# Improving the Performance of Deep Learning Techniques using Nature Inspired Algorithms and Applying them in Porosity Prediction 

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#### Abstract

Within the field of Artificial Intelligence (AI), Deep Learning (DL) based on Convolutional Neural Network (CNN) can be used for analysing images. However, the performance of the DL models depends on the design of the CNN topology to achieve their best performance. Hence, firstly, this work addresses this problem by proposing a novel nature inspired hybrid algorithm called BA-CNN where a swarm based Bees Algorithm (BA) is used to optimize the CNN parameters. In addition, another algorithm called BA-BO-CNN is proposed that combines the BA with Bayesian Optimization (BO) to increase the CNN performance and that of BA-CNN and BO-CNN. This study shows that applying the hybrid BA-CNN to the 'Cifar10DataDir' benchmark image did not improve the validation and testing accuracy compared to the existing CNN and BO-CNN. However, the hybrid BA-BO-CNN achieved better validation accuracy of $82.22 \%$ compared to $80.34 \%$ and $80.72 \%$ for the CNN and BO-CNN, and also with a better testing accuracy of $80.74 \%$ compared to $80.54 \%$ and $80.69 \%$ for the CNN and BO-CNN respectively. The BA-BOCNN achieved lower computational time than the BO-CNN algorithm by 2 minutes and 11 seconds. Although applying both algorithms to the 'digits' dataset produced almost similar accuracies with a difference of $0.01 \%$ between BA-CNN and BO-CNN, the BA-CNN achieved a computational time reduction of 4 minutes and 14 seconds compared to the BOCNN, making it the best algorithm in terms of cost-effectiveness. Applying BA-CNN and BA-BO-CNN to identify 'concrete cracks' images produced almost similar results to some of the other existing algorithms with a difference of $0.02 \%$ between BA-CNN and original CNN. Finally, applying them to the 'ECG' images improved the testing accuracy from $90 \%$ for the BO-CNN to $92.50 \%$ for the BA-CNN and $95 \%$ for the BA-BO-CNN with a similar trend for validation accuracy and computational time.

Secondly, the CNN that was adopted for the purpose of regression which is called RCNN was applied in the manufacturing context, particularly to predict the percent of porosity in the finished Selective Laser Melting (SLM) parts. Because testing the performance of the RCNN algorithm requires a large amount of experimental data which is generally difficult to obtain, in this study an artificial porosity image creation method is proposed where 3000 artificial porosity images were created mimicking real CT scan slices of the SLM part with a similarity index of 0.9976 . Applying the RCNN to the 3000 artificial


porosity images slices showed the porosity prediction accuracy to improve from $68.60 \%$ for the image binarization method to $75.50 \%$ for the RCNN, while the proposed novel hybrid BA-BO-RCNN and BA-RCNN yielded better prediction accuracies of $83 \%$ and 85.33\% respectively.

Thirdly, in order to improve the performance even further, this study proposes to add Long Short Term Memory (LSTM) to BA-CNN because of their ability to deal with sequential data to produce another novel hybrid algorithm called BA-CNN-LSTM and the results showed an increase in the prediction accuracy reaching $95.50 \%$.

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## List of Abbreviations

Additive Manufacturing (AM)
Analysis of Variance (ANOVA)
Artificial Bee Colony (ABC)
Artificial Intelligence (AI)

Artificial Neural Network (ANN)
Auto Encoder Network (AEN)
Bayesian Convolutional Neural Network (BO-CNN)
Bayesian Optimization (BO)
Bayesian Regression Convolutional Neural Network (BO-RCNN)
Bees Algorithm (BA)
Bees Bayesian Convolutional Neural Network (BA-BO-CNN)
Bees Bayesian Regression Convolutional Neural Network (BA-BO-RCNN)
Bees Convolutional Neural Network (BA-CNN)
Bees Convolutional Neural Network Long Short-Term Memory (BA-CNN-LSTM)
Bees Regression Convolutional Neural Network (BA-RCNN)
Binder Jetting (BJT)
Charged-Coupled Device (CCD)
Computer Aided Design (CAD)
Computer-Aided Manufacturing (CAM)
Computed Tomography (CT)
Convolutional Neural Network (CNN)
Convolutional Neural Network Long Short-Term Memory (CNN-LSTM)

Convolutional Neural Network with Evolutional Algorithm (EA-CNN)
Convolutional Neural Network with Fuzzy Logic (FL-CNN)

Convolutional Neural Network with Genetic Algorithm (GA-CNN)
Cyber-Physical System (CPS)
Deconvolutional Neural Network (DNN)
Deep Belief Network (DBN)
Deep Convolutional Inverse Graphics Neural Network (DCIGNN)

Deep Convolutional Neural Network (DCNN)
Deep Learning (DL)

Deep Recurrent Network (DRN)
Denoising Auto Encoder Network (DAEN)
Design of Experiments (DOE)
Differential Evolution (DE)
Digital Light Processing (DLP)
Directed Energy Deposition (DED)
Direct Metal Deposition (DMD)
Direct Metal Laser Sintering (DMLS)

Electrocardiogram (ECG)
Expected Improvement (EI)

Evolutionary Algorithm (EA)
Fused Deposition Modelling (FDM)
Fuzzy Logic (FL)

Gated Recurrent Network (GRN)

Generative Adversarial Network (GAN)
Genetic Algorithm (GA)
Infrared (IR)
Initial Learning Rate (ILR)
Internet of Things (IoT)
Laminated Object Manufacturing (LOM)
Laser Engineered Lens Shaping (LENS)
Laser Metal Deposition (LMD)
Long Short-Term Memory (LSTM)
Machine Learning (ML)
Magnetic Resonance Imaging (MRI)
Material Jetting (MJT)
Momentum (M)
Paper Lamination Technology (PLT)
Particle Swarm Optimization (PSO)
PolyJet (PJ)
Powder Bed Fusion (PBF)
Recurrent Neural Network (RNN)
Recursive Network (RN)
Regression Convolutional Neural Network (RCNN)
Regularization (R)
Restricted Boltzmann Machine (RBM)
Root Mean Square Error (RMSE)

Scanning Electron Microscope (SEM)
Section Depth (SD)

Selective Laser Melting (SLM)
Selective Laser Sintering (SLS)

Sequence to Sequence Model (S2SM)
Sparse Auto Encoder Network (SAEN)
Stereolithography (SLA)

Stochastic Gradient Descent (SGD)
Stochastic Gradient Descent Momentum (SGDM)

Structural Similarity Index (SSI)
Ternary Bees Algorithm (BA-3+)
Ultrasonic Additive Manufacturing (UAM)
Validation Accuracy (VA)
Variational Auto Encoder Network (VAEN)

Vat Photopolymerization (VPP)

## List of Symbols

X: The input vector to the SoftMax function
$z_{j}$ : The input of all elements in the vector
$e^{z}$ : The exponential function applied to each element
$\sum \mathrm{e}^{\mathrm{z}}$ : The normalization term
K: The number of classes
$\mu(f(x))$ : The prediction from the gaussian process for new data point $x$ $\phi(\mathrm{z})$ : The standard normal cumulative probability density
$\sigma(\mathrm{f}(\mathrm{x}))$ : The standard deviation of the prediction for new data point x $\phi(\mathrm{z})$ : The standard normal probability density
$\mu_{\mathrm{x}}$ : The local mean for image x
$\mu_{\mathrm{y}}$ : The local mean for image y
$\sigma_{\mathrm{x}}$ : The standard deviation for images x
$\sigma_{\mathrm{y}}$ : The standard deviations for images y
$\sigma_{\mathrm{xy}}$ : The cross-covariance for images x and y .
$\alpha$ : The exponent for luminance
$\beta$ : The exponent for contrast
$\gamma$ : The exponent for structural
$\mathrm{X}_{\mathrm{t}}$ : The current time cycle input
$\mathrm{U}_{\mathrm{f}}$ : The input weight matrix
$\mathrm{H}_{\mathrm{t}-1}$ : The previous time cycle hidden state
$\mathrm{W}_{\mathrm{f}}$ : The hidden state weight matrix

## List of Publications

## Journal Articles:

1. Alamri NMH, Packianather M, Bigot S. Optimizing the Parameters of Long ShortTerm Memory Networks Using the Bees Algorithm. Applied Sciences. 2023; 13(4):2536. https://doi.org/10.3390/app13042536.
2. Alamri NMH, Packianather M, Bigot S. Predicting the Porosity in Selective Laser Melting Parts Using Hybrid Regression Convolutional Neural Network. Applied Sciences. 2022; 12(24):12571. https://doi.org/10.3390/app122412571.
3. Alamri, N. M. H., Packianather, M., \& Bigot, S. (2022). Deep learning: parameter optimization using proposed novel hybrid bees Bayesian convolutional neural network. Applied Artificial Intelligence, 1-25.

## Conference Papers:

1. Alamri, N. M. H., Packianather, M., \& Bigot, S. (2023). A Novel Hybrid Bees Regression Convolutional Neural Network (BA-RCNN) Applied to Porosity Prediction in Selective Laser Melting Parts. Cardiff University School of Engineering Research Conference 2023. (Submitted on 28 Feb 2023 and it will be presented if accepted on $\mathbf{1 2 - 1 4}$ July 2023 - it will be published after the presentation).
2. N. M. H. Alamri, M. Packianather and S. Bigot, "Optimization of Convolutional Neural Network Topology and Training Parameters using Bees Algorithm," 2022 IEEE 2nd International Symposium on Sustainable Energy, Signal Processing and Cyber Security (iSSSC), Gunupur, Odisha, India, 2022, pp. 1-6, doi: 10.1109/iSSSC56467.2022.10051487.

## Chapter Book:

1. Alamri, N. M. H., Packianather, M. (2022). Chapter Book with the title "Optimisation of Convolutional Neural Network Parameters using Bees Algorithm" (Accepted on 14 Nov 2022 - expected to be published at the end of 2023).

## Chapter 1: Introduction

### 1.1 Background

Artificial Intelligence (AI) is an essential concept used to facilitate the development of intelligent systems (Li et al., 2017) in order to increase the productivity and maximize the efficiency of the processes such as manufacturing machines. The most popular AI techniques are based on Artificial Neural Network (ANN), a type of Machine Learning (ML) inspired by the biological nervous system. These computing systems can be used to model big data and find complex relationships (De Filippis et al., 2017). ANNs are capable of handling high-dimensional real-time data and extracting implicit meaningful patterns that can be used to predict the future state of complex systems (Wuest et al., 2016). In addition, ANNs are capable of handling complex dynamic problems due to their ability to deal with nonlinearity. It is worth noting that ANNs are trained on historic data with relative ease by adjusting their control parameters such as learning rate and momentum.

Big Data analytics (Geissbauer et al., 2016) is an integral part of the industry 4.0 paradigm, known as the fourth industrial revolution which aims at creating smart systems where technologies are transformed by the Internet of Things (IoTs), Cyber-Physical Systems (CPSs) and cloud computing. Modelling an IoT system is based on modelling a stochastic system addressing the relationship between process and system performance and providing a quantitative analysis of system performance (Ciortea, 2018). On the other hand, many challenges are remaining when applying ANNs (Wuest et al., 2016), the biggest one is the data acquisition issue as the availability of relevant data is not guaranteed. In addition, applying appropriate data mining after collecting a dataset can also be a challenging task, particularly for cases where a high amount of irrelevant data may have been collected, thus affecting the performance of the produced models.

As an extension to ANN capabilities, Deep Learning (DL) techniques are now wellestablished, producing better learning capability as stated in (Singh et al., 2018). They have the advantage of using automatic feature extraction by learning a large number of nonlinear filters before the decision making stage. One of the most popular DL networks is Convolutional Neural Network (CNN) (Singh et al., 2018) which is used mainly with image data. It can be integrated with other intelligent swarm optimization algorithms to optimize its parameters in order to improve the performance of the CNN model in analysing a large number of images for classification and prediction problems.

Firstly, this thesis addresses the need for designing better CNN topology by proposing a novel nature inspired hybrid algorithm that takes into account the advantages of global, local, and intense searches in the Bees Algorithm (BA) which is known to mimic the behaviour of honeybees, to optimize the CNN parameters which is called the Bees Convolutional Neural Network (BA-CNN) algorithm. Furthermore, another nature inspired hybrid algorithm is proposed which combines the BA with Bayesian Optimization (BO) in order to increase the performance of the CNN which is referred to as BA-BO-CNN algorithm.

In addition, Long Short-Term Memory (LSTM) is one of the DL networks that deals with time series or sequential data, it is an advanced Recurrent Neural Network (RNN) that persists the information for a long period so that it can remember long-term dependencies (the-learning-machine). The RNN can persist the information as well, but for a shorter period, so it cannot remember the dependencies in the long term, the LSTM is established to address this problem in RNN (Thakur, 2018). It consists of three gates, the first one is the forget gate that decides if it is needed to remember the information coming from the previous time scale or not, the second one is the input gate that learns information from the cell input, and the last gate is the output gate where the cell transfers the updated information to the next time cycle. In addition, it has a cell state that carries the information along with all cycles and a hidden state for short-term memory (www.analyticsvidhya.com). The performance of the LSTM in dealing with the sequential data can be improved by optimizing the parameters related to the three gates and cell state.

Secondly, this thesis proposes a novel hybrid nature inspired algorithm that uses the BA to improve the performance of three gates and cell state, specifically by optimizing the learning rate factor so that each part has its learning rate determined based on the global learning rate. Having a more optimum learning rate means more optimum updates for the network weight (Brownlee, 2020). The hybrid Bees Convolutional Neural Network Long Short-Term Memory referred to as BA-CNN-LSTM combines the best DL networks in dealing with images and sequential data as CNN is the most powerful DL network in analysing images (Elngar et al., 2021) and (Chaganti et al., 2020). In addition, the LSTM network is the best algorithm for dealing with sequential data, as it persists the information
for a long period remembering long-term dependencies which address the problem of normal RNN (the-learning-machine).

CNN and LSTM algorithms are effective DL networks that can be applied in the manufacturing context, particularly to analyse images related to Additive manufacturing (AM). It is a process that builds objects by joining material in successive layers, under computer control and using data from a 3D model (Farinia Group, 2018). AM is also referred by other terms such as 3D printing, rapid prototyping, digital manufacturing, and layered manufacturing. Initially, AM or 3D printing technologies were used mainly for rapid prototyping, but with improvements in the reliability and efficiency of the AM processes as well as in the material properties of the components produced, they are increasingly used in more advanced applications such as to create highly customized products, producing a small volume of serial components and visualizing tool in design. Future applications may concern human organ creation, clothes manufacturing, and food confection (Farinia Group, 2018).

There are seven AM processes: powder bed fusion, material extrusion, material deposition, binder jetting, sheet lamination, vat photopolymerization, and directed energy deposition. The focus of this thesis will be on powder bed fusion. (Sun et al., 2017) stated that it is a laser-based additive manufacturing in which the laser beam scans the selected locations of the powder bed at a controlled speed and then it fuses the powder to the solid material by either partial melting in Selective Laser Sintering (SLS) or full melting in Selective Laser Melting (SLM) which is a metal-based process that uses the laser selectively to melt the powder after layer by layer fabrication as mentioned in (Shrestha, et al., 2019). They mentioned that metal-based AM has many issues such as porosity, part deformation and cracks. The porosity is the most challenging issue as stated in (Snell et al., 2020). The paper mentioned that the porosity has a significant effect on the mechanical properties as it causes structural failures. Assessing the porosity in the SLM parts is a challenging issue, the drawback of using the existing gray value analysis method to assess the porosity is the difficulty and subjectivity in selecting a uniform grayscale threshold to convert a single slice into binary images to highlight the porosity.

Thirdly, this thesis proposes a new approach based on the use of a Regression Convolutional Neural Network (RCNN) algorithm to predict the percent of porosity in CT scans of the finished SLM parts, without the need for subjective difficult thresholding determination to convert a single slice into binary images. In order to test the algorithm, as the training of the RCNN would require a large amount of experimental data, artificial porosity images mimicking real CT scan slices of the finished SLM parts are created using a new efficient method. In addition, the LSTM network is added to CNN (CNN-LSTM) to enhance the porosity prediction as it has better capability in dealing with the sequential layers of the SLM parts. BA is used as well to optimize the parameters of DL networks in order to improve the model's performance in predicting the percent of porosity.

### 1.2 Aim and Objectives

The aim of this thesis is to improve the performance of convolutional neural networks using nature inspired algorithms and apply them to predict the porosity in the finished parts manufactured by the selective laser melting process.

The objectives to achieve the aim in terms of CNN are:

1. Optimize CNN parameters using BA and BO techniques.
2. Apply the developed hybrid CNN algorithms to predict the percent of porosity in the finished parts of the SLM process based on porosity images.
3. Analyse the results and make further improvements to the developed algorithms as necessary.

The objectives to achieve the aim in terms of the SLM process are:

1. Investigate the limitations of the existing method used to predict the percent of porosity in the finished parts of the SLM process.
2. Apply the existing approach to predict the percent of porosity.
3. Compare the prediction results of the existing method with the hybrid CNN algorithms in order to validate the issue.

### 1.3 Research Questions

The research questions that will be addressed are:

- Q1: How to design the optimum topology for the Convolutional Neural Network using the Bees Algorithm that can be used for several applications including porosity prediction?
- Q2: How to improve the way of analysing the porosity in the parts produced by the Selective Laser Melting process using the novel optimised Bees Convolutional Neural Network?
- Q3: How to improve the performance of the Long Short-Term Memory Network in dealing with sequential data using the Bees Algorithm for enhancing the porosity prediction in the sequential layers of the Selective Laser Melting parts?


### 1.4 Thesis Outline

This thesis consists of the following chapters:
Chapter 1- Introduction: gives the background to the topic of research, states the aim, objectives, research questions, thesis outline, and the limitations and assumptions made in this study.

Chapter 2- Literature Review: presents a review of DL in general and of CNN and LSTM in particular in order to find gaps and open issues that need to be fulfilled in the future to improve the performance of the DL models. Also, it shows the impact and recent applications of optimizing DL algorithms using nature inspired algorithms showing the gap that will be addressed in the next chapter. In addition, it states AM processes, applications, advantages, and gaps and open issues that need to be addressed. It focuses on powder bed fusion processes showing the way of working, thermodynamical phenomena, parameters, open issues, three porosity types, and state of the art studies about adopting DL techniques to improve the performance of SLM process.

Chapter 3- Convolutional Neural Network Parameters Optimization using Nature Inspired Algorithms: investigates the significant CNN parameters that affect the classification accuracy on the validation set. The chapter proposes a new hybrid BA-CNN
algorithm that uses the BA to optimize CNN parameters in order to increase the classification accuracy of the network. In addition, it proposes a novel nature inspired hybrid algorithm that combines the BA with the BO in order to increase the overall performance of CNN which is referred to as BA-BO-CNN algorithm. The results of applying the hybrid BA-CNN and BA-BO-CNN algorithms to four benchmark image data are shown in this chapter. In addition to these datasets, the following chapter creates artificial porosity images mimicking the real CT scans of the finished SLM parts that can be analysed using the hybrid algorithm developed in this chapter.

The contributions of the chapter are:

- Developing a novel hybrid Bees Convolutional Neural Network (BA-CNN) algorithm in order to improve the performance of CNN.
- Developing a novel hybrid Bees Bayesian Convolutional Neural Network (BA-BOCNN ) algorithm in order to improve the performance of CNN.

Chapter 4- Artificial Porosity Images Creation for Selective Laser Melting Parts: proposes a new efficient approach of creating artificial porosity images mimicking the real CT scan slices of the finished SLM parts with a similarity index of 0.9967 . This chapter's contribution which will be continued further in the following chapter is:

- Developing a new approach to create a large amount of experimental artificial porosity images similar to real images by a similarity index of 0.9967 which can be used in the research environment efficiently and effectively in order to predict the percent of porosity in the finished SLM part using the developed hybrid CNN algorithms as will be described in the following chapter.

Chapter 5- Hybrid Regression Convolutional Neural Network for Predicting the Percent of Porosity in Selective Laser Melting Parts: highlights the limitations of predicting the percent of porosity in the finished SLM parts using the existing image binarization method and it proposes a new approach based on the use of the RCNN algorithm in order to predict the percent of porosity in CT scans of the finished SLM parts, without the need for subjective difficult thresholding determination to convert a single slice into binary images. The algorithm is then further developed by optimizing its parameters
using the BA to produce a better prediction accuracy using Bees Regression Convolutional Neural Network (BA-RCNN). Chapters 4 and 5 produce the following contribution:

- Proposing and validating a new approach for predicting the percent of porosity in the finished SLM parts, using hybrid Bees Regression Convolutional Neural Network (BA-RCNN). It was demonstrated that a better accuracy than the existing image binarization method could be achieved (approximately $17 \%$ improvement with the data set used). In order to test the algorithm, as the training of the RCNN would require a large amount of experimental data, artificial porosity images mimicking real CT scan slices of the finished SLM part were created with a similarity index of 0.9976 with real images.


## Chapter 6- Hybrid Long Short-Term Memory Network with Bees Algorithm for

 Enhancing the Porosity Prediction in Selective Laser Melting Parts: proposes a nature inspired algorithm that improves the performance of LSTM in dealing with the sequential data by optimizing the parameters related to the three gates and cell state. The novel hybrid nature inspired algorithm uses the BA to improve the performance of three gates and cell state, specifically by optimizing the learning rate factor so that each part has its learning rate determined based on the global learning rate. Having a more optimum learning rate means more optimum updates for the network weight. Artificial porosity images are used for testing the algorithms; as the input data are images, CNN is added in order to extract the features in the images for feeding it into the LSTM in order to predict the percent of porosity in the sequential layers of artificial porosity images that mimic real CT scan images of products manufactured by SLM process. In addition, it is applied in other contexts such as in signal processing to classify Electrocardiogram (ECG) benchmark image data. Also, it can deal with time series numerical data, CNN is not needed in this case as there is no feature extraction task for the images. The contribution of this chapter is:- Improving the performance of the LSTM network in predicting sequential data using BA. As the input data are images, CNN is added to extract the image features yielding a hybrid algorithm (BA-CNN-LSTM) that provides a $10 \%$ more accurate prediction of porosity percentage appearing in the sequential layers of artificial porosity images that mimic CT scan images of parts manufactured by SLM process.

Chapter 7- Conclusion: summarises the thesis contributions to knowledge, shows study limitations and suggests recommendations for future work.

### 1.5 Study Limitations and Assumptions

One of the limitations of this study is the number of evaluations used in conducting BA and BO to optimize DL parameters, they are limited to the computer capability in advanced research computing at Cardiff University. As DL networks require high computations, the number of evaluations is limited.

This research is not aimed to study the porosities in depth, so no experiments have been conducted, but the work proposes DL methods that will enhance such studies, particularly in predicting the percent of porosity in the finished SLM part.

The creation of artificial porosity images is only based on the laser power and scanning speed parameters as the dataset used to create the images presents only data about laser power and scanning speed. Finally, the created artificial porosity images illustrate only one type of pore which is keyhole porosity considering one shape of this type which is the nearly spherical shape.

## Chapter 2: Literature Review

### 2.1 Deep Learning

This section presents a brief review of DL showing its history, definition, advantages, limitations, and applications.

### 2.1.1 History and Definition

The history of ANN started in 1943 with using threshold logic to create a computer model based on the neural network of the human brain by Walter Pitts and Warren McCulloch (Foote, 2022). Then, the perceptron was created in 1957 by Frank Rosenblatt (Machine Learning Knowledge, 2019). In 1960, the back propagation model was developed by Henry Kelley, it was simplified by Stuart Dreyfus to be based on chain rule only. In the early 1980s, John Hopfield created a recurrent neural network (Machine Learning Knowledge, 2019) and Kunihiko Fukushima designed the first CNN with multiple convolutional and pooling layers in the 1970s. The first practical lab for backpropagation demonstration was provided by Yann LeCun in 1989, he combined it with CNN to detect handwritten digits. The development of the LSTM network was in the 2000s to solve the vanishing gradient problem (Kamalika, 2018). In 2009, ImageNet was launched by a professor at Stanford Fei-Fei Li, it assembled 14 million of labelled images to be used for free. In 2011, GPU speed had increased significantly making DL an efficient tool which result in the development of a pre-trained CNN called AlexNet. Generative Adversarial Network was developed by Ian Goodfellow in 2014 to imitate images using a generator that generates the image and a discriminator that discriminates the real and generated images, both networks compete against each other until the near perfect image is produced (Foote, 2022).

DL techniques are well-established as an extension to ANN capabilities, producing better learning capability as stated in (Singh et al., 2018), they said that deep learning is a class of ML techniques which utilizes multiple processing layers where the output from a previous layer is used as an input for the following layer, to learn representations of data with multiple levels of abstraction. The difference between traditional learning and DL can be seen in terms of the feature extraction process, which depends on the data and the model types. Using the traditional learning leads to significant time being consumed while applying a trial-and-error approach to the feature extraction process and the success depends on the user experience. On the other hand, the DL approach will benefit from an
automatic feature extraction process through the learning of a large number of nonlinear filters before making decisions. Thus, DL combines feature extraction and decision making within one model and avoids the often-suboptimal manual handcrafting.

### 2.1.2 Advantages, Limitations, and Applications

DL have many network structures that can be used in different real-life applications. Each network will have its advantages and limitations depending on the applications as shown in the following table 2.1:

Table 2.1: Deep Learning Networks

| Network | Advantages | Limitations | Applications | References |
| :---: | :---: | :---: | :---: | :---: |
| Convolutional <br> Neural Network <br> (CNN) | Eliminating the need for extracting the features manually, it is achieved by alternating and stacking pooling and convolutional layers that convolve with the input data to extract the most significant features <br> Can be used with image data, text data, time series data and sequence input data <br> Can be built from scratch or retrained enabling to build on the previous existing networks <br> Has many pre-trained architectures like AlexNet, SqueezNet, GoogLeNet, ZFNet, RESNet and VGGNet <br> Sparse interaction with local connectivity <br> Reducing the number of parameters | High <br> computational complexity in model training | Image, pattern, and speech recognition Image and sentence classification Prediction problems Regression problems | (Singh et al., 2018) <br> (Wang et al., 2018) <br> (MathWorks-1) <br> (Tch, 2017) |


| Network | Advantages | Limitations | Applications | References |
| :---: | :---: | :---: | :---: | :---: |
| Deconvolutional Neural Network (DNN) | Producing a vector related to an image and using that vector to draw that image. It is reversed convolutional neural network | High <br> computational complexity in model training | Image drawing | (Tch, 2017) |
| Deep <br> Convolutional <br> Inverse Graphics Neural Network <br> (DCIGNN) | Training images that have not previously been trained before Removing an object from the image and replacing it with another object or repainting it | High computational complexity in model training | Image processing | (Tch, 2017) |
| Deep Recurrent <br> Network (DRN) | Making a directed cycle so that the outputs do not only depend on the immediately previous input <br> Can be used with text data, speech data, time Series data, tabular data, and generative models <br> Allowing the information to persist in a hidden layer and capturing the previous states and temporal correlation | Cannot be used with image data <br> Difficult to <br> memorize the <br> long-term <br> interaction in training | Generate novel sentences Document summaries Speech and connected handwriting recognition Classification problems Regression prediction problems | (Wang et al., 2018) <br> (Tch, 2017) <br> (Davydova, <br> 2017) |
| Sequence to Sequence Model (S2SM) | It is a model with two recurrent networks, including an encoder to process the input and a decoder to produce the output | It is limited to sequence problems | Chatbots <br> System for answering <br> questions and machine <br> translation | (Tch, 2017) <br> (Davydova, <br> 2017) |


| Network | Advantages | Limitations | Applications | References |
| :---: | :---: | :---: | :---: | :---: |
| Long Short-Term Memory (LSTM) | Modelling temporal sequences along with their long-term dependencies more accurately than traditional recursive neural network | There is no activation function and no modification for the stored values | Speech recognition Classification problems Regression prediction problems | (Tch, 2017) <br> (Davydova, <br> 2017) |
| Gated Recurrent <br> Network (GRN) | Modelling temporal sequences along with their long-term dependencies more accurately than traditional recursive neural network <br> It is similar to the LSTM network but without an output gate | There is no activation function and no modification for the stored values | Speech recognition Classification problems Regression prediction problems | (Tch, 2017) |
| Deep Belief Network (DBN) | Inferring the states of the unobserved variables <br> Adjusting the interaction between variables to make the network generate observed data <br> Can be trained without supervision <br> Training using a very fast algorithm to initialize the network and parameters | It is limited to binary inputs <br> The parameters are fine-tuned using a slow algorithm | Image recognition <br> Face recognition <br> Video <br> sequence <br> recognition <br> Motion-capture <br> data | (Wang et al., 2018) <br> (Chandrayan, <br> 2017) |


| Network | Advantages | Limitations | Applications | References |
| :---: | :---: | :---: | :---: | :---: |
| Restricted <br> Boltzmann <br> Machine (RBM) | Can quickly discover unbiased samples from the posterior distribution <br> Can be trained without supervision <br> Automatic training for the datasets avoiding the local minimum values <br> Robust to ambiguous inputs | It is limited to binary inputs <br> There is no output layer <br> Restricted <br> connection <br> between hidden units <br> Time consuming | Filtering <br> Prediction | (Wang et al., 2018) <br> (Chandrayan, <br> 2017) |
| Recursive Network (RN) | It has the ability to make structured predictions | Used only when applying the same weights recursively | Speech recognition | (Davydova, 2017) |
| Auto Encoder <br> Network (AEN) | Can be trained without supervision <br> Eliminating the irrelevance in the input and preserving the meaningful information | Used only when output cells are equal to input cells and hidden cells are less than input cells <br> Error propagation | Classification <br> Clustering <br> Feature <br> compression | (Wang et al., 2018) <br> (Tch, 2017) |
| Variational Auto Encoder Network (VAEN) | Using probability compression instead of feature compression <br> Can be trained without supervision <br> Eliminating the irrelevance in the input and preserve the meaningful information | Used only when output cells are equal to input cells and hidden cells are less than input cells <br> Error propagation | Classification <br> Clustering <br> Probability <br> compression | (Wang et al., 2018) <br> (Tch, 2017) |


| Network | Advantages | Limitations | Applications | References |
| :---: | :---: | :---: | :---: | :---: |
| Denoising Auto Encoder Network (DAEN) | Varying the data by random bit and reconstructing output from a bit input making it more general which helps to select more common features <br> Can be trained without supervision Eliminate the irrelevance in the input and preserve the meaningful information | Used only when output cells are equal to input cells and hidden cells is less than input cells <br> Error propagation | Classification <br> Clustering <br> Feature compression | (Wang et al., 2018) (Tch, 2017) |
| Sparse Auto Encoder Network (SAEN) | Can reveal hidden grouping pattern Can be trained without supervision Eliminating the irrelevance in the input and preserve the meaningful information | Used only when the number of hidden cells is more than the input and output cells <br> Error propagation | Classification Clustering <br> Feature compression | (Wang et al., 2018) <br> (Tch, 2017) |
| Generative <br> Adversarial <br> Network (GAN) | Very large family of double networks <br> Leaning a map from input to output image | Generator and discriminator fool each other | Image generation | (Tch, 2017) |

These applications are coming from many fields, such as manufacturing. (Wang et al., 2018) mentioned that DL enables advanced analytics for smart manufacturing systems in terms of objects, equipment, process, people, and environment using aggregated big data. DL can help describe what happened in a process by capturing products' conditions and then by supporting the diagnoses of why particular issues occurred, examining the causes, and detecting specific failures. After that, DL can be used to predict what will happen, for example predicting products' quality deviations, and finally to assist in the prescription of corrective actions by identifying measures to be taken in order to improve the quality of a
product. The deep insights brought by DL can support a company's decision making process throughout a product lifecycle by improving the analyses of data emerging from the design, manufacturing, and supply chain, enhancing the process control, and reducing the downtime. DL has been applied in a wide range of manufacturing systems particularly in the area of fault diagnosis and product quality inspection.

In addition to the manufacturing context, there are other fields in which DL has great applications. It has been applied in the pharmaceutical context (Ekins, 2016), such as to predict aqueous solubility, the epoxidation site in molecules, and liver injuries induced by drugs as well as to diagnose cancer, extract pattern in gene expression, predict protein disorder, analyse the content of breast cancer, repurpose drugs, and classify microscope images. Thus, while DL appears to be a promising tool in the biological context, it is generally expected to have even greater applications in the future.

### 2.2 Convolutional Neural Network

This section presents a brief review of CNN principles in order to find the gaps and open issues that may need to be solved in the future in order to improve the performance of CNN models.

### 2.2.1 Definition and Way of Working

CNN is one of the most popular DL networks and is used mainly to perform image analysis tasks. (MathWorks-1) stated that it is useful for detecting patterns in images that help in the automatic recognition of real physical objects. These patterns are extracted by CNN directly from image datasets without the need for extracting features manually, which is the most important factor that makes CNN very popular. In addition, it produces highly accurate recognition results and has the flexibility to be retrained to perform new recognition and to be built on previously created models. It provides a better model architecture, enabling advances in detecting and recognizing objects, thus it is a key technology in automated facial recognition.

CNN might have hundreds of layers helping to detect patterns in images. Filters are used to extract information and can start from simple features, such as brightness, to more complex ones that uniquely identify an object. This filtering is applied to each training image and the output of each image after convolution can be used as an input to the following layer. CNNs are composed of an input layer, an output layer and many hidden
layers. Every neuron in the hidden layer connects to all inputs neurons as shown in figure 2.1, as mentioned in (Le, 2015):


Figure 2.1: Inputs and Hidden Layers Connection in CNN (Le, 2015)
The hidden layers perform learning feature tasks using the most common feature learning layers which are:

- Convolution: it activates some features in the images using convolutional filters which are represented by a matrix of weights that slide along the pixel brightness input matrix to create a feature map matrix using special dot product as mentioned in (Hui, 2017).
- Rectified linear unit (ReLU): it is used after each convolutional layer to increase the speed and effectiveness of training by mapping negative values to zeros and maintaining positive values which is helpful as an activation.
- Batch normalization: it is used as supplement layers after each convolutional layer to mitigate the risk of overfitting by normalizing the input values of the following layers (Yamashita et al., 2018).
- Pooling: it is used between the convolutional layers to reduce the dimensionality of the output volume (McDermott, 2021) without losing the important features which contribute to minimize the computational cost. It reduces the number of parameters needed to learn by making nonlinear down-sampling that simplifies the output. There are two types of this layer, max pooling which takes the most activated feature and average pooling takes the average presence of the feature, so max pooling is better with a dark background and average pooling is better with a white background as mentioned in (Ouf, 2017).

Furthermore, it uses two classification layers:

- Fully connected: it shows the probability of each image being classified for each class.
- SoftMax: it is an activation function that works better with multi-class classification problems rather than a binary classification problem that requires a sigmoid logistic function which is a special case of SoftMax function as shown in (McDermott, 2021), it provides the classification output and may not have any parameters as mentioned in (Wu, 2017). It turns the real values inputs into values between 0 and 1 (Wood) through the following equation (www.redcrabsoftware.com):

$$
\sigma(\mathrm{x})_{\mathrm{j}}=\mathrm{e}_{\mathrm{j}}^{\mathrm{z}} / \sum \mathrm{e}^{\mathrm{z}_{\mathrm{k}}}(\text { for } \mathrm{j}=1,2, \ldots \ldots \ldots ., \mathrm{K})
$$

(Equation 2.1)
Where:
X is the input vector to the SoftMax function
$\mathrm{z}_{\mathrm{j}}$ is the input of all elements in the vector
$\mathrm{e}^{\mathrm{Z}_{j}}$ is the exponential function applied to each element
$\sum \mathrm{e}^{\mathrm{z}}$ is the normalization term
K is the number of classes

Figure 2.2 demonstrates the way of working for CNN showing feature learning and classification layers.


