to 25 K, and six 180° ω scans (Δω = 0.1°) were carried out with χ positioned at 0°, 20°, and 40°, using 2θ-values of 0° and −10°. Data were collected with a Dectris PILATUS3 X 1M CdTe detector (λ = 0.248233 Å). A local program (Pilatus-fc)²⁹ was used to convert the obtained data to files readable by APEX3.³⁰ Lorentz and polarization corrected integrated intensities were obtained using Saint V8.38A³¹ up to a maximum resolution of sin(θ)/λ = 1.11 Å⁻¹. Scale frame factors were refined using SADABS,³² while the program SORTAV³³ was used to merge equivalent reflections. The structure was solved with ShelXT,³⁴ while ShelXL³⁵ was used for structure refinement. Hydrogen atoms were included in a riding model using the AFIX-137 command in ShelXL. The resulting geometry was used as a starting point for the multipole refinement in the program XD2016.³⁶

**Experimental Multipole Modeling**

The Multipole Model formalism introduced by Hansen and Coppens³⁷ was used to describe the electron density. The multipole model partitions the electron density into three separate
components: the spherical core density, the spherical valence density, and the aspherical valence density. Each component corresponds to a term in equation (1) below:

$$\rho_{\text{atom}}(r) = P_c \rho_c(r) + P_v \kappa^3 \rho_v(\kappa r) + \sum_{l=0}^{l_{\text{max}}} \kappa'^3 R_l(\kappa' r) \sum_{m=0}^{l} P_{lm \pm} d_{lm \pm}(\theta, \phi)$$

where $P_c$, $P_v$ and $P_{lm \pm}$ are the multipole population parameters for the core, spherical valence and aspherical valence density, respectively, and $\kappa$ and $\kappa'$ are the expansion/contraction-parameters for the spherical and aspherical parts of the valence electron density, respectively. The radial functions, $R_l(\kappa' r)$, are nodeless, single-zeta Slater functions with optimized coefficients and exponents. The functions denoted $d_{lm \pm}$ are angular orbital-like functions.$^{38}$ To enhance aspherical features, we used the Laplacian of the electron density. The negative of the Laplacian will have maxima in regions of accumulated density and minima in regions of charge depletion.$^{39}$

In the development of a multipole model, it is important to consider the choice of the local coordinate system. Firstly, any local non-crystallographic symmetry may significantly reduce the number of multipole parameters of a given atom, which improves convergence issues and limits possible correlations between parameters. The applied symmetries in the initial refinements are listed in Table S2. Secondly, the analysis of the d-orbital distribution on metal atoms is completely tied to the choice of $x$, $y$, $z$ axes. The choice of local coordinate system for the Ni-atoms is displayed in Figure S1.

As seen from Figure 1, compound 1 features a two-fold axis passing through Ni(1) and Ni(3), which constrains the positional and the thermal parameters on these two atoms. Additional constraints were added for hydrogen atoms, for which specific C–H bond distances were set depending on the bonding environment. The values are based on tabulated neutron diffraction data.$^{40}$ In addition, isotropic atomic displacement parameters (ADPs) of the hydrogen atoms were
also constrained such that they depend on the anisotropic ADPs of the atom to which they are bonded. Atoms in the compound with similar chemical environments were furthermore constrained by multipole population constraints in the initial refinements. Refinement details are provided in the Supporting Information.

Refinement of the multipole model revealed systematic errors in the diffraction data (Figure S3, grey data), which we ascribe to thermal diffuse scattering, which is inelastic scattering and variably affects the integrated intensities in the X-ray diffraction experiment. This type of scattering can be corrected according to a procedure published by Niepötter et al.,\textsuperscript{41} which substantially improves the model as seen from the fractal dimensionality plot in Figure S3.\textsuperscript{42}

**Theoretical Multipole Model**

Metal–metal bonding in 1 was previously analyzed using DFT.\textsuperscript{8} Here, to enable a comparison between the experimental model for 1 and the theoretical model in the same multipole framework, theoretical structure factors were obtained from a DFT calculation performed on 1. The theoretical structure factors, $F_H$, were calculated as a Fourier transform of the electron density:

$$F_H = Tr[D^0 I^H]$$

where $D^0$ is a one-electron density matrix, and $I^H$ is a matrix of the averaged Fourier integrals of the basis function products.\textsuperscript{43} In the current study, ORCA was used with the B3LYP functional and def2-SV(P) basis set and auxiliary basis sets generated by ORCA.\textsuperscript{44, 45} The calculation was based on the experimental atomic positions in 1 determined at 25 K, excluding the hexane molecule. The resulting quasi-restricted orbitals appear visually very similar to those previously reported (Figure S6).\textsuperscript{8} To calculate the theoretical structure factors, a fictitious crystal structure was created by placing one molecule of 1 inside a $20 \times 20 \times 20$ Å$^3$ cubic unit cell without symmetry
and subsequently the theoretical structure factors were calculated, which were then used to obtain a theoretical multipole model for comparison with experiment. The basis functions used in the multipole model are different from those used in the DFT calculation. Thus, some residual density is expected after the refinement. To improve the theoretical model, all atoms were split into two parts: one containing the core electrons and another containing the valence electrons. This approach enables the electron density belonging to the core of the atoms to be described in a more flexible manner with their own $\kappa$-parameters. The fractal dimensionality plot for the theoretical model of 1 is shown in Figure S4. Based on the narrow parabola shape seen in the plot, there are no indications of systematic errors in the model.

**Total Energy Density**

It has been shown that the total energy density, $H(r)$, is more sensitive for analyzing bonding effects than the electron density itself or the Laplacian of the electron density.$^{46,47}$ The total energy density is the sum of the kinetic energy density, $G(r)$, and the potential energy density, $V(r)$:

$$H(r) = G(r) + V(r)$$

(3)

Analysis of the total energy density for the theoretical model of 1 was performed using the AIMAll software.$^{48}$

**Interacting Quantum Atom Analysis**

Within the QTAIM analysis, the molecular energy can be partitioned into the following one- and two-basin contributions:
\[ E = \sum_A \int_{\Omega_A} d\mathbf{r}_1 \left[ \hat{T} - \sum_B \frac{Z_B}{r_{1B}} \right] \rho_1(\mathbf{r}_1; \mathbf{r}_1') + \frac{1}{2} \sum_{A,B} \int_{\Omega_A} d\mathbf{r}_1 \int_{\Omega_B} d\mathbf{r}_2 \frac{\rho_2(\mathbf{r}_1; \mathbf{r}_2)}{r_{12}} + \sum_{A>B} \frac{Z_A Z_B}{R_{AB}} \]  

(4)

where \( \Omega_A \) is the atomic basin of atom A, and \( \rho_1(\mathbf{r}_1; \mathbf{r}_1') \) and \( \rho_2(\mathbf{r}_1; \mathbf{r}_2) \) are the first- and second-order reduced density matrices, respectively. \( \rho_2(\mathbf{r}_1; \mathbf{r}_2) \) can be decomposed into a Coulombic and an exchange correlation contribution:

\[ \rho_2(\mathbf{r}_1; \mathbf{r}_2) = \rho(\mathbf{r}_1)\rho(\mathbf{r}_2) - \rho^{xc}_2(\mathbf{r}_1; \mathbf{r}_2) \]  

(5)

By rearranging equation (4), it can be shown that the energy can be partitioned into the following two terms: the atomic self-energy defined by the intra-basin contributions and the sum of all inter-basin energies.

\[ E = \sum_A \left( T_A + V_{en}^{AA} + V_{ee}^{AA} \right) + \sum_{A>B} \left( V_{nn}^{AB} + V_{en}^{AB} + V_{en}^{BA} + V_{ee}^{AB} \right) \]

\[ = \sum_A E_{self}^A + \sum_{A>B} E_{int}^{AB} \]  

(6)

The term \( V_{ee}^{AB} \) in equation (6) has two contributions, a purely Coulombic term, \( V_C^{AB} \), and an exchange-correlation contribution, \( V_{xc}^{AB} \). These are defined as:

\[ V_C^{AB} = \int_{\Omega_A} d\mathbf{r}_1 \int_{\Omega_B} d\mathbf{r}_2 \rho(\mathbf{r}_1)\rho(\mathbf{r}_2) \frac{1}{r_{12}} \]  

(7)

\[ V_{xc}^{AB} = -\int_{\Omega_A} d\mathbf{r}_1 \int_{\Omega_B} d\mathbf{r}_2 \rho^{xc}(\mathbf{r}_1; \mathbf{r}_2) \frac{1}{r_{12}} \]  

(8)