Figure 2.2: The Way of Working for CNN (MathWorks-1)

### 2.2.2 Gaps and Open Issues

According to (Joshi et al., 2019), the most important challenge in training CNN is the generalization to unseen datasets so that the model does not overfit datasets and can give judgment on unknown data. Overfitting is a common issue in training CNN, where the
model fits well enough to the training data but does not have the capability to generalize to other datasets. It can be controlled by increasing the sample data using data augmentation techniques, reducing the complexity of the architecture and stopping the training earlier. In addition, (Liang \& Liu, 2015) and (Cogswell et al., 2015) discussed the same overfitting issue and suggested another way to prevent it using dropout, (Pan, 2017) highlighted that it is an efficient method to randomly remove a unit from the network with related edges independently for each hidden unit and sample. (Wu et al., 2017) used a novel regularization technique that helps in reducing kernel redundancy and thus preventing overfitting. However, improving the learning capability is still an open challenge and can be enhanced continuously. In addition, (Joshi et al., 2019) reported other issues, such as exploding gradient problem where the model stops learning after a certain number of epochs which causes instability in the learning process resulting in NAN values, this issue can be overcome by redesigning the network architecture and selecting appropriate activation function. Also, (Shah et al., 2016) suggested using residual and highway networks that learn in earlier layers allowing for earlier representation. In addition to (Joshi et al., 2019), (Fu et al., 2016), and (Masko \& Hensman, 2015) addressed the third issue which is training the data using imbalanced classes where the sample is not uniformly distributed, it is a significant and long-standing challenge in training CNN models. Improving the convergence speed is another future challenge because it sometimes increases the time of convergence in order to get better accuracy as stated in (Chiroma et al., 2019).

Furthermore, five research papers (Zhang et al., 2018), (Baldominos, et al., 2018), (Sinha et al., 2017), (Ma et al., 2018), and (Panwar et al., 2017) discussed the most challenging aspect in training CNN, which is designing better topology, the traditional heuristic approach of using trial and error might result in a less accurate model depending on user experience. Applying optimization techniques such as nature inspired algorithms to optimize the parameters of CNN can improve the performance of the model. However, designing a better CNN topology is still an open issue and there is no approach found yet that can give the best CNN topology. Section 2.4 will discuss the impact of developing hybrid CNN with nature inspired algorithms in improving the model performance.

### 2.3 Long Short-Term Memory Network

This section shows a review of LSTM network presenting the definition and way of working along with the gaps and open issues that need to be addressed.

### 2.3.1 Definition and Way of Working

LSTM is one of the DL networks that deal with time series or sequence problems. It is an extension of RNN that can remember long-term dependencies as it persists in the information for a long period, the normal RNN is not able to do so resulting in a vanishing gradient problem (www.analyticsvidhya.com). It is a situation when the RNN is not able to propagate useful information from the end of the network back to the beginning of the network as information is stored only for a short period (www.engati.com).

The structure of the LSTM consists of three gates, the first one is the forget gate that decides if the information coming from the previous time scale is relevant to be remembered or irrelevant to be forgotten, the second one is the input gate that tries learning new information from the cell input, and the last gate is the output gate where the cell transfers the updated information from the previous time cycle to the next time cycle. In addition, it has a cell state that carries the information along with all cycles as it stores the information for a long period and a hidden state for short-term memory, so it is present in RNN as well (www.analyticsvidhya.com). The following figure 2.3 illustrates the basic structure of the LSTM network where the first part is the forget gate, the second part is the input gate, and the last one is the output gate. In addition, $\mathrm{C}_{\mathrm{t}-1}$ is the cell state for the previous time cycle, $\mathrm{C}_{\mathrm{t}}$ is the cell state for the current time cycle, $\mathrm{H}_{\mathrm{t}-1}$ is the hidden state for the previous time cycle, and $H_{t}$ is the hidden state for the current time cycle.


Figure 2.3: The Basic Structure for LSTM (www.analyticsvidhya.com)
The way of working for the gates starts with the forget gate that decides if the information coming from the previous time scale is relevant to be remembered or irrelevant to be forgotten. Then, the input gate is used to quantify the importance of the input of new information. In the output, the cell transfers the updated information from the previous time cycle to the next time cycle. The output with the maximum score is the predicted value.

### 2.3.2 Gaps and Open Issues

One of the most important challenges in training LSTM is reducing overfitting (www.machinelearningmastery.com), it is the case when the model fits well enough for training data and performs poorly in validation and testing data so that it is not able to generalize to unseen data (Joshi et al., 2019). This issue can be overcome by adding a dropout layer (Liang \& Liu, 2015) and (Cogswell et al., 2015), trying more optimum regularization value ( Wu et al., 2017), reducing the number of epochs or augmenting the datasets (www.machinelearningmastery.com).

Exploding and vanishing gradient is a problem in RNN when the model stops learning after a certain number of epochs, LSTM addressed this issue (www.analyticsvidhya.com). However, the optimum weight change can be improved further by having a more optimum learning rate as the gradient is multiplied by the learning rate resulting in the optimum set of weights (Varikuti, 2021). So, having a more optimum learning rate means more optimum updates for the network weight (Brownlee, 2020).

Furthermore, improving the LSTM performance is an ongoing challenge (Mattioli et al., 2019), and there is no approach found yet that develops the best architecture. However,
adopting nature inspired algorithms in optimizing the parameters of the network may improve the performance of the model as it reduces the need for human input in assigning the parameters. The following section will present state of the art studies about using nature inspired algorithms to optimize LSTM parameters (Zhang et al., 2018).

### 2.4 Impact and Recent Applications of Optimizing Deep Learning Parameters using Nature Inspired Algorithms

This section presents the state of the art studies about integrating nature inspired algorithms with DL algorithms along with the gaps and open issues that need to be addressed.

### 2.4.1 State of the Art Studies

(Chiroma et al., 2019) discussed the synergy between nature inspired algorithms with DL. They mentioned that the inspiration for such algorithms can be from animals' behaviour, human activities and biological systems. The paper presented nature inspired algorithms such as harmony search, firefly, cuckoo search, evolutionary, ant colony optimization, practical swarm optimization, genetic, simulated annealing and gravitational search algorithm. The authors stated that combining DL with nature inspired algorithms has the advantage of solving local minimum problems and improving the performance of the network by increasing the accuracy of its models. In addition, the need for trial and error techniques in determining the parameters of DL architecture is eliminated as nature inspired algorithms can realize the best parameters values automatically. Though, the optimum parameters setting is still an open problem in the research area. The authors suggested to eliminate the need for human interventions in determining the parameters by obtaining parameter-less nature inspired algorithms in the future. Finally, the paper suggested applying meta-optimization which is excessive in the DL area, and it helps to tune optimization methods by using another optimization method.

Furthermore, other research papers discussed the hybrid CNN with nature inspired sward-based optimization techniques such as CNN with Evolutionary Algorithm (EACNN) and CNN with Genetic Algorithm (GA-CNN) in addition to other techniques like CNN with Long Short-Term Memory (CNN-LSTM), Artificial Bee Colony with CNN-

LSTM (ABC-CNN-LSTM) and CNN with Fuzzy Logic (FL-CNN). Table 2.2 summarizes the accuracy of the original CNN and improved accuracy after hybridization.

Table 2.2: Hybrid CNN Accuracy

| Hybrid Algorithm | Accuracy |  | Dataset | Reference |
| :---: | :---: | :---: | :---: | :---: |
|  | Original CNN | Hybrid CNN |  |  |
| (EA-CNN) | - | 98.88\% | MNIST database for handwritten digits recognition | (Badan, 2019) |
|  | - | 62.37\% | CIFAR10 dataset for animals' image classification |  |
| (GA-CNN) | 71.69\% | 75.95\% | Stock market fluctuation prediction | (Chung \& Shin, 2019) |
| (CNN-LSTM) | 82.1\% | 97\% | Motion data and site video to recognize workers' unsafe actions | (Ding et al., 2018) |
| ABC-CNN-LSTM | 95\% | 97\% | Products review dataset to detect fake reviews | (Jacob et al., 2022) |
| (FL-CNN) | 97.35\% | 99.10\% | Handwritten digits recognition | (Popko \& Weinstein, 2016) |

Applying the evolutionary algorithm yielded a highly accurate CNN with $98.88 \%$ accuracy for handwritten digit recognition and a lower percentage of $62.37 \%$ for animal image classification. The author used the weight inheritance technique which considers the training process as a kind of mutation that reduces the evolution cycle time. (Bernard \& Leprevost, 2018) explained the process of evolution by reproducing the population through generation by crossing members and inducing random mutation, evolving input image would maximize feature activation.

GA is one of the evolutionary algorithms that has been applied to optimize the parameters of the CNN model to predict the stock market, (Mallawaarachchi, 2017) described the natural selection of selecting the fittest individual in the population which improved the accuracy from $71.69 \%$ to $75.95 \%$. The algorithm produces offspring that
inherit the parents' characteristics, so that they have a chance to survive if their parents have better fitness. So, the algorithm consists of five phases: initial population, fitness function, selection, crossover and mutation.

In addition to nature inspired algorithms, CNN can be integrated with another DL algorithm which is the LSTM to automatically recognize worker unsafe actions in motion data, the use of LSTM would enable the sequence of learning features. Dealing with sequential data is an important advantage of using this algorithm as stated in (Motepe et al., 2019), it is an effective technique when capturing dependencies in the long term avoiding RNN challenges such as vanishing gradient problem using nonlinear gating that regulates the flow of information. The hybrid CNN-LSTM analyses motion data in a video to recognize unsafe actions done by the workers. Applying only CNN achieved an accuracy of $82 \%$, but adding LSTM improved the model accuracy to $97 \%$ as it stores the information for a long period which allows considering the long-term dependencies (Ding et al., 2018). The hybrid CNN-LSTM was integrated as well with ABC that optimized the type of the network, the number of epochs, LSTM hidden units, global learning rate, activation function, step size, fully connected layer, and pooling size (Jacob et al., 2022). The authors used the hybrid ABC-CNN-LSTM algorithm to detect the fake reviews of the product with an accuracy of $97 \%$ compared to $95 \%$ for the CNN-LSTM algorithm (Jacob et al., 2022).

Furthermore, the hybridization of CNN with FL would add one more layer, a fuzzy selforganization layer. (Korshunova, 2018) explained its function that distributes input data into clusters not equivalent to the number of output classes where the output of this layer is the membership function values for the fuzzy clusters. This new hybrid model improved the handwritten digit recognition accuracy from $97.35 \%$ to $99.10 \%$.

However, there are still opportunities to test the integration of ANN with other popular swarm-based algorithms, such as ABC. Such integration was done in other applications, for example, to optimize the hyperparameters of ANN as presented in (Rashid, \& Abdullah, 2018). They integrated ABC , genetic algorithm, and back propagation neural network that is used to classify and diagnose diabetes. Adding a genetic operator helps to avoid sucking in local optima, an issue mentioned in (Packianather et al., 2014).

In addition, (Bullinaria \& AlYahya, 2014) made a comparison between training ANN with the back propagation and ABC , they found that back propagation is significantly better than ABC. (Xu et al., 2019) applied a modified ABC that has better performance in utilizing the neighbour information in order to accelerate the convergence, this new algorithm was used to train ANN. (Qolomany et al., 2017) optimized two variables of the DL model which are the number of hidden layers and the number of neurons in each layer using Particle Swarm Optimization (PSO). Furthermore, (Badem et al., 2017) applied BA along with limited memory Broyden-Fletcher-Goldfarb-Shannon to train autoencoder network while (Lee et al., 2018) optimized the hyperparameters of CNN using free harmony search technique.

In addition, (Zeybek et al., 2021) presented a novel metaheuristic algorithm that trains deep RNN using an enhanced Ternary Bees Algorithm (BA-3+) for the sentiment classification task. BA-3+ algorithm finds the optimal set of parameters for deep RNN architecture by collaborative search of three bees, the authors found that it outperformed other optimization algorithms such as Stochastic Gradient Descent (SGD), Differential Evolution (DE) and PSO. Training deep RNN using the BA-3+ algorithm achieved an accuracy rate between $80 \%-90 \%$; while training it using SGD produced an accuracy between $50 \%-60 \%$ for most datasets.

Furthermore, the GA is one of the nature inspired algorithms used to find the optimal parameters in the LSTM network for predictive maintenance (Kim \& Choi, 2021), the authors optimized the time steps, the number of LSTM layers, and the number of hidden neurons in each layer using GA. They suggested a procedure that starts with population initialization followed by fitness computation for chromosomes, then genetic operators application for new population creation if needed. The design of GA is based on chromosome structure, fitness function, crossover operator, mutation operator, and population updating and termination (Kim \& Choi, 2021). The proposed model achieved an accuracy of $98.14 \%$. Another study used GA to optimize five parameters related to LSTM hidden layer size, number of hidden layers, batch size, number of times steps and number of epochs. The hybrid GA-LSTM is used to predict the next word in the sentence which achieved an accuracy of 56\% (Gorgolis et al., 2019).

Furthermore, PSO which is a swarm-based metaheuristic optimization algorithm is applied to improve the performance of the LSTM network by optimizing hidden layers, number of neurons, activation function, loss function, optimizer, batch size, and number of epochs. The hybrid PSO-LSTM is applied to predict the pollution level based on the weather dataset; it achieved a lower RMSE than the original LSTM by a value of 0.0007 (Pranolo et al., 2022).

A study used ABC to optimize the weights of ANN (Qureshi et al., 2019). The author used the hybrid algorithm to propose a new intrusion detection system achieving an accuracy of $95.02 \%$ (Qureshi et al., 2019). Another study used BA to train RNN for sentiment classification which improved the accuracy from $60 \%$ for traditional RNN to $90 \%$ for the BA-RNN algorithm (Zeybek et al., 2021). Also, ABC was used to optimize LSTM parameters (window size, LSTM units, dropout probability, number of epochs, batch size and global learning rate) (Kumar et al., 2022). They used the hybrid ABC-LSTM algorithm for stock market prediction which achieved a lower RMSE by 5.6836 (Kumar et al., 2022).

### 2.4.2 Gap and Open Issue

Looking at the literature, there is a lack of hybridization between BA and CNN which is an important gap as BA is one of the most popular swarm-based optimization techniques that use a global search, followed by a local search and an intense search in order to find the optimal parameters that yield the minimum error.

In addition, there is a lack of optimizing the learning rate adjustment factor for convolutional layers in CNN and each gate in the LSTM network which is an important gap as the learning rate control the weight update. Having a more optimum learning rate means more optimum updates for the network weight (Brownlee, 2020). The CNN gap will be addressed in the following chapter by proposing two novel hybrid algorithms that take the advantage of global, local and intense searches in the BA in order to optimize the parameters and train CNN.

### 2.5 Machine Learning in Manufacturing

(Li et al., 2017) stated that AI is an essential concept used to facilitate the development of intelligent systems to increase the productivity and maximize the efficiency of various processes such as in the manufacturing context. The life cycle of new intelligent
manufacturing systems uses autonomous sensing, learning, interconnection and decision making to integrate and optimize different aspects of manufacturing enterprise leading to increase the productivity, maximize the efficiency, improve the quality, and reduce the cost. (Wuest et al., 2016) stated that the applications of machine learning in manufacturing include machine condition monitoring, fault diagnosis leading to applying predictive maintenance, image recognition that helps to classify damaged products and building a simulator for the advanced manufacturing process to predict its parameters.

In addition, (De Filippis et al., 2017) showed that manufacturing applications include modelling and scheduling the processes which solve issues related to operational decision making. The procedure for using ANN starts by collecting experimental observations and pre-processing them to be ready for network training. Then, establishing a numerical relationship between the parameters and mechanical features of the part. Finally, the time and cost parameters of the process will be evaluated to identify the benefits and costs incurred from the prediction model. Multilayer perceptron can be used for process modelling and product quality prediction for manufacturing processes such as injection moulding and arc welding processes (De Filippis et al., 2017).
(Saric et al., 2013) simulated and predicted steel surface roughness using three different neural network algorithms which are back-propagation, modular and radial basis function neural networks. The input variables were the parameters that control the process (feed rate, depth of cut, cutting speed, and the number of revolutions) while the output variable is machined surface roughness. The results show that Root Mean Square Error (RMSE) in the radial basis function is $5.24 \%$ in the learning phase and $8.53 \%$ in the validation phase, the modular neural network produced an error of $6.02 \%$ in the learning phase and $8.87 \%$ in the validation phase. Finally, the results of the back-propagation neural network in terms of RMSE is $6.46 \%$ in the learning phase and $7.75 \%$ in the validation phase. Furthermore, (Moyne \& Iskandar, 2017) applied big data analytics in the semiconductor manufacturing industry which helps to improve the current capabilities such as detecting faults and supporting the recent capabilities like predictive maintenance. The most important factor was the quality of the dataset in order to deliver high quality solutions. In the future, they expected that digital twin will be used to improve the ability of the analytics.

### 2.6 Additive Manufacturing Overview

Additive manufacturing (AM) is defined in ISO/ASTM 52900:2021 standard (ISO/ASTM 52900:2021) as a process that builds parts by joining a material layer by layer, using 3D model data. The standard defined seven process categories for AM namely binder jetting, directed energy deposition, material extrusion, material jetting, powder bed fusion, sheet lamination, and vat photopolymerization. AM is also referred to using other terms such as 3D printing, rapid prototyping, digital manufacturing, and layered manufacturing. AM started in the 1980s when Dr. Hideo Kodama used 3D scanning knowledge and 3D topographical maps layering patterns to create a prototyping machine (www.TriMech.com). Then, in 1987 stereolithography process was invented by Chuck Hull, the long processing time of production led to this patent that creates 3D objects using Ultraviolet laser (Office of Energy Efficiency and Renewable Energy, 2017). Fused Deposition Modelling (FDM) was invented in 1991 by Scott Crump. In 1995 German scientists invented Selective Laser Melting (SLM) (Ratna, 2022), and in the 2000s more companies were interested in 3D printing benefits and capabilities (Markforged).

There are two levels for AM processes, the first one is the digital level where the CAD model is prepared, converted to a stl.file, and G-code is generated. The second level is the physical level which contains part manufacturing using one of the seven processes mentioned previously (Lastra et al.,2022). Initially, AM or 3D printing technologies were used mainly for rapid prototyping, but with improvements in the reliability and efficiency of AM processes as well as in the material properties of the components produced, they are increasingly used in more advanced applications such as to create highly customized products, producing a small volume of serial components and visualizing tool in design. Future applications may concern human organ creation, clothes manufacturing, and food confection (Farinia Group, 2018).
(Abdulhameed et al., 2019) stated that there are certainly many advantages associated with the use of AM processes such as the flexibility in the producible designs, the facilitated customization of products and the capability to print highly complex structures. However, many challenges and drawbacks remain. More specifically, some major disadvantages are void formation between the sequential layer due to reduced binding, the appearance of stair
stepping effect in the fabricated part, the variation in microstructure and mechanical proprieties, the small build volume that leads to scaling down large parts or cutting them to subparts consuming effort and long time, complying with safety standards for fabricated food and medical devices, and finally fabricating and producing parts that can be used for criminal purposes such as drugs and weapons as it can deal with complex structures as mentioned previously.

The typical applications for AM processes are prototyping during the development phase of a product, producing parts in pilot series production or short series where costs related to casting or injection moulding are high and producing parts with complex geometry which cannot be done by other manufacturing means (www.Metal AM.com). This is the main advantage of using AM when compared to other manufacturing processes, for example, it allows the integration of additional functionality in components such as the production of repeating internal patterns. Thus, AM is capable of combining complex internal structures with more regular outer geometries, reducing weight while keeping structural and aesthetic integrity. (Bauer, 2021) mentioned that there are many applications of the SLM process in real life, such as in the medical field with dental implants (highly complex, small in dimension, and one-off patient products) or with specialized surgery equipment. Another large field is in the aerospace industry where hard to machine materials, such as nickel-based super alloy, require high quality, complex shapes, and low to medium production lots like a hydraulic manifold. Also, it can be used in the manufacturing of a bike frame. Furthermore, applications are emerging in the context of the highly regulated aerospace and automotive sector. For instance, metal parts suitable for aircraft were directly manufactured using titanium material, reducing the lead time by $30 \%$ - $70 \%$, non-recurring fabrication costs by $45 \%$ and abatement in manufacturing cost for parts with low volume by $30 \%-35 \%$ (Abdulhameed et al., 2019).

### 2.7 Additive Manufacturing Processes

As shown in table 2.3, seven AM processes can be used for the production of complex parts:

Table 2.3: Additive Manufacturing Processes (Farinia Group, 2018)

| Process | Techniques | Materials |
| :---: | :---: | :---: |
| Powder bed fusion | Direct Metal Laser Sintering (DMLS), <br> Selective Laser Sintering (SLS), Selective <br> Laser Melting (SLM), and Electron Beam <br> Melting (EBM) | Polymers, metals: miraging steel, <br> stainless steel 316L, 15-5PH, nickel- <br> based superalloys: Inconel 718, Inconel <br> 625, Hastelloy X, titanium TA6V, <br> chrome-cobalt, and aluminium AISi10mg |
| Material extrusion | Fused Deposition Modelling (FDM) | Thermoplastic filament |

(Lastra et al.,2022) presented AM technologies classification based on material according to ISO/ASTM 52900 as shown in figure 2.4 below:


Figure 2.4: AM Technologies Classification According to ISO/ASTM 52900 (Lastra et al.,2022)

### 2.8 Powder Bed Fusion

Powder bed fusion (PBF) is one of the most promising AM processes due to its ability to process a wide range of hard metals. This section presents a review of the PBF process, showing the way of working, thermodynamical phenomena, parameters, open issues, three porosity types, and state of the art studies about adopting DL techniques to improve the performance of SLM process.

### 2.8.1 Definition and Way of Working

(Sun et al., 2017) stated that PBF processes are laser-based additive manufacturing in which the laser beam scans selected locations of a powder bed at a controlled speed and then fuses the powder to obtain solid material layer by layer by either partial melting, such as in SLS or full melting, such as in the metal-based SLM process as mentioned in (Shrestha, et al., 2019). Figure 2.5 presented in (Sun et al., 2017) illustrates the laser-based PBF process.


Figure 2.5: Elements of Powder Bed Fusion Process (Sun et al., 2017)
(Bauer, 2021) stated that the first crucial part of the SLM process is the build job preparation for any given 3D model. It consists of four main steps: geometry importation, alignment/orientation within a build envelope (critical as surfaces with an angle less than $45^{\circ}$ need to be supported), support creation to allow stable processing conditions and finally slicing based on machine specific requirements. After preparing and loading a build job onto a machine, the manufacturing process can be initiated starting with the alignment of the recoating device or levelling of the substrate to enable the deposition of powder. Then, the laser scans a specific area based on a predefined scanning strategy and controllable parameters to selectively solidify the material. After finishing a layer scanning, the build plate is lowered, and new powder is deposited on top of the build area to produce a new layer. The following figure 2.6 illustrates the influential factors of a typical SLM process:


Figure 2.6: Ishikawa Diagram of Influential Factors in the SLM Process (Bauer, 2021)

### 2.8.2 Thermodynamical Phenomena

The PBF process involves complicated thermodynamical phenomena and physiochemical behaviour as powder particles are melted using a laser beam with high energy. Thermodynamic monitoring is important to control the performance of the process, but it is difficult as the molten pool has a small size and moves quickly. Recently, numerical modelling has been developed to study the physical mechanism deeply. Metal SLM process involves principles for multiscale coordinate control, they include deformation and stress (macroscale), melting behaviour and laser absorption (mesoscale), and the development of microstructure (microscale) (Gu et al., 2017).

The limited energy on the powder bed and low operating temperature resulting from low laser power value in SLM lead to generating residual pores between the neighbouring small molten pools. The low temperature decreased the liquid surface tension leading to the melt flow (Gu et al., 2017). These conditions cause a remarkable reduction of the melt pool convection, and also simultaneously they lead to a weakening of the melt migration between the current and solidified neighbouring tracks. As a result, the porosity is shown obviously on the top surface and cross-section of the SLM part. Conversely, increasing the laser power results in a larger molten pool size with a longer lifetime of the liquid. The considerable laser energy input leads to an intensified convection within the melt pool with sufficient melt migrations between the high laser power tracks which produce high-quality SLM parts without distinct defects on both the cross-section and top surface. In addition,
cellular morphology is presented with the microstructure surrounding the tracks with no obvious defects. The following two figures 2.7 and 2.8 for the top surface morphology of the produced Inconel 718 part with two different laser power 90 W and 120 W are presented in (Gu et al., 2017):


Figure 2.7: Top Surface Morphology with Laser Power of 90 W (Gu et al., 2017)


Figure 2.8: High Magnitude Microstructure Morphology of Top Surface with Laser Power of 120 W (Gu et al., 2017)

So, with a low laser power value of 90 W , irregularly shaped porosity was shown distinctively in the tracks where heat transfer and limited mass occurred. Increasing the laser power value to 120 W leads to decreasing porosity. So, producing high-quality Inconel 718 parts are achievable with optimal laser power that can be specified using mesoscale simulation and analysis (Gu et al., 2017).

### 2.8.3 Parameters

(Sun et al., 2017) mentioned that the parameters for PBF processes can be divided into four categories, the first one is the laser-based set of parameters that includes laser power, wavelength, spot size, pulse duration, and pulse frequency. The second category includes parameters related to the scanning strategy (scanning speed, scanning spacing, scanning patterns, and layer thickness). The third category is the set of powder-related parameters which include particle size and distribution, particle shape, powder bed density, layer thickness and material proprieties. The last category is the set of temperature-related parameters, including powder bed temperature, powder feeder temperature and temperature uniformity.

### 2.8.4 Open Issues

(Shrestha et al., 2019) mentioned that metal-based AM has many issues such as porosity, part deformation and cracks, but as mentioned previously porosity is one of the most challenging issue due to its effect on the mechanical properties, structural integrity, strength and Young's modulus of the produced material. In addition, producing a large amount of experimental data is not cost-effective for SLM parts (www.facfox.com, 2022) since there are many types of production costs for pre-processing, processing and postprocessing cost including preparing geometry data, CAD model, machine setup, material cost, building up the part, and postprocessing cost (Rickenbacher, 2013).

Furthermore, when using CT scans of sample parts, there is a problem related to assessing accurately the porosity in SLM parts. One main drawback is when using gray value analysis to assess the porosity of SLM parts visible in CT scan slices. The difficulty is the subjectivity in selecting an appropriate grayscale threshold that would convert a single slice into binary images highlighting defective regions, as well as determining the true level of porosity. When an inappropriately low grayscale threshold is applied to the
original slice image for binary image conversion, a certain amount of tiny undesired white spots are not filtered. However, if a higher grayscale threshold is adopted, the morphological features of the defective area, specifically near the boundary, are altered dramatically. These thresholds would result in significantly different predictions of porosity levels (Gong et al., 2019). Hence an intelligent method is needed for assessing and predicting the porosity level in SLM parts.

There are three main types of pores, namely gas, keyholes and lack of fusion porosity (Snell et al., 2020). The following subsections will explain each type showing its characteristics and mechanism of formation.

### 2.8.5 Gas Porosity

Gas pores belong to the most common type of pore. They are the most spherical and the smallest type. It is characterized by smooth edges and a wide range of sizes from submicron to several microns (Tan et al., 2020). The following figure 2.9 shows an illustrative example of the gas porosity using the scanning electron microscope (SEM):


Figure 2.9: Illustrative Example of Gas Porosity using SEM (Tan et al., 2020)

Gas pores are connected to trapped gas that might have different sources of origin whether during or before the process starts such as the entrapped gas in the powder of the alloy during the process of gas atomization. However, increasing the laser power or decreasing the scanning speed might enlarge this type of pore. (Tan et al., 2020) fabricated SLMed 2024 Al alloy samples at a specific scanning speed of $1200 \mathrm{~mm} / \mathrm{s}$ and with laser power values between 225 W to 375 W to investigate the gas porosity evolution. They found that increasing the laser power from 225 W to 300 W leads to raising the fraction of gas pore from $1.3 \%$ to $1.6 \%$, but increasing the laser power further from 300 W to 375 W reduced the fraction to $0.7 \%$ as the thermal gradient between the centre and boundary of melt pool is increased which leads to facilitating the process of outgassing. So, it was concluded that it is difficult to fully understand the effect of SLM process parameters on gas porosity formation since it is a dynamic process that involves pore nucleation, growth, and outgassing during rapid solidification (Tan et al., 2020).

### 2.8.6 Keyhole Porosity

Keyhole pores arise from energy input excess with high energy density (Tan et al., 2020), which is a result of increasing the laser power or decreasing scanning speed. It is characterized by large-size cavities reaching hundreds of microns and tended to be nearspherical in shape, so sometimes it is difficult to distinguish between large gas pores and keyhole pores. The following two figures 2.10 and 2.11 show the 3D view of the keyhole pore at a laser power value of 195 W and scanning speed value of $400 \mathrm{~mm} / \mathrm{s}$ and different shapes of 2D images:


Figure 2.10: 3D View of Keyhole Pores (Shrestha et al., 2019)


Figure 2.11: 2D Images of Different Keyhole Pores Morphologies (Shrestha et al., 2019)
Unlike gas pores, the surface and contour are bumpy, these cavities are the most common type of keyhole porosity that appear in the SLM part (Tan et al., 2020). It is caused when trapping bubbles of vapour within the melt pool (Shrestha et al., 2019), changing the melting mode from conduction to keyhole mode at high laser energy intensity leads to the formation of this type of pore. In the conduction mode, the laser energy input is low to moderate which mediates the heat transfer through conduction. The material melting happens in this mode without vaporization which results in less porosity, but in keyhole mode, the high laser intensity causes metal evaporation which generates recoil pressure at the bottom of the melt pool. The instability of the dynamic behaviour in the melt pool leads to the formation of keyhole porosity with near-spherical morphology at the bottom of the melt pool, which acts as a stress concentrator causing material property deterioration (Tan et al., 2020).

### 2.8.7 Lack of Fusion Porosity

Lack of fusion pores have irregular voids morphology that commonly appeared in SLM alloy, they are featured with large sizes reaching hundreds of micrometres as shown in the following figure 2.12 (Tan et al., 2020):


Figure 2.12: Lack of Fusion Pores Morphology (Tan et al., 2020)
Irregular voids are formed because of un-melting in some regions caused by the reduction in energy density, which is generally a result of the low value of laser power or fast scanning speed (Tan et al., 2020). The energy density is a function consisting of laser power, scanning speed, layer thickness, and hatch distance, these parameters have a significant effect on pores formation (Shrestha et al., 2019). Having insufficient laser energy to induce the overlapping between the adjacent layers leads to the formation of this type of pore. Also, the high reflectivity and dense oxide presence on the powder particles' surface might form such defects as the laser penetrability is lowered (Tan et al., 2020).

Thus, when optimizing the SLM process it is essential to accurately study the pore formation occurring when using various combinations of parameters.

### 2.8.8 State of the Art Studies

AM products need advanced quality control processes to achieve the desired reliability, so it is valuable to review quality-related research in AM context by focusing on issues and considerations that need development and optimization, in addition to future directions toward improving the quality of AM products. This section shows the new trend of using cameras and sensors to acquire real-time data for quality monitoring purposes in addition
to showing advanced data analytics and predictive algorithms to optimize the process parameters.
(Kim et al., 2018) mentioned that most of the powder bed fusion processes melt powderbased material using a high source of thermal energy, it might be partial melting as in SLS, full melting as in SLM or using EBM. Detecting porosities has a significant contribution toward improving the quality of products.
(Kim et al., 2018) showed a study that developed a method for continuous data capturing using an infrared (IR) camera to detect porosities inside materials. In addition, they showed another study that developed an automatic feedback control system that stops the printing process at a certain porosity level, they used an IR camera as well to capture images and applied image processing techniques to optimize the process parameters.
(Zhang et al., 2019) monitored the porosity during the process of laser AM, they used a deep learning-based method namely CNN to predict the porosity based on melt pool cross-section images acquired by the coaxial camera. The model achieved an accuracy of $91.2 \%$ in detecting porosity occurrence. Similarly, (Coeck et al., 2019) predicted a lack of fusion porosity based on melt pool data collected during the SLM process, they used a DMP monitoring system to monitor the melt pool during the processing with titanium alloy material, and then they created an algorithm that correlates the porosity with melt pool monitoring data which achieved prediction sensitivity of $90 \%$ for lack of fusion events with pores volume grated that $160 \mu \mathrm{~m}$.

Recently, the Deep Belief Network (DBN) has been used to analyse plasma acoustic signals generated at the surface of the powder bed specifically in the SLM process. The signals are collected using a microphone, and then DBN is used to recognize the conditions of the melt track (slight balling, balling, normal, slight overheating, and overheating) (Wang et al., 2020). In addition, they used acoustic signals in porosity classification, particularly in achieving the balance between classification accuracy and spatial resolution in porosity detection. High sensitivity fibre Bragg grating sensor was adopted to collect acoustic signals for airborne, the time span for each running window was 160 ms and 300 patterns represented each of the three porosity levels without overlapping between the
training and testing set in terms of the running window. The parts with different porosity levels were classified using spectral CNN with a classification accuracy between 83-89\%.

### 2.9 Smart Manufacturing Technologies

There are six smart manufacturing technologies (Autodesk) that can be used to improve the product performance and maximize the operational efficiency as shown in the following table 2.4:

Table 2.4: Smart Manufacturing Technologies (Autodesk)

| Technology | Techniques | Benefits |
| :---: | :---: | :---: |
| Manufacturing-Led <br> Design | Computer-Aided Design \& Computer-Aided <br> Manufacturing (CAD/CAM) | Design and manufacture <br> prototypes |
| 3D Printing (AM) | Powder Bed Fusion, Material Extrusion, Material <br> Jetting, Binder Jetting, Sheet Lamination, Vat <br> Photopolymerization, and Directed Energy <br> Deposition | Create highly complex <br> geometry products |
| CNC Machining and <br> Probing | Roughing, 2 Axis Vs 3 Axis Milling and Turing | Control the movement cutting <br> tools through generated codes <br> from computer software |
| Manufacturing | Netfabb (Additive) and Power Mill (Subtractive) | Create high quality products <br> with less material waste |
| Simulation | Finite Element Analysis, Computational Fluid <br> Dynamics, Plastic Injection Molding, and <br> Generative Design | Predict the product performance <br> and optimize the product design |
| Robot Automation | Autonomous 3D Printing Robots | Automate large-scale additive <br> and subtractive processes |

### 2.10 Summary

This chapter presented a review of DL in general and of CNN and LSTM in particular in order to find gaps and open issues that need to be fulfilled in the future to improve the performance of DL models. It was found that the most challenging aspect in training DL is designing a better topology where the traditional heuristic approach of using trial and error will result in a less accurate model depending on user experience. In this case, applying optimization techniques such as nature inspired algorithms to optimize the parameters of DL algorithms can improve the performance of the model. However, designing a better DL topology is still an open issue and no approach has been found yet that can give the best DL topology.

In addition, this chapter presented the AM processes, applications, advantages, and gaps and open issues that need to be addressed. It focused on the powder bed fusion process showing the way of working, thermodynamical phenomena, parameters, open issues, three porosity types, and state of the art studies about adopting DL techniques to improve the performance of SLM process. The review found an important gap in using CT scans of sample parts, there is a problem related to assessing accurately the porosity in SLM parts. One main drawback is when using gray value analysis to assess the porosity of SLM parts visible in CT scan slices. The difficulty is the subjectivity in selecting an appropriate grayscale threshold that would convert a single slice into a binary image highlighting defective regions, as well as determining the true level of porosity. When an inappropriately low grayscale threshold is applied to the original slice image for binary image conversion, a certain amount of tiny undesired white spots are not filtered. However, if a higher grayscale threshold is adopted, the morphological features of the defective area, specifically near the boundary, are altered dramatically. These thresholds would result in significantly different predictions of porosity levels. Hence an intelligent method is needed for assessing and predicting the porosity level in SLM parts.

Chapter 3: Convolutional Neural Network

# Parameters Optimization using Nature Inspired 

 Algorithms
### 3.1 Proposed Novel Hybrid BA-CNN \& BA-BO-CNN Algorithms

Designing a better CNN topology is an ongoing issue. This chapter addresses this issue by proposing a novel approach for optimizing the parameters of CNN through the BA and BO.