In this way, the interaction energy between atoms A and B, \( E_{int}^{AB} \), in equation (6) can be further composed into two terms:

\[ E_{int}^{AB} = V_{cl}^{AB} + V_{xc}^{AB} \]  

(9)

where the Coulombic term, \( V_{cl}^{AB} \), is the classical interaction energy:

\[ V_{cl}^{AB} = V_{nn}^{AB} + V_{en}^{AB} + V_{en}^{BA} + V_C^{AB} \]  

(10)
and the exchange correlation term, $V^{AB}_{xc}$, contains the covalent interaction between atoms A and B.\textsuperscript{49}

Determination of the interaction energy in equation (9) requires a wavefunction, which was obtained from a DFT calculation for 1. All atomic basins were initially found, and the three terms in equation (9) were then determined from the desired atom pairs. The calculations were carried out with the AIMAll software.\textsuperscript{48}

**Bond Delocalization Index**

We also employed the delocalization index to investigate the bonding properties in 1.\textsuperscript{50, 51} At the Hartree-Fock level, the delocalization index can be interpreted as the number of electron pairs shared between two basins\textsuperscript{17} and is calculated according to equation (11):

$$\delta(A, B) = 2 \int_{\Omega_A} d\mathbf{r}_1 \int_{\Omega_B} d\mathbf{r}_2 \rho^{xc}(\mathbf{r}_1; \mathbf{r}_2)$$

(11)

The two basins, $\Omega_A$ and $\Omega_B$, do not need to have a common interatomic surface for the delocalization index to be determined, meaning that the delocalization index can be calculated for any pair of atoms, regardless of whether or not they are formally bonded.\textsuperscript{52} Delocalization indices are only available from theoretical densities and were calculated from the theoretical wave function of 1 using the program AIMAll,\textsuperscript{48} which first integrates the atomic basins and subsequently determines the delocalization index between each atom pair of interest in the cluster. We note that while DIs and the underlying two-particle density are not fully defined in Kohn-Sham DFT, their use in this context is common and widely accepted.

**Results and Discussion**
**Low-Temperature Molecular Structure.** The molecular structure of 1 determined at 25 K is shown in Figure 1 (see the caption for selected average angles and distances and Tables S2 and S3 for additional bond distances and angles). As previously reported, the compound crystallizes in the space group $C2/c$ with a single hexane molecule in the unit cell. The asymmetric unit consists of half a molecule, with the other half generated by a two-fold rotation through Ni(1) and Ni(3), such that the four metal atoms are exactly in the same plane. Each of the four $[\text{Bu}_3\text{PN}]^-$ ligands bridges two Ni$^1$ ions through nitrogen, forming the vertices of a distorted molecular square cluster with nearly linear N–Ni–N edges (average N–Ni–N angle of 180.25(1)$^\circ$). Each N adopts a distorted trigonal planar geometry, with average P–N–Ni and Ni–N–Ni angles of 138.7$^\circ$ and 79.1$^\circ$, respectively. The average distance between neighboring Ni atoms is 2.361 Å, in good agreement with the previously reported structure of 1. This Ni···Ni separation is within the range of reported distances for Ni–Ni single bonds, thus the geometry does not exclude the possibility for direct metal–metal bonding between neighboring Ni centers. Of note, there are significant differences between the two Ni···Ni distances across the Ni$_4$-square. The distance between Ni(1) and Ni(3) along the two-fold rotation is 3.448 Å, whereas between Ni(2) and Ni(2) the distance is only 3.225 Å. The Ni$_4$ square is thus slightly asymmetric; however, the Ni atoms experience similar local chemical environments.
Figure 1. Single-crystal X-ray diffraction structure of 1 shown with 50% probability ellipsoids. Light blue, red, dark blue, and grey ellipsoids represent Ni, P, N, and C atoms, respectively; hydrogen atoms and the disordered hexane molecule have been omitted for clarity. The compound features a two-fold axis running through Ni(1) and Ni(3). The average Ni⋯Ni distances for neighboring and diagonal Ni centers are 2.36079(4) and 3.33680(5) Å, respectively, and the average Ni–N distance is 1.8545(2) Å. The average N–Ni–N and Ni–N–Ni angles are 180.25(1)° and 79.063(5)°, respectively.