### 3.1.1 Design of Experiments

First, the design of experiments (DOE) technique is conducted to investigate the significant factors affecting CNN validation accuracy (VA). Four factors and three levels are used in designing Taguchi orthogonal array (L9). The four variables which are selected based on the topology of the CNN and its learning capability as mentioned in (MathWorks3). It stated the benefit of CNN parameters that will be optimized using BO in the hybrid BO-CNN and BA-BO-CNN algorithms and using BA in the hybrid BA-CNN algorithm which are shown in the following table 3.1:

Table 3.1: CNN Optimization Variables Information

| Variable | Benefit | Range | Type |
| :---: | :---: | :---: | :---: |
| Section Depth | Control the depth of the network | $1-3$ | Integer |
| Initial Learning Rate | Allow for learning the features | $1 \mathrm{e}-2-1$ | Logarithm |
| Momentum | Update the hyperparameters | $0.8-0.98$ | Logarithm |
| Regularization | Prevent overfitting | $1 \mathrm{e}-10-1 \mathrm{e}-2$ | Logarithm |

The four factors with three levels are used in designing Taguchi orthogonal array (L9) (Fraley et al., 2020) as shown in table 3.2:

Table 3.2: Factors and Levels Definition

| Factors | Level 1 | Level 2 | Level 3 |
| :---: | :---: | :---: | :---: |
| Section Depth | 1 | 2 | 3 |
| Initial Learning Rate | 0.01 | 0.055 | 0.1 |
| Momentum | 0.88 | 0.9 | 0.92 |
| Regularization | $1 \mathrm{e}-10$ | $2.5 \mathrm{e}-4$ | 0.0005 |

The nine experiments are applying the original CNN without hybridization to nine different combinations of parameters on the 'Cifar10DataDir' benchmark image data (Machine Learning Repository) that consists of 10 classes airplane, automobile, bird, cat, deer, dog, frog, horse, ship, and truck. Each class has 6,000 images so, the total sample size is 60,0000 images, the results of VA are shown in the following table 3.3:

Table 3.3: Taguchi Orthogonal Array for CNN Parameters (L9) (Fraley et al., 2020)

| Experiment <br> $\#$ | Section <br> Depth | Initial <br> Learning Rate | Momentum | Regularization | VA <br> $(\%)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{1}$ | 1 | 0.01 | 0.88 | $1 \mathrm{e}-10$ | 67.96 |
| $\mathbf{2}$ | 1 | 0.055 | 0.9 | $2.5 \mathrm{e}-4$ | 72.20 |
| $\mathbf{3}$ | 1 | 0.1 | 0.92 | 0.0005 | 70.90 |
| $\mathbf{4}$ | 2 | 0.01 | 0.9 | 0.0005 | 76.40 |
| $\mathbf{5}$ | 2 | 0.055 | 0.92 | $1 \mathrm{e}-10$ | 78.44 |
| $\mathbf{6}$ | 2 | 0.1 | 0.88 | $2.5 \mathrm{e}-4$ | 77.40 |
| $\mathbf{7}$ | 3 | 0.01 | 0.92 | $2.5 \mathrm{e}-4$ | 77.74 |
| $\mathbf{8}$ | 3 | 0.055 | 0.88 | 0.0005 | 79.56 |
| $\mathbf{9}$ | 3 | 0.1 | 0.9 | $1 \mathrm{e}-10$ | 80.34 |

After Running the experiments and recording VA for each run, analysis of variance (ANOVA) is applied using Minitab software in order to investigate the most influential factors affecting VA, the ANOVA results are shown in table 3.4:

Table 3.4: ANOVA Results

| Source | Degree of <br> Freedom | Sum of <br> Squares | Mean <br> Square | F-value | P-Value |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Section Depth | 2 | 131.58 | 65.79 | $*$ | $*$ |
| Initial Learning Rate | 2 | 12.31 | 6.15 | $*$ | $*$ |
| Momentum | 2 | 2.69 | 1.34 | $*$ | $*$ |
| Regularization | 2 | 0.06 | 0.03 | $*$ | $*$ |
| Error | 0 | $*$ | $*$ |  |  |
| Total | 8 | 146.66 |  |  |  |

The regression equation is shown in figure 3.1:

| Coefficients |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | SE |  |  |  |
| Term | Coef | Coef | T-Value | P-Value | VIF |
| Constant | 75.66 | * | * | * |  |
| Section Depth |  |  |  |  |  |
| 1 | -5.307 | * | * | * | 1.33 |
| 2 | 1.753 | * | * | * | 1.33 |
| Initial Learning Rate |  |  |  |  |  |
| 0.010 | -1.627 | * | * | * | 1.33 |
| 0.055 | 1.073 | * | * | * | 1.33 |
| Momentum |  |  |  |  |  |
| 0.88 | -0.6867 | * | $*$ | * | 1.33 |
| 0.90 | 0.6533 | * | * | * | 1.33 |
| Regularization |  |  |  |  |  |
| 0.0000000 | -0.08000 | * | * | * | 1.33 |
| 0.0002500 | 0.1200 | * | * | $*$ | 1.33 |
| Regression Equation |  |  |  |  |  |
| $\begin{aligned} \mathrm{VA}\left(\frac{\%}{5}\right)= & 75 . \\ & -1 \\ & +0 \\ & +0 \\ & +0 \end{aligned}$ | Section l Learni ial Learn ntum_0.9 larizati | pth <br> Rat <br> ng Ra <br> - 0. <br> 0.00 | $\begin{gathered} +1.753 \\ -0.010+ \\ \text { e_0.100- } \\ 8000 \text { Regu } \\ 2500-0 . \end{gathered}$ | $\begin{aligned} & \text { Section } \\ & 1.073 \text { Inj } \\ & 0.6867 \\ & \text { larizatid } \\ & 04000 \text { Reg } \end{aligned}$ | epth_2 <br> tial I <br> mentu <br> _ 0.00 <br> ulariz |

Figure 3.1: Regression Equation
Looking at the results, it is revealed that all four factors have a significant effect on VA, so they will be optimized using the BA and BO in order to minimize the classification error on the validation set, which is the objective function. It is a complex function of section depth, initial learning rate, momentum, and regularization, it is complicated to be formulated.

### 3.1.2 Bayesian Optimization Method

BO algorithm builds the probability model of the objective function to be used to select the hyperparameters of the network and then evaluate them in the true objective function. It maintains a Gaussian process model as a surrogate model in the objective function that uses network variables as inputs to specify the network architecture, (Nag, 2021) mentioned that initial runs of the function are used as starting points "prior" and then they are enriched with "posterior" data points in each iteration, the acquisition function is used as a metric function to decide the optimal parameters, the formula of expected improvement (EI) function is as follow (Nag, 2021):

$$
\operatorname{EI}(\mathrm{x})=[\mu(\mathrm{f}(\mathrm{x}))-\max \{\mathrm{f}(\mathrm{x})\}] \times \phi(\mathrm{z})-\sigma(\mathrm{f}(\mathrm{x})) \mathrm{x} \varnothing(\mathrm{z}) \quad \text { if } \sigma(\mathrm{f}(\mathrm{x}))>0(\text { Equation 3.1) }
$$

$\mathrm{EI}(\mathrm{x})=0$

$$
\text { if } \sigma(f(x))<=0
$$

(Equation 3.2)
Where:
$Z=\mu(f(x))-\max \{f(x)\} / \sigma(f(x))$
(Equation 3.3)
$\mu(f(x))$ is the prediction from the gaussian process for new data point $x$
$\max \{f(x)\}$ is the maximum prediction from the entire list of prior at the current stage $\phi(\mathrm{z})$ is the standard normal cumulative probability density
$\sigma(\mathrm{f}(\mathrm{x}))$ is the standard deviation of the prediction for new data point x
$\emptyset(\mathrm{z})$ is the standard normal probability density
The improvement is checked by the difference between the prediction at the current stage and the maximum prediction of the entire list of prior. If the difference is high, it means that the new prediction is significantly higher than the maximum obtained so far. Multiplying the difference by the standard normal cumulative probability density gives overall or expected mean improvement which is the exploitation part. The standard deviation gives the uncertainty and it is the secret of the exploration part. Applying BO in conjunction with Stochastic Gradient Descent Momentum (SGDM) as one of the training options in CNN architecture, momentum adds inertia that helps the current update to make a proportional contribution to the previous iteration update.

### 3.1.3 The Bees Algorithm

According to (Al-Musawi, 2019), BA is one of the most important swarm-based optimization techniques that performs an intense search after a local search to optimize the variables, so combining it with the BO technique will contribute to optimize CNN parameters that minimize the classification error on the validation set. Its way of working is inspired by honeybees' foraging behaviour. The algorithm requires setting the following parameters:

- Number of scout bees: n
- Number of selected bees: $m$
- Number of elite bees: e
- Number of recruited bees for elite (e) sites: nep
- Number of recruited bees for other best (m-e) sites: nsp
- Neighbourhood size for each selected patch (local search): ngh

The algorithm starts with the global search when the scout bees (n) arrive at random positions and evaluate them based on the fitness value. Then, a local search stage starts by selecting the best sites ( m ) and abandoning the remaining sites. After that, an intense search is initiated by selecting elite sites (e), which are the best among the best sites. The next step is selecting the size of the neighbourhood search space in order to recruit more bees for the elite sites (e) and fewer bees for non-elite sites (m-e) to conduct a local search. The global and local searches will be performed simultaneously, while the recruited bees are exploring the best solutions around the neighbourhood, the global search on the remaining sites is carried out randomly. This iterative process is stopped by one of the following conditions:

- The optimal solution found
- The iteration number exceeded
- No improvement over a specific sequential number of iterations
(Koc, 2010) described the basic flowchart for BA as shown in the following figure 3.2:


Figure 3.2: The Basic Flowchart for the BA (Koc, 2010)

In addition to the basic BA, (Pham et al., 2005) showed other two types of this technique shrinking and the standard algorithm. The idea behind the shrinking approach is taking the samples from increasingly small regions in solution space during the local search while the standard algorithm includes abandoning a site when stagnating local search in addition to the shrinking procedure. (Lindfield \& Penny, 2017) introduced further modification by counting the number of times a recruited bee failed to explore an improved site, it is used as a guide in the exploration process to improve the efficiency and effectiveness of the search. Other enhancements which were introduced in (Imanguliyev, 2013) include an early neighbourhood search strategy that starts the search from promising patches, an efficiency based recruitment strategy that changes the number of recruited bees dynamically based on the efficiency of the related sites, a hybrid Tabu bee's algorithm, and autonomous bees algorithm. (Packianather et al., 2019) proposed a new version of BA discovering the rule automatically by adding two parameters namely quality weight and coverage weight to avoid ambiguous situations in the prediction stage. They formulated the new two parameters to carry out meta-pruning and make the algorithm suitable for classification tasks, it achieved better classification accuracy and reduced the number of rules making it a more efficient algorithm than other classification methods such as Jrip and other evolutionary algorithms.

In this thesis, the values of hyperparameters for BA are assigned based on the computer capability since the maximum number of iterations that can be performed for complicated CNN function is one and the number of scout bees that can be assigned is six with one elite site to be selected, the remaining parameters are selected based on the equations in (MathWorks-4) which are shown below:

- Maximum number of iterations $=1$
- Number of scout bees $(\mathrm{n})=6$
- Number of selected bees $(\mathrm{m})=0.5 \times \mathrm{n}=0.5 \times 6=3$
- Number of elite bees $(e)=1$
- Number of recruited bees for elite (e) sites (nep) $=2 \times \mathrm{m}=2 \times 3=6$
- Number of recruited bees for other best (m-e) sites (nsp) $=0.5 \times \mathrm{n}=0.5 \times 6=3$
- Neighbourhood size for each selected patch (local search) (ngh) $=0.1 \times($ Var max - Var min)
- Section depth: $0.1 \times(3-1)=0.1 \times 2=0.2$
- Initial learning rate: $0.1 \times(1-1 \mathrm{e}-2)=0.1 \times 0.99=0.099$
- Momentum: $0.1 \times(0.98-0.8)=0.1 \times 0.18=0.018$
- Regularization: $0.1 \times(1 \mathrm{e}-2-1 \mathrm{e}-10)=0.1 \times 0.01=0.001$
- Weight learning rate factor: $0.1 \times(1.1-0.9)=0.1 \times 0.2=0.02$


### 3.1.4 Convolutional Neural Network Architecture

The CNN architecture for classifying the 'Cifar10DataDir' images data into 10 classes composes of 15 layers of which one input layer, three convolutional layers, three rectified linear unit layers, three batch normalization layers, two max pooling layers, one fully connected layer, one SoftMax layer, and one classification layer.

The input layers are represented by a matrix of size height by width ( $32 \times 32$ ) that consists of pixel brightness numbers between 0 to 255 ( 0 for black and 255 for white). The convolutional layers contain filters represented by matrix of weights that slide along the pixel brightness input matrix to create a feature map matrix using a special dot product as mentioned in (Hui, 2017). Rectified linear unit layers are used after each convolutional layer to increase the speed and effectiveness of the training by mapping negative values to zero and maintaining positive values as mentioned in (MathWorks-1). In addition, batch normalization layers are used as supplement layers after each convolutional layer to mitigate the risk of overfitting by normalizing the input values of the following layers (Yamashita et al., 2018). Pooling layers are used between the convolutional layers to reduce the dimensionality of the output volume (McDermott, 2021) without losing the important features which contribute to minimize the computational cost. The classification layer performs the classification with a fully connected layer that shows the probability of each
image being classified for each class and the SoftMax layer that provides the classification output as presented in (MathWorks-1).

The normal number of convolutional layers to start is between two to three layers with a filter size of $3 \times 3$ or $5 \times 5$ as advised in (Hui, 2017). CNN is designed with three convolutional layers and two max pooling layers in between, the number of filters ranges between 11 for the first layer and 44 for the last one, and each layer has twice the number of filters of the previous layer (Brownlee, 2019). The filter size is $3 \times 3$, the section depth is 3 , and the padding that helps to detect the edges of the images is set as 'same' so that the software calculates the size of the padding at the training time automatically and produces output size equal to the input size if the stride (number of pixel shift) is one.

The pooling type is 'max' which takes the most activated feature while the average pooling layer takes the average presence of the feature, so the average pooling is better with white background and max pooling is better with dark background as mentioned in (Ouf, 2017), the default size of pooling layer is $2 \times 2$ (Hui, 2017), but it yielded high computational cost since the image input size is big ( $32 \times 32$ ), the size was changed to $3 \times 3$ with a stride value of 3 to minimize the training time.

The classification layer that performs the classification contains a fully connected layer with 10 classes parameters (airplane, automobile, bird, cat deer, dog, frog, horse, ship, and truck) and a SoftMax activation function that works better with multi-class classification problems rather than a binary classification problem that requires sigmoid logistic function as shown in (McDermott, 2021).

The CNN is trained using SGDM which is the most common training algorithm (Yamashita et al., 2018), the default values for this algorithm are an initial learning rate of 0.01 , a momentum of 0.9 , a regularization of $1 \mathrm{e}-04$, and the maximum number of epochs is 20 as presented in (MathWorks-6). After applying some experiments and monitoring the validation accuracy, the initial learning rate was changed to 0.1 , regularization became 1 e 10 and the number of epochs was 30 .

### 3.1.5 The Existing BO-CNN Algorithm

First, the existing hybrid Bayesian Convolutional Neural Network (BO-CNN) (MathWorks-3) is applied where BO is used to optimize the four CNN parameter values
for section depth, initial learning rate, momentum, and regularization in order to minimize the classification error on the validation set.

In the hybrid BA-CNN, the BA is used instead of BO to optimize the same four CNN parameter values in order to minimize the classification error on the validation set.

Finally, the hybrid BA-BO-CNN algorithm uses BO to optimize the same four parameters while BA is used to optimize the weight learning rate factor to adjust the global learning rate obtained by BO algorithm in each convolutional layer and fully connected layer. Optimal learning rate means the optimum amount of weight update (Brownlee, 2020) in the convolutional filters and fully connected layer that performs the classification, so the classification accuracy on the validation set is improved.

The following figures 3.3 and 3.4 illustrate where BO and BA are inserted in the newly developed algorithms in order to optimize CNN parameters. It is followed by two subsections explaining each algorithm in detail.


Figure 3.3: An Illustrative Diagram for BA-CNN Algorithm


Figure 3.4: An Illustrative Diagram for BA-BO-CNN Algorithm

### 3.1.6 The Proposed Novel BA-CNN Algorithm

In the proposed hybrid BA-CNN algorithm, BA is used to optimize the four parameter values for section depth, initial learning rate, momentum, and regularization that yielded the minimum classification error on the validation set, they are the same four parameters that were optimized using BO technique in BO-CNN algorithm. The steps of the MATLAB code for the proposed hybrid BA-CNN algorithm are shown in figure 3.5. Some of the steps are taken from (MathWorks-4), but the architecture of the CNN, the selection of training, validation, and testing sets, defining the objective function and optimization variable, and adopting BA steps to optimize CNN parameters are developed in this thesis.


Figure 3.5: The Steps of the MATLAB Code for BA-CNN

In the BA-CNN algorithm, BA is used to optimize section depth, initial learning rate, momentum, and regularization which are the same parameters optimized using BO in the previous BO-CNN algorithm. BA starts with six scout bees arriving at random positions and evaluating them based on the validation error value. Then, a local search starts by selecting the three best sites and abandoning the remaining sites. The next step is selecting the size of the neighbourhood search space, which is 0.2 for section depth, 0.099 for initial learning rate, 0.018 for momentum, and 0.001 for regularization in order to recruit six bees for the elite sites and three bees for non-elite sites to conduct the local search within neighbourhood size and update the four parameters. The global and local searches will be performed simultaneously, while the recruited bees are exploring the best solutions around the neighbourhood, the global search on the remaining sites is carried out randomly.

### 3.1.7 The Proposed Novel BA-BO-CNN Algorithm

The hybrid BA-BO-CNN algorithm uses BO to optimize the same four parameters (section depth, initial learning rate, momentum, and regularization) while BA is used to optimize the adjustment factor for the global learning rate in each convolutional layer and fully connected layer in order to have a more optimum learning rate which results in a more optimum amount of weight update (Brownlee, 2020) in the convolutional filters and fully connected layer that perform the classification, so the classification accuracy on validation set is improved. The steps of the MATLAB code for the proposed hybrid BA-BO-CNN algorithm are shown in figure 3.6. Some of the steps are taken from (MathWorks-4), but the architecture of the CNN, the selection of training, validation, and testing sets, defining the objective function and optimization variable, and adopting BA steps to optimize CNN parameters are developed in this thesis.

## Loading the datasets

|
Defining training, validation, and testing sets
।
Defining CNN architecture mentioned previously |
Defining the objective function for the BO algorithm which is minimizing the classification error on the validation set of CNN
|
Defining optimization variables section depth, initial learning rate, momentum, and regularization
|
Assigning BA parameters as mentioned previously

Initializing empty bee structure of position and error
|
Initializing bees array

Creating new solutions to optimize the weight learning rate factor
|
Sorting the solutions
|
Updating the best solutions found ever
।
Creating array to hold the best solutions
|
Defining BA main loop for elite sites

Selecting nonelite sites
।
Abandoning non-selected sites

In addition, the following figure 3.7 shows the workflow diagram that explains the way of working for the BA-BO scheme to optimize CNN parameters:


Figure 3.7: Workflow Diagram for the Hybrid BA-BO-CNN Algorithm

### 3.2 Results and Discussion of the Proposed BA-CNN \& BA-BO-CNN

 AlgorithmsMATLAB software is used to apply the hybrid BA-CNN and BA-BO-CNN algorithms on four benchmark datasets taken from (Machine Learning Repository). The first one is 'Cifar10DataDir' benchmark image data that consists of 60,000 images classified evenly into 10 classes airplane, automobile, bird, cat deer, dog, frog, horse, ship, and truck. The second dataset is handwritten digits with ten classes from 0 to 9 with 1,000 images in each class. The third set of data is concrete crack images with two classes, 5,000 negative images without cracks present in the road and 5,000 positive images with cracks. Finally, the algorithms are applied to 162 human Electrocardiogram (ECG) signals with three classes, 96 observations from persons with arrhythmia, 30 recordings from people with congestive heart failure, and 36 images from persons with normal sinus rhythms. For the last dataset, pre-trained CNN called 'SqueezNet' (MathWorks-7) is used to classify ECG images since the available data is not large enough to train CNN from scratch, this is one of the threats in using CNN that it needs a large sample to train it, but it is the most powerful image classification tool as stated in (Elngar et al., 2021) and (Chaganti et al., 2020). The system configuration consists of a single CPU with a memory of 256 GB . As the DL algorithms require high computations, limited BA evaluations are applied to optimize CNN parameters. The datasets are shuffled at every epoch and the training, validation and testing sets are selected randomly after each shuffle in order to minimize the data biases and improve the validity of the experiments. The 60,000 images in the 'Cifar10DataDir' are divided into 50,000 images for training and 5,000 for each of the validation and testing sets. The handwritten digits and concrete cracks images are divided into 8,000 images for training and 1,000 for validation, and the same for the testing set. Finally, the number of samples for training set in the ECG images is 81 images, while the validation set consists of 41 observations, and the testing set has 40 samples.

In addition to existing CNN and BO-CNN, the novel hybrid BA-CNN is applied to the 'Cifar10DataDir' benchmark image dataset. BA is used to find the optimal parameter values for section depth, initial learning rate, momentum, and regularization that yielded the minimum classification error on the validation set, they are the same four parameters
that were optimized using the BO technique in BO-CNN algorithm. Table 3.5 shows the optimal parameters optimized by BA along with classification error on the validation set:

Table 3.5: Optimal CNN Parameters Values for BA-CNN

| Optimized Variable using BA | Value |
| :---: | :---: |
| Optimal Section Depth | 3 |
| Optimal Initial Learning Rate | 0.0289 |
| Optimal Momentum | 0.8734 |
| Optimal Regularization | 0.0049 |
| Classification Error on the Validation Set | 0.1928 |

The minimum classification error value is 0.1928 , it is a result of a section depth value of 3 , an initial learning rate of 0.0289 , a momentum of 0.8734 , and a regularization of 0.0049. The following figure 3.8 shows the training progress in blue line and validation accuracy in black line for BA-CNN:


Figure 3.8: Training Progress for BA-CNN
The following three figures $3.9,3.10$, and 3.11 present the confusion matrix for training, validation and testing set for the BA-CNN algorithm showing precision and false alarm in the blue and red rows, and recall and miss out in the blue and red columns respectively:


Figure 3.9: Confusion Matrix for Training Data for BA-CNN


Figure 3.10: Confusion Matrix for Validation Data for BA-CNN


Figure 3.11: Confusion Matrix for Testing Data for BA-CNN
In the other hybrid BA-BO-CNN, the BO technique is applied to 'Cifar10DataDir' benchmark image data to find the optimum CNN parameters, figure 3.12 shows the minimum observed objective function and estimated minimum objective function:


Figure 3.12: Number of Functions Evaluations

Table 3.6 shows the optimum parameters values for section depth, initial learning rate, momentum, and regularization that yielded the minimum classification error obtained by the BO technique after 8 evaluations for approximately 4 hours:

Table 3.6: Optimal CNN Parameters Values for BO-CNN

| Optimized Variable using BO | Value |
| :---: | :---: |
| Optimal Section Depth | 3 |
| Optimal Initial Learning Rate | 0.6893 |
| Optimal Momentum | 0.8407 |
| Optimal Regularization | $4.5857 \mathrm{e}-05$ |
| Classification Error on the Validation Set | 0.1928 |

The minimum classification error value is 0.1928 , it is a result of section depth value of 3 , initial learning rate of 0.6893 , momentum of 0.8407 and regularization of $4.5857 \mathrm{e}-05$.

Then, BA is added to adjust the global learning rate in each of the three convolutional layers and fully connected layer. Table 3.7 shows the optimal weight learning rate factors optimized by BA along with classification error on the validation set:

Table 3.7: Optimal Weight Learning Rate Factors for BA-BO-CNN

| Optimized Variable using BA | Value |
| :---: | :---: |
| Optimal Weight Learning Rate Factor for <br> Convolutional Layer 1 | 0.9308 |
| Optimal Weight Learning Rate Factor for <br> Convolutional Layer 2 | 1.0924 |
| Optimal Weight Learning Rate Factor for <br> Convolutional Layer 3 | 1.0753 |
| Optimal Weight Learning Rate Factor for <br> Fully Connected Layer | 0.9977 |
| Classification Error on the Validation Set | 0.1778 |

So, the global learning rate of 0.68934 obtained by BO is adjusted by multiplying it by 0.9308 in the first convolutional layer to become 0.6416 . In the second convolutional layer, the adjustment factor is 1.0924 resulting in a learning rate value of 0.7530 , the factor for the third convolutional layer is 1.0753 , so the adjusted value is 0.7412 . Finally, the new learning rate value for the fully connected layer is 0.6877 after adjusting it by a factor of 0.9977 . Figure 3.13 shows the training progress in blue line and validation accuracy in black line after adding BA, the training progress curve for CNN, BO-CNN and BA-BOCNN are similar.


Figure 3.13: Training Progress for BA-BO-CNN
The following three figures $3.14,3.15$, and 3.16 present the confusion matrix for training, validation and testing set for the BA-BO-CNN algorithm showing precision and false alarm in the blue and red rows, and recall and miss out in the blue and red columns respectively:


Figure 3.14: Confusion Matrix for Training Data for BA-BO-CNN


Figure 3.15: Confusion Matrix for Validation Data for BA-BO-CNN

| airplane automobile | Confusion Matrix for Testing Data |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 384 | 4 | 22 | 9 | 6 | 1 | 5 | 1 | 40 | 8 |
|  | 6 | 483 | 3 | 2 |  |  | 1 | 1 | 8 | 27 |
|  | 30 | 2 | 338 | 22 | 37 | 19 | 21 | 12 | 6 |  |
|  | 12 | 3 | 30 | 330 | 31 | 51 | 20 | 13 | 9 | 3 |
|  | 5 | 1 | 24 | 20 | 416 | 7 | 6 | 16 | 8 | 1 |
|  | 2 | 2 | 9 | 78 | 15 | 352 | 8 | 23 | 7 | 2 |
|  | 4 |  | 34 | 20 | 18 | 3 | 404 | 2 | 2 | 1 |
|  | 8 |  | 14 | 16 | 18 | 10 | 2 | 424 | 3 | 1 |
|  | 13 | 10 | 5 | 5 | 3 | 2 | 1 |  | 472 | 7 |
|  | 11 | 25 | 4 | 1 |  |  | 2 | 6 | 7 | 440 |



Figure 3.16: Confusion Matrix for Testing Data for BA-BO-CNN
The following table 3.8 shows the training, validation, and testing accuracy along with computational time for the best iteration for the original CNN, BO-CNN, hybrid BA-CNN, and BA-BO-CNN:

Table 3.8: Classification Accuracy and Computational Time for Algorithms (Cifar10DataDir Dataset)

|  | Existing <br> Original CNN | Existing <br> BO-CNN | Novel Hybrid <br> BA-CNN | Novel Hybrid <br> BA-BO-CNN |
| :---: | :---: | :---: | :---: | :---: |
| Training Accuracy | $92.68 \%$ | $90.27 \%$ | $83.54 \%$ | $90.53 \%$ |
| Validation Accuracy | $80.34 \%$ | $80.72 \%$ | $80.72 \%$ | $82.22 \%$ |
| Testing Accuracy | $80.54 \%$ | $80.69 \%$ | $80.02 \%$ | $80.74 \%$ |
| Computational Time | 42 Min 56 Sec | 43 Min 24 Sec | 41 Min 46 Sec | 41 Min 13 Sec |

It is seen that the BA-CNN algorithm performs slightly better than the original CNN in terms of validation accuracy, but it is the same as the existing BO-CNN. In addition, it has better performance than the EA-CNN model designed in (Badan, 2019) that achieved an accuracy of $62.37 \%$ on the same 'Cifar10DataDir' dataset as was shown in table 2.2. The hybrid BA-BO-CNN algorithm has the best validation and testing accuracy, so it has the best classification performance and generalization capability to unseen data. In addition, it is the best algorithm in terms of cost-effectiveness since it achieved lower computational time than the BO-CNN algorithm by 2 minutes and 11 seconds.

The same procedure is followed to apply the original CNN, BO-CNN, hybrid BA-CNN, and BA-BO-CNN on the other three benchmark datasets, the results are shown in the following three tables $3.9,3.10$, and 3.11 :

Table 3.9: Classification Accuracy and Computational Time for Algorithms (Digits Dataset)

|  | Existing <br> Original CNN | Existing <br> BO-CNN | Novel Hybrid <br> BA-CNN | Novel Hybrid <br> BA-BO-CNN |
| :---: | :---: | :---: | :---: | :---: |
| Training Accuracy | $99.94 \%$ | $100 \%$ | $100 \%$ | $100 \%$ |
| Validation Accuracy | $98.80 \%$ | $100 \%$ | $99.90 \%$ | $100 \%$ |
| Testing Accuracy | $99.20 \%$ | $99.99 \%$ | $100 \%$ | $99.99 \%$ |
| Computational Time | 2 Min 35 Sec | 6 Min 42 Sec | 2 Min 28 Sec | 3 Min 30 Sec |

The table shows that the novel hybrid BA-BO-CNN algorithm produces the same accuracy as the BO-CNN algorithm due to simple features in the digits images which can be classified with high accuracy using existing algorithms, but the computational time in the hybrid algorithm is better by 3 minutes and 12 seconds reduction, so it is better in terms of cost-effectiveness. The novel hybrid BA-CNN algorithm produces almost similar results to existing BO-CNN in terms of accuracy, but it has the lowest computational time with 4 minutes and 14 seconds reduction compared to the BO-CNN model, so it is the best algorithm in terms of cost-effectiveness.

Table 3.10: Classification Accuracy and Computational Time for Algorithms (Concrete Cracks Dataset)

|  | Existing <br> Original CNN | Existing <br> BO-CNN | Novel Hybrid <br> BA-CNN | Novel Hybrid <br> BA-BO-CNN |
| :---: | :---: | :---: | :---: | :---: |
| Training Accuracy | $99.96 \%$ | $99.90 \%$ | $98.90 \%$ | $99.95 \%$ |
| Validation Accuracy | $99.50 \%$ | $99.67 \%$ | $98.50 \%$ | $99.67 \%$ |
| Testing Accuracy | $99.83 \%$ | $99.30 \%$ | $98.85 \%$ | $99.35 \%$ |
| Computational Time | 3 Min 20 Sec | 2 Min 46 Sec | 2 Min 22 Sec | 2 Min 50 Sec |

In this dataset, the new hybrid algorithms have almost similar results to the existing original CNN and BO-CNN models since the dataset consists of only two classes, so applying the existing algorithms produced high accuracy.

Table 3.11: Classification Accuracy and Computational Time for Algorithms (ECG Dataset)

|  | Existing <br> Original CNN | Existing <br> BO-CNN | Novel Hybrid <br> BA-CNN | Novel Hybrid <br> BA-BO-CNN |
| :---: | :---: | :---: | :---: | :---: |
| Training Accuracy | $100 \%$ | $97.53 \%$ | $100 \%$ | $96.29 \%$ |
| Validation Accuracy | $87.80 \%$ | $90.24 \%$ | $87.80 \%$ | $90.24 \%$ |
| Testing Accuracy | $92.50 \%$ | $90 \%$ | $92.50 \%$ | $95 \%$ |
| Computational Time | 1 Min 20 Sec | 1 Min 20 Sec | 1 Min 29 Sec | 1 Min 20 Sec |

It is seen that the best algorithms in terms of validation accuracy are BO-CNN and BA-BO-CNN algorithms with a value of $90.24 \%$, while the best testing accuracy of $95 \%$ comes with a hybrid BA-BO-CNN model. So, it is concluded that the hybrid BA-BO-CNN algorithm has the best classification performance and generalization capability to unseen data, the computational time is almost similar for all algorithms. The hybrid BA-CNN model performs the same as the original CNN, but it is better than the BO-CNN algorithm in terms of testing accuracy. The computational time is almost similar for all algorithms, it is assumed that the computational time will be higher if a large dataset is available to train CNN from scratch instead of using pre-trained CNN 'SqueezNet'.

The developed hybrid CNN algorithms can be applied in the manufacturing context, particularly to analyse porosity images of parts manufactured by the SLM process, so the following chapter will create artificial porosity images mimicking the real CT scan of the finished SLM part which will be used to predict the percent of porosity in the finished SLM parts using the developed hybrid CNN algorithms in this chapter.

### 3.3 Summary

This chapter proposed a novel hybrid Bees Convolutional Neural Network (BA-CNN) algorithm which uses the BA to optimize CNN's four parameters (section depth, initial learning rate, momentum, and regularization) in order to increase the classification accuracy of the network. In addition, another novel nature inspired hybrid algorithm was proposed which combines BO with BA in order to increase the overall performance of CNN which is referred to as the BA-BO-CNN algorithm. BO was used to optimize four CNN parameters section depth, initial learning rate, momentum, and regularization while BA was applied to optimize the weight learning rate factor to adjust the global learning rate obtained by BO algorithm in each convolutional layer and fully connected layer.

Applying the hybrid BA-CNN algorithm to the 'Cifar10DataDir' benchmark image data performed slightly better than original CNN in terms of validation accuracy, but it is the same as existing BO-CNN. In addition, it has better performance than the EA-CNN model designed in (Badan, 2019) that achieved an accuracy of $62.37 \%$ on the same 'Cifar10DataDir' dataset as was shown in table 2.2. Applying it to the digit dataset produced the lowest computational time with 4 minutes and 14 seconds reduction compared to BO-CNN, thus showing that it is the best algorithm in terms of cost-effectiveness. However, applying it to concrete cracks images and artificial porosity images produced almost similar results to existing algorithms. Finally, applying it to ECG images improved the testing accuracy from $90 \%$ for BO-CNN to $92.50 \%$ for the BA-CNN algorithm.

Furthermore, applying the hybrid BA-BO-CNN algorithm to 'Cifar10DataDir' benchmark image data yielded an increase in the validation accuracy from $80.72 \%$ to $82.22 \%$, while applying it to the digit dataset showed the same accuracy as the existing original CNN and BO-CNN models, but with an improvement in the computational time by 3 minutes and 12 seconds reduction. Applying it to concrete cracks images produced almost similar results to the existing algorithms, and finally applying it to human Electrocardiogram (ECG) signals improved the testing accuracy from $92.50 \%$ for the original CNN to $95 \%$ for the BA-BO-CNN algorithm.

The contributions of this chapter are:

- Developing a novel hybrid Bees Convolutional Neural Network (BA-CNN) algorithm in order to improve the performance of CNN.
- Developing a novel hybrid Bees Bayesian Convolutional Neural Network (BA-BOCNN) algorithm in order to improve the performance of CNN.


## Chapter 4: Artificial Porosity Images Creation for Selective Laser Melting Parts

### 4.1 Artificial Porosity Images Creation Process

Training CNN algorithms would require a large amount of experimental data, which is expensive for SLM parts (www.facfox.com, 2022) since there are many types of production cost for pre-processing, processing, and post-processing cost including preparing geometry data, CAD model, machine setup, material cost, building up the part, and post-processing cost (Rickenbacher, 2013), so producing a large amount of porosity images to train the RCNN is not cost-effective.

This chapter proposes a new efficient approach of creating artificial keyhole porosity images mimicking the real CT scan slices of the finished SLM parts that can be used in the research environment effectively and efficiently. In particular, the artificial images are used to validate the training of an accurate RCNN for the automatic prediction of porosity in CT scans of SLM parts. The steps for creating the artificial porosity images are:

- Establishing regression equations
- Generating pores number and diameter
- Creating 3D cubes
- Slicing 3D cubes into 2D images
- Labelling 2D slices
- Adding noisy background

They are shown in the following figure 4.1 which is followed by subsections explaining each step in detail.


Figure 4.1: Flowchart for the Steps of Creating Artificial Porosity Images

### 4.1.1 Establishing Regression Equations

The formulation of two regression equations is based on laser power and scanning speed data found in (Shrestha, et al., 2019), the first one correlates the number of pores (Y1) with laser power (X1) and scanning speed (X2) and other equation correlates pores diameter (Y2) with the same parameters (X1 and X2). The data used to establish the two equations are related to keyhole porosity and they will be used as a demonstration for an example of pore types formation.

The following table 4.1 shows the corresponding number of pores for each combination of laser power and scanning speed:

Table 4.1: Number of Pores Data (Shrestha, et al., 2019)

| \# | Laser Power (W) | Scanning Speed (mm/s) | Number of Pores in $2.6 \mathbf{~ m m}^{3}$ Volume |
| :---: | :---: | :---: | :---: |
| 1 | 195 | 200 | 101 |
| 2 | 175 | 200 | 121 |
| 3 | 150 | 200 | 121 |
| 4 | 125 | 200 | 101 |
| 5 | 195 | 400 | 41 |
| 6 | 175 | 400 | 75 |
| 7 | 150 | 400 | 55 |
| 8 | 195 | 600 | 4 |
| 9 | 125 | 400 | 30 |
| 10 | 175 | 600 | 19 |
| 11 | 150 | 600 | 4 |
| 12 | 195 | 800 | 0 |
| 13 | 175 | 800 | 1 |
| 14 | 125 | 600 | 2 |
| 15 | 150 | 800 | 0 |
| 16 | 195 | 1000 | 0 |
| 17 | 175 | 1000 | 0 |
| 18 | 125 | 800 | 0 |
| 19 | 195 | 1200 | 0 |
| 20 | 150 | 1000 | 1 |
| 21 | 175 | 1200 | 0 |
| 22 | 125 | 1000 | 0 |
| 23 | 150 | 1200 | 0 |
| 24 | 125 | 1200 | 0 |

The Minitab software is used to establish the first regression equation that fits the 24 observations (Shrestha, et al., 2019) mentioned in table 4.1, thus correlating the number of pores with the laser power and the scanning speed which result in the following equation: Number of Pores $=89.3+0.063 x L$ Laser Power $-0.1017 x$ Scanning Speed
(Equation 4.1)
Similarly, another regression equation is established to fit pores diameter with laser power and scanning speed data found in (Shrestha, et al., 2019), the dataset is shown in the following table 4.2:

Table 4.2: Pores Diameter Data (Shrestha, et al., 2019)

| $\#$ | Laser Power <br> $(\mathbf{W})$ | Scanning Speed <br> $(\mathbf{m m} / \mathbf{s})$ | Pores Diameter $(\boldsymbol{\mu m})$ |
| :---: | :---: | :---: | :---: |
| $\mathbf{1}$ | 195 | 200 | 47 |
| $\mathbf{2}$ | 175 | 200 | 46 |
| $\mathbf{3}$ | 150 | 200 | 42 |
| $\mathbf{4}$ | 125 | 200 | 45 |
| $\mathbf{5}$ | 195 | 400 | 36 |
| $\mathbf{6}$ | 175 | 400 | 41 |
| $\mathbf{7}$ | 150 | 400 | 27 |
| $\mathbf{8}$ | 125 | 400 | 26 |
| $\mathbf{9}$ | 195 | 600 | 25 |
| $\mathbf{1 0}$ | 175 | 600 | 27 |
| $\mathbf{1 1}$ | 150 | 600 | 25 |

Once again, the Minitab software is used to establish the regression equation that fits the 11 observations (Shrestha, et al., 2019) mentioned in table 4.2 correlating the pores diameter with the laser power and the scanning speed, which results in the following equation:

Pores Diameter $=37.88+0.1044 x$ Laser Power $-0.05207 x$ Scanning Speed (Equation 4.2)

### 4.1.2 Generating Pores Number and Diameter

The two regression equations established in the previous step are used to generate 30 values for the number of pores and pores diameter by substituting 30 combinations of laser power and scanning speed found in (Shrestha, et al., 2019). The following is an illustrative example with a laser power of 15 W and a scanning speed of $50 \mathrm{~mm} / \mathrm{s}$ :

$$
\begin{aligned}
& \text { Number of Pores }=89.3+0.063 \times(15)-0.1017 \times(50)=85 \text { Pores } \\
& \text { Pores Diameter }=37.88+0.1044 \times(15)-0.05207 \times(50)=36.94 \mu \mathrm{~m}
\end{aligned}
$$

The following table 4.3 shows 30 combinations of laser power and scanning speed found in (Shrestha, et al., 2019) along with the corresponding number of pores after scaling down from a $2.6 \mathrm{~mm}^{3}$ to a $1 \mathrm{~mm}^{3}$ volume, the volume of the cube in which the pores will be positioned and used to train the RCNN. Variations of $+/-10 \mu \mathrm{~m}$ are applied randomly to the generated pore diameters mimicking variations occurring in real porosity images:

Table 4.3: Number of Pores and Pores Diameter for Combined Laser Power and Scanning Speed

| $\#$ | Laser Power <br> $(\mathbf{W})$ | Scanning Speed <br> $(\mathbf{m m} / \mathbf{s})$ | Number <br> of Pores in <br> $\mathbf{2 . 6} \mathbf{~ m m}^{\mathbf{3}}$ <br> volume | Number of Pores <br> After Scaling <br> (Divided by 2.6 to <br> scale it to 1 mm <br> ( | Average <br> Pores <br> Diameter <br> $(\boldsymbol{\mu m})$ | Maximum <br> Pores <br> Diameter <br> $(\boldsymbol{\mu m})$ | Minimum <br> Pores <br> Diameter <br> $(\boldsymbol{\mu m})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{1}$ | $\mathbf{1 6}$ | $\mathbf{5 0}$ | 85 | 33 | 36.9469 | 46.9469 | 26.9469 |
| $\mathbf{2}$ | $\mathbf{2 0}$ | $\mathbf{5 0}$ | 85 | 33 | 37.3645 | 47.3645 | 27.3645 |
| $\mathbf{3}$ | $\mathbf{2 4}$ | $\mathbf{5 0}$ | 86 | 33 | 37.7821 | 47.7821 | 27.7821 |
| $\mathbf{4}$ | $\mathbf{3 2}$ | $\mathbf{1 0 0}$ | 81 | 31 | 36.0138 | 46.0138 | 26.0138 |
| $\mathbf{5}$ | $\mathbf{4 0}$ | $\mathbf{1 0 0}$ | 82 | 32 | 36.8490 | 46.8490 | 26.8490 |
| $\mathbf{6}$ | $\mathbf{4 8}$ | $\mathbf{1 0 0}$ | 82 | 32 | 37.6842 | 47.6842 | 27.6842 |
| $\mathbf{7}$ | $\mathbf{4 8}$ | $\mathbf{1 5 0}$ | 77 | 30 | 35.0807 | 45.0807 | 25.0807 |
| $\mathbf{8}$ | $\mathbf{6 0}$ | $\mathbf{1 5 0}$ | 78 | 30 | 36.3335 | 46.3335 | 26.3335 |
| $\mathbf{9}$ | $\mathbf{7 2}$ | $\mathbf{1 5 0}$ | 79 | 30 | 37.5863 | 47.5863 | 27.5863 |
| $\mathbf{1 0}$ | $\mathbf{6 4}$ | $\mathbf{2 0 0}$ | 73 | 28 | 34.1476 | 44.1476 | 24.1476 |


| 11 | 80 | 200 | 74 | 28 | 35.818 | 45.818 | 25.818 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 12 | 96 | 200 | 75 | 29 | 37.4884 | 47.4884 | 27.4884 |
| 13 | 80 | 250 | 69 | 27 | 33.2145 | 43.2145 | 23.2145 |
| 14 | 100 | 250 | 70 | 27 | 35.3025 | 45.3025 | 25.3025 |
| 15 | 120 | 250 | 71 | 27 | 37.3905 | 47.3905 | 27.3905 |
| 16 | 96 | 300 | 65 | 25 | 32.2814 | 42.2814 | 22.2814 |
| 17 | 120 | 300 | 66 | 25 | 34.7870 | 44.7870 | 24.7870 |
| 18 | 144 | 300 | 68 | 26 | 37.2926 | 47.2926 | 27.2926 |
| 19 | 112 | 350 | 61 | 23 | 31.3483 | 41.3483 | 21.3483 |
| 20 | 140 | 350 | 63 | 24 | 34.2715 | 44.2715 | 24.2715 |
| 21 | 168 | 350 | 64 | 25 | 37.1947 | 47.1947 | 27.1947 |
| 22 | 130 | 406.2 | 56 | 22 | 30.3011 | 40.3011 | 20.3011 |
| 23 | 162.5 | 406.2 | 58 | 22 | 33.6941 | 43.6941 | 23.6941 |
| 24 | 195 | 406.2 | 60 | 23 | 37.0871 | 47.0871 | 27.0871 |
| 25 | 144 | 450 | 53 | 20 | 29.4821 | 39.4821 | 19.4821 |
| 26 | 180 | 450 | 55 | 21 | 33.2405 | 43.2405 | 23.2405 |
| 27 | 156 | 487.5 | 50 | 19 | 28.7822 | 38.7822 | 18.7822 |
| 28 | 195 | 487.5 | 52 | 20 | 32.8538 | 42.8538 | 22.8538 |
| 29 | 176 | 550 | 44 | 17 | 27.6159 | 37.6159 | 17.6159 |
| 30 | 195 | 609.4 | 40 | 15 | 26.5065 | 36.5065 | 16.5065 |

### 4.1.3 Creating 3D Cubes

30 samples of 3D cubes are created with a volume of $1 \mathrm{~mm}^{3}$ for each cube, they contain the number of pores and the pores diameter generated in the previous section (table 4.3), Thus, the first cube has 33 pores with an average diameter of $36.94 \mu \mathrm{~m}$. In (Maskery et al., 2016), the position of pores was considered by analysing the porosity distribution in real images of pores found in alloy $\mathrm{Al}-\mathrm{Si} 10-\mathrm{Mg}$ parts produced by SLM process with laser power of 200 W , scanning speed $318 \mathrm{~mm} / \mathrm{s}$, and hatch spacing of $80 \mu \mathrm{~m}$. They observed 975 porosity positions in X and Y . In this research, the Minitab platform is used to conduct
a normality test on these observations to check if their statistical distribution is normal or not, as shown in the following figures 4.2 and 4.3:


Figure 4.2: Probability Plot for X-Position


Figure 4.3: Probability Plot for Y-Position

With a P-value of less than 0.005 , the probability that these data are not coming from a normal distribution is very low, so it is concluded that the observed porosity positions are normally distributed, with a mean and a standard deviation of 0.48 and 0.27 for X-positions and 0.44 and 0.26 for Y- positions. Therefore, in this research, it is decided to produce porosity positions with the same statistical distribution as observed in (Maskery et al., 2016).

Thus, the MATLAB software is used to generate normally distributed porosity positions inside each of the 30 cubes (Appendix 1.5) with the mean and the standard deviation mentioned previously, in the X and Y positions, while the Z position is arbitrarily given the average between X and Y to produce normal distribution pores in a volume. The pores morphology is created to be similar to the 3D view of the pores shown in figure 2.10 in section 2.8.6 (Shrestha et al., 2019). The following figure 4.4 shows an illustrative example of the cube with 33 pores and an average diameter of $36.94 \mu \mathrm{~m}$ as mentioned in the first combination of table 4.3:


Figure 4.4: 3D Cube with 33 Pores and Average Pores Diameter of $36.94 \mu \mathrm{~m}$

### 4.1.4 Slicing 3D Cubes into 2D Images

Each cube created in the previous step is sliced into 100 slices using the MATLAB software (Appendix 1.5) with a thickness of 0.01 mm resulting in 3000 slices of 2D images, an illustrative example for the cube and three not sequential slices is shown in the following figure 4.5:
(Slice 1)

(Slice 31)

(Slice 59)


Figure 4.5: An Illustrative Example of the Cube Slicing

The first slices are expected to be with no pore as shown at the bottom of the cube, thereafter part of a pore is shown in some slices and parts of many pores are shown in other slices. The pore morphology tended to be near-spherical in shape as described in section 2.8.6 (Tan et al., 2020).

### 4.1.5 Labelling $2 D$ Slices

The slices are labelled with the actual percent of porosity for each slice using the MATLAB software (Appendix 1.5), it is calculated by dividing the number of elements with specific pore unique pixel value by the total image size ( $650 \times 630 \times 3$ ). The pixel values for the pores are determined by inspecting the pixel values of porosity seen in real CT Scan images (figure 4.9) (Feng et al., 2022), they are between 110 and 124. The first slice has no elements with a pixel value in the range between 110 and 124 , so the actual percent of the pore is 0 . In slice 31, there are 258 elements with pixel values in the range specified, so the actual percent of the pore is $(258 /(650 \times 630 \times 3)) \times 100=0.0210$. Similarly for slice 59 with 2193 elements of pixel values between 110 and 124, the actual percent of the pore is $(2193 /(650 \times 630 \times 3)) \times 100=0.1785$, the average actual percent of the pore for the 3000 slices is 0.0134 .

### 4.1.6 Adding Noisy Background

First, image processing in the MATLAB platform is conducted to reduce the pixel brightness values of the background to different gray values between 180 and 150 resulting in the first version of the artificial images shown in the following figure 4.6:
(Slice 1)

(Slice 30)

(Slice 62)


Figure 4.6: An Illustrative Example of the First Version of Artificial Porosity Images
As shown in the previous slices, the background is clean and does not mimic the real CT scan slices of the finished SLM part.

The noisy background of 100 existing real porosity images made in (Feng et al., 2022) are fused with every 100 slices of each cube resulting in the following second version of artificial porosity images shown in figure 4.7:
(Slice 1)

(Slice 60)


## Figure 4.7: An Illustrative Example of the Second Version of Artificial Porosity Images

In the artificial images, the edges of the pores have a uniform shading making them clearly distinguishable from the background. This is not a true representation of porosity seen on real CT scans, where shade variations make it difficult to properly distinguish pores' edges. Thus, in a third version, once again image processing in the MATLAB platform is conducted to further filter the artificial porosity images by creating similar noise, so the background of a sample of 100 existing images is inserted into 100 pores slices extracted from 3D cube after reducing the pixel value for its white background from 255 to

155 to convert it to gray background. The artificial images are overlayed with the noisy background of real images. The degree of overlaying is determined by a factor (between 0 and 1) following the method described in (MathWorks-8) (Appendix 1.5). Thus, with a factor of 1 , the pore image is shown without noisy background and with a factor of 0 , the noisy background is shown without pores. After many trial and error experiments, a factor of 0.125 is considered to visually be the best value that combined both pore and noisy background images as shown in the following figure 4.8 :
(Slice 1)


Figure 4.8: An Illustrative Example of the Final Version of Artificial Porosity Images
As shown in the slices, the noise in the background and the pores appear more like real porosity images as the edges are not as clearly defined, but this is a subjective evaluation.

The following section 4.2 will measure the similarity between real and artificial porosity images to make sure the created artificial images are realistic.

### 4.2 Results and Discussion of the Similarity between Artificial and Real Porosity Images

The created artificial porosity images are compared with real CT scan slices of finished SLM parts (Feng et al., 2022) to verify that the simulated images are close to the reality. The real images are only used as a demonstration and are not directly linked with the pore formation equations mentioned in section 4.1.1. The following figure 4.9 shows an illustrative example of the real slices before and after processing, which was required to focus on the bulk of the material and to obtain images of the same size as the artificial images.


Figure 4.9: An Illustrative Example of the Real Existing Porosity Images (Feng et al., 2022)
A sample of 100 slices of the real images is taken and compared with the created artificial porosity images in the previous section using a quantitative method called Structural Similarity Index (SSI). It is a measure that assesses the images based on three computational terms: the luminance (l), the contrast (c), and the structural terms (s), multiplying three terms results in the overall index. If two images are exactly the same, the index is 1 and if they are totally different the index is close to zero. (MathWorks-9) described the mathematical equations to calculate SSI for images $x$ and $y$ :
$\operatorname{SSI}(\mathrm{x}, \mathrm{y})=[\mathrm{l}(\mathrm{x}, \mathrm{y})]^{\alpha} \cdot[\mathrm{c}(\mathrm{x}, \mathrm{y})]^{\beta} \cdot[\mathrm{s}(\mathrm{x}, \mathrm{y})]^{\gamma}$
(Equation 4.3)
Where:

$$
\begin{align*}
& 1(x, y)=\left(2 \mu_{x} \mu_{y}+C 1\right) /\left(\mu_{x}^{2}+\mu_{y}^{2}+\mathrm{C} 1\right)  \tag{Equation4.4}\\
& \mathrm{c}(\mathrm{x}, \mathrm{y})=\left(2 \sigma_{\mathrm{x}} \sigma_{\mathrm{y}}+\mathrm{C} 2\right) /\left(\sigma_{\mathrm{x}}^{2}+\sigma_{\mathrm{y}}^{2}+\mathrm{C} 2\right) \\
& \mathrm{s}(\mathrm{x}, \mathrm{y})=\left(\sigma_{\mathrm{xy}}+\mathrm{C} 3\right) /\left(\sigma_{\mathrm{x}} \sigma_{\mathrm{y}}+\mathrm{C} 3\right)
\end{align*}
$$

(Equation 4.5)
(Equation 4.6)
where $\mu_{\mathrm{x}}$ and $\mu_{\mathrm{y}}$ are local means, $\sigma_{\mathrm{x}}$ and $\sigma_{\mathrm{y}}$ are the standard deviations for images x and y , and $\sigma_{\mathrm{xy}}$ is cross-covariance for images x and y . The exponents for luminance, contrast and structural are alpha $(\alpha)$, beta $(\beta)$, and gamma $(\gamma)$, while $\mathrm{C} 1, \mathrm{C} 2$, and C 3 are constants added to avoid instability for image regions where the local mean or standard deviation is close to zero.

MATLAB platform is used to calculate the structural similarity index between the real and first version of artificial images (Appendix 1.5), the first index is 0.7085 for the following two images in figure 4.10:


Figure 4.10: Real Image (Left) Vs First Version of Artificial Image (Right)
In order to improve the SSI, the average grayscale value of the artificial image is reduced to 152 instead of 182 since the average grayscale value for the real image is 152 , in addition, the mean and variance of gaussian noise were reduced from 0.001 to 0.00005
after many trials to reach the best SSI value which becomes 0.8764 for the following two images in figure 4.11:


Figure 4.11: Real Image (Left) Vs Improved First Version of Artificial Image (Right)
Furthermore, the SSI algorithm is applied to the second version of artificial porosity images with normally distributed porosity positions and backgrounds of real images, the following figure 4.12 shows real and artificial images:


Figure 4.12: Real Image (Left) Vs Second Version of Artificial Image (Right)

A sample of 100 real images and 100 slices for each of the 30 cubes are compared, the average similarity index for 3000 slices is 0.9586 . The same sample of 100 real images are used to compare them with the final version of artificial porosity images shown in the following figure 4.13:


Figure 4.13: Real Image (Left) Vs Final Version of Artificial Image (Right)
The average similarity index for 3000 slices is improved to 0.9967 which means that the final version of artificial porosity images mimics better real images since the index is closer to 1 .

The created artificial porosity images in this chapter will be used only to test the proposed RCNN algorithms that will be developed in the next chapter 5. The study is not aimed to study the porosities in depth, so no experiments have been conducted, but the next chapter proposes a method that will enhance such studies, particularly in predicting the percent of porosity as will be demonstrated in the next chapter. In the future, real experiments can be conducted in order to produce real porosity images.

### 4.3 Summary

This chapter proposed a new efficient approach of creating artificial keyhole porosity images mimicking the real CT scan slices of finished SLM parts that can be used in the research environment effectively and efficiently to validate the training of an accurate RCNN for the automatic prediction of porosity in CT scans of SLM parts. Training CNN
algorithms would require a large amount of experimental data which can be expensive for SLM parts (www.facfox.com, 2022) since there are many types of production costs for preprocessing, processing and post processing including preparing geometry data, CAD model, machine setup, material cost, and building up the part (Rickenbacher, 2013). Thus, producing large amount of porosity images to train RCNN is not cost-effective.

The steps for creating the artificial porosity images are:

- Establishing regression equations
- Generating pores number and diameter
- Creating 3D cubes
- Slicing 3D cubes into 2D images
- Labelling 2D slices
- Adding noisy background

This chapter's contribution which will be continued in the following chapter is:

- Developing a new approach to create a large amount of experimental artificial porosity images similar to real images by a similarity index of 0.9967 which can be used in the research environment efficiently and effectively in order to predict the percent of porosity in the finished SLM part using the developed hybrid CNN algorithms as will be described in the following chapter.

Chapter 5: Hybrid Regression Convolutional Neural Network for Predicting the Percent of Porosity in Selective Laser Melting Parts

### 5.1 Predicting the Porosity using the Existing Image Binarization Method

Using the artificial porosity images created in chapter 4, this chapter shows three methods for predicting the percent of porosity in the finished SLM parts. The first one is the existing image binarization method which is one of the main methods for measuring the porosity along with the Archimedes method (Arvieu et al., 2020). Archimedes's principle might be used in the case of producing real SLM parts, as this study uses artificial porosity images, so the image binarization method will be conducted and explained in this section. The second and third methods are Regression Convolutional Neural Network (RCNN) and hybrid Bees Regression Convolutional Neural Network (BA-RCNN) which will be explained in detail in section 5.2 and their results will be shown in section 5.3.

### 5.1.1 Porosity Assessment Gap using the Image Binarization Method

(Gong et al., 2019) mentioned that using CT scans of sample parts, there is a problem related to assessing accurately the porosity in the SLM parts. One main drawback is when using gray value analysis to assess the porosity of SLM parts visible in CT scan slices. The difficulty is the subjectivity in selecting an appropriate grayscale threshold that would convert a single slice into binary images highlighting defective regions, as well as determining the true level of porosity. For example, in figure 5.1 when an inappropriately low grayscale threshold is applied to the original slice image for binary image conversion, a certain amount of tiny undesired white spots are not filtered as shown in 5.1b. However, if a higher grayscale threshold is adopted, the morphological features of the defective area, specifically near the boundary, are altered dramatically as shown in figure 5.1c. These thresholds would result in significantly different predictions of porosity levels.


Figure 5.1: Original Slice and Binary Images (Gong et al., 2019)
To evaluate this issue further, the authors of this study (Gong et al., 2019) proposed an empirical method to estimate the porosity in the finished SLM parts using a naturalized threshold for CT scan slices. When compared with the Archimedes method, they found similar increasing or decreasing trends in the predicted percentage of porosity and concluded that the naturalized grayscale threshold is not the best solution to estimate the porosity in CT scan slices due to radiodensity variation and mutual influence of CT setup and it is difficult to compensate these variations with a unique grayscale (Gong et al., 2019). This limitation is found in one of the two main existing methods used in porosity estimation along with the Archimedes method as mentioned in (Arvieu et al., 2020).

### 5.1.2 Porosity Assessment Gap Validation

The second version of artificial porosity images created in the previous chapter are binarized using an adaptive thresholding algorithm in the MATLAB platform that selects the threshold based on local mean intensity in the pixel neighbourhood with a sensitivity factor between 0 and 1 that indicates the sensitivity toward thresholding more pixels as a foreground (MathWorks-10). The following figure 5.2 shows the artificial image along with the binarized image with sensitivity factor of 0.66 :


Figure 5.2: Second Version of Artificial Image (Left) Vs Binarized Artificial Image (Right)
As can be seen in figure 5.2, there are tiny undesired black spots in different positions in the binarized image, they appear also in slices with no pores as shown in the following figure 5.3:


Figure 5.3: Second Version of Artificial Image with No Pore (Left) Vs Binarized Artificial Image (Right)

The actual percent of porosity for artificial images is calculated during the creation process by dividing the number of elements with specific pore unique pixel value by the total image size as mentioned previously in section 4.1.5, the average percent of the pore for 3000 slices of the second version is 0.0134 while the average percent of the pore for the 3000 binarized images is overestimated with a value of 0.0578 , so the absolute error is 0.0444 . The prediction accuracy with a difference less than the threshold of 0.02 (percent of observations with error less than 0.02 ) is $64.47 \%$. The same approach is followed for the final version of artificial porosity images, the following figure 5.4 shows the artificial image along with the binarized image with sensitivity factor of 0.66 :


Figure 5.4: Final Version of Artificial Image (Left) Vs Binarized Artificial Image (Right)
As can be seen in figure 5.4, again there are tiny undesired black spots in different positions in the binarized image confirming the problem stated in (Gong et al., 2019), it is a result of inconsistent grayscale in CT scan slices because of the mutual influence of CT setup and radiodensity variation. Removing these spots using image processing is time consuming since they appear in different positions in each slice without a simple pattern, so the processing needs to be performed image by image to distinguish between the undesired black spots and the pores first. Then, unwanted spots need to be replaced with a white background because they are counted in the porosity calculation which overestimates the percent of porosity. Such an issue also occurs in the pores, as tiny white spots would
alter their morphological feature and slightly reduce the percent of porosity. However, the effect of this on porosity calculations is negligible when compared to the effect of the small black spots occurring in the large background. Depending on the sensitivity factor used, the black spots also appear in slices with no pores as shown in the following figure 5.5:


Figure 5.5: Final Version of Artificial Image with No Pore (Left) Vs Binarized Artificial Image (Right)

Experimenting different sensitivity factors between 0.63 to 0.74 resulted in the following binary images with different percent of porosity as shown in figure 5.6:


Figure 5.6: Binary Images with Different Sensitivity Factors and Percent of Porosity

As can be seen from the images, increasing the sensitivity factors reduces the black spots resulting from the noisy background, but it alters the pores' morphological feature dramatically. The sensitivity factor of 0.69 is relatively better and it will be selected to binarize all 3000 slices since it yielded the most accurate percent of porosity of $0.17 \%$ which is close to the actual percent of the pore for the original slice with a value of $0.1785 \%$. It is worth noting that in the case of producing the real porosity images, sensitivity factor selection will be subjective and difficult since the actual percent of porosity will be unknown. The average percent of the pore for 3000 slices of the final version is 0.0203 while the average percent of the pore for 3000 binarized images is overestimated with a value of 0.0424 , so the absolute error is 0.0221 . The prediction accuracy with a difference of less than a threshold value of 0.02 (percent of observations with error less than 0.02 ) is 68.60\%.

### 5.2 Predicting the Porosity using Hybrid Regression Convolutional Neural Networks

CNN can be used for regression problems to predict numerical values based on images, so regression CNN will be used to predict the percent of porosity based on the created artificial porosity images in the previous chapter. As mentioned previously (in section 4.1.5), the images are labelled using the actual percent of porosity calculated during the creation process by dividing the number of elements with specific pore unique pixel value by the total image size. CNN learns the porosity pattern in artificial porosity images that mimic CT scan images of the finished SLM part and predict the percent of porosity without the need for subjective difficult thresholding determination to convert a single slice into binary images which ultimately achieves automized quality assessment.

### 5.2.1 Regression Convolutional Neural Network Architecture

The CNN architecture for predicting the percent of porosity composes of 22 layers of which one input layer, five convolutional layers, five rectified linear unit layers, five batch normalization layers, four average pooling layers, one fully connected layer, and one regression layer.

The input layer is represented by a matrix of size height by width ( $650 \times 630$ ) that consists of pixel brightness numbers between 0 to 255 ( 0 for black and 255 for white). The
convolutional layers contain filters represented by matrix of weights that slide along the pixel brightness input matrix to create feature map matrix using special dot product as mentioned in (Hui, 2017). Rectified linear unit layers are used after each convolutional layer to increase the speed and effectiveness of the training by mapping negative values to zero and maintaining positive values as mentioned in (MathWorks-1). In addition, batch normalization layers are used as supplement layers after each convolutional layer to mitigate the risk of overfitting by normalizing the input values of the following layers (Yamashita et al., 2018). Pooling layers are used between the convolutional layers to reduce the dimensionality of the output volume (McDermott, 2021) without losing the important features which contribute to minimize the computational cost. Regression and fully connected layers are the output layers that show the predicted percent of the pores.

The normal number of convolutional layers to start is between two to three layers with a filter size of $3 \times 3$ or $5 \times 5$ as advised in (Hui, 2017), CNN is designed with five convolutional layers with four average pooling layers in between, the number of filters ranges between 8 for the first layer and 128 for the last one, each layer has twice number of filters of the previous layer (Brownlee, 2019). The filter size is $5 \times 5$, the section depth is 3 , and the padding that helps to detect the edges of the images is set as 'same' so that the software calculates the size of the padding at the training time automatically and produce output size equal to the input size if the stride (number of pixel shift) is one.

The pooling type is 'average' which takes the average presence of the feature while the max pooling layer takes the most activated feature, so the average pooling is better with light background and max pooling is better with dark background as mentioned in (Ouf, 2017), the default size of pooling layer is $2 \times 2$ (Hui, 2017), but it yielded high computational cost since the image input size is big ( 650 x 630 x 3 ), the size was changed to 4 x 4 with stride value of 4 to minimize the training time.

The CNN is trained using SGDM which is the most common training algorithm (Yamashita et al., 2018), the default values for this algorithm are an initial learning rate of 0.01 , a momentum of 0.9 , a regularization of $1 \mathrm{e}-04$, and the maximum number of epochs is 20 as presented in (MathWorks-6). After applying some experiments and monitoring the
validation accuracy, the momentum was changed to 0.8 and the regularization value became 1e-10.

### 5.2.2 The Proposed Hybrid BA-BO-RCNN \& BA-RCNN Algorithms

The hybrid regression CNN (BA-BO-RCNN and BA-RCNN) algorithms will train the artificial porosity images of the SLM part to predict the percent of porosity without the need for subjective difficult threshold determination to convert a single slice into binary images as mentioned in (Gong et al., 2019).

The following are the values of BA parameters which are assigned based on the computer capability of a single GPU with 256 GP and using the equations stated in (MathWorks-4).

- Maximum number of iterations $=1$
- Number of scout bees ( n ) $=4$
- $\quad$ Number of selected bees $(\mathrm{m})=0.5 \times \mathrm{n}=0.5 \times 4=2$
- Number of elite bees $(\mathrm{e})=1$
- Number of recruited bees for elite (e) sites (nep) $=2 \times \mathrm{m}=2 \times 2=4$
- Number of recruited bees for other best (m-e) sites (nsp) $=0.5 \times n=0.5 \times 4=2$
- Neighbourhood size for each selected patch (local search) (ngh) $=0.1 \times$ (Var max - Var min)
- Section depth: $0.1 \times(3-1)=0.1 \times 2=0.2$
- Initial learning rate: $0.1 \times(1-1 \mathrm{e}-2)=0.1 \times 0.99=0.099$
- Momentum: $0.1 \times(0.98-0.8)=0.1 \times 0.18=0.018$
- Regularization: $0.1 \times(1 \mathrm{e}-2-1 \mathrm{e}-10)=0.1 \times 0.01=0.001$
- Weight learning rate factor: $0.1 \times(1.1-0.9)=0.1 \times 0.2=0.02$

The following figures 5.7 and 5.8 summarizes the task for the hybrid algorithms:


The Benefit of ML Algorithm
Learning the porosity pattern in artificial porosity images that mimic CT scan images of the finished SLM part and predicting the percent of porosity without the need for subjective difficult thresholding determination to convert the single slice to binary image which ultimately achieve automized quality assessment

Figure 5.7: An Illustrative Diagram for Hybrid BA-BO-RCNN Algorithm


Figure 5.8: An Illustrative Diagram for Hybrid BA-RCNN Algorithm
The steps of MATLAB code for the hybrid regression CNN algorithms are shown in the following figure 5.9:


Figure 5.9: The Steps of MATLAB Code for Hybrid Regression CNN Algorithms

### 5.3 Results and Discussion for Hybrid Regression Convolutional Neural Networks

MATLAB software is used to apply the original Regression CNN (RCNN), hybrid Bayesian Regression CNN (BO-RCNN), hybrid Bees Bayesian Regression CNN (BA-BORCNN), and hybrid Bees Regression CNN (BA-RCNN) to the newly created 3,000 artificial porosity images of which 1800 images for training, 600 for each of the validation and testing sets to predict the percent of porosity without the need for subjective difficult thresholding determination to convert a single slice into binary images which ultimately achieve automized quality assessment. The system configuration consists of a single GPU with a memory of 256 GB to be able to handle the 3000 artificial porosity images of size ( $650 \times 630 \times 3$ ). As the DL algorithms require high computations, limited BA evaluations are applied to optimize CNN parameters. The datasets are shuffled at every epoch and the training, validation and testing sets are selected randomly after each shuffle in order to minimize the data biases and improve the validity of the experiments.

### 5.3.1 Results of Applying the Proposed Hybrid BA-BO-RCNN \& BA-RCNN Algorithms to

 the Second Version of Artificial Porosity ImagesFirst, the second version of artificial porosity images created in the previous chapter will be the input of the hybrid BA-BO-RCNN and BA-RCNN algorithms. The following table 5.1 shows the prediction accuracy with a difference less than a threshold of 0.02 (percent of observations with error less than 0.02 ) for training, validation, and testing sets along with the computational time for the best iteration for all algorithms:

Table 5.1: Prediction Accuracy and Computational Time for Algorithms (Second Version)

|  | Existing <br> Original RCNN | Existing <br> BO-RCNN | Novel Hybrid <br> BA-BO-RCNN | Novel Hybrid <br> BA-RCNN |
| :---: | :---: | :---: | :---: | :---: |
| Training Accuracy | $81.22 \%$ | $78.83 \%$ | $80.11 \%$ | $82.06 \%$ |
| Validation Accuracy | $81.50 \%$ | $79.67 \%$ | $82.50 \%$ | $81.67 \%$ |
| Testing Accuracy | $78.83 \%$ | $76.83 \%$ | $80.17 \%$ | $80.67 \%$ |
| Computational Time | 18 Min 17 Sec | 18 Min 14 Sec | $15 \operatorname{Min} 23 \mathrm{Sec}$ | 18 Min 13 Sec |

The existing original RCNN produced $78.83 \%$ prediction accuracy in the testing set which is approximately $14 \%$ better than the accuracy resulting from the image binarization method with a value of $64.47 \%$ for the second version of artificial porosity images. The hybrid BO-RCNN has lower accuracy than the original RCNN with a value of $76.83 \%$, so BO is not recommended to be used in this case as it performs poorly with a high dimensional objective function of more than 20 dimensions (www.stackexchange.com).

Adding BA to BO-RCNN improved the testing accuracy to $80.17 \%$ and it is the most efficient algorithm since it has lower computational time than other algorithms by approximately 3 minutes. The following table 5.2 shows the optimal weight learning rate factors optimized by BA:

Table 5.2: Optimal Weight Learning Rate Factors for BA-BO-RCNN (Second Version)

| Optimized Variable using BA | Value |
| :---: | :---: |
| Optimal Weight Learning Rate <br> Factor for Convolutional Layer 1 | 1.0629 |
| Optimal Weight Learning Rate <br> Factor for Convolutional Layer 2 | 1.0812 |
| Optimal Weight Learning Rate <br> Factor for Convolutional Layer 3 | 0.9254 |
| Optimal Weight Learning Rate <br> Factor for Convolutional Layer 4 | 1.0963 |
| Optimal Weight Learning Rate <br> Factor for Convolutional Layer 5 | 1.0265 |
| Optimal Weight Learning Rate <br> Factor for Fully Connected Layer | 0.9195 |

The improved testing accuracy is a result of adjusting the global learning rate of 0.010041 obtained by BO by multiplying it by 1.0629 in the first convolutional layer to become 0.0106 . In the second convolutional layer, the adjustment factor is 1.0812 resulting in a learning rate value of 0.008 , the factors for the third, fourth and fifth convolutional layers are $0.9254,1.0827$, and 1.0265 , so the adjusted values are $0.0092,0.0108$, and 0.0103
respectively. Finally, the new learning rate value for the fully connected layer is 0.0092 after adjusting it by a factor of 0.9195 .