Electron Density Analysis of Ni⋯Ni Interactions. The main purpose of this work was to study the nature of chemical bonding in the central Ni$_4$N$_4$ moiety in 1. The static deformation density is a relevant tool for this purpose, given that it highlights the aspherical features of the electron density by showing accumulated density in the bonding and lone-pair regions. The static deformation density is the difference between the density from the experimental or theoretical multipole model (see the Experimental Section for details) and the density from the independent
atom model,\textsuperscript{54} and is plotted in four different two-dimensional (2D) planes for the experimental and theoretical models of 1 in Figures S7 and S8. Figure S7b clearly shows the pronounced, direct Ni–N bonding as positive deformation density, indicating that more electron density is located here in the multipole model compared to the independent atom model.

In the original study of the magnetism of 1,\textsuperscript{8} it was suggested that the bonding between neighboring Ni atoms possesses some degree of $\pi$-character; thus Figures S8a and S8b show the experimental and theoretical deformation density in planes perpendicular to the Ni$_4$ plane. In Figure S8a, the plane bisects Ni(1) and Ni(2), whereas Ni(2) and Ni(3) are bisected in Figure S8b. In the theoretical model, there is positive deformation density in an extended region covering neighboring Ni atoms on one side of the Ni$_4$ plane in both Figure S8a and Figure S8b. This could in fact be interpreted as a signature of neighboring Ni atoms being involved in direct $\pi$-bonding; however, the positive deformation density is only present on one side of the Ni$_4$ plane, which is where the bridging nitrogen atom is located. Thus, this observed accumulation of electron density can be ascribed to the periphery of the Ni–N bonding, which is seen as large positive contours in Figure S7b. These plots demonstrate the potential limitations of relying solely on 2D-slicing through the three-dimensional electron density. In general, the unusual coordination environment around the Ni centers in 1 makes definite conclusions regarding the chemical bonding difficult to draw using the deformation density.

To derive more accurate insights into the chemical bonding in 1, we examined the Laplacian of the electron density ($\nabla^2 \rho(r)$), which can be used to identify local charge depletions ($\nabla^2 \rho(r) > 0$) and charge concentrations ($\nabla^2 \rho(r) < 0$). The calculated Laplacian is shown in Figure 2 in various planes for both the experimental and theoretical models of 1. The plots in Figures 2a, 2b, 2e, and 2f show no sign of charge accumulation between the Ni atoms. In the Ni$_4$-plane shown in
Figures 2a and 2e, the valence shell charge concentrations on all Ni atoms (represented by blue contour lines) are seen perpendicular to the diagonal Ni···Ni direction. In Figures 2b and 2f, the two maxima of the Laplacian in the valence shell of N(1) point towards the valence shell depletion regions on Ni(1) and Ni(2) in the typical key-lock fashion.\textsuperscript{55}

Figure 2. Two-dimensional plots of the negative Laplacian for the experimental (a–d) and theoretical (e–h) model of 1 in several different planes: (a) and (e) in the Ni\textsubscript{4}-plane; (b) and (f) in the Ni(1)–N(1)–Ni(2) plane; (c) and (g) in the plane perpendicular to the Ni\textsubscript{4}-plane through Ni(1) and Ni(2); and (d) and (h) in the plane perpendicular to the Ni\textsubscript{4}-plane through Ni(2) and Ni(3). The solid blue lines indicate positive contours in the negative Laplacian, $\nabla^2 \rho(\mathbf{r}) < 0$, and the dashed red lines indicate negative contours in the negative Laplacian, $\nabla^2 \rho(\mathbf{r}) > 0$. The contours are drawn at $\pm 2 \times 10^n$, $\pm 4 \times 10^n$ and $\pm 8 \times 10^n$ e Å\textsuperscript{-5} ($n = \pm 3, \pm 2, \pm 1, 0$).

Ultimately, neither the analysis of the static deformation density (Figures S7 and S8) nor the Laplacian (Figure 2) gives a clear indication of whether there is direct Ni–Ni bonding. The primary
reason is that the spatial prevalence of the Ni–N bonding features into the adjacent Ni···Ni interatomic region and renders clear conclusions impossible. On the other hand, a topological analysis of the electron density supports the absence of direct Ni–Ni bonding. Figure 3 displays all the bond paths and associated critical points—the so-called molecular graph—for the Ni₄N₄ unit. This representation shows highly directional Ni–N bonding in what becomes an eight-membered ring structure with a ring critical point at the center, and there are no signs of bonding interactions between Ni centers. The value of the electron density at the bond critical points, $\rho_b$, and the Laplacian, $\nabla^2 \rho_b$, are listed in Table S4.

**Figure 3.** Overhead (a) and side (b) views of the molecular graph of the critical points in the electron density for the experimental model of 1. The red and yellow spheres are (3,$-1$) and (3,$+1$) critical points, respectively. Bond paths and straight lines between bonding atoms are marked with golden cylinders. Light blue and dark blue spheres represent Ni and N atoms, respectively. A similar molecular graph is obtained for the theoretical model of 1 (Figure S9).
**Energy Density Analysis of Ni···Ni Interactions.** While our analysis of the electron density revealed no indication of bonding between the Ni atoms, it must be acknowledged that the classification of metal–metal bonds is a complicated matter, for which a localized description such as the QTAIM analysis has proven insufficient on several occasions,\(^{17}\) and the use of other descriptors has been encouraged.\(^{46, 56}\) An important factor causing ambiguity in the topology around these metal–metal bonding regions is the fact that the electron density landscape is often rather flat.\(^{17}\) This point is perhaps best exemplified by the study of metal···metal interactions in metal carbonyl complexes, which bear some structural resemblance to I given their very acute bond angles and bridging ligands. Chemical knowledge (principally the 18-electron rule and short metal···metal distances) unambiguously point to the presence of metal–metal bonding in compounds, such as Fe\(_2\)(CO)\(_9\) and the bridged and unbridged isomers of Co\(_2\)(CO)\(_8\).\(^{56-61}\) However, topological analysis of the electron density does not consistently reveal bond critical points between the metal atoms in such compounds. Further, a study of Fe\(_2\)(CO)\(_9\) by Reinhold *et al.* found that the type of critical point between the two Fe atoms was highly dependent upon the basis set used in the calculation.\(^{57}\) Similarly, a topological analysis of the electron density in the bridged Co\(_2\)(CO)\(_8\) complex failed to show a direct Co–Co bond critical point. In contrast, the total energy density produced a distinct minimum in \(H(r)\), coinciding with the midpoint of the hypothetical Co–Co bond, suggesting that the energy density may afford a clearer view of the properties of these weak metal–metal bonds.\(^{56}\) This point is also apparent from an electron density study of the dinuclear bridged complex Co\(_2\)(CO)\(_6\)(HC≡CC\(_6\)H\(_{10}\)OH). While a bond critical point was not observed in the electron density, inspection of the total energy density did indicate a stabilizing interaction between the Co atoms in the Co\(_2\)C triangle.\(^{26}\)
Considering these studies, we also explored the energy density distribution in 1. In an extension of previous work described above, where the energy density was qualitatively examined only along a select few lines, we present here also a full topological analysis of this property. The topology of $K(r) = -H(r)$ can be analyzed in the same way as the electron density, and an analogous “molecular graph” can be created (see Figure 4). In complete accordance with the electron density, the topology of the energy density recovers the ring structure with eight $(3, -1)$ critical points forming the $(\text{Ni–N–})_4$ chain, and a central $(3, +1)$ critical point. However, additional critical points appear in the analysis of $K(r)$ in the Ni$_4$ square along with their symmetry-related critical points: two $(3, -1)$ critical points linking Ni(2) and Ni(2)$'$ across the diagonal of the Ni$_4$ square and four $(3, -3)$ critical points located in the Ni–N–Ni planes between neighboring Ni atoms. Recalling that $H(r) = -K(r)$, the $(3, -3)$ critical points correspond to local minima in $H(r)$, and each minimum may be interpreted as the signature of a stabilizing interaction (see Figure S10 for visualization of one such minimum in the plot of $H(r)$ from Ni(1) to Ni(2)). Thus, in all, our exploration of chemical bonding between the Ni centers in 1 using topological analysis provides rather ambiguous results.
Figure 4. Overhead (a) and side (b) views of the molecular graph of the critical points in $K(r)$ for the theoretical wavefunction of 1. Red, green, and yellow spheres are $(3,-1)$, $(3,-3)$, and $(3,+1)$ critical points, respectively.
Figure 5. Two-dimensional contour maps of $K(r)$ (a, c) and $\rho(r)$ (b, d) for the theoretical wavefunction of 1 plotted in the Ni$_4$-plane (upper) and in the Ni(1)–N(1)–Ni(2) plane (lower). Selected contour values are shown in Hartree/Å$^3$ and e/Å$^3$ for $K(r)$ and $\rho(r)$, respectively. Contour values used for plotting are listed in Supporting Information.
Interacting Quantum Atoms. We turned to the Interacting Quantum Atoms (IQA) approach to examine the interatomic interaction energies and explore a global measure of chemical bonding. The interaction energy, $E_{int}^{AB}$, is the sum of a Coulombic contribution, $V_{cl}^{AB}$, and an exchange correlation contribution, $V_{xc}^{AB}$, that can be interpreted as a covalent term (see the Experimental Section and equation (9) for details). The IQA energies for 1 are listed in Table 1. The interaction energy between neighboring Ni centers is negative and thus constitutes a stabilizing interaction. The Coulombic contribution is necessarily positive, given that the Ni centers are positively charged ions. The negative total IQA energy is therefore a consequence of a strong covalent term, that is, a signature of significant electron sharing between the two atomic basins. In contrast, both pairs of Ni ions related diagonally on the Ni$_4$-square exhibit positive overall IQA energies, which can therefore be regarded as destabilizing.