The novel hybrid BA-RCNN produced the best prediction accuracy with a value of $80.67 \%$ in the testing set. The following table 5.3 shows the optimal CNN parameters values optimized by BA:

Table 5.3: Optimal CNN Parameters Values for BA-RCNN (Second Version)

| Optimized Variable using BA | Value |
| :---: | :---: |
| Optimal Section Depth | 3 |
| Optimal Initial Learning Rate | 0.0118 |
| Optimal Momentum | 0.8229 |
| Optimal Regularization | 0.0091 |

The best-achieved prediction accuracy of $80.67 \%$ is a result of a section depth value of 3 , an initial learning rate of 0.0118 , a momentum of 0.8229 and a regularization of 0.0091 . 5.3.2 Results of Applying the Proposed Hybrid BA-BO-RCNN \& BA-RCNN Algorithms to the Final Version of Artificial Porosity Images

The same approach is followed to predict the percent of porosity for the final version of artificial porosity images with a difference less than a threshold value of 0.02 (percent of observations with error less than 0.02 ), the following table 5.4 shows the prediction accuracy for training, validation, and testing sets along with computational time for best iteration for all algorithms:

Table 5.4: Prediction Accuracy and Computational Time for Algorithms (Final Version)

|  | Existing <br> Original RCNN | Existing <br> BO-RCNN | Novel Hybrid <br> BA-BO-RCNN | Novel Hybrid <br> BA-RCNN |
| :---: | :---: | :---: | :---: | :---: |
| Training Accuracy | $74.94 \%$ | $67.50 \%$ | $82.61 \%$ | $85.94 \%$ |
| Validation Accuracy | $76 \%$ | $66.67 \%$ | $84.17 \%$ | $87.33 \%$ |
| Testing Accuracy | $75.50 \%$ | $67.50 \%$ | $83 \%$ | $85.33 \%$ |
| Computational Time | 15 Min 43 Sec | 15 Min 38 Sec | 15 Min 30 Sec | 13 Min 40 Sec |

The existing original RCNN produced a prediction accuracy of $75.50 \%$ in the testing set which is approximately $7 \%$ better than the accuracy resulted from the image binarization method with a value of $68.60 \%$ for the final version of artificial porosity images. The hybrid BO-RCNN has lower accuracy than original RCNN with a value of $67.50 \%$, so it confirms the conclusion that BO is not recommended to be used in this objective function as it has more than 20 dimensions where BO performs poorly (www.stackexchange.com).

Adding BA to BO-RCNN improved the accuracy to $83 \%$, the following table 5.5 shows the optimal weight learning rate factors optimized by BA:

Table 5.5: Optimal Weight Learning Rate Factors for BA-BO-RCNN (Final Version)

| Optimized Variable using BA | Value |
| :---: | :---: |
| Optimal Weight Learning Rate <br> Factor for Convolutional Layer 1 | 0.9703 |
| Optimal Weight Learning Rate <br> Factor for Convolutional Layer 2 | 0.9376 |
| Optimal Weight Learning Rate <br> Factor for Convolutional Layer 3 | 1.0859 |
| Optimal Weight Learning Rate <br> Factor for Convolutional Layer 4 | 0.9813 |
| Optimal Weight Learning Rate <br> Factor for Convolutional Layer 5 | 0.9993 |
| Optimal Weight Learning Rate <br> Factor for Fully Connected Layer | 1.0982 |

The improved testing accuracy is a result of adjusting the global learning rate of 0.011964 obtained by BO by multiplying it by 0.9703 in the first convolutional layer to become 0.0116 . In the second convolutional layer, the adjustment factor is 0.9376 resulting in a learning rate value of 0.0112 , the factors for third, fourth and fifth convolutional layers are $1.0859,0.9813$, and 0.9993 , so the adjusted values are $0.0123,0.0117$, and 0.0112 respectively. Finally, the new learning rate value for fully connected layer is 0.0131 after adjusting it by a factor of 1.0982 .

The novel hybrid BA-RCNN produced the best prediction accuracy with a value of $85.33 \%$ in the testing set. In addition, the hybrid BA-RCNN is better as well in terms of cost-effectiveness since it has a lower computational time by approximately 2 minutes. The following table 5.6 shows the optimal CNN parameters values optimized by BA:

Table 5.6: Optimal CNN Parameters Values for BA-RCNN (Final Version)

| Optimized Variable using BA | Value |
| :---: | :---: |
| Optimal Section Depth | 1 |
| Optimal Initial Learning Rate | 0.0101 |
| Optimal Momentum | 0.9568 |
| Optimal Regularization | 0.0097 |

The best achieved prediction accuracy of $85.33 \%$ is a result of a section depth value of 1 , initial learning rate of 0.0101 , momentum of 0.9568 and regularization of 0.0097 .

### 5.3.3 Sensitivity to Noise in Artificial Porosity Images

This section compares between the image binarization method and the hybrid BARCNN algorithm in terms of sensitivity to noise in the artificial porosity images. Two different levels of noise are added to the final version of created artificial porosity images. As described in section 4.1.6, the artificial images were overlayed with the noisy background of real images. So, the noise is determined based on the degree of overlaying which is a factor with a value between 0 and 1 (MathWorks-8). Thus, with a factor of 1 , the pore image is shown without noisy background and with a factor of 0 , the noisy background is shown without pores. A factor of 0.125 was selected in section 4.1.6 to visually be the best value that combined both pore and noisy background. In this section, two more factors are arbitrarily selected which are 0.2 and 0.25 resulting in more noisy images. The following two figures 5.10 and 5.11 show illustrative examples of the noisy slices along with the binarized images:


Figure 5.10: Artificial Image with Noise of 0.2 (Left) Vs Binarized Artificial Image (Right)


Figure 5.11: Artificial Image with Noise of 0.25 (Left) Vs Binarized Artificial Image (Right)

Applying the image binarization method to 3000 slices with three different levels of noise $(0.125,0.2$ and 0.25$)$ results in the following table 5.7 that shows the prediction accuracy for the percent of porosity:

Table 5.7: Prediction Accuracy using Image Binarization Method with Different Levels of Noise

| Level of Noise | Prediction Accuracy |
| :---: | :---: |
| 0.125 | $68.60 \%$ |
| 0.2 | $40.73 \%$ |
| 0.25 | $26.6 \%$ |

Similarly, the hybrid BA-RCNN algorithm is applied to artificial porosity images with the same three levels of noise. The following table 5.8 shows the testing accuracy for predicting the percent of porosity:

Table 5.8: Prediction Accuracy using BA-RCNN Algorithm with Different Levels of Noise

| Level of Noise | Prediction Accuracy |
| :---: | :---: |
| 0.125 | $85.33 \%$ |
| 0.2 | $79.21 \%$ |
| 0.25 | $77.33 \%$ |

To clearly investigate the variations in the prediction accuracy of both techniques, the following figure 5.12 is created which presents the accuracies at different levels of noise:


Figure 5.12: Prediction Accuracy for Percent of Porosity at Different Levels of Noise
As can be seen in figure 5.12, the difference between the minimum and maximum accuracy in the BA-RCNN algorithm is less than the range of accuracies in the image binarization method, so it is concluded that the BA-RCNN algorithm is less sensitive to noise. The convolutional filters in CNN that slide along the pixel brightness input matrix can deal with the level of noise in the artificial porosity images so that the creation of feature map matrix is not affected (Hui, 2017). On the other hand, the image binarization method is affected by the level of noise as increasing the sensitivity factors to binarize the images reduces the black spots resulted from the noisy background, but it alters the pores morphological feature dramatically resulting in underestimating the percent of porosity. If the sensitivity factor is decreased, the pore morphology is not significantly changed, but the black spots appear more in the binarized images which overestimate the percent of porosity. So, these thresholds would result in significantly different predictions of porosity levels.

The following chapter will show a better DL algorithm in dealing with sequential layers of the SLM part, which is the LSTM network, it will be hybridized with CNN that extracts
the features in the artificial porosity images for feeding it into LSTM network that considers the long-term dependencies.

### 5.4 Summary

Using the artificial images created in chapter 4, this chapter showed three methods for predicting the percent of porosity in SLM parts. The first one is the existing image binarization method which is one of the main methods for measuring the porosity along with the Archimedes method (Arvieu et al., 2020). Archimedes's principle might be used in the case of producing real SLM parts, as this study used artificial porosity images, so the image binarization method was conducted. The second and third methods were RCNN and BA-RCNN.
(Gong et al., 2019) mentioned that using CT scans of sample parts, there is a problem related to assessing accurately the porosity in SLM parts. One main drawback is when using gray value analysis to assess the porosity of SLM parts visible in CT scan slices. The difficulty is the subjectivity in selecting an appropriate grayscale threshold that would convert a single slice into binary images highlighting defective regions, as well as determining the true level of porosity. When an inappropriately low grayscale threshold is applied to the original slice for binary image conversion, a certain amount of tiny undesired white spots is not filtered. However, if a higher grayscale threshold is adopted, the morphological features of the defective area, specifically near the boundary, are altered dramatically. These thresholds would result in significantly different predictions of porosity levels.

So, in this chapter, an intelligent method based on CNN was used for the regression problem to predict the percent of porosity in the finished SLM part without the need for subjective difficult threshold determination to convert the single slice to binary image. Applying RCNN on 3000 slices of the second version of artificial porosity images, similar to real CT-scan images by a similarity index of 0.9586 , improved porosity prediction accuracy from $64.47 \%$ for image binarization method to $78.83 \%$ for RCNN, while integrating BA produced the best prediction accuracy with a value of $80.67 \% \%$ which is approximately $16 \%$ better than existing image binarization method. The following table 5.9 summarizes the prediction accuracy:

Table 5.9: Porosity Prediction Accuracy (Second Version)

|  | Image Binarization | Original RCNN | Novel Hybrid <br> BA-RCNN |
| :---: | :---: | :---: | :---: |
| Porosity Prediction <br> Accuracy | $64.47 \%$ | $78.83 \%$ | $80.67 \%$ |

Applying RCNN on 3000 slices of the final version of artificial porosity images, similar to real CT-scan images by a similarity index of 0.9967 , improved porosity prediction accuracy from $68.60 \%$ for image binarization method to $75.50 \%$ for RCNN, while integrating BA produced the best prediction accuracy with a value of $85.33 \%$ which is approximately $17 \%$ better than existing image binarization method. The following table 5.10 summarizes the prediction accuracy:

Table 5.10: Porosity Prediction Accuracy (Final Version)

|  | Image Binarization | Original RCNN | Novel Hybrid <br> BA-RCNN |
| :---: | :---: | :---: | :---: |
| Porosity Prediction <br> Accuracy | $68.60 \%$ | $75.50 \%$ | $85.33 \%$ |

The contribution made in chapter 5 by combining the outcome of chapter 4 is :

- Proposing and validating a new approach for predicting the percent of porosity in the finished SLM parts, using hybrid Bees Regression Convolutional Neural Network (BA-RCNN). It was demonstrated that a better accuracy than the existing image binarization method could be achieved (approximately $17 \%$ improvement with the data set used). In order to test the algorithm, as the training of the RCNN would require a large amount of experimental data, artificial porosity images mimicking real CT scan slices of the finished SLM part were created with a similarity index of 0.9976 with real images.


# Chapter 6: Hybrid Long Short-Term Memory <br> Network with Bees Algorithm for Enhancing the Porosity Prediction in Selective Laser Melting Parts 

### 6.1 Proposed Novel Hybrid BA-CNN-LSTM Algorithm

Improving the performance of the LSTM network is an ongoing challenge, the traditional approach of assigning the parameters using trial and error is less accurate since it depends on the user experience. However, using a nature inspired algorithm to automatically select the optimum parameters values may improve the performance of the network (Panwar et al., 2017). The existing studies addressed optimizing hidden layers, number of neurons, activation function, loss function, optimizer, batch size, and number of epochs using different nature inspired algorithms as was shown in section 2.4.1. This chapter addresses optimizing the learning rate in the forget, input, and output gates in addition to the cell candidate and fully connected layer so that each step has a customized learning rate for more optimum performance.

In particular, the weights update in each of the three gates, cell candidate, and fully connected layer depends on the learning rate value, so using a customized learning rate for each part would result in a more optimum update for the weights (Brownlee, 2020). This chapter addresses this issue by proposing a new approach that improves the performance of the LSTM network by optimizing the parameters related to the gates, cell state, and fully connected layer. The novel hybrid nature inspired algorithm adopts the BA to improve the performance of three gates and cell state, specifically by optimizing the learning rate factor so that each part has its learning rate determined based on the global learning rate. Having a more optimum learning rate means more optimum updates for the network weight (Brownlee, 2020).

As the bidirectional LSTM layer is used as will be explained later in section 6.1.2, which trains the input as is and on the reverse copy of the input (Brownlee, 2021), so four parameters are related for the forward side and the other four parameters for the backwards and one parameter related to fully connected layer. The following figure 6.1 illustrates the general framework for the proposed BA-CNN-LSTM algorithm, followed by subsections explaining each part in detail.


Figure 6.1: The General Framework for the Proposed BA-CNN-LSTM Algorithm

### 6.1.1 Convolutional Neural Network Architecture

The features in the artificial porosity images are extracted using CNN which uses filters in the convolutional layer to activate some features in the images. The architecture of CNN consists of 19 layers starting with five convolutional layers each accompanied by a rectified linear unit layer and batch normalization layer with four average pooling layers in between.

The filter in the convolutional layers is a matrix that contains weights, this matrix is slid along the input matrix that will be described in the next section and performs a special dot product which results in a feature map matrix (Hui, 2017). Each convolutional layer is accompanied by a rectified linear unit layer that maps the negative values to zero and keeps the positive values for faster effective training (MathWorks-1). Also, each convolutional layer is followed by a batch normalization layer to minimize the overfitting risk (Yamashita et al., 2018). The pooling layers are used between the convolutional layers to reduce the output dimensions with keeping the features of interest in the images (McDermott, 2021), this reduction contributes to minimizing the computational cost.

The normal filter size is $3 \times 3$ or $5 \times 5$ as advised in (MathWorks-1), after trying both sizes, the $5 \times 5$ size is selected in all five convolutional layers, and the numbers of filters are $8,16,32,64$ and 128 so each layer has twice the filter number of the previous layer as advised in (Brownlee, 2020). The edges of the images are detected using padding with a stride value of one, so the pixel shift is one cell. The pooling size is 4 x 4 with a stride value of 4 to minimize the computational cost since the image size is big ( $650 \times 630 \times 3$ ). There are two types of pooling, average pooling calculates the average pixel brightness value of the four numbers in the pooling matrix. It is compatible with the lighter background, so it is used in the architecture rather than the max pooling type that selects the maximum pixel value taking the most activated feature making it better with the dark background (Ouf, 2017).

The most popular training algorithm is SGDM (Yamashita et al., 2018), so it is used to train on the artificial porosity images with 20 epochs (MathWorks-6), a section depth value of 1 to control the depth of the network, an initial learning rate of 0.0101 that allows for feature learning, a momentum of 0.9568 for parameters updating, and a regularization value of 0.0097 to mitigate the overfitting risk (MathWorks-3). They are the same set of parameters found using BA in the hybrid BA-RCNN algorithm developed in chapter 5.

The hybrid BA-RCNN algorithm was used to predict the percent of porosity in each layer of the SLM part. Since the layers are sequential, LSTM is added after the CNN to deal with sequential data for better prediction accuracy as will be described in the following subsection.

### 6.1.2 Long Short-Term Memory Architecture

The features extracted from the artificial porosity images using CNN feed the LSTM network that persists the information for a long period so that it can remember long-term dependencies (the-learning-machine). The mathematical equations for the three gates are shown in the following:

## - Forget Gate

The first step in the LSTM cell is to decide if the information coming from the previous time scale is relevant to be remembered or irrelevant to be forgotten, it is based on the following forget gate equation (www.analyticsvidhya.com):
$\mathrm{f}_{\mathrm{t}}=\sigma \times\left(\mathrm{X}_{\mathrm{t}} \times \mathrm{U}_{\mathrm{f}}+\mathrm{H}_{\mathrm{t}-1} \times \mathrm{W}_{\mathrm{f}}\right)$
(Equation 6.1)
Where:
$\mathrm{X}_{\mathrm{t}}$ is the current time cycle input
$\mathrm{U}_{\mathrm{f}}$ is the input weight matrix
$\mathrm{H}_{\mathrm{t}-1}$ is the previous time cycle hidden state
$\mathrm{W}_{\mathrm{f}}$ is the hidden state weight matrix
Then, the sigmoid function shown in the following is applied resulting in a $f_{t}$ value between 0 and 1 (MathWorks-2).
$\sigma(x)=\left(1+e^{-x}\right)^{-1}$
(Equation 6.2)
The ft is multiplied by the cell state of the previous time cycle:
$\mathrm{C}_{\mathrm{t}-1} \times \mathrm{f}_{\mathrm{t}}=0$ (Forget everything)
(Equation 6.3)
$\mathrm{C}_{\mathrm{t}-1} \times \mathrm{f}_{\mathrm{t}}=\mathrm{C}_{\mathrm{t}-1}$ (Forget nothing)
(Equation 6.4)

- Input Gate

This gate is used to quantify the importance of the new information, it is based on the following input gate equation (www.analyticsvidhya.com):
$\mathrm{i}_{\mathrm{t}}=\sigma \times\left(\mathrm{X}_{\mathrm{t}} \times \mathrm{U}_{\mathrm{i}}+\mathrm{H}_{\mathrm{t}-1} \times \mathrm{W}_{\mathrm{i}}\right)$
(Equation 6.5)
Where:
$\mathrm{X}_{\mathrm{t}}$ is the current time cycle input
$\mathrm{U}_{\mathrm{f}}$ is the input weight matrix
$\mathrm{H}_{\mathrm{t}-1}$ is the previous time cycle hidden state
$\mathrm{W}_{\mathrm{f}}$ is the hidden state weight matrix
Similarly, the sigmoid function is applied resulting in $i_{t}$ value between 0 and 1. Passing the information to the cell state is based on a function of the hidden state of the previous time cycle:
$\mathrm{N}_{\mathrm{t}}=\tanh \left(\mathrm{X}_{\mathrm{t}} \times \mathrm{U}_{\mathrm{c}}+\mathrm{H}_{\mathrm{t}-1} \times \mathrm{W}_{\mathrm{c}}\right)$ (new information)
(Equation 6.6)
Using the tanh function results in an $\mathrm{N}_{\mathrm{t}}$ value between -1 and 1. If it is positive, it will be added to the cell state, and if it is negative, the information will be subtracted from the cell state as shown in the following equation:
$\mathrm{C}_{\mathrm{t}}=\mathrm{f}_{\mathrm{t}} \times \mathrm{C}_{\mathrm{t}-1}+\mathrm{i}_{\mathrm{t}} \times \mathrm{N}_{\mathrm{t}}$ (updating cell state)
(Equation 6.7)

- Output Gate

In this gate, the cell transfers the updated information from the previous time cycle to the next time cycle, it is based on the following output gate equation (www.analyticsvidhya.com):
$\mathrm{O}_{\mathrm{t}}=\sigma \times\left(\mathrm{X}_{\mathrm{t}} \times \mathrm{U}_{\mathrm{o}}+\mathrm{H}_{\mathrm{t}-1} \times \mathrm{W}_{\mathrm{o}}\right)$
(Equation 6.8)
Also, the $\mathrm{O}_{\mathrm{t}}$ value is between 0 and 1 because of applying the sigmoid function. The current hidden state is a function of long-term memory and the output and it is calculated based on the following equation:

$$
\begin{equation*}
\mathrm{H}_{\mathrm{t}}=\mathrm{O}_{\mathrm{t}} \times \tanh \left(\mathrm{C}_{\mathrm{t}}\right) \tag{Equation6.9}
\end{equation*}
$$

The output of the current time cycle is found using the SoftMax function as shown in the following equation:

$$
\begin{equation*}
\text { Output }=\operatorname{SoftMax}\left(\mathrm{H}_{\mathrm{t}}\right) \tag{Equation6.10}
\end{equation*}
$$

The output with the maximum score is the predicted value. (Thakur, 2018) presented a more intuitive architecture of LSTM as shown in figure 6.2:


Figure 6.2: Intuitive Diagram of LSTM (Thakur, 2018)
The created artificial porosity images in chapter 4 consist of 303 D cubes, each one was sliced into 100 2D sequential slices resulting in 3000 slices. So, there are 30 sequences with 100 layers in each sequence, 18 sequences are used for training and 6 sequences for each of the validation and testing sets.

The design of LSTM architecture consists of 8 layers, it starts with a sequence input layer that inputs the sequential data to the network, followed by a sequence folding layer that converts the image sequences to a batch of images so that the convolution operation described in the previous section can be performed on the layers independently (MathWorks-2). After folding, the convolution is applied to input data which is a matrix that contains the pixel value with a range between $0-255$ where 0 represents the black regions and 255 is for the white regions, the size of this matrix depends on the image size which is $650 \times 630$ (Hui, 2017). After performing the convolution operations to extract the image features, the sequence unfolding layer is added to restore the sequence structure of the input data followed by a flatten layer that make collapsing for the input spatial dimensions to the channel dimension (MathWorks-2).

Then, the bidirectional LSTM layer is added which takes the input from both directions (forward and backward). The output of both the forward and backward at each stage is transferred to an activation layer (neural network), the output from this activation layer considers the relationship between the past and future layers (Mungalpara, 2021) which increases the prediction accuracy of the percent of porosity in each layer. The following figure 6.3 illustrates the way of working for the bidirectional LSTM layer:


Figure 6.3: The Way of Working for the Bidirectional LSTM Layer (Newman, 2020)

The number of hidden units is 200 , having more hidden units increase the computation cost without an improvement in the prediction accuracy, and also it increases the probability of overfitting (www.machinelearningmastery.com). The bidirectional LSTM layer is followed by a dropout layer which minimizes the risk of overfitting (www.machinelearningmastery.com), a fully connected layer is added with one predictor (percent of porosity) and the last layer is the regression layer.

### 6.1.3 The Novel Hybrid BA-CNN-LSTM Architecture Algorithm

BA is a swarm-based optimization technique that performs global and local searches to find the optimal solution. The following are the values of BA parameters which are assigned based on the capability of the computer and using the equations stated in (MathWorks-4).

- Maximum number of iterations $=1$
- $\quad$ Number of scout bees $(\mathrm{n})=4$
- $\quad$ Number of selected bees $(\mathrm{m})=0.5 \times \mathrm{n}=0.5 \times 4=2$
- $\quad$ Number of elite bees (e) $=1$
- Number of recruited bees for elite (e) sites (nep) $=2 \times \mathrm{m}=2 \times 2=4$
- Number of recruited bees for other best (m-e) sites (nsp) $=0.5 \times n=0.5 \times 4=2$
- Neighbourhood size for each selected patch (local search) (ngh) $=0.1 \times($ Var $\max -\operatorname{Var} \min )=0.1 \times(1.1-0.9)=0.1 \times 0.2=0.02$

The BA process is used to find the optimal values for nine LSTM parameters in order to improve the performance of three gates, cell state and fully connected layer, particularly by optimizing the learning rate factor so that each part has its own learning rate determined based on the global learning rate. Having a more optimum learning rate means a more optimum update for the network weights described in the previous section (Brownlee, 2020). As the bidirectional LSTM layer is used, which trains the input as is and on the reverse copy of the input (Brownlee, 2021), so four parameters are related for the forward side and the other four parameters for the backwards and one parameter is related to the fully connected layer. So, the nine optimization variables are:

- Learning rate factor for input gate (Forward)
- Learning rate factor for forget gate (Forward)
- Learning rate factor for cell candidate (Forward)
- Learning rate factor for output gate (Forward)
- Learning rate factor for input gate (Backward)
- Learning rate factor for forget gate (Backward)
- Learning rate factor for cell candidate (Backward)
- Learning rate factor for output gate (Backward)
- Learning rate factor for fully connected layer

The optimal adjustment factors obtained by BA (ranging between 0.9 and 1.1) are multiplied by the global learning rate of 0.0101 resulting in a more optimum learning rate for each part stated above so that the network weights described in the previous section are updated with more optimum values in order to improve the performance of LSTM.

The steps of MATLAB code for the proposed hybrid BA-CNN-LSTM algorithm are presented in the following figure 6.4:


Figure 6.4: The Steps of MATLAB Code for the Proposed Hybrid BA-CNN-LSTM Algorithm

In addition, the following figure 6.5 shows a flow chart for the workflow diagram for the proposed hybrid BA-CNN-LSTM algorithm.


Figure 6.5: Workflow Diagram for the Proposed Hybrid BA-CNN-LSTM Algorithm

### 6.2 Results and Discussion

This section presents the results of applying the LSTM network on three sets of data, the first one is the artificial porosity images to predict the percent of porosity in the SLM part as mentioned previously. Also, it is applied in the signal processing context to classify Electrocardiogram (ECG) benchmark image data (MathWorks-7). In addition, the turbofan
engine degradation simulation dataset (MathWorks-11) is used to predict the remaining useful life (RUL) of engines using LSTM.

MATLAB platform is used to design the LSTM network, CNN and BA and apply the hybrid algorithms to three benchmark datasets. The system configuration consists of a single GPU with a memory of 256 GB to be able to handle the 3000 artificial porosity images of size ( $650 \times 630 \times 3$ ). As the DL algorithms require high computations, limited BA evaluations are applied to optimize LSTM parameters. The datasets are shuffled at every epoch and the training, validation and testing sets are selected randomly after each shuffle in order to minimize the data biases and improve the validity of the experiments. The 3000 slices are divided into 1800 images used for training, 600 images for validation, and the same for the testing set. The number of samples for training set in the ECG images is 81 images, while the validation set consists of 41 observations, and the testing set has 40 samples. For the turbofan engine degradation simulation dataset, 100 samples are used for training, validation, and testing sets.

### 6.2.1 Results of Applying BA-CNN-LSTM on Artificial Porosity Images

The novel hybrid BA-CNN-LSTM algorithm is developed using the MATLAB platform, it is applied to the created artificial porosity images described in chapter 4 to predict the percent of porosity in sequential layers of SLM parts. The 30 sequences are divided into 18 sequences for training and 6 sequences for each of the validation and testing sets, since each sequence has 100 layers, so 1800 slices are used for training and 600 slices for each of the validation and testing sets. The following table 6.1 shows the values of LSTM parameters for the four evaluations of BA:

Table 6.1: The Values of LSTM Parameters in the Four Evaluations of BA (Artificial Porosity Images)

| LSTM Parameter | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ |
| :---: | :---: | :---: | :---: | :---: |
| Learning rate factor for input gate <br> (Forward) | 1.0618 | 0.9737 | 1.0629 | 1.0810 |
| Learning rate factor for forget gate <br> (Forward) | 0.9472 | 0.9706 | 1.0812 | 1.0177 |
| Learning rate factor for cell candidate <br> (Forward) | 0.9151 | 1.0451 | 0.9254 | 0.9291 |
| Learning rate factor for output gate <br> (Forward) | 1.0349 | 1.0273 | 1.0827 | 1.0300 |
| Learning rate factor for input gate <br> (Backward) | 1.0684 | 1.0604 | 1.0265 | 0.9429 |
| Learning rate factor for forget gate <br> (Backward) | 1.0258 | 1.0236 | 0.9195 | 1.0386 |
| Learning rate factor for cell candidate <br> (Backward) | 0.9749 | 0.9621 | 0.9557 | 1.0006 |
| Learning rate factor for output gate |  |  |  |  |
| (Backward) |  |  |  |  |

As can be seen in table 6.1, the first evaluation yielded the minimum prediction error on the validation set with a value of 0.0115 , so the global learning rate of 0.0101 is adjusted in the forward side of the input gate by multiplying it by 1.0618 resulting in a more optimum learning rate value of 0.0107 . Similarly, the learning rate in the forward side of forget gate is improved to 0.0095 using an adjustment factor of 0.9472 . The new learning rate value for the forward cell candidate is 0.0092 after multiplying the global learning rate by 0.9151 . The adjustment factor for the forward output gate is 1.0348 which results in a learning rate value of 0.0104 . The new values for four backward parameters are $0.0108,0.0103,0.0098$, and 0.0103 for input gate, forget gate, cell candidate and output gate respectively, they are
adjusted using factors of $1.0684,1.0258,0.9749$, and 1.0253. Finally, the performance of the fully connected layer is improved as well by specifying a customized learning rate of 0.0097 after multiplying the global learning rate by 0.9623 . The following table 6.2 summarizes the new learning rate values for LSTM parameters:

Table 6.2: The New Learning Rate Values of LSTM Parameters (Artificial Porosity Images)

| LSTM Parameter | Adjusted Learning Rate Value |
| :---: | :---: |
| Input gate (Forward) | 0.0107 |
| Forget gate (Forward) | 0.0095 |
| Cell candidate (Forward) | 0.0092 |
| Output gate (Forward) | 0.0104 |
| Input gate (Backward) | 0.0108 |
| Forget gate (Backward) | 0.0103 |
| Cell candidate (Backward) | 0.0098 |
| Output gate (Backward) | 0.0103 |
| Fully connected layer | 0.0097 |

The following figure 6.6 shows the training progress for the proposed BA-CNN-LSTM algorithm using the new learning rate values stated above. The blue line represents the training progress and the black line for the validation set.


Figure 6.6: Training Progress for the Proposed Hybrid BA-CNN-LSTM Algorithm (Artificial Porosity Images)

As can be seen in figure 6.6, the training starts with RMSE of 0.2 and decreased significantly in the first 200 iterations and then the chart experienced a steady state around RMSE value of 0.02. In the validation set, the chart starts with RMSE value of 0.05 and it
is alternating in the first 150 iterations reaching to RMSE value of 0.0152 at the end of the chart.

The following table 6.3 shows the average porosity error (the difference between the actual and predicted percent of porosity) in training, validation and testing sets. The novel hybrid BA-CNN-LSTM algorithm is compared with an existing algorithm that uses Bayesian Optimization (BO) to optimize the same LSTM parameters (BO-CNN-LSTM) (MathWorks-12), also it is compared with the CNN-LSTM algorithm without BA and with the BA-RCNN algorithm developed in chapter 5 using the same CNN structure.

Table 6.3: The Average Error for Percent of Porosity (Artificial Porosity Images)

|  | BA-RCNN | CNN-LSTM | BO-CNN-LSTM | BA-CNN-LSTM |
| :---: | :---: | :---: | :---: | :---: |
| Average Error for <br> the Percent of <br> Porosity in the <br> Training Data | 0.0230 | 0.0157 | 0.0166 | 0.0159 |
| Average Error for <br> the Percent of <br> Porosity in the <br> Validation Data | 0.0214 | 0.0121 | 0.0128 | 0.0115 |
| Average Error for <br> the Percent of <br> Porosity in the <br> Testing Data | 0.0234 | 0.0131 | 0.0133 | 0.0122 |

Adding the LSTM network to CNN reduced the prediction error in all training, validation and testing sets. The hybrid BO-CNN-LSTM did not perform better than the original CNN-LSTM, so BO is not recommended to be used in regression problems as it performs poorly with a high dimensional objective function of more than 20 dimensions (www.stackexchange.com). The CNN-LSTM algorithm is further developed by adding BA to optimize the LSTM parameters which reduced the prediction error further in the validation and testing sets reaching the minimum error value of 0.0115 that comes in the validation set of the novel hybrid BA-CNN-LSTM algorithm.

The following table 6.4 presents the training, validation and testing prediction accuracy for all three algorithms within a 0.02 threshold (the acceptable difference between the actual and predicted percent of porosity), in addition to the time taken for computations in the best iteration.

Table 6.4: The Prediction Accuracy and Time for Percent of Porosity (Artificial Porosity Images)

|  | BA-RCNN | CNN-LSTM | BO-CNN-LSTM | BA-CNN-LSTM |
| :---: | :---: | :---: | :---: | :---: |
| Training Accuracy | $85.94 \%$ | $88.33 \%$ | $88.33 \%$ | $88.33 \%$ |
| Validation Accuracy | $87.33 \%$ | $95.67 \%$ | $95.33 \%$ | $96.33 \%$ |
| Testing Accuracy | $85.33 \%$ | $93.17 \%$ | $93.13 \%$ | $95.50 \%$ |
| Computational Time | 13 Min 40 Sec | 17 Min 57 Sec | 18 Min 22 Sec | 18 Min 7 Sec |

As can be seen from table 6.4, adding the LSTM network to CNN improved the prediction accuracy in all training, validation and testing sets. The testing accuracy is increased by $8 \%$ in the testing set to be $93.17 \%$. Optimizing LSTM parameters using BO did not improve the testing accuracy and it is almost the same with a value of $93.13 \%$. The CNN-LSTM algorithm is further developed by adding BA to optimize LSTM parameters which increased the prediction accuracy in the validation from $95.67 \%$ to $96.33 \%$ and in the testing sets from $93.17 \%$ to $95.50 \%$, so the improvement in the testing set is approximately $2 \%$ from the CNN-LSTM algorithm and $10 \%$ from BA-RCNN algorithm. The improvement is similar to the improvement discussed in section 2.4.1 as the hybrid ABC-CNN-LSTM algorithm used to detect the fake reviews of the product yielded an accuracy of $97 \%$ compared to $95 \%$ for CNN-LSTM algorithm (Jacob et al., 2022). Although the newly developed algorithm requires a longer time for training due to adding another deep learning algorithm (LSTM), but it is more accurate in predicting the sequential data.

So, the performance of the LSTM network in predicting the porosity in the sequential layers is improved after using BA as the hybrid BA-CNN-LSTM provided a more accurate prediction by improving it by $10 \%$ for the percent of porosity in sequential layers of artificial porosity images that mimic CT scan images of parts manufactured by the SLM process.

### 6.2.2 Results of Applying BA-CNN-LSTM on Electrocardiogram (ECG) Dataset

The novel hybrid BA-CNN-LSTM algorithm developed using the MATLAB platform can be designed to deal with classification problems as well. It is applied to Electrocardiogram (ECG) benchmark images described in (MathWorks-7) to classify human ECG time series signals into three classes cardiac arrhythmia (ARR), congestive heart failure (CHF), and normal sinus rhythms (NSR). The following figure 6.7 is an illustrative example of the three classes of ECG time series signals:


Figure 6.7: An Illustrative Example of the Three Classes of ECG Time Series Signals

There are 162 recordings with 96 observations from ARR, 30 recordings from CHF, and 36 from NSR. As the dataset is not large enough, the "SqueezeNet" pre-trained CNN network is used to extract the features in the images. The data are divided into 81 for training and 41 recordings for the validation set and 40 observations for the testing set. The following table 6.5 shows the values of LSTM parameters for the evaluations of BA:

Table 6.5: The Values of LSTM Parameters in the Evaluations of BA (ECG Dataset)

| LSTM Parameter | $\mathbf{1}$ | $\mathbf{2}$ |
| :---: | :---: | :---: |
| Learning rate factor for input gate <br> (Forward) | 0.9483 | 1.0422 |
| Learning rate factor for forget gate <br> (Forward) | 0.9808 | 1.0948 |
| Learning rate factor for cell candidate <br> (Forward) | 0.9193 | 0.9703 |
| Learning rate factor for output gate <br> (Forward) | 0.9264 | 1.0198 |
| Learning rate factor for input gate <br> (Backward) | 1.0884 | 1.0804 |
| Learning rate factor for cell candidate <br> (Backward) | 1.0150 | 0.9603 |
| Learning rate factor for output gate |  |  |
| (Backward) |  |  |

As can be seen in table 6.5, the second evaluation yielded the minimum classification error on the validation set with a value of 0.1220 , so the global learning rate of 0.00029 is adjusted in the forward side of the input gate by multiplying it by 1.0422 resulting in a more optimum learning rate value of 0.0003 . Similarly, the learning rate in the forward side of forget gate is improved to 0.00031 using an adjustment factor of 1.0984. The new learning rate value for the forward cell candidate is 0.00028 after multiplying the global learning rate by 0.9703 . The adjustment factor for the forward output gate is 1.0198 which results in a learning rate value of 0.00029 . The new values for four backward parameters are $0.00031,0.00031,0.00027$, and 0.0003 for input gate, forget gate, cell candidate and output
gate respectively, they are adjusted using factors of $1.0804,1.0722,0.9603$, and 1.0578 . Finally, the performance of the fully connected layer is improved as well by specifying a customized learning rate of 0.00027 after multiplying the global learning rate by 0.9413 . The following table 6.6 summarizes the new learning rate values for LSTM parameters:

Table 6.6: The New Learning Rate Values of LSTM Parameters (ECG Dataset)

| LSTM Parameter | Adjusted Learning Rate Value |
| :---: | :---: |
| Input gate (Forward) | 0.000302238 |
| Forget gate (Forward) | 0.000317492 |
| Cell candidate (Forward) | 0.000281387 |
| Output gate (Forward) | 0.000295742 |
| Input gate (Backward) | 0.000313316 |
| Forget gate (Backward) | 0.000310938 |
| Cell candidate (Backward) | 0.000278487 |
| Output gate (Backward) | 0.000306762 |
| Fully connected layer | 0.000272977 |

The following figure 6.8 shows the training progress for the proposed BA-CNN-LSTM algorithm using the new learning rate values stated above. The blue line represents the training progress and the black line for the validation set.


Figure 6.8: Training Progress for the Proposed Hybrid BA-CNN-LSTM Algorithm (ECG Dataset)

As can be seen in figure 6.8, the training starts with a low classification accuracy and increased steadily reaching a percentage value of $100 \%$. In the validation set, the chart has almost the same pattern reaching to validation accuracy of $87.80 \%$ at the end of the chart. The following three figures $6.9,6.10$, and 6.11 show the confusion matrix for the BA-CNNLSTM algorithm for all three sets. Recall and miss out in the blue and red columns while precision and false alarm in the blue and red rows respectively:


Figure 6.9: Confusion Matrix for the Training Set of the Proposed Hybrid BA-CNNLSTM Algorithm


Predicted Class
Figure 6.10: Confusion Matrix for the Validation Set of the Proposed Hybrid BA-CNN-LSTM Algorithm


Figure 6.11: Confusion Matrix for the Testing Set of the Proposed Hybrid BA-CNNLSTM Algorithm

The following table 6.7 presents the training, validation and testing classification accuracy for CNN, CNN-LSTM, BO-CNN-LSTM, and BA-CNN-LSTM algorithms, in addition to the time taken for computations in the best iteration.

Table 6.7: The Classification Accuracy and Time (ECG Dataset)

|  | CNN | CNN-LSTM | BO-CNN-LSTM | BA-CNN-LSTM |
| :---: | :---: | :---: | :---: | :---: |
| Training Accuracy | $100 \%$ | $100 \%$ | $100 \%$ | $100 \%$ |
| Validation Accuracy | $85.37 \%$ | $87.80 \%$ | $87.80 \%$ | $87.80 \%$ |
| Testing Accuracy | $92.50 \%$ | $92.50 \%$ | $95 \%$ | $95 \%$ |
| Computational Time | 3 Min 43 Sec | 3 Min 56 Sec | 4 Min 5 Sec | 3 Min 56 Sec |

As can be seen in table 6.7, adding the LSTM network to CNN improved the validation accuracy in the validation set by $2.5 \%$. Optimizing the LSTM parameters using BO or BA improved the testing accuracy from $92.50 \%$ to $95 \%$, so both algorithms perform well with classification problems. The computational time is almost similar in all algorithms.

### 6.2.3 Results of Applying BA-CNN-LSTM on Turbofan Engine Degradation Simulation

## Dataset

The dataset consists of time series data of 100 engines that starts normally at the beginning and then some faults appear during the series. The numerical data contain 26 columns starting with a unit number, time in cycles, three operational settings, and 21 sensor measurements (Saxena et al., 2008). The dataset contains 100 sequences as each engine represents a sequence that varies in length. There are 100 observations for each of the training, validation, and testing. As the dataset is numerical, CNN is not needed to extract the features, so the hybrid BA-LSTM algorithm is applied using the MATLAB platform to predict the remaining operational cycles before engine failure. As forward LSTM is used in developing the LSTM architecture (MathWorks-11), only four parameters related to this layer are optimized using BA which are the learning rate factor for input gate, forget gate, cell candidate, and fully connected layer In addition to fully connected layer. The following table 6.8 shows the values of LSTM parameters for the four evaluations of BA:

Table 6.8: The Values of LSTM Parameters in the Four Evaluations of BA (Engine Dataset)

| LSTM Parameter | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ |
| :---: | :---: | :---: | :---: | :---: |
| Learning rate factor for input gate | 1.0712 | 0.9557 | 1.0413 | 0.9048 |
| Learning rate factor for forget gate | 1.0167 | 0.9147 | 1.0244 | 0.9898 |
| Learning rate factor for cell candidate | 1.0747 | 1.0939 | 1.0716 | 1.0878 |
| Learning rate factor for output gate | 1.0526 | 0.9989 | 0.9378 | 1.0041 |
| Learning rate factor for fully connected layer | 0.9915 | 1.0902 | 0.9613 | 1.0519 |
| Prediction error on the validation set | 4.4272 | 5.2740 | 6.7158 | 11.6459 |

As can be seen in table 6.8, the first evaluation yielded the minimum prediction error on the validation set with a value of 4.4272 , so the global learning rate of 0.01 (MathWorks$11)$ is adjusted in the input gate by multiplying it by 1.0712 resulting in a more optimum learning rate value of 0.0107 . Similarly, the learning rate in the forget gate is improved to 0.0101 using an adjustment factor of 1.0167 . The new learning rate value for the cell candidate is 0.0107 after multiplying the global learning rate by 1.0747. The adjustment factor for the output gate is 1.0526 which results in a learning rate value of 0.0105 . Finally,
the performance of the fully connected layer is improved as well by specifying a customized learning rate of 0.0099 after multiplying the global learning rate by 0.9915 . The following table 6.9 summarizes the new learning rate values for LSTM parameters:

Table 6.9: The New Learning Rate Values of LSTM Parameters (Engine Dataset)

| LSTM Parameter | Adjusted Learning Rate Value |
| :---: | :---: |
| Input gate (Forward) | 0.0107 |
| Forget gate (Forward) | 0.0101 |
| Cell candidate (Forward) | 0.0107 |
| Output gate (Forward) | 0.0105 |
| Fully connected layer | 0.0099 |

The following figure 6.12 shows the training progress for the BA -LSTM algorithm using the new learning rate values stated above. The blue line represents the training progress and the black line for the validation set.


Figure 6.12: Training Progress for the Proposed Hybrid BA-LSTM Algorithm (Engine Dataset)

As can be seen in figure 6.12, the training starts with a root mean square error (RMSE) of almost 80 and decreased significantly in the first 20 iterations and then the chart experienced a steady state around RMSE value of 20 . In the validation set, the chart followed the same pattern reaching RMSE value of 15.846 at the end of the chart.

The following table 6.10 presents the training, validation and testing prediction accuracy for LSTM, BO-LSTM and BA-LSTM algorithms within 20 cycles threshold (the acceptable difference between the actual and predicted RUL), in addition to the time taken for computations in the best iteration.

Table 6.10: The Prediction Accuracy and Time (Engine Dataset)

|  | LSTM | BO-LSTM | BA-LSTM |
| :---: | :---: | :---: | :---: |
| Training Accuracy | $72 \%$ | $72 \%$ | $73 \%$ |
| Validation Accuracy | $74 \%$ | $74 \%$ | $76 \%$ |
| Testing Accuracy | $74 \%$ | $74 \%$ | $77 \%$ |
| Computational Time | 4 Min 10 Sec | 4 Min 10 Sec | 4 Min |

As can be seen in table 6.10, using BO to optimize LSTM parameters did not improve the performance of LSTM, so it confirms the conclusion that it is not recommended to use BO in regression problems as it performs poorly with a high dimensional objective function of more than 20 dimensions (www.stackexchange.com). Adding the BA to optimize LSTM parameters improved the prediction accuracy in all training, validation and testing sets. The testing accuracy is increased by $3 \%$ in the testing set to be $77 \%$ in BA-LSTM. The computational time is almost similar in both algorithms.

### 6.3 Summary

Improving the performance of DL algorithms is an ongoing challenge where LSTM which is one of the DL networks that deal with time series or sequential data can be of use. This chapter addressed designing better LSTM topology by optimizing its parameters using one of the most popular nature inspired algorithms that mimic the honey bees' behaviour which is the BA. Artificial porosity images were used for testing the algorithms. Since the input data are images, CNN was added in order to extract the features in the images and to feed them into LSTM to predict the percent of porosity in sequential layers of artificial porosity images that mimic real CT scan images of products manufactured by selective laser melting process. Applying Convolutional Neural Network Long Short-Term Memory (CNN-LSTM) yielded a porosity prediction accuracy of $93.17 \%$. Although using BO to optimize LSTM parameters did not improve the performance of the LSTM as BO performs poorly with a high dimensional objective function of more than 20 dimensions which is the
case in regression problems. Adding BA to optimize LSTM parameters improved its performance in predicting the porosity with an accuracy of $95.50 \%$ using hybrid Bees Convolutional Neural Network Long Short-Term Memory (BA-CNN-LSTM). Furthermore, the hybrid BA-CNN-LSTM algorithm can be designed to deal with classification problems as well. Applying it to Electrocardiogram (ECG) benchmark images improved the classification accuracy on the testing set from $92 \%$ to $95 \%$. In addition, the turbofan engine degradation simulation numerical dataset was used to predict the remaining useful life (RUL) of engines using LSTM. CNN is not needed in this case as there is no feature extraction for the images, adding the BA to optimize LSTM parameters improved the prediction accuracy by $3 \%$ in the testing set to be $77 \%$ in the hybrid BALSTM algorithm.

The outcome of this chapter is improving the performance of the LSTM network in predicting sequential data using BA. As the input data are images, CNN is added to extract the image features yielding a hybrid algorithm (BA-CNN-LSTM) that provides a $10 \%$ more accurate prediction of porosity percentage appearing in sequential layers of artificial porosity images that mimic CT scan images of parts manufactured by SLM process. The following table 6.11 compares the prediction accuracy of the algorithms developed in this chapter and the previous chapter:

Table 6.11: Comparison between All Algorithms Used for Porosity Prediction Accuracy (Final Version)

| Prediction Method | Porosity Prediction <br> Accuracy |
| :---: | :---: |
| Image Binarization | $68.60 \%$ |
| Original RCNN | $75.50 \%$ |
| Hybrid <br> BA-RCNN <br> Hybrid <br> CNN-LSTM <br> Hybrid <br> BA-CNN-LSTM | $85.33 \%$ |
|  | $93.17 \%$ |

The contribution of this chapter is:

- Improving the performance of LSTM network in predicting sequential data using BA. As the input data are images, CNN is added to extract the image features yielding a hybrid algorithm (BA-CNN-LSTM) that provides a $10 \%$ more accurate prediction of porosity percentage appearing in the sequential layers of artificial porosity images that mimic CT scan images of parts manufactured by SLM process.


## Chapter 7: Conclusion

### 7.1 Conclusion

Artificial Neural Network (ANN) has the ability to handle high dimensional real-time data and extracts implicit meaningful patterns that can be used to predict the future state of complex systems. The performance of ANNs depends on the significance of the features extracted from the training data used in training which is often a time consuming process leading to sub-optimal solutions. However, this problem could be overcome by Deep Learning (DL) which is a type of machine learning technique. DL has better learning capability as it has the advantage of automatic feature extraction by learning a large number of nonlinear filters before making decisions.

In this work, a review of DL has been conducted showing all its networks along with their advantages, limitations, and applications. The most popular DL network is the Convolutional Neural Network (CNN) which uses feature learning layers namely convolution, rectified linear unit, batch normalization, and pooling layers in addition to two classification layers one of which is the fully connected layer, and the other is a SoftMax layer used mainly for multiclass image classification. It has been found from the review that there are five open issues namely overfitting, exploding gradient problem, training the model using imbalanced classes, the convergence speed and designing better CNN topology, all of which need to be addressed in order to improve the performance of CNN models further. The most challenging aspect in training CNN is designing better topology where the traditional heuristic approach of using trial and error will result in a less accurate model depending on user experience. In case of applying optimization techniques such as nature inspired algorithms to optimize the parameters of CNN can improve the performance of the model. However, designing better CNN topology is still an open issue where no approach has been found yet that can give the best CNN topology. In addition, nature inspired algorithms have been included showing their contribution to increase the classification performance of CNN models.

This work addressed the most challenging issue stated above which is designing a better CNN topology by proposing a novel nature inspired hybrid algorithm that uses the Bees Algorithm (BA) which is known to mimic the behaviour of honeybees, to optimize four CNN parameters namely section depth, initial learning rate, momentum, and regularization. The proposed novel hybrid algorithm is called Bees Convolutional Neural Network (BA-

CNN ) algorithm. Furthermore, another nature inspired hybrid algorithm is proposed which combines the BA with Bayesian Optimization (BO) to increase the performance of CNN which is referred to as BA-BO-CNN. BO was used to optimize the same four parameters while BA was applied to optimize the weight learning rate factor to adjust the global learning rate obtained by BO algorithm in each convolutional layer and fully connected layer. Different data sets have been used to test the proposed novel algorithms.

1. Applying the hybrid BA-CNN algorithm to the 'Cifar10DataDir' benchmark image data did not improve the validation and testing accuracy compared to the existing CNN and BO-CNN, but it yielded better performance than EA-CNN model designed in (Badan, 2019) that achieved an accuracy of $62.37 \%$ on the same 'Cifar10DataDir' dataset as was shown in table 2.2 while BA-CNN achieved testing accuracy of $80.02 \%$. Applying it to the digits dataset yielded similar accuracy to the existing algorithms, but it produced the lowest computational time with 4 minutes and 14 seconds reduction compared to the BO-CNN, so it is the best algorithm in terms of cost-effectiveness. Applying it to concrete cracks images produced almost similar results to existing algorithms. Finally, applying it to the ECG images improved the testing accuracy from $90 \%$ for the BO-CNN to $92.50 \%$ for the novel hybrid BA-CNN algorithm with similar validation accuracy and computational time.
2. In addition, applying the other hybrid BA-BO-CNN algorithm to the 'Cifar10DataDir' benchmark image data produced validation accuracy better than the existing algorithms with a validation accuracy of $82.22 \%$ compared to $80.34 \%$ and $80.72 \%$ for the CNN and BO-CNN respectively, also it has a better testing accuracy of $80.74 \%$ compared to $80.52 \%$ and $80.69 \%$ for the CNN and BO-CNN respectively. Applying it to the digits dataset showed the same accuracy as the existing original CNN and BO-CNN, but with an improvement in the computational time by 3 minutes and 12 seconds reduction. Applying it to concrete cracks images produced almost similar results to the existing algorithms. Finally, applying it to human Electrocardiogram (ECG) signals improved the testing accuracy from $92.50 \%$ for the original CNN to $95 \%$ for
the novel hybrid BA-BO-CNN algorithm with similar validation accuracy and computational time.

Furthermore, this work presented Additive Manufacturing (AM) processes, applications, advantages, and gaps and open issues that needed to be addressed. It focused on powder bed fusion process showing the way of working, thermodynamical phenomena, parameters, open issues, three porosity types, and state of the art studies about adopting DL techniques to improve the performance of SLM process. It was found that there is a problem related to assessing accurately the porosity in SLM parts when using CT scans of sample parts. One main drawback with the conventional image binarization method has been when using gray value analysis to assess the porosity of SLM parts visible in CT scan slices. The difficulty is the subjectivity in selecting an appropriate grayscale threshold that would convert a single slice into binary images highlighting defective regions, as well as determining the true level of porosity. When an inappropriately low grayscale threshold was applied to the original slice image for binary image conversion, a certain amount of tiny undesired white spots were not filtered. However, if a higher grayscale threshold was adopted, the morphological features of the defective area, specifically near the boundary, were altered dramatically. These thresholds resulted in significantly different predictions of porosity levels.

In addition to classification, CNN has been used for regression problems to predict the percent of porosity in the finished SLM part without the need for subjective difficult threshold determination to convert the single slice to binary image. Applying Regression CNN (RCNN) on 3000 artificially created porosity images, similar to real CT-scan images by a similarity index of 0.9967 , improved porosity prediction accuracy from $68.60 \%$ for the image binarization method to $75.50 \%$ for RCNN, while integrating the BA with the last algorithm produced the best prediction accuracy with a value of $85.33 \%$ for Bees Regression Convolutional Neural Network (BA-RCNN).

In addition, the MATLAB platform was used to develop and apply Convolutional Neural Network Long Short-Term Memory (CNN-LSTM) yielding better porosity prediction accuracy of $93.17 \%$. Although using BO to optimize LSTM parameters did not improve the performance of LSTM as BO performs poorly with a high dimensional
objective function of more than 20 dimensions which is the case in regression problems. Adding BA to optimize LSTM parameters improved its performance in predicting the porosity with an accuracy of $95.50 \%$ using hybrid Bees Convolutional Neural Network Long Short-Term Memory (BA-CNN-LSTM).

Furthermore, the hybrid BA-CNN-LSTM algorithm was designed to deal with classification problems as well. Applying it to ECG benchmark images improved the classification accuracy on the testing set from $92 \%$ to $95 \%$. In addition, the turbofan engine degradation simulation dataset was used to predict the remaining useful life (RUL) of engines using LSTM, adding the BA to optimize LSTM parameters improved the prediction accuracy by $3 \%$ in the testing set to be $77 \%$ in the hybrid BA-LSTM algorithm.

### 7.2 Contributions to Knowledge

In summary, the following are the four contributions to knowledge:

1. Developing a novel hybrid Bees Convolutional Neural Network (BA-CNN) algorithm in order to improve the performance of CNN.
2. Developing a novel hybrid Bees Bayesian Convolutional Neural Network (BA-BO-CNN) algorithm in order to improve the performance of CNN.
3. Proposing and validating a new approach for predicting the percent of porosity in the finished SLM parts, using hybrid Bees Regression Convolutional Neural Network (BA-RCNN). It was demonstrated that a better accuracy than the existing image binarization method could be achieved (approximately $17 \%$ improvement with the data set used). In order to test the algorithm, as the training of the RCNN would require a large amount of experimental data, artificial porosity images mimicking real CT scan slices of the finished SLM part were created with a similarity index of 0.9976 with real images.
4. Improving the performance of LSTM network in predicting sequential data using BA. As the input data are images, CNN was added to extract the features in the images yielding a hybrid algorithm (BA-CNN-LSTM) that provided a more accurate prediction by improving it by $10 \%$ for the percent of porosity in the sequential layers of artificial porosity images that mimic CT scan images of parts manufactured by SLM process.

The first two contributions address the first research question Q1 mentioned in section 1.3 which is about the way of designing the optimum topology for CNN using the BA. The third contribution considers the second research question Q2 which deals with the way of analysing the porosity in the parts produced by the SLM process using novel CNN. Finally, the fourth contribution to the knowledge addresses the last research question Q3 for improving the performance of LSTM network in dealing with sequential data using the BA.

### 7.3 Study Limitations

The study can be done with more number of evaluations used in conducting BA to optimize DL parameters. In this study, they were limited to the computer capability in advanced research computing at Cardiff University. As DL networks require high computations, the number of evaluations was limited. In addition, the BA parameters of the number of iterations, scout bees, and elite sites were also assigned based on the computer capability in advanced research computing at Cardiff University.

This research study was not aimed to study the porosities in depth, so no experiments have been conducted, but the work proposed DL methods that enhanced such studies, particularly in predicting the percent of porosity in the finished SLM part. So, the created artificial porosity images in chapter 4 were used only to test the proposed DL algorithms developed in chapters 5 and 6.

The creation of artificial porosity images were only based on the laser power and scanning speed parameters as the dataset used to create the images presents only data about laser power and scanning speed. It is assumed that the pores are created in 3D cube with a volume of $1 \mathrm{~mm}^{3}$ with Z-position represents the average between the X-position and Yposition as Z coordinates are not available in the study used for porosity position analysis. Finally, the created artificial porosity images illustrated only one type of pore which is keyhole porosity considering one shape of this type which is the nearly spherical shape.

### 7.4 Future Work

The newly developed hybrid CNN algorithms can be developed further by optimizing the weight regularization factor in the convolutional layers and fully connected layer using the BA in order to improve the performance of the algorithms, particularly in preventing the network overfitting. For LSTM network, the BA can be used to optimize the adjustment factor for the regularization in the forget, input, and output gates in both forward and backward directions in addition to the cell candidate. Having more optimum regularization value, reduce the probability of overfitting. The proposed CNN and LSTM algorithms can be used in different contexts such as in the robotics field to build robots with obstacles sense in their path.

In addition, further work is required to tune the artificial porosity images creation approach to be mimicking a wider range of porosity types with more complex shapes closer to the cavities than the spheres and considering all the influential factors that affect the formation of keyhole and lack of fusion porosity, not only laser power and scanning speed. If the research fund can cover the cost of producing real porosity images enough for training DL techniques, then real experiments can be conducted in order to produce real porosity images giving more accurate prediction results, this is helpful in case of assessing the gas porosity as it is not linked directly with the laser power and scanning speed.

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## Appendix 1: MATLAB Codes

### 1.1 Convolutional Neural Network (CNN)

clc;
clear;
close all;

## \%Load and Explore Image Data

url = 'https://www.cs.toronto.edu/~kriz/cifar-10-matlab.tar.gz';
cifar10DataDir = tempdir;
filename = fullfile(cifar10DataDir,'cifar-10-matlab.tar.gz');
dataFolder $=$ fullfile(cifar10DataDir,'cifar-10-batches-mat');
if ~exist(dataFolder,'dir')
fprintf("Downloading CIFAR-10 dataset (175 MB)... ");
websave(filename,url);
untar(filename,cifar10DataDir);
fprintf("Done.\n")
end
oldpath = addpath(fullfile(matlabroot,'examples','nnet','main'));
[XTraining,YTraining,XTesting,YTesting] = loadCIFARData(cifar10DataDir); idx $=$ randperm(numel(YTesting),5000);

XValidation $=$ XTesting(:,:,:,idx);
XTesting(:,:,:,idx $)=[]$;
YValidation $=$ YTesting(idx);
YTesting(idx) $=[] ;$

```
%Specify Convolutional Neural Network Architecture
imageSize = [32 32 3];
numClasses = numel(unique(YTraining));
layers = [
    imageInputLayer(imageSize)
convBlock(3,11,3)
maxPooling2dLayer(3,'Stride',2,'Padding','same')
convBlock(3,22,3)
maxPooling2dLayer(3,'Stride',2,'Padding','same')
convBlock(3,44,3)
averagePooling2dLayer(8)
    fullyConnectedLayer(numClasses)
    softmaxLayer
    classificationLayer];
miniBatchSize =256;
validationFrequency = floor(numel(YTraining)/miniBatchSize);
options = trainingOptions('sgdm', ...
    'InitialLearnRate', 0.1, ...
    'Momentum', 0.9, ...
    'L2Regularization', 1e-10, ...
    'MaxEpochs',30, ...
    'MiniBatchSize',miniBatchSize, ...
```

'ValidationFrequency', validationFrequency, ...
'ValidationData',\{XValidation, YValidation\}, ...
'Shuffle','every-epoch', ...
'Plots','training-progress');

## \%Train Network using Training Data

net $=$ trainNetwork(XTraining,YTraining,layers,options);

## \%Classify Images and Compute Accuracy and Error

PredictedTraining = classify (net,XTraining);
TrainingAccuracy $=\operatorname{sum}($ PredictedTraining $==$ YTraining $) /$ numel(YTraining);
TrainingError $=1-$ TrainingAccuracy;

PredictedValidation $=$ classify $($ net,$X V$ alidation $)$;
ValidationAccuracy $=\operatorname{sum}($ PredictedValidation $==$ YValidation)/numel(YValidation);
ValidationError $=1$ - ValidationAccuracy;

PredictedTesting $=$ classify(net,XTesting);
TestingAccuracy $=\operatorname{sum}($ PredictedTesting $==$ YTesting $) /$ numel $($ YTesting $)$;
TestingError $=1-$ TestingAccuracy;

## \%Create Confusion Matrix

figure('Units','normalized','Position',[0.2 0.20 .4 0.4]);
TrainingCM = confusionchart(YTraining,PredictedTraining);
TrainingCM.Title = 'Confusion Matrix for Training Data';
TrainingCM.ColumnSummary = 'column-normalized';
TrainingCM.RowSummary = 'row-normalized';
figure('Units','normalized','Position',[0.2 0.2 0.4 0.4]);
ValidationCM = confusionchart(YValidation,PredictedValidation);
ValidationCM.Title = 'Confusion Matrix for Validation Data';

ValidationCM.ColumnSummary = 'column-normalized';
ValidationCM.RowSummary = 'row-normalized';
figure('Units','normalized','Position',[0.2 0.2 0.4 0.4]);
TestingCM = confusionchart(YTesting,PredictedTesting);
TestingCM.Title = 'Confusion Matrix for Testing Data';
TestingCM.ColumnSummary = 'column-normalized';
TestingCM.RowSummary = 'row-normalized';

```
function layers = convBlock(FilterSize,NumberofFilters,SectionDepth)
layers = [
    convolution2dLayer(FilterSize,NumberofFilters,'Padding','same')
    batchNormalizationLayer
    reluLayer];
layers = repmat(layers,SectionDepth,1);
end
```


### 1.2 Bayesian Convolutional Neural Network (BO-CNN)

clc;
clear;
close all;

## \%Load and Explore Image Data

url = 'https://www.cs.toronto.edu/~kriz/cifar-10-matlab.tar.gz';
cifar10DataDir = tempdir;
filename = fullfile(cifar10DataDir,'cifar-10-matlab.tar.gz');
dataFolder $=$ fullfile(cifar10DataDir,'cifar-10-batches-mat');
if $\sim \operatorname{exist}($ dataFolder, 'dir')
fprintf("Downloading CIFAR-10 dataset (175 MB)... ");
websave(filename,url);
untar(filename,cifar10DataDir);

```
    fprintf("Done.\n")
```

end
oldpath = addpath(fullfile(matlabroot,'examples','nnet','main'));
[XTraining, YTraining,XTesting, YTesting] = loadCIFARData(cifar10DataDir); $\mathrm{idx}=\operatorname{randperm}($ numel $(\mathrm{YTesting}), 5000)$;
XValidation $=$ XTesting(:,:,:,idx);
$X T e s t i n g(:,:, ;, i d x)=[] ;$
YValidation $=$ YTesting(idx);
YTesting(idx) $=[] ;$

## \%Define the Problem (Objective Function)

ObjFcn $=$
makeObjFcn(XTraining,YTraining,XValidation, YValidation,XTesting,YTesting);
optimVars $=[$
optimizableVariable('SectionDepth',[1 3],'Type','integer')
optimizableVariable('InitialLearnRate',[1e-2 1],'Transform','log')
optimizableVariable('Momentum',[0.8 0.98])
optimizableVariable('L2Regularization',[1e-10 1e-2],'Transform','log')];

## \%Optimize Variables

BayesObject $=$ bayesopt $($ ObjFcn,optimVars, $\ldots$
'MaxTime', $4 * 60 * 60, \ldots$
'IsObjectiveDeterministic',false, ...
'UseParallel',false);
function $\mathrm{ObjFcn}=$
makeObjFcn(XTraining,YTraining,XValidation, YValidation,XTesting,YTesting)

ObjFcn = @ ValidationErrorFunction;
function ValidationError $=$ ValidationErrorFunction(optimVars)

```
%Specify Convolutional Neural Network Architecture
imageSize = [32 32 3];
numClasses = numel(unique(YTraining));
layers = [
    imageInputLayer(imageSize)
convBlock(3,11,optimVars.SectionDepth)
maxPooling2dLayer(3,'Stride',2,'Padding','same')
convBlock(3,22,optimVars.SectionDepth)
maxPooling2dLayer(3,'Stride',2,'Padding','same')
convBlock(3,44,optimVars.SectionDepth)
averagePooling2dLayer(8)
    fullyConnectedLayer(numClasses)
    softmaxLayer
    classificationLayer];
miniBatchSize =256;
validationFrequency = floor(numel(YTraining)/miniBatchSize);
options = trainingOptions('sgdm', ...
    'InitialLearnRate',optimVars.InitialLearnRate, ...
    'Momentum',optimVars.Momentum, ...
    'L2Regularization',optimVars.L2Regularization, ...
    'MaxEpochs',30, ...
```

'MiniBatchSize',miniBatchSize, ...
'ValidationFrequency',validationFrequency, ...
'ValidationData', \{XValidation, YValidation \}, ...
'Shuffle','every-epoch', ...
'Plots','training-progress');

## \%Train Network using Training Data

net $=$ trainNetwork(XTraining,YTraining,layers,options);

## \%Classify Images and Compute Accuracy and Error

PredictedTraining $=$ classify $($ net,XTraining $)$;
TrainingAccuracy $=\operatorname{sum}($ PredictedTraining $==$ YTraining)/numel(YTraining);
TrainingError $=1-$ TrainingAccuracy;

PredictedValidation $=$ classify $($ net, XV alidation $)$;
ValidationAccuracy $=\operatorname{sum}($ PredictedValidation $==$ YValidation)/numel(YValidation);
ValidationError $=1$ - ValidationAccuracy;

PredictedTesting $=$ classify $($ net, XTesting$)$;
TestingAccuracy $=\operatorname{sum}($ PredictedTesting $==$ YTesting $) /$ numel(YTesting);
TestingError $=1-$ TestingAccuracy;

## \%Create Confusion Matrix

figure('Units','normalized','Position',[0.2 0.20 .4 0.4]);
TrainingCM = confusionchart(YTraining,PredictedTraining);
TrainingCM.Title = 'Confusion Matrix for Training Data';
TrainingCM.ColumnSummary = 'column-normalized';
TrainingCM.RowSummary = 'row-normalized';
figure('Units','normalized','Position',[0.2 0.20 .4 0.4]);
ValidationCM $=$ confusionchart(YValidation,PredictedValidation);

ValidationCM.Title = 'Confusion Matrix for Validation Data';
ValidationCM.ColumnSummary = 'column-normalized';
ValidationCM.RowSummary = 'row-normalized';
figure('Units','normalized','Position',[0.2 0.20 .4 0.4]);
TestingCM = confusionchart(YTesting,PredictedTesting);
TestingCM.Title = 'Confusion Matrix for Testing Data';
TestingCM.ColumnSummary = 'column-normalized';
TestingCM.RowSummary = 'row-normalized';
end
end
function layers $=\operatorname{convBlock}($ FilterSize,NumberofFilters,SectionDepth $)$
layers $=[$
convolution2dLayer(FilterSize,NumberofFilters,'Padding','same')
batchNormalizationLayer
reluLayer];
layers $=$ repmat(layers,SectionDepth,1);
end

### 1.3 Bees Convolutional Neural Network (BA-CNN)

clc;
clear;
close all;

## \%Load and Explore Image Data

url = 'https://www.cs.toronto.edu/~kriz/cifar-10-matlab.tar.gz';
cifar10DataDir = tempdir;
filename = fullfile(cifar10DataDir,'cifar-10-matlab.tar.gz');
dataFolder $=$ fullfile $($ cifar10DataDir,'cifar-10-batches-mat');
if $\sim \operatorname{exist}($ dataFolder,'dir')
fprintf("Downloading CIFAR-10 dataset (175 MB)... ");
websave(filename, url);
untar(filename,cifar10DataDir);
fprintf("Done.\n")
end
oldpath $=\operatorname{addpath}(f u l l f i l e(m a t l a b r o o t, ' e x a m p l e s ', ' n n e t ', ' m a i n ')) ; ~ ;$
[XTraining,YTraining,XTesting,YTesting] = loadCIFARData(cifar10DataDir);
idx $=\operatorname{randperm}($ numel $(Y T e s t i n g), 5000) ;$
XValidation = XTesting(:,:,:,idx);
XTesting(:,:,:,idx $)=[]$;
YValidation $=$ YTesting(idx);
YTesting $(\mathrm{idx})=[] ;$
\%Define the Problem (Objective Function)
ObjFcn $=$
makeObjFcn(XTraining,YTraining,XValidation,YValidation,XTesting,YTesting);
nVar=4; \% Number of Variables
VarSize=[1 nVar]; \%Size of Variables
VarMin=[11e-2 0.8 1e-10]; \%Lower Bound of Variables
VarMax=[ 310.98 1e-2 1 ; \% \%pper Bound of Variables
\%Define Bees Algorithm Parameters
MaxIt=1; \%Maximum Number of Iterations
nScoutBee=6; \%Scout Bees
nSelectedSite=round $(0.5 *$ nScoutBee); \%Selected Sites
nEliteSite=1; \%Selected Elite Sites
nSelectedSiteBee=round $(0.5 *$ nScoutBee $)$; \% Recruited Bees for Selected Sites

```
nEliteSiteBee=2*nSelectedSiteBee; %Recruited Bees for Elite Sites
r=0.1*(VarMax-VarMin); %Neighbourhood Radius
rdamp=0.95; %Neighbourhood Radius Damp Rate
%Initialize Empty Bee Structure
empty_bee.Position=[];
empty_bee.Error=[];
%Initialize Bees Array
bee=repmat(empty_bee,nScoutBee,1);
%Create New Solutions
for i=1:nScoutBee
    bee(i).Position=unifrnd(VarMin,VarMax,VarSize);
    bee(i).Error=ObjFcn(bee(i).Position);
end
%Sort the Solution
[~, SortOrder]=sort([bee.Error]);
bee=bee(SortOrder);
%Update Best Solution Ever Found
BestSol=bee(1);
% Create Array to Hold Best Error Values
LowestError=zeros(MaxIt,1);
```


# \%Create Bees Algorithm Main Loop 

for $\mathrm{it}=1$ :MaxIt

```
%Elite Sites
for i=1:nEliteSite
    bestnewbee.Error=inf;
    for j=1:nEliteSiteBee
        newbee.Position=PerformBeeDance(bee(i).Position,r);
        newbee.Error=ObjFcn(newbee.Position);
        if newbee.Error<bestnewbee.Error
            bestnewbee=newbee;
        end
    end
    if bestnewbee.Error<bee(i).Error
        bee(i)=bestnewbee;
    end
end
```

\%Selected Non-Elite Sites
for $\mathrm{i}=\mathrm{nEliteSite}+1$ :nSelectedSite
bestnewbee.Error=inf;
for $\mathrm{j}=1$ :nSelectedSiteBee
newbee.Position=PerformBeeDance(bee(i).Position,r);
newbee.Error=ObjFcn(newbee.Position);
if newbee.Error<bestnewbee.Error
bestnewbee=newbee;
end
end

```
        if bestnewbee.Error<bee(i).Error
            bee(i)=bestnewbee;
        end
    end
%Non-Selected Sites
    for i=nSelectedSite+1:nScoutBee
        bee(i).Position=unifrnd(VarMin,VarMax,VarSize);
        bee(i).Error=ObjFcn(bee(i).Position);
    end
    %Sort the Solution
    [~, SortOrder]=sort([bee.Error]);
    bee=bee(SortOrder);
    %Update Best Solution Ever Found
    BestSol=bee(1);
    %Store Best Error Ever Found
    LowestError(it)=BestSol.Error;
    OptimalSolution=BestSol.Position;
    %Display Iteration Information
    disp(['Iteration ' num2str(it) ': Lowest Error = ' num2str(LowestError(it))]);
    %Define Damp Neighborhood Radius
    r=r*rdamp;
end
```


## \%Display the Results

figure;

```
%Make a Plot for Lowest Error
semilogy(LowestError,'LineWidth',2);
xlabel('Iteration');
ylabel('Lowest Error');
function ObjFcn =
makeObjFcn(XTraining,YTraining,XValidation,YValidation,XTesting,YTesting)
ObjFcn=@ ValidationErrorFunction;
    function ValidationError = ValidationErrorFunction(OptimalSolution)
```