Table 1. Table of IQA energetic profiles for the theoretical model of 1. The term $E_{int}^{AB}$ is the interaction energy between atoms A and B, $V_{cl}^{AB}$ is the classical Coulombic interaction energy and $V_{xc}^{AB}$ is the exchange correlation interaction energy. All energies are listed in atomic units.

<table>
<thead>
<tr>
<th>Atom Pair</th>
<th>$E_{int}^{AB}$</th>
<th>$V_{cl}^{AB}$</th>
<th>$V_{xc}^{AB}$</th>
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</thead>
<tbody>
<tr>
<td>Ni(1)–Ni(2)</td>
<td>−0.0152</td>
<td>0.0797</td>
<td>−0.0948</td>
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<tr>
<td>Ni(2)–Ni(3)</td>
<td>−0.0162</td>
<td>0.0789</td>
<td>−0.0951</td>
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<td>Ni(1)–Ni(3)</td>
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<td>0.0387</td>
<td>−0.0076</td>
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<tr>
<td>Ni(2)–Ni(2)'</td>
<td>0.0329</td>
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<td>−0.0133</td>
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<tr>
<td>Ni–N (avg.)</td>
<td>−0.4756</td>
<td>−0.3027</td>
<td>−0.1729</td>
</tr>
</tbody>
</table>

Bond Delocalization Index. Highly related to the energetics of the system obtained using the IQA approach are the delocalization indices (Table 2). In well-defined molecular systems of lighter elements, the delocalization index represents the number of electron pairs shared between two
atoms, irrespective of whether the two atoms involved share a bond critical point. The situation is a little less clear when metal atoms are involved and bond orders of significantly less than unity are found, even when bond critical points are present. For instance, in the unbridged $D_{3d}$ isomer of Co$_2$(CO)$_8$ which has a bond critical point at the Co–Co midpoint, the Co–Co delocalization index is 0.48. For the corresponding bridged $C_{2v}$ isomer with no Co–Co bond critical point, however, the delocalization index is slightly smaller at 0.37.\textsuperscript{62}

Although no Ni-Ni bond critical points were found in the analysis of the experimental electron density of 1, the delocalization indices between pairs of neighboring Ni atoms were found to be ~0.6 (Table 2). The size of these delocalization indices suggests relatively strong interactions between the neighboring Ni atoms in 1 and is only slightly smaller than the ones found for the ligand Ni-N interactions being ~0.7. The ligand-metal delocalization indices fit well with other reported metal-ligand delocalization indices. For example, in dimeric copper and silver $m$-terphenyl complexes with comparable metal coordination geometries and short metal–metal distances, the delocalization indices between each metal and the bridging carbon atom of the $m$-terphenyl ligand were found to be in the range 0.51–0.61.\textsuperscript{63} For the bridged $C_{2v}$ isomer of Co$_2$(CO)$_8$, the delocalization indices between the cobalt centers and the bridging CO were found to have an average value of around 0.82.\textsuperscript{61}

Comparison of the magnitude of the Ni-N and Ni-Ni delocalization indices offers a simplistic, yet intuitive interpretation of the delocalization indices: At each corner of the Ni$_4$N$_4$-square, there is a Ni$_2$N triangle (e.g., Ni(1)-N(1)-Ni(2)). Within each interaction triangle, two electron pairs are shared, and each of three interactions in the triangle has a bond order of around 2/3.
The strong Ni-Ni interactions are predominantly present between the neighboring Ni-atoms, as much lower values are found for the delocalization indices between Ni atoms across the diagonal of the Ni$_4$-square (0.071 and 0.107 for Ni(1)-Ni(3) and Ni(2)-Ni(2)$'$, respectively).

A total delocalization index of 2.6 is obtained for all six individual Ni-Ni interactions, including the two Ni-Ni interactions across the diagonal which exhibit values of 0.071 and 0.107 (Table 2). This may be compared to the bond orders obtained from the previously published DFT calculations on this complex. One interpretation of the molecular orbitals in that study of 1 is that a total of 4 electrons take part in direct Ni-Ni bonding, or a total bond order of 2.0, comparable to the value of 2.6 found here.

Table 2. Calculated delocalization indices for selected atom pairs in the central part of 1 based on the theoretical wavefunction from the DFT calculation.

<table>
<thead>
<tr>
<th>Atom pair</th>
<th>Delocalization Index</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ni(1)--N(1)</td>
<td>0.723</td>
</tr>
<tr>
<td>Ni(2)--N(1)</td>
<td>0.729</td>
</tr>
<tr>
<td>Ni(2)--N(2)</td>
<td>0.725</td>
</tr>
<tr>
<td>Ni(3)--N(2)</td>
<td>0.723</td>
</tr>
<tr>
<td>Ni(1)--Ni(2)</td>
<td>0.594</td>
</tr>
<tr>
<td>Ni(2)--Ni(3)</td>
<td>0.596</td>
</tr>
<tr>
<td>N(1)--P(1)</td>
<td>0.842</td>
</tr>
<tr>
<td>N(2)--P(2)</td>
<td>0.843</td>
</tr>
<tr>
<td>Ni(1)--Ni(3)</td>
<td>0.071</td>
</tr>
<tr>
<td>Ni(2)--Ni(2)$'$</td>
<td>0.107</td>
</tr>
</tbody>
</table>

Conclusions

We have developed experimental and theoretical models of the electron density in Ni$_4$(NP$'$Bu$_3$)$_4$ (1) based on high-resolution single-crystal synchrotron X-ray diffraction data, in an attempt to better understand the proposed metal–metal bonding interactions in this structure. Despite the exceptional quality of the diffraction data and derived multipole models for Ni$_4$(NP$'$Bu$_3$)$_4$, the
topological analysis of the electron density of the metal–metal bonding in the molecule proved to be challenging.

The analysis of the static deformation density and the Laplacian distribution did not reveal any clear indication of intramolecular Ni–Ni bonding, due to the overwhelming contribution from the stronger Ni–N interactions. Further, topological analysis of the electron density showed no bond critical points between Ni centers; however, some additional critical points were present in the analysis of the energy density. The interacting quantum atom approach revealed that interactions between neighboring Ni atoms—but not those across the diagonal—do indeed stabilize the complex via a dominant covalent interaction energy. In addition, the delocalization indices gave strong indications of delocalized electron density between the neighboring Ni-atoms, giving almost similar sized values for metal–metal and metal–ligand pairs.

The results from the topological analysis of the experimental electron density highlight the challenges encountered in the characterization of metal–metal bonding interactions. The relatively flat electron density landscape in the interatomic regions is often overwhelmed by the stronger nearby metal–ligand interactions, rendering the study of metal–metal interactions difficult. In the context of the magnetic interactions, the current analysis shows that Ni–Ni interactions are in fact present. The bonding interaction allows the kinetic energy of the electrons to overcome pairing energy of a bond, which is critical for ensuring maximal spin in accord to Hund’s rule via electron exchange pathways. Therefore, we reason that the metal–metal interactions of the type evaluated here are a key to the intriguing magnetic properties of such molecules.

ASSOCIATED CONTENT
The following files are available free of charge.

Information about data and model quality, DRK-plots, fractal dimensionality plots, structural results, theoretical molecular orbitals, topological analysis, d-orbital populations (PDF)

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Author Contributions

The manuscript was written through contributions of all authors. All authors have given approval to the final version of the manuscript.

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REFERENCES


Electron density analysis of the magnetically interesting Ni$_4$ cluster compound in the Figure based on extremely accurate synchrotron diffraction data could did not disclose any direct Ni-Ni chemical bonding. On the contrary, advanced theoretical bonding descriptors such as the delocalization indices and interacting quantum atoms clearly show discernible and rather strong direct Ni-Ni bonding, comparable in strength to the Ni-N metal ligand bonds.