\%Specify Convolutional Neural Network Architecture
imageSize = [lllll 3232 3];
numClasses $=$ numel $($ unique $($ YTraining $)$ );
layers $=[$
imageInputLayer(imageSize)
$\operatorname{convBlock}(3,11$, round(OptimalSolution(1,1)))
maxPooling2dLayer(3,'Stride',2,'Padding','same')
$\operatorname{convBlock}(3,22, \operatorname{round}(O p t i m a l S o l u t i o n(1,1)))$
maxPooling2dLayer(3,'Stride',2,'Padding','same')
$\operatorname{convBlock}(3,44, \operatorname{round}(O p t i m a l S o l u t i o n(1,1)))$
averagePooling2dLayer(8)
fullyConnectedLayer(numClasses)
softmaxLayer
classificationLayer];
miniBatchSize $=256$;
validationFrequency $=$ floor(numel(YTraining)/miniBatchSize);
options $=$ trainingOptions('sgdm', $\ldots$
'InitialLearnRate', OptimalSolution(1,2), ...
'Momentum',OptimalSolution(1,3), ...
'L2Regularization',OptimalSolution(1,4), ...
'MaxEpochs',30, ...
'MiniBatchSize',miniBatchSize, ...
'ValidationFrequency',validationFrequency, ...
'ValidationData',\{XValidation,YValidation \}, ...
'Shuffle','every-epoch', ...
'Plots','training-progress');

## \%Train Network using Training Data

net $=$ trainNetwork(XTraining,YTraining,layers,options);

## \%Classify Images and Compute Accuracy and Error

PredictedTraining = classify(net,XTraining);
TrainingAccuracy $=\operatorname{sum}($ PredictedTraining $==$ YTraining $) /$ numel(YTraining);
TrainingError $=1-$ TrainingAccuracy;

PredictedValidation $=$ classify(net,XValidation);
ValidationAccuracy $=\operatorname{sum}($ PredictedValidation $==$ YValidation $) /$ numel $($ YValidation $)$;
ValidationError = 1 - ValidationAccuracy;

PredictedTesting = classify(net,XTesting);
TestingAccuracy $=\operatorname{sum}($ PredictedTesting $==$ YTesting $) /$ numel $($ YTesting $)$;
TestingError $=1-$ TestingAccuracy;

## \%Create Confusion Matrix

figure('Units','normalized','Position',[0.2 0.20 .4 0.4]);
TrainingCM = confusionchart(YTraining,PredictedTraining);
TrainingCM.Title = 'Confusion Matrix for Training Data';
TrainingCM.ColumnSummary = 'column-normalized';
TrainingCM.RowSummary = 'row-normalized';
figure('Units','normalized','Position',[0.2 0.20 .4 0.4]);
ValidationCM = confusionchart(YValidation,PredictedValidation);
ValidationCM.Title = 'Confusion Matrix for Validation Data';
ValidationCM.ColumnSummary = 'column-normalized';
ValidationCM.RowSummary = 'row-normalized';
figure('Units','normalized','Position',[0.2 0.2 0.4 0.4]);
TestingCM = confusionchart(YTesting,PredictedTesting);
TestingCM.Title = 'Confusion Matrix for Testing Data';
TestingCM.ColumnSummary = 'column-normalized';
TestingCM.RowSummary = 'row-normalized';
end
end
function layers $=$ convBlock(FilterSize,NumberofFilters,SectionDepth $)$
layers $=$ [
convolution2dLayer(FilterSize,NumberofFilters,'Padding','same')
batchNormalizationLayer
reluLayer];
layers $=$ repmat(layers,SectionDepth,1);
end

### 1.4 Bees Bayesian Convolutional Neural Network (BA-BO-CNN)

clc;
clear;
close all;

## \%Load and Explore Image Data

url = 'https://www.cs.toronto.edu/~kriz/cifar-10-matlab.tar.gz';
cifar10DataDir = tempdir;
filename = fullfile(cifar10DataDir,'cifar-10-matlab.tar.gz');
dataFolder $=$ fullfile(cifar10DataDir,'cifar-10-batches-mat');
if $\sim \operatorname{exist}($ dataFolder, 'dir')
fprintf("Downloading CIFAR-10 dataset (175 MB)... ");
websave(filename,url);
untar(filename,cifar10DataDir);
fprintf("Done.\n")
end
oldpath $=$ addpath(fullfile(matlabroot,'examples','nnet','main'));
[XTraining,YTraining,XTesting,YTesting] = loadCIFARData(cifar10DataDir);
$\mathrm{idx}=\operatorname{randperm}($ numel $(\mathrm{YTesting}), 5000)$;
XValidation $=$ XTesting(:,:,:,idx);
XTesting(:,:,:,idx) = [];
YValidation $=$ YTesting(idx);
YTesting (idx) $=[] ;$

## \%Define the Problem (Objective Function)

ObjFcn $=$ makeObjFcn (XTraining, YT Training, XV alidation, YV alidation,
XTesting,YTesting);

```
nVar=4; %Number of Weight Learning Rate Factors
VarSize=[1 nVar]; %Matrix Size for Factors
VarMin=0.9; %Lower Bound for Factors
VarMax=1.1; %Upper Bound for Factors
%Define Bees Algorithm Parameters
MaxIt=1; %Maximum Number of Iterations
nScoutBee=6; %Scout Bees
nSelectedSite=round(0.5*nScoutBee); %Selected Sites
nEliteSite=1; %Selected Elite Sites
nSelectedSiteBee=round(0.5*nScoutBee); % Recruited Bees for Selected Sites
nEliteSiteBee=2*nSelectedSiteBee; %Recruited Bees for Elite Sites
r=0.1*(VarMax-VarMin); %Neighbourhood Radius
rdamp=0.95; %Neighbourhood Radius Damp Rate
%Initialize Empty Bee Structure
empty_bee.Position=[];
empty_bee.Error=[];
%Initialize Bees Array
bee=repmat(empty_bee,nScoutBee,1);
%Create New Solutions
for i=1:nScoutBee
    bee(i).Position=unifrnd(VarMin,VarMax,VarSize);
    bee(i).Error=ObjFcn(bee(i).Position);
end
%Sort the Solution
[~, SortOrder]=sort([bee.Error]);
bee=bee(SortOrder);
```

```
%Update Best Solution Ever Found
BestSol=bee(1);
%Create Array to Hold Best Error Values
LowestError=zeros(MaxIt,1);
%Create Bees Algorithm Main Loop
for it=1:MaxIt
%Elite Sites
for i=1:nEliteSite
    bestnewbee.Error=inf;
    for j=1:nEliteSiteBee
        newbee.Position=PerformBeeDance(bee(i).Position,r);
        newbee.Error=ObjFcn(newbee.Position);
        if newbee.Error<bestnewbee.Error
            bestnewbee=newbee;
        end
    end
    if bestnewbee.Error<bee(i).Error
        bee(i)=bestnewbee;
    end
end
%Selected Non-Elite Sites
for i=nEliteSite+1:nSelectedSite
    bestnewbee.Error=inf;
```

```
    for j=1:nSelectedSiteBee
        newbee.Position=PerformBeeDance(bee(i).Position,r);
        newbee.Error=ObjFcn(newbee.Position);
        if newbee.Error<bestnewbee.Error
        bestnewbee=newbee;
        end
    end
    if bestnewbee.Error<bee(i).Error
    bee(i)=bestnewbee;
    end
end
%Non-Selected Sites
for i=nSelectedSite+1:nScoutBee
    bee(i).Position=unifrnd(VarMin,VarMax,VarSize);
    bee(i).Error=ObjFcn(bee(i).Position);
end
%Sort the Solution
[~, SortOrder]=sort([bee.Error]);
bee=bee(SortOrder);
%Update Best Solution Ever Found
BestSol=bee(1);
%Store Best Error Ever Found
LowestError(it)=BestSol.Error;
OptimalWeightLearningRateFactor=BestSol.Position;
```

```
    %Display Iteration Information
    disp(['Iteration ' num2str(it) ': Lowest Error = ' num2str(LowestError(it))]);
    %Define Damp Neighborhood Radius
    r=r*rdamp;
end
%Display the Results
figure;
%Make a Plot for Lowest Error
semilogy(LowestError,'LineWidth',2);
xlabel('Iteration');
ylabel('Lowest Error');
function ObjFcn = makeObjFcn(XTraining,YTraining,XValidation,YValidation,
XTesting,YTesting)
ObjFcn=@ ValidationErrorFunction;
    function ValidationError =
ValidationErrorFunction(OptimalWeightLearningRateFactor)
%Specify Convolutional Neural Network Architecture
imageSize = [32 32 3];
numClasses = numel(unique(YTraining));
layers = [
    imageInputLayer(imageSize)
        convBlock(3,11,3,OptimalWeightLearningRateFactor(1,1))
```

maxPooling2dLayer(3,'Stride',2,'Padding','same')
convBlock(3,22,3,OptimalWeightLearningRateFactor(1,2))
maxPooling2dLayer(3,'Stride',2,'Padding','same')
convBlock(3,44,3,OptimalWeightLearningRateFactor(1,3))
averagePooling2dLayer(8)
fullyConnectedLayer(numClasses,'WeightLearnRateFactor',OptimalWeightLearningRate Factor(1,4))
softmaxLayer
classificationLayer];
miniBatchSize $=256$;
validationFrequency $=$ floor(numel(YTraining) $/$ miniBatchSize $)$;
options $=$ trainingOptions('sgdm', $\ldots$
'InitialLearnRate',0.68934, ...
'Momentum',0.84074, ...
'L2Regularization',4.5857e-05, ...
'MaxEpochs',30, ...
'MiniBatchSize',miniBatchSize, ...
'ValidationFrequency', validationFrequency, ...
'ValidationData',\{XValidation,YValidation \}, ...
'Shuffle','every-epoch', ...
'Plots','training-progress');
\%Train Network using Training Data
net $=$ trainNetwork(XTraining,YTraining,layers,options);

## \%Classify Images and Compute Accuracy and Error

PredictedTraining = classify(net,XTraining);
TrainingAccuracy $=\operatorname{sum}($ PredictedTraining $==Y$ Training $) /$ numel(YTraining);
TrainingError $=1$ - TrainingAccuracy;

PredictedValidation $=$ classify $($ net,$X V$ alidation $) ;$
ValidationAccuracy $=\operatorname{sum}($ PredictedValidation $==$ YValidation)/numel(YValidation);
ValidationError $=1$ - ValidationAccuracy;

PredictedTesting = classify(net,XTesting);
TestingAccuracy $=\operatorname{sum}($ PredictedTesting $==$ YTesting $) /$ numel $($ YTesting $)$;
TestingError $=1-$ TestingAccuracy;

## \%Create Confusion Matrix

figure('Units','normalized','Position',[0.2 0.20 .4 0.4]);
TrainingCM = confusionchart(YTraining,PredictedTraining);
TrainingCM.Title = 'Confusion Matrix for Training Data';
TrainingCM.ColumnSummary = 'column-normalized';
TrainingCM.RowSummary = 'row-normalized';
figure('Units','normalized','Position',[0.2 0.2 0.4 0.4]);
ValidationCM = confusionchart(YValidation, PredictedValidation);
ValidationCM.Title = 'Confusion Matrix for Validation Data';
ValidationCM.ColumnSummary = 'column-normalized';
ValidationCM.RowSummary = 'row-normalized';
figure('Units','normalized','Position',[[0.2 0.2 0.4 0.4]);
TestingCM = confusionchart(YTesting,PredictedTesting);
TestingCM.Title = 'Confusion Matrix for Testing Data';
TestingCM.ColumnSummary = 'column-normalized';
TestingCM.RowSummary = 'row-normalized';
end
end
function layers $=\operatorname{convBlock}($ FilterSize,NumberofFilters,SectionDepth,
OptimalWeightLearningRateFactor)
layers $=$ [
convolution2dLayer(FilterSize,NumberofFilters,'Padding','same','WeightLearnRateFactor' ,OptimalWeightLearningRateFactor)
batchNormalizationLayer
reluLayer];
layers $=$ repmat(layers,SectionDepth,1);
end

### 1.5 Artificial Porosity Images Creation and Labelling

This code creates artificial porosity images with different shapes of the pores and different pixel values for the background and more importantly for pore itself, in addition it calculates the actual percent of porosity by identifying the ratio of the area of pores to the total area of the surface, (MathWorks-5) was the guide in writing this code.
clear ; clc ; clf;

## \%Define the Main Loop

for $\mathrm{x}=1: 30$

## \%Set the Number of Pores to Plot

$\mathrm{n}=[33 ; 33 ; 33 ; 31 ; 32 ; 32 ; 30 ; 30 ; 30 ; 28 ; 28 ; 29 ; 27 ; 27 ; 27 ; 25 ; 25 ; 26 ; 23 ; 24 ; 25 ; 22$;
22; 23; 20; 21; 19; 20; 17; 15];
Radius $=\operatorname{zeros}(\mathrm{n}(\mathrm{x}, 1), 1)$;
Position $=\operatorname{zeros}(\mathrm{n}(\mathrm{x}, 1), 3)$;

Random_X_Position $=$ randn $(\mathrm{n}(\mathrm{x}, 1), 1)$;
Random_X_Position(Random_X_Position<0) $=0$;
Normalized_X_Position $=$ Random_X_Position $/ \max (\operatorname{Random}$ _X_Position);

X_Position $=0.4854 *($ Normalized_X_Position $)+0.2742$;

```
Random_Y_Position = randn(n(x, 1),1);
Random_Y_Position(Random_Y_Position<0) = 0;
Normalized_Y_Position = Random_Y_Position / max(Random_Y_Position);
Y_Position = 0.4455*(Normalized_Y_Position)+ 0.2685;
Z_Position = (X_Position + Y_Position)/ 2;
r = [0.0369469; 0.0373645; 0.0377821; 0.0360138; 0.036849; 0.0376842; 0.0350807;
0.0363335; 0.0375863; 0.0341476; 0.035818; 0.0374884; 0.0332145; 0.0353025;
0.0373905; 0.0322814; 0.034787; 0.0372926; 0.0313483; 0.0342715; 0.0371947;
0.030301166; 0.033694166; 0.037087166; 0.0294821; 0.0332405; 0.028782275;
0.032853875; 0.0276159; 0.026506542];
```

for $\operatorname{idx}=1: n(x, 1)$
is_good = false;
\%Generate Positions and Radius
Radius $(\mathrm{idx})=((\mathrm{r}(\mathrm{x}, 1)+\operatorname{rand} *(-0.01: 0.01)) / 2)$;
Position(idx, :) = [X_Position(idx) Y_Position(idx) Z_Position(idx)];
\%Ensure we are inside the big surface
if $\left.\left(\left(\operatorname{sqrt}\left(\operatorname{sum}(\operatorname{Position(idx},:) .^{\wedge}\right)\right)+\operatorname{Radius}(\operatorname{idx})\right)<0.7\right)$
\&\& ( $(\mathrm{idx}==1) \| \ldots$
all(sqrt(sum((Position(1:(idx-1), :) - repmat(Position(idx, :), idx-1, 1)).^2, 2)) >
Radius(1:(idx-1))+Radius(idx))) \%All distances are bigger than the pores radius sum
end
end

```
%Generate Surface
clf;
hold on
daspect([1, 1, 1])
set(gca,'XColor','none','YColor','none','ZColor','none');
h(1) = axes('Position',[0}000101])
vert = [llll
    010;
    011;
    111;
    0 1;
    101;
    100;
    0 0];
fac = [llllll
    4356;
    6785;
    1287;
    6714;
    23 5 8];
```

patch('Faces',fac,'Vertices',vert,'FaceColor', uint8([150 150 150]),'EdgeColor', uint8([150
150 150]));
material metal;
alpha('color');
$\operatorname{axis}([0,1,0,1,0,1]) ;$
axis equal;
set(gca,'XColor','none','YColor','none','ZColor','none');
hold on;
\%Generate Pores
for $\operatorname{idx}=1: \operatorname{round}(n(x, 1) / 4)$
[x1,x2,x3] = sphere(24);
$\operatorname{surf}((\mathrm{x} 1 * \operatorname{Radius}(\mathrm{idx}))+0.1+\operatorname{Position}(\mathrm{idx}, 1),(\mathrm{x} 2 * \operatorname{Radius}(\mathrm{idx}))+0.1+\operatorname{Position}(\mathrm{idx}, 2)$, (x3*Radius(idx))+0.1+Position(idx,3),'FaceColor', uint8([110 110 110]),'EdgeColor', uint8([110 110 110]));
$\operatorname{surf}((\mathrm{x} 1 * \operatorname{Radius}(\mathrm{idx}))+0.1+\operatorname{Position}(\mathrm{idx}, 1),(\mathrm{x} 2 * \operatorname{Radius}(\mathrm{idx}))+0.1+\operatorname{Position}(\mathrm{idx}, 2)$,
(x3*1.5*Radius(idx))+0.1+Position(idx,3),'FaceColor', uint8([112 112 112]),'EdgeColor', uint8([112 112 112]));
material metal;
alphamap('rampdown');
$\operatorname{axis}([0,1,0,1,0,1]) ;$
axis equal;
set(gca,'XColor','none','YColor','none','ZColor','none');
end
for $\mathrm{idx}=\operatorname{round}((\mathrm{n}(\mathrm{x}, 1) / 4)+1): \operatorname{round}(\mathrm{n}(\mathrm{x}, 1) / 2)$
[x1,x2,x3] = sphere(24);
$\operatorname{surf}((\mathrm{x} 1 * \operatorname{Radius}(\mathrm{idx}))+0.3+\operatorname{Position}(\mathrm{idx}, 1),(\mathrm{x} 2 * \operatorname{Radius}(i d x))+0.3+\operatorname{Position}(\mathrm{idx}, 2)$, (x3*Radius(idx))+0.3+Position(idx,3),'FaceColor', uint8([114 114 114]),'EdgeColor', uint8([114 114 114]));
$\operatorname{surf}((\mathrm{x} 1 * \operatorname{Radius}(\mathrm{idx}))+0.3+\operatorname{Position}(\mathrm{idx}, 1),(\mathrm{x} 2 * 1.5 * \operatorname{Radius}(\mathrm{idx}))+0.3+\operatorname{Position}(\mathrm{idx}, 2)$, (x3*Radius(idx))+0.3+Position(idx,3),'FaceColor', uint8([116 116 116]),'EdgeColor', uint8([116 116 116]));
material metal;
alphamap('rampdown');
$\operatorname{axis}([0,1,0,1,0,1])$;
axis equal;
set(gca,'XColor','none','YColor','none','ZColor','none');
end
for $\mathrm{idx}=\operatorname{round}((\mathrm{n}(\mathrm{x}, 1) / 2)+1)$ :round $(3 * \mathrm{n}(\mathrm{x}, 1) / 4)$
[x1,x2,x3] = sphere(24);
$\operatorname{surf}((\mathrm{x} 1 * \operatorname{Radius}(\operatorname{idx}))+0.2+\operatorname{Position}(\mathrm{idx}, 1),(\mathrm{x} 2 * \operatorname{Radius}(\operatorname{idx}))+0.2+\operatorname{Position}(\mathrm{idx}, 2)$, (x3*Radius(idx))+0.2+Position(idx,3),'FaceColor', uint8([118 118 118]),'EdgeColor', uint8([118 118 118]));
$\left.\operatorname{surf}\left(\left(\mathrm{x} 1^{*} 1.5 * \operatorname{Radius}(\mathrm{idx})\right)+0.2+\operatorname{Position(idx}, 1\right),(\mathrm{x} 2 * \operatorname{Radius}(\mathrm{idx}))+0.2+\operatorname{Position(idx}, 2\right)$, (x3*Radius(idx))+0.2+Position(idx,3),'FaceColor', uint8([120 120 120]),'EdgeColor', uint8([120 120 120]));
material metal;
alphamap('rampdown');
$\operatorname{axis}([0,1,0,1,0,1])$;
axis equal;
set(gca,'XColor','none','YColor','none','ZColor','none');
end
for idx $=\operatorname{round}((3 * n(x, 1) / 4)+1): n(x, 1)$
[x1,x2,x3] = sphere(24);
$\operatorname{surf}((\mathrm{x} 1 * \operatorname{Radius}(\mathrm{idx}))+\operatorname{Position}(\mathrm{idx}, 1),(\mathrm{x} 2 * \operatorname{Radius}(\mathrm{idx}))+\operatorname{Position(idx}, 2)$,
(x3*Radius(idx))+Position(idx,3),'FaceColor', uint8([122 122 122]),'EdgeColor', uint8([122 122 122]));
$\operatorname{surf}((\mathrm{x} 1 * 1.5 * \operatorname{Radius}(\mathrm{idx}))+\operatorname{Position}(\mathrm{idx}, 1),(\mathrm{x} 2 * 0.5 * \operatorname{Radius}(\mathrm{idx}))+\operatorname{Position(idx}, 2)$, (x3*1.5*Radius(idx))+Position(idx,3),'FaceColor', uint8([124 124 124]),'EdgeColor', uint8([124 124 124]));
material metal;
alphamap('rampdown');

```
axis([0, 1, 0, 1, 0, 1]);
axis equal;
set(gca,'XColor','none','YColor','none','ZColor','none');
end
DiameterandPosition(1:n(x),(4*x)-3)=2 * Radius;
DiameterandPosition(1:n(x),((4*x)-2):4*x)= Position;
view(3)
saveas(gca, "LP-SS" + x + " 3D.jpg")
for i = 0.01:0.01:1
S = surface([0 1; 0 1], [0 0; 1 1], [i i; i i],'FaceColor', uint8([255 255 255]), 'EdgeColor',
uint8([255 255 255]));
axis([0, 1, 0, 1, 0, i+0.0099]);
set(gca,'XColor','mone','YColor','none','ZColor','none');
SN = 100*i;
view(2);
saveas(gca, "LP-SS" + x + "." + SN + " White Background.jpg")
Im = imread("LP-SS" + x + "." + SN + " White Background.jpg");
Imc = imcrop(Im,centerCropWindow2d(size(Im),[650 630]));
```

```
Actual_Percent_of_Pores(round(SN + ((x-1)*100)), 1) = ((numel(find(Imc(:,:,:) == 110))
+numel(find(Imc(:,:,:) == 112)) + numel(find(Imc(:,:,:) == 114)) + numel(find(Imc(:,:,:)
== 116)) + numel(find(Imc(:,:,:) == 118)) + numel(find(Imc(:,:,:) == 120)) +
numel(find(Imc(:,,,:) == 122)) + numel(find(Imc(:,:,:) == 124))) / (650*630*3)) * 100;
```

Background = imread("Background (" + SN + ").jpg");
Imcd $=$ Imc - 100;
alph $=0.125$;
sza $=\operatorname{size}(\operatorname{Imcd}) ;$
ArtificialImages = Background;
Croi $=$ ArtificialImages(end-sza(1)+1:end,end-sza(2)+1:end,:);
ArtificialImages $=$ Imcd*alph + Croi* $(1-\mathrm{alph})$;
imwrite(ArtificialImages, "Slice LP-SS" + x + "." + SN + ".jpg")
end
end
for Cube $=1: 30$
for Slice $=1: 100$
Ref = imread("Ref (" + Slice + ").jpg");
Art = imread("Slice LP-SS" + Cube + "." + Slice + ".jpg");
[ssimval(round(Slice $+\left(\left(\right.\right.$ Cube-1) $\left.\left.\left.{ }^{*} 100\right)\right), 1\right)$, ssimmap $]=\operatorname{ssim}($ Art,Ref $) ;$
AvgSSI = sum(ssimval,'all') / 3000;
imshow(ssimmap,[])

```
AbsDiffImage = imabsdiff(Art,Ref);
AvgDiffImage(round(Slice + ((Cube-1)*100)),1)= sum(AbsDiffImage,'all') /
(650*630*3);
AvgofAvgDiffImage = sum(AvgDiffImage,'all') / 3000;
```

$\mathrm{T}=$ adaptthresh(Art, 0.69);
$\mathrm{IB}=$ imbinarize $($ Art, T$)$;
imshowpair(Art, IB, 'montage')

Binary_Percent_of_Pores(round(Slice $+(($ Cube-1)*100) $), 1)=(($ numel(find(IB(:,:,:) $)==$ 0))) / $(650 * 630 * 3)) * 100$;
imwrite(IB, "LP-SS" + Cube + "." + Slice + " After Binarization.jpg")
end
end

### 1.6 Actual Percent of Porosity Dataset

The actual percent of porosity calculated in the previous code by identifying the ratio of the area of pores to the total area of the surface is shown in the following table appendix 1.1:

Table Appendix 1.1: Actual Percent of Porosity Dataset

| \# | Actual <br> Percent <br> of Pores (\%) | \# | Actual <br> Percent <br> of Pores (\%) | \# | Actual <br> Percent <br> of Pores (\%) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{1}$ | 0.0000 | $\mathbf{1 0 0 1}$ | 0.0000 | $\mathbf{2 0 0 1}$ | 0.0000 |
| $\mathbf{2}$ | 0.0000 | $\mathbf{1 0 0 2}$ | 0.0000 | $\mathbf{2 0 0 2}$ | 0.0000 |
| $\mathbf{3}$ | 0.0000 | $\mathbf{1 0 0 3}$ | 0.0000 | $\mathbf{2 0 0 3}$ | 0.0000 |
| $\mathbf{4}$ | 0.0000 | $\mathbf{1 0 0 4}$ | 0.0000 | $\mathbf{2 0 0 4}$ | 0.0000 |
| $\mathbf{5}$ | 0.0000 | $\mathbf{1 0 0 5}$ | 0.0000 | $\mathbf{2 0 0 5}$ | 0.0000 |
| $\mathbf{6}$ | 0.0000 | $\mathbf{1 0 0 6}$ | 0.0000 | $\mathbf{2 0 0 6}$ | 0.0000 |
| $\mathbf{7}$ | 0.0000 | $\mathbf{1 0 0 7}$ | 0.0000 | $\mathbf{2 0 0 7}$ | 0.0000 |
| $\mathbf{8}$ | 0.0000 | $\mathbf{1 0 0 8}$ | 0.0000 | $\mathbf{2 0 0 8}$ | 0.0000 |
| $\mathbf{9}$ | 0.0000 | $\mathbf{1 0 0 9}$ | 0.0000 | $\mathbf{2 0 0 9}$ | 0.0000 |
| $\mathbf{1 0}$ | 0.0000 | $\mathbf{1 0 1 0}$ | 0.0000 | $\mathbf{2 0 1 0}$ | 0.0000 |
| $\mathbf{1 1}$ | 0.0000 | $\mathbf{1 0 1 1}$ | 0.0000 | $\mathbf{2 0 1 1}$ | 0.0000 |
| $\mathbf{1 2}$ | 0.0000 | $\mathbf{1 0 1 2}$ | 0.0000 | $\mathbf{2 0 1 2}$ | 0.0000 |
| $\mathbf{1 3}$ | 0.0000 | $\mathbf{1 0 1 3}$ | 0.0000 | $\mathbf{2 0 1 3}$ | 0.0000 |
| $\mathbf{1 4}$ | 0.0000 | $\mathbf{1 0 1 4}$ | 0.0000 | $\mathbf{2 0 1 4}$ | 0.0000 |
| $\mathbf{1 5}$ | 0.0000 | $\mathbf{1 0 1 5}$ | 0.0000 | $\mathbf{2 0 1 5}$ | 0.0000 |


| $\mathbf{1 6}$ | 0.0000 | $\mathbf{1 0 1 6}$ | 0.0000 | $\mathbf{2 0 1 6}$ | 0.0000 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1 7}$ | 0.0000 | $\mathbf{1 0 1 7}$ | 0.0000 | $\mathbf{2 0 1 7}$ | 0.0000 |
| $\mathbf{1 8}$ | 0.0000 | $\mathbf{1 0 1 8}$ | 0.0000 | $\mathbf{2 0 1 8}$ | 0.0000 |
| $\mathbf{1 9}$ | 0.0000 | $\mathbf{1 0 1 9}$ | 0.0000 | $\mathbf{2 0 1 9}$ | 0.0000 |
| $\mathbf{2 0}$ | 0.0000 | $\mathbf{1 0 2 0}$ | 0.0000 | $\mathbf{2 0 2 0}$ | 0.0000 |
| $\mathbf{2 1}$ | 0.0000 | $\mathbf{1 0 2 1}$ | 0.0000 | $\mathbf{2 0 2 1}$ | 0.0000 |
| $\mathbf{2 2}$ | 0.0000 | $\mathbf{1 0 2 2}$ | 0.0000 | $\mathbf{2 0 2 2}$ | 0.0000 |
| $\mathbf{2 3}$ | 0.0000 | $\mathbf{1 0 2 3}$ | 0.0239 | $\mathbf{2 0 2 3}$ | 0.0000 |
| $\mathbf{2 4}$ | 0.0000 | $\mathbf{1 0 2 4}$ | 0.0110 | $\mathbf{2 0 2 4}$ | 0.0259 |
| $\mathbf{2 5}$ | 0.0000 | $\mathbf{1 0 2 5}$ | 0.0154 | $\mathbf{2 0 2 5}$ | 0.0266 |
| $\mathbf{2 6}$ | 0.0000 | $\mathbf{1 0 2 6}$ | 0.0000 | $\mathbf{2 0 2 6}$ | 0.0129 |
| $\mathbf{2 7}$ | 0.0000 | $\mathbf{1 0 2 7}$ | 0.0000 | $\mathbf{2 0 2 7}$ | 0.0840 |
| $\mathbf{2 8}$ | 0.0100 | $\mathbf{1 0 2 8}$ | 0.0281 | $\mathbf{2 0 2 8}$ | 0.0093 |
| $\mathbf{2 9}$ | 0.0132 | $\mathbf{1 0 2 9}$ | 0.0276 | $\mathbf{2 0 2 9}$ | 0.0000 |
| $\mathbf{3 0}$ | 0.0173 | $\mathbf{1 0 3 0}$ | 0.0200 | $\mathbf{2 0 3 0}$ | 0.0496 |
| $\mathbf{3 1}$ | 0.0000 | $\mathbf{1 0 3 1}$ | 0.0449 | $\mathbf{2 0 3 1}$ | 0.0125 |
| $\mathbf{3 2}$ | 0.0000 | $\mathbf{1 0 3 2}$ | 0.0147 | $\mathbf{2 0 3 2}$ | 0.0393 |
| $\mathbf{3 3}$ | 0.0000 | $\mathbf{1 0 3 3}$ | 0.0063 | $\mathbf{2 0 3 3}$ | 0.0105 |
| $\mathbf{3 4}$ | 0.0105 | $\mathbf{1 0 3 4}$ | 0.0256 | $\mathbf{2 0 3 4}$ | 0.0000 |
| $\mathbf{3 5}$ | 0.0327 | $\mathbf{1 0 3 5}$ | 0.0190 | $\mathbf{2 0 3 5}$ | 0.0000 |
| $\mathbf{3 6}$ | 0.0227 | $\mathbf{1 0 3 6}$ | 0.0440 | $\mathbf{2 0 3 6}$ | 0.0000 |
| $\mathbf{3 7}$ | 0.0227 | $\mathbf{1 0 3 7}$ | 0.0623 | $\mathbf{2 0 3 7}$ | 0.0000 |
| $\mathbf{3 8}$ | 0.0098 | $\mathbf{1 0 3 8}$ | 0.0889 | $\mathbf{2 0 3 8}$ | 0.0000 |
| $\mathbf{3 9}$ | 0.0295 | $\mathbf{1 0 3 9}$ | 0.0422 | $\mathbf{2 0 3 9}$ | 0.0000 |
| $\mathbf{4 0}$ | 0.0142 | $\mathbf{1 0 4 0}$ | 0.0808 | $\mathbf{2 0 4 0}$ | 0.0000 |
| $\mathbf{4 1}$ | 0.0264 | $\mathbf{1 0 4 1}$ | 0.0549 | $\mathbf{2 0 4 1}$ | 0.0000 |
| $\mathbf{4 2}$ | 0.0000 | $\mathbf{1 0 4 2}$ | 0.0449 | $\mathbf{2 0 4 2}$ | 0.0000 |
| $\mathbf{4 3}$ | 0.0332 | $\mathbf{1 0 4 3}$ | 0.0476 | $\mathbf{2 0 4 3}$ | 0.0000 |
| $\mathbf{4 4}$ | 0.0252 | $\mathbf{1 0 4 4}$ | 0.0256 | $\mathbf{2 0 4 4}$ | 0.0000 |
| $\mathbf{4 5}$ | 0.0322 | $\mathbf{1 0 4 5}$ | 0.0376 | $\mathbf{2 0 4 5}$ | 0.0000 |
| $\mathbf{4 6}$ | 0.0054 | $\mathbf{1 0 4 6}$ | 0.0232 | $\mathbf{2 0 4 6}$ | 0.0000 |
| $\mathbf{4 7}$ | 0.0000 | $\mathbf{1 0 4 7}$ | 0.0000 | $\mathbf{2 0 4 7}$ | 0.0000 |
| $\mathbf{4 8}$ | 0.0032 | $\mathbf{1 0 4 8}$ | 0.0005 | $\mathbf{2 0 4 8}$ | 0.0000 |
| $\mathbf{4 9}$ | 0.0144 | $\mathbf{1 0 4 9}$ | 0.0110 | $\mathbf{2 0 4 9}$ | 0.0000 |
| $\mathbf{5 0}$ | 0.0291 | $\mathbf{1 0 5 0}$ | 0.0151 | $\mathbf{2 0 5 0}$ | 0.0000 |
| $\mathbf{5 1}$ | 0.0613 | $\mathbf{1 0 5 1}$ | 0.0166 | $\mathbf{2 0 5 1}$ | 0.0000 |
| $\mathbf{5 2}$ | 0.0195 | $\mathbf{1 0 5 2}$ | 0.0374 | $\mathbf{2 0 5 2}$ | 0.0000 |
| $\mathbf{5 3}$ | 0.0286 | $\mathbf{1 0 5 3}$ | 0.0718 | $\mathbf{2 0 5 3}$ | 0.0000 |
| $\mathbf{5 4}$ | 0.0107 | $\mathbf{1 0 5 4}$ | 0.0476 | $\mathbf{2 0 5 4}$ | 0.0000 |
| $\mathbf{5 5}$ | 0.0154 | $\mathbf{1 0 5 5}$ | 0.0869 | $\mathbf{2 0 5 5}$ | 0.0000 |
|  |  |  |  |  |  |


| $\mathbf{5 6}$ | 0.0000 | $\mathbf{1 0 5 6}$ | 0.0381 | $\mathbf{2 0 5 6}$ | 0.0000 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{5 7}$ | 0.0000 | $\mathbf{1 0 5 7}$ | 0.0171 | $\mathbf{2 0 5 7}$ | 0.0000 |
| $\mathbf{5 8}$ | 0.0000 | $\mathbf{1 0 5 8}$ | 0.0525 | $\mathbf{2 0 5 8}$ | 0.0000 |
| $\mathbf{5 9}$ | 0.0198 | $\mathbf{1 0 5 9}$ | 0.0249 | $\mathbf{2 0 5 9}$ | 0.0000 |
| $\mathbf{6 0}$ | 0.0117 | $\mathbf{1 0 6 0}$ | 0.0122 | $\mathbf{2 0 6 0}$ | 0.0000 |
| $\mathbf{6 1}$ | 0.0176 | $\mathbf{1 0 6 1}$ | 0.0313 | $\mathbf{2 0 6 1}$ | 0.0000 |
| $\mathbf{6 2}$ | 0.0227 | $\mathbf{1 0 6 2}$ | 0.0261 | $\mathbf{2 0 6 2}$ | 0.0000 |
| $\mathbf{6 3}$ | 0.0085 | $\mathbf{1 0 6 3}$ | 0.0122 | $\mathbf{2 0 6 3}$ | 0.0000 |
| $\mathbf{6 4}$ | 0.0017 | $\mathbf{1 0 6 4}$ | 0.0071 | $\mathbf{2 0 6 4}$ | 0.0000 |
| $\mathbf{6 5}$ | 0.0000 | $\mathbf{1 0 6 5}$ | 0.0244 | $\mathbf{2 0 6 5}$ | 0.0000 |
| $\mathbf{6 6}$ | 0.0000 | $\mathbf{1 0 6 6}$ | 0.0049 | $\mathbf{2 0 6 6}$ | 0.0000 |
| $\mathbf{6 7}$ | 0.0000 | $\mathbf{1 0 6 7}$ | 0.0000 | $\mathbf{2 0 6 7}$ | 0.0024 |
| $\mathbf{6 8}$ | 0.0000 | $\mathbf{1 0 6 8}$ | 0.0032 | $\mathbf{2 0 6 8}$ | 0.0000 |
| $\mathbf{6 9}$ | 0.0000 | $\mathbf{1 0 6 9}$ | 0.0183 | $\mathbf{2 0 6 9}$ | 0.0000 |
| $\mathbf{7 0}$ | 0.0000 | $\mathbf{1 0 7 0}$ | 0.0190 | $\mathbf{2 0 7 0}$ | 0.0054 |
| $\mathbf{7 1}$ | 0.0000 | $\mathbf{1 0 7 1}$ | 0.0335 | $\mathbf{2 0 7 1}$ | 0.0271 |
| $\mathbf{7 2}$ | 0.0010 | $\mathbf{1 0 7 2}$ | 0.0205 | $\mathbf{2 0 7 2}$ | 0.0320 |
| $\mathbf{7 3}$ | 0.0103 | $\mathbf{1 0 7 3}$ | 0.0386 | $\mathbf{2 0 7 3}$ | 0.0505 |
| $\mathbf{7 4}$ | 0.0151 | $\mathbf{1 0 7 4}$ | 0.0215 | $\mathbf{2 0 7 4}$ | 0.0694 |
| $\mathbf{7 5}$ | 0.0161 | $\mathbf{1 0 7 5}$ | 0.0222 | $\mathbf{2 0 7 5}$ | 0.0252 |
| $\mathbf{7 6}$ | 0.0071 | $\mathbf{1 0 7 6}$ | 0.0107 | $\mathbf{2 0 7 6}$ | 0.0161 |
| $\mathbf{7 7}$ | 0.0000 | $\mathbf{1 0 7 7}$ | 0.0005 | $\mathbf{2 0 7 7}$ | 0.0054 |
| $\mathbf{7 8}$ | 0.0000 | $\mathbf{1 0 7 8}$ | 0.0000 | $\mathbf{2 0 7 8}$ | 0.0000 |
| $\mathbf{7 9}$ | 0.0000 | $\mathbf{1 0 7 9}$ | 0.0000 | $\mathbf{2 0 7 9}$ | 0.0000 |
| $\mathbf{8 0}$ | 0.0000 | $\mathbf{1 0 8 0}$ | 0.0000 | $\mathbf{2 0 8 0}$ | 0.0000 |
| $\mathbf{8 1}$ | 0.0000 | $\mathbf{1 0 8 1}$ | 0.0000 | $\mathbf{2 0 8 1}$ | 0.0000 |
| $\mathbf{8 2}$ | 0.0000 | $\mathbf{1 0 8 2}$ | 0.0000 | $\mathbf{2 0 8 2}$ | 0.0000 |
| $\mathbf{8 3}$ | 0.0000 | $\mathbf{1 0 8 3}$ | 0.0000 | $\mathbf{2 0 8 3}$ | 0.0000 |
| $\mathbf{8 4}$ | 0.0000 | $\mathbf{1 0 8 4}$ | 0.0000 | $\mathbf{2 0 8 4}$ | 0.0000 |
| $\mathbf{8 5}$ | 0.0000 | $\mathbf{1 0 8 5}$ | 0.0000 | $\mathbf{2 0 8 5}$ | 0.0000 |
| $\mathbf{8 6}$ | 0.0000 | $\mathbf{1 0 8 6}$ | 0.0000 | $\mathbf{2 0 8 6}$ | 0.0000 |
| $\mathbf{8 7}$ | 0.0000 | $\mathbf{1 0 8 7}$ | 0.0000 | $\mathbf{2 0 8 7}$ | 0.0000 |
| $\mathbf{8 8}$ | 0.0000 | $\mathbf{1 0 8 8}$ | 0.0000 | $\mathbf{2 0 8 8}$ | 0.0000 |
| $\mathbf{8 9}$ | 0.0000 | $\mathbf{1 0 8 9}$ | 0.0000 | $\mathbf{2 0 8 9}$ | 0.0000 |
| $\mathbf{9 0}$ | 0.0000 | $\mathbf{1 0 9 0}$ | 0.0000 | $\mathbf{2 0 9 0}$ | 0.0000 |
| $\mathbf{9 1}$ | 0.0000 | $\mathbf{1 0 9 1}$ | 0.0000 | $\mathbf{2 0 9 1}$ | 0.0000 |
| $\mathbf{9 2}$ | 0.0000 | $\mathbf{1 0 9 2}$ | 0.0000 | $\mathbf{2 0 9 2}$ | 0.0000 |
| $\mathbf{9 3}$ | 0.0000 | $\mathbf{1 0 9 3}$ | 0.0000 | $\mathbf{2 0 9 3}$ | 0.0000 |
| $\mathbf{9 4}$ | 0.0000 | $\mathbf{1 0 9 4}$ | 0.0000 | $\mathbf{2 0 9 4}$ | 0.0000 |
| $\mathbf{9 5}$ | 0.0000 | $\mathbf{1 0 9 5}$ | 0.0000 | $\mathbf{2 0 9 5}$ | 0.0000 |


| $\mathbf{9 6}$ | 0.0000 | $\mathbf{1 0 9 6}$ | 0.0000 | $\mathbf{2 0 9 6}$ | 0.0000 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{9 7}$ | 0.0000 | $\mathbf{1 0 9 7}$ | 0.0000 | $\mathbf{2 0 9 7}$ | 0.0000 |
| $\mathbf{9 8}$ | 0.0000 | $\mathbf{1 0 9 8}$ | 0.0000 | $\mathbf{2 0 9 8}$ | 0.0000 |
| $\mathbf{9 9}$ | 0.0000 | $\mathbf{1 0 9 9}$ | 0.0000 | $\mathbf{2 0 9 9}$ | 0.0000 |
| $\mathbf{1 0 0}$ | 0.0000 | $\mathbf{1 1 0 0}$ | 0.0000 | $\mathbf{2 1 0 0}$ | 0.0000 |
| $\mathbf{1 0 1}$ | 0.0000 | $\mathbf{1 1 0 1}$ | 0.0000 | $\mathbf{2 1 0 1}$ | 0.0000 |
| $\mathbf{1 0 2}$ | 0.0000 | $\mathbf{1 1 0 2}$ | 0.0000 | $\mathbf{2 1 0 2}$ | 0.0000 |
| $\mathbf{1 0 3}$ | 0.0000 | $\mathbf{1 1 0 3}$ | 0.0000 | $\mathbf{2 1 0 3}$ | 0.0000 |
| $\mathbf{1 0 4}$ | 0.0000 | $\mathbf{1 1 0 4}$ | 0.0000 | $\mathbf{2 1 0 4}$ | 0.0000 |
| $\mathbf{1 0 5}$ | 0.0000 | $\mathbf{1 1 0 5}$ | 0.0000 | $\mathbf{2 1 0 5}$ | 0.0000 |
| $\mathbf{1 0 6}$ | 0.0000 | $\mathbf{1 1 9 6}$ | 0.0000 | $\mathbf{2 1 0 6}$ | 0.0000 |
| $\mathbf{1 0 7}$ | 0.0000 | $\mathbf{1 1 0 7}$ | 0.0000 | $\mathbf{2 1 0 7}$ | 0.0000 |
| $\mathbf{1 0 8}$ | 0.0000 | $\mathbf{1 1 9 8}$ | 0.0000 | $\mathbf{2 1 0 8}$ | 0.0000 |
| $\mathbf{1 0 9}$ | 0.0000 | $\mathbf{1 1 0 9}$ | 0.0000 | $\mathbf{2 1 0 9}$ | 0.0000 |
| $\mathbf{1 1 0}$ | 0.0000 | $\mathbf{1 1 1 0}$ | 0.0000 | $\mathbf{2 1 1 0}$ | 0.0000 |
| $\mathbf{1 1 1}$ | 0.0000 | $\mathbf{1 1 1}$ | 0.0000 | $\mathbf{2 1 1 1}$ | 0.0000 |
| $\mathbf{1 1 2}$ | 0.0000 | $\mathbf{1 1 2 2}$ | 0.0000 | $\mathbf{2 1 1 2}$ | 0.0000 |
| $\mathbf{1 1 3}$ | 0.0000 | $\mathbf{1 1 1 3}$ | 0.0000 | $\mathbf{2 1 1 3}$ | 0.0000 |
| $\mathbf{1 1 4}$ | 0.0000 | $\mathbf{1 1 4}$ | 0.0000 | $\mathbf{2 1 1 4}$ | 0.0000 |
| $\mathbf{1 1 5}$ | 0.0000 | $\mathbf{1 1 1 5}$ | 0.0000 | $\mathbf{2 1 1 5}$ | 0.0000 |
| $\mathbf{1 1 6}$ | 0.0000 | $\mathbf{1 1 6}$ | 0.0000 | $\mathbf{2 1 1 6}$ | 0.0000 |
| $\mathbf{1 1 7}$ | 0.0000 | $\mathbf{1 1 7}$ | 0.0000 | $\mathbf{2 1 1 7}$ | 0.0000 |
| $\mathbf{1 1 8}$ | 0.0000 | $\mathbf{1 1 8}$ | 0.0000 | $\mathbf{2 1 1 8}$ | 0.0000 |
| $\mathbf{1 1 9}$ | 0.0000 | $\mathbf{1 1 9}$ | 0.0000 | $\mathbf{2 1 1 9}$ | 0.0000 |
| $\mathbf{1 2 0}$ | 0.0000 | $\mathbf{1 1 2 0}$ | 0.0000 | $\mathbf{2 1 2 0}$ | 0.0000 |
| $\mathbf{1 2 1}$ | 0.0000 | $\mathbf{1 1 2 1}$ | 0.0000 | $\mathbf{2 1 2 1}$ | 0.0015 |
| $\mathbf{1 2 2}$ | 0.0000 | $\mathbf{1 1 2 2}$ | 0.0088 | $\mathbf{2 1 2 2}$ | 0.0020 |
| $\mathbf{1 2 3}$ | 0.0000 | $\mathbf{1 1 2 3}$ | 0.0295 | $\mathbf{2 1 2 3}$ | 0.0017 |
| $\mathbf{1 2 4}$ | 0.0000 | $\mathbf{1 1 2 4}$ | 0.0125 | $\mathbf{2 1 2 4}$ | 0.0000 |
| $\mathbf{1 2 5}$ | 0.0000 | $\mathbf{1 1 2 5}$ | 0.0371 | $\mathbf{2 1 2 5}$ | 0.0000 |
| $\mathbf{1 2 6}$ | 0.0015 | $\mathbf{1 1 2 6}$ | 0.0000 | $\mathbf{2 1 2 6}$ | 0.0000 |
| $\mathbf{1 2 7}$ | 0.0090 | $\mathbf{1 1 2 7}$ | 0.0000 | $\mathbf{2 1 2 7}$ | 0.0000 |
| $\mathbf{1 2 8}$ | 0.0049 | $\mathbf{1 1 2 8}$ | 0.0000 | $\mathbf{2 1 2 8}$ | 0.0000 |
| $\mathbf{1 2 9}$ | 0.0347 | $\mathbf{1 1 2 9}$ | 0.0000 | $\mathbf{2 1 2 9}$ | 0.0000 |
| $\mathbf{1 3 0}$ | 0.0164 | $\mathbf{1 1 3 0}$ | 0.0000 | $\mathbf{2 1 3 0}$ | 0.0000 |
| $\mathbf{1 3 1}$ | 0.0562 | $\mathbf{1 1 3 1}$ | 0.0269 | $\mathbf{2 1 3 1}$ | 0.0000 |
| $\mathbf{1 3 2}$ | 0.0225 | $\mathbf{1 1 3 2}$ | 0.0129 | $\mathbf{2 1 3 2}$ | 0.0000 |
| $\mathbf{1 3 3}$ | 0.0488 | $\mathbf{1 1 3 3}$ | 0.0232 | $\mathbf{2 1 3 3}$ | 0.0000 |
| $\mathbf{1 3 4}$ | 0.0295 | $\mathbf{1 1 3 4}$ | 0.0310 | $\mathbf{2 1 3 4}$ | 0.0125 |
| $\mathbf{1 3 5}$ | 0.0259 | $\mathbf{1 1 3 5}$ | 0.0117 | $\mathbf{2 1 3 5}$ | 0.0000 |


| $\mathbf{1 3 6}$ | 0.0122 | $\mathbf{1 1 3 6}$ | 0.0752 | $\mathbf{2 1 3 6}$ | 0.0000 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1 3 7}$ | 0.0286 | $\mathbf{1 1 3 7}$ | 0.0376 | $\mathbf{2 1 3 7}$ | 0.0000 |
| $\mathbf{1 3 8}$ | 0.0151 | $\mathbf{1 1 3 8}$ | 0.0840 | $\mathbf{2 1 3 8}$ | 0.0000 |
| $\mathbf{1 3 9}$ | 0.0122 | $\mathbf{1 1 3 9}$ | 0.0554 | $\mathbf{2 1 3 9}$ | 0.0000 |
| $\mathbf{1 4 0}$ | 0.0000 | $\mathbf{1 1 4 0}$ | 0.0759 | $\mathbf{2 1 4 0}$ | 0.0000 |
| $\mathbf{1 4 1}$ | 0.0000 | $\mathbf{1 1 4 1}$ | 0.0698 | $\mathbf{2 1 4 1}$ | 0.0000 |
| $\mathbf{1 4 2}$ | 0.0000 | $\mathbf{1 1 4 2}$ | 0.0510 | $\mathbf{2 1 4 2}$ | 0.0000 |
| $\mathbf{1 4 3}$ | 0.0000 | $\mathbf{1 1 4 3}$ | 0.0269 | $\mathbf{2 1 4 3}$ | 0.0000 |
| $\mathbf{1 4 4}$ | 0.0000 | $\mathbf{1 1 4 4}$ | 0.0144 | $\mathbf{2 1 4 4}$ | 0.0000 |
| $\mathbf{1 4 5}$ | 0.0000 | $\mathbf{1 1 4 5}$ | 0.0259 | $\mathbf{2 1 4 5}$ | 0.0000 |
| $\mathbf{1 4 6}$ | 0.0000 | $\mathbf{1 1 4 6}$ | 0.0325 | $\mathbf{2 1 4 6}$ | 0.0000 |
| $\mathbf{1 4 7}$ | 0.0000 | $\mathbf{1 1 4 7}$ | 0.0264 | $\mathbf{2 1 4 7}$ | 0.0000 |
| $\mathbf{1 4 8}$ | 0.0000 | $\mathbf{1 1 4 8}$ | 0.0581 | $\mathbf{2 1 4 8}$ | 0.0000 |
| $\mathbf{1 4 9}$ | 0.0000 | $\mathbf{1 1 4 9}$ | 0.0591 | $\mathbf{2 1 4 9}$ | 0.0000 |
| $\mathbf{1 5 0}$ | 0.0000 | $\mathbf{1 1 5 0}$ | 0.0596 | $\mathbf{2 1 5 0}$ | 0.0000 |
| $\mathbf{1 5 1}$ | 0.0335 | $\mathbf{1 1 5 1}$ | 0.0303 | $\mathbf{2 1 5 1}$ | 0.0000 |
| $\mathbf{1 5 2}$ | 0.0171 | $\mathbf{1 1 5 2}$ | 0.0371 | $\mathbf{2 1 5 2}$ | 0.0000 |
| $\mathbf{1 5 3}$ | 0.0593 | $\mathbf{1 1 5 3}$ | 0.0706 | $\mathbf{2 1 5 3}$ | 0.0000 |
| $\mathbf{1 5 4}$ | 0.0300 | $\mathbf{1 1 5 4}$ | 0.0388 | $\mathbf{2 1 5 4}$ | 0.0000 |
| $\mathbf{1 5 5}$ | 0.0308 | $\mathbf{1 1 5 5}$ | 0.0444 | $\mathbf{2 1 5 5}$ | 0.0000 |
| $\mathbf{1 5 6}$ | 0.0205 | $\mathbf{1 1 5 6}$ | 0.0295 | $\mathbf{2 1 5 6}$ | 0.0000 |
| $\mathbf{1 5 7}$ | 0.0151 | $\mathbf{1 1 5 7}$ | 0.0139 | $\mathbf{2 1 5 7}$ | 0.0000 |
| $\mathbf{1 5 8}$ | 0.0335 | $\mathbf{1 1 5 8}$ | 0.0186 | $\mathbf{2 1 5 8}$ | 0.0000 |
| $\mathbf{1 5 9}$ | 0.0347 | $\mathbf{1 1 5 9}$ | 0.0103 | $\mathbf{2 1 5 9}$ | 0.0000 |
| $\mathbf{1 6 0}$ | 0.0237 | $\mathbf{1 1 6 0}$ | 0.0061 | $\mathbf{2 1 6 0}$ | 0.0000 |
| $\mathbf{1 6 1}$ | 0.0063 | $\mathbf{1 1 6 1}$ | 0.0098 | $\mathbf{2 1 6 1}$ | 0.0000 |
| $\mathbf{1 6 2}$ | 0.0000 | $\mathbf{1 1 6 2}$ | 0.0134 | $\mathbf{2 1 6 2}$ | 0.0000 |
| $\mathbf{1 6 3}$ | 0.0000 | $\mathbf{1 1 6 3}$ | 0.0315 | $\mathbf{2 1 6 3}$ | 0.0000 |
| $\mathbf{1 6 4}$ | 0.0000 | $\mathbf{1 1 6 4}$ | 0.0083 | $\mathbf{2 1 6 4}$ | 0.0000 |
| $\mathbf{1 6 5}$ | 0.0000 | $\mathbf{1 1 6 5}$ | 0.0129 | $\mathbf{2 1 6 5}$ | 0.0000 |
| $\mathbf{1 6 6}$ | 0.0000 | $\mathbf{1 1 6 6}$ | 0.0212 | $\mathbf{2 1 6 6}$ | 0.0283 |
| $\mathbf{1 6 7}$ | 0.0115 | $\mathbf{1 1 6 7}$ | 0.0188 | $\mathbf{2 1 6 7}$ | 0.0391 |
| $\mathbf{1 6 8}$ | 0.0164 | $\mathbf{1 1 6 8}$ | 0.0088 | $\mathbf{2 1 6 8}$ | 0.0276 |
| $\mathbf{1 6 9}$ | 0.0142 | $\mathbf{1 1 6 9}$ | 0.0325 | $\mathbf{2 1 6 9}$ | 0.0525 |
| $\mathbf{1 7 0}$ | 0.0151 | $\mathbf{1 1 7 0}$ | 0.0078 | $\mathbf{2 1 7 0}$ | 0.0486 |
| $\mathbf{1 7 1}$ | 0.0020 | $\mathbf{1 1 7 1}$ | 0.0000 | $\mathbf{2 1 7 1}$ | 0.0364 |
| $\mathbf{1 7 2}$ | 0.0000 | $\mathbf{1 1 7 2}$ | 0.0027 | $\mathbf{2 1 7 2}$ | 0.0357 |
| $\mathbf{1 7 3}$ | 0.0061 | $\mathbf{1 1 7 3}$ | 0.0149 | $\mathbf{2 1 7 3}$ | 0.0642 |
| $\mathbf{1 7 5}$ | 0.0149 | $\mathbf{1 1 7 4}$ | 0.0117 | $\mathbf{2 1 7 4}$ | 0.0212 |
| $\mathbf{1 1 7 5}$ | 0.0166 | $\mathbf{2 1 7 5}$ | 0.0217 |  |  |


| $\mathbf{1 7 6}$ | 0.0063 | $\mathbf{1 1 7 6}$ | 0.0100 | $\mathbf{2 1 7 6}$ | 0.0000 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1 7 7}$ | 0.0000 | $\mathbf{1 1 7 7}$ | 0.0000 | $\mathbf{2 1 7 7}$ | 0.0054 |
| $\mathbf{1 7 8}$ | 0.0000 | $\mathbf{1 1 7 8}$ | 0.0000 | $\mathbf{2 1 7 8}$ | 0.0000 |
| $\mathbf{1 7 9}$ | 0.0000 | $\mathbf{1 1 7 9}$ | 0.0000 | $\mathbf{2 1 7 9}$ | 0.0000 |
| $\mathbf{1 8 0}$ | 0.0000 | $\mathbf{1 1 8 0}$ | 0.0000 | $\mathbf{2 1 8 0}$ | 0.0000 |
| $\mathbf{1 8 1}$ | 0.0000 | $\mathbf{1 1 8 1}$ | 0.0000 | $\mathbf{2 1 8 1}$ | 0.0000 |
| $\mathbf{1 8 2}$ | 0.0000 | $\mathbf{1 1 8 2}$ | 0.0000 | $\mathbf{2 1 8 2}$ | 0.0000 |
| $\mathbf{1 8 3}$ | 0.0000 | $\mathbf{1 1 8 3}$ | 0.0000 | $\mathbf{2 1 8 3}$ | 0.0000 |
| $\mathbf{1 8 4}$ | 0.0000 | $\mathbf{1 1 8 4}$ | 0.0000 | $\mathbf{2 1 8 4}$ | 0.0000 |
| $\mathbf{1 8 5}$ | 0.0000 | $\mathbf{1 1 8 5}$ | 0.0000 | $\mathbf{2 1 8 5}$ | 0.0000 |
| $\mathbf{1 8 6}$ | 0.0000 | $\mathbf{1 1 8 6}$ | 0.0000 | $\mathbf{2 1 8 6}$ | 0.0000 |
| $\mathbf{1 8 7}$ | 0.0000 | $\mathbf{1 1 8 7}$ | 0.0000 | $\mathbf{2 1 8 7}$ | 0.0000 |
| $\mathbf{1 8 8}$ | 0.0000 | $\mathbf{1 1 8 8}$ | 0.0000 | $\mathbf{2 1 8 8}$ | 0.0000 |
| $\mathbf{1 8 9}$ | 0.0000 | $\mathbf{1 1 8 9}$ | 0.0000 | $\mathbf{2 1 8 9}$ | 0.0000 |
| $\mathbf{1 9 0}$ | 0.0000 | $\mathbf{1 1 9 0}$ | 0.0000 | $\mathbf{2 1 9 0}$ | 0.0000 |
| $\mathbf{1 9 1}$ | 0.0000 | $\mathbf{1 1 9 1}$ | 0.0000 | $\mathbf{2 1 9 1}$ | 0.0000 |
| $\mathbf{1 9 2}$ | 0.0000 | $\mathbf{1 1 9 2}$ | 0.0000 | $\mathbf{2 1 9 2}$ | 0.0000 |
| $\mathbf{1 9 3}$ | 0.0000 | $\mathbf{1 1 9 3}$ | 0.0000 | $\mathbf{2 1 9 3}$ | 0.0000 |
| $\mathbf{1 9 4}$ | 0.0000 | $\mathbf{1 1 9 4}$ | 0.0000 | $\mathbf{2 1 9 4}$ | 0.0000 |
| $\mathbf{1 9 5}$ | 0.0000 | $\mathbf{1 1 9 5}$ | 0.0000 | $\mathbf{2 1 9 5}$ | 0.0000 |
| $\mathbf{1 9 6}$ | 0.0000 | $\mathbf{1 1 9 6}$ | 0.0000 | $\mathbf{2 1 9 6}$ | 0.0000 |
| $\mathbf{1 9 7}$ | 0.0000 | $\mathbf{1 1 9 7}$ | 0.0000 | $\mathbf{2 1 9 7}$ | 0.0000 |
| $\mathbf{1 9 8}$ | 0.0000 | $\mathbf{1 1 9 8}$ | 0.0000 | $\mathbf{2 1 9 8}$ | 0.0000 |
| $\mathbf{1 9 9}$ | 0.0000 | $\mathbf{1 1 9 9}$ | 0.0000 | $\mathbf{2 1 9 9}$ | 0.0000 |
| $\mathbf{2 0 0}$ | 0.0000 | $\mathbf{1 2 0 0}$ | 0.0000 | $\mathbf{2 2 0 0}$ | 0.0000 |
| $\mathbf{2 0 1}$ | 0.0000 | $\mathbf{1 2 0 1}$ | 0.0000 | $\mathbf{2 2 0 1}$ | 0.0000 |
| $\mathbf{2 0 2}$ | 0.0000 | $\mathbf{1 2 0 2}$ | 0.0000 | $\mathbf{2 2 0 2}$ | 0.0000 |
| $\mathbf{2 0 3}$ | 0.0000 | $\mathbf{1 2 0 3}$ | 0.0000 | $\mathbf{2 2 0 3}$ | 0.0000 |
| $\mathbf{2 0 4}$ | 0.0000 | $\mathbf{1 2 0 4}$ | 0.0000 | $\mathbf{2 2 0 4}$ | 0.0000 |
| $\mathbf{2 0 5}$ | 0.0000 | $\mathbf{1 2 0 5}$ | 0.0000 | $\mathbf{2 2 0 5}$ | 0.0000 |
| $\mathbf{2 0 6}$ | 0.0000 | $\mathbf{1 2 0 6}$ | 0.0000 | $\mathbf{2 2 0 6}$ | 0.0000 |
| $\mathbf{2 0 7}$ | 0.0000 | $\mathbf{1 2 0 7}$ | 0.0000 | $\mathbf{2 2 0 7}$ | 0.0000 |
| $\mathbf{2 0 8}$ | 0.0000 | $\mathbf{1 2 0 8}$ | 0.0000 | $\mathbf{2 2 0 8}$ | 0.0000 |
| $\mathbf{2 0 9}$ | 0.0000 | $\mathbf{1 2 0 9}$ | 0.0000 | $\mathbf{2 2 0 9}$ | 0.0000 |
| $\mathbf{2 1 0}$ | 0.0000 | $\mathbf{1 2 1 0}$ | 0.0000 | $\mathbf{2 2 1 0}$ | 0.0000 |
| $\mathbf{2 1 1}$ | 0.0000 | $\mathbf{1 2 1 1}$ | 0.0000 | $\mathbf{2 2 1 1}$ | 0.0000 |
| $\mathbf{2 1 2}$ | 0.0000 | $\mathbf{1 2 1 2}$ | 0.0000 | $\mathbf{2 2 1 2}$ | 0.0000 |
| $\mathbf{2 1 3}$ | 0.0000 | $\mathbf{1 2 1 3}$ | 0.0107 | $\mathbf{2 2 1 3}$ | 0.0000 |
| $\mathbf{2 1 4}$ | 0.0000 | $\mathbf{1 2 1 4}$ | 0.0266 | $\mathbf{2 2 1 4}$ | 0.0000 |
| $\mathbf{2 1 5}$ | 0.0000 | $\mathbf{1 2 1 5}$ | 0.0147 | $\mathbf{2 2 1 5}$ | 0.0000 |


| $\mathbf{2 1 6}$ | 0.0000 | $\mathbf{1 2 1 6}$ | 0.0349 | $\mathbf{2 2 1 6}$ | 0.0000 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{2 1 7}$ | 0.0000 | $\mathbf{1 2 1 7}$ | 0.0000 | $\mathbf{2 2 1 7}$ | 0.0000 |
| $\mathbf{2 1 8}$ | 0.0000 | $\mathbf{1 2 1 8}$ | 0.0000 | $\mathbf{2 2 1 8}$ | 0.0000 |
| $\mathbf{2 1 9}$ | 0.0000 | $\mathbf{1 2 1 9}$ | 0.0000 | $\mathbf{2 2 1 9}$ | 0.0000 |
| $\mathbf{2 2 0}$ | 0.0000 | $\mathbf{1 2 2 0}$ | 0.0000 | $\mathbf{2 2 2 0}$ | 0.0000 |
| $\mathbf{2 2 1}$ | 0.0000 | $\mathbf{1 2 2 1}$ | 0.0000 | $\mathbf{2 2 2 1}$ | 0.0000 |
| $\mathbf{2 2 2}$ | 0.0000 | $\mathbf{1 2 2 2}$ | 0.0000 | $\mathbf{2 2 2 2}$ | 0.0000 |
| $\mathbf{2 2 3}$ | 0.0000 | $\mathbf{1 2 2 3}$ | 0.0000 | $\mathbf{2 2 2 3}$ | 0.0000 |
| $\mathbf{2 2 4}$ | 0.0000 | $\mathbf{1 2 2 4}$ | 0.0000 | $\mathbf{2 2 4}$ | 0.0000 |
| $\mathbf{2 2 5}$ | 0.0032 | $\mathbf{1 2 2 5}$ | 0.0000 | $\mathbf{2 2 5}$ | 0.0000 |
| $\mathbf{2 2 6}$ | 0.0440 | $\mathbf{1 2 2 6}$ | 0.0000 | $\mathbf{2 2 2 6}$ | 0.0454 |
| $\mathbf{2 2 7}$ | 0.0134 | $\mathbf{1 2 2 7}$ | 0.0000 | $\mathbf{2 2 2 7}$ | 0.0386 |
| $\mathbf{2 2 8}$ | 0.0542 | $\mathbf{1 2 2 8}$ | 0.0000 | $\mathbf{2 2 2 8}$ | 0.0198 |
| $\mathbf{2 2 9}$ | 0.0398 | $\mathbf{1 2 2 9}$ | 0.0000 | $\mathbf{2 2 2 9}$ | 0.0000 |
| $\mathbf{2 3 0}$ | 0.0139 | $\mathbf{1 2 3 0}$ | 0.0000 | $\mathbf{2 2 3 0}$ | 0.0195 |
| $\mathbf{2 3 1}$ | 0.0728 | $\mathbf{1 2 3 1}$ | 0.0388 | $\mathbf{2 2 3 1}$ | 0.0000 |
| $\mathbf{2 3 2}$ | 0.0098 | $\mathbf{1 2 3 2}$ | 0.0129 | $\mathbf{2 2 3 2}$ | 0.0000 |
| $\mathbf{2 3 3}$ | 0.0234 | $\mathbf{1 2 3 3}$ | 0.0291 | $\mathbf{2 2 3 3}$ | 0.1101 |
| $\mathbf{2 3 4}$ | 0.0000 | $\mathbf{1 2 3 4}$ | 0.0059 | $\mathbf{2 2 3 4}$ | 0.0657 |
| $\mathbf{2 3 5}$ | 0.0000 | $\mathbf{1 2 3 5}$ | 0.0000 | $\mathbf{2 2 3 5}$ | 0.0466 |
| $\mathbf{2 3 6}$ | 0.0000 | $\mathbf{1 2 3 6}$ | 0.0000 | $\mathbf{2 2 3 6}$ | 0.0000 |
| $\mathbf{2 3 7}$ | 0.0000 | $\mathbf{1 2 3 7}$ | 0.0242 | $\mathbf{2 2 3 7}$ | 0.0000 |
| $\mathbf{2 3 8}$ | 0.0095 | $\mathbf{1 2 3 8}$ | 0.0803 | $\mathbf{2 2 3 8}$ | 0.0000 |
| $\mathbf{2 3 9}$ | 0.0381 | $\mathbf{1 2 3 9}$ | 0.0906 | $\mathbf{2 2 3 9}$ | 0.0000 |
| $\mathbf{2 4 0}$ | 0.0547 | $\mathbf{1 2 4 0}$ | 0.0716 | $\mathbf{2 2 4 0}$ | 0.0000 |
| $\mathbf{2 4 1}$ | 0.0637 | $\mathbf{1 2 4 1}$ | 0.0972 | $\mathbf{2 2 4 1}$ | 0.0000 |
| $\mathbf{2 4 2}$ | 0.0513 | $\mathbf{1 2 4 2}$ | 0.0464 | $\mathbf{2 2 4 2}$ | 0.0000 |
| $\mathbf{2 4 3}$ | 0.0615 | $\mathbf{1 2 4 3}$ | 0.0505 | $\mathbf{2 2 4 3}$ | 0.0000 |
| $\mathbf{2 4 4}$ | 0.0694 | $\mathbf{1 2 4 4}$ | 0.0591 | $\mathbf{2 2 4 4}$ | 0.0000 |
| $\mathbf{2 4 5}$ | 0.0549 | $\mathbf{1 2 4 5}$ | 0.0520 | $\mathbf{2 2 4 5}$ | 0.0000 |
| $\mathbf{2 4 6}$ | 0.0894 | $\mathbf{1 2 4 6}$ | 0.0579 | $\mathbf{2 2 4 6}$ | 0.0000 |
| $\mathbf{2 4 7}$ | 0.0281 | $\mathbf{1 2 4 7}$ | 0.0161 | $\mathbf{2 2 4 7}$ | 0.0000 |
| $\mathbf{2 4 8}$ | 0.1451 | $\mathbf{1 2 4 8}$ | 0.0488 | $\mathbf{2 2 4 8}$ | 0.0000 |
| $\mathbf{2 4 9}$ | 0.0359 | $\mathbf{1 2 4 9}$ | 0.0081 | $\mathbf{2 2 4 9}$ | 0.0000 |
| $\mathbf{2 5 0}$ | 0.0559 | $\mathbf{1 2 5 0}$ | 0.0000 | $\mathbf{2 2 5 0}$ | 0.0000 |
| $\mathbf{2 5 1}$ | 0.0200 | $\mathbf{1 2 5 1}$ | 0.0632 | $\mathbf{2 2 5 1}$ | 0.0000 |
| $\mathbf{2 5 2}$ | 0.0168 | $\mathbf{1 2 5 2}$ | 0.0757 | $\mathbf{2 2 5 2}$ | 0.0000 |
| $\mathbf{2 5 3}$ | 0.0139 | $\mathbf{1 2 5 3}$ | 0.1092 | $\mathbf{2 2 5 3}$ | 0.0000 |
| $\mathbf{2 5 4}$ | 0.0117 | $\mathbf{1 2 5 4}$ | 0.1541 | $\mathbf{2 2 5 4}$ | 0.0000 |
| $\mathbf{2 5 5}$ | 0.0159 | $\mathbf{1 2 5 5}$ | 0.1153 | $\mathbf{2 2 5 5}$ | 0.0000 |


| $\mathbf{2 5 6}$ | 0.0234 | $\mathbf{1 2 5 6}$ | 0.0618 | $\mathbf{2 2 5 6}$ | 0.0000 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{2 5 7}$ | 0.0530 | $\mathbf{1 2 5 7}$ | 0.0383 | $\mathbf{2 2 5 7}$ | 0.0000 |
| $\mathbf{2 5 8}$ | 0.0310 | $\mathbf{1 2 5 8}$ | 0.0518 | $\mathbf{2 2 5 8}$ | 0.0000 |
| $\mathbf{2 5 9}$ | 0.0525 | $\mathbf{1 2 5 9}$ | 0.0422 | $\mathbf{2 2 5 9}$ | 0.0000 |
| $\mathbf{2 6 0}$ | 0.0486 | $\mathbf{1 2 6 0}$ | 0.0105 | $\mathbf{2 2 6 0}$ | 0.0000 |
| $\mathbf{2 6 1}$ | 0.0274 | $\mathbf{1 2 6 1}$ | 0.0237 | $\mathbf{2 2 6 1}$ | 0.0000 |
| $\mathbf{2 6 2}$ | 0.0122 | $\mathbf{1 2 6 2}$ | 0.1189 | $\mathbf{2 2 6 2}$ | 0.0000 |
| $\mathbf{2 6 3}$ | 0.0303 | $\mathbf{1 2 6 3}$ | 0.0918 | $\mathbf{2 2 6 3}$ | 0.0000 |
| $\mathbf{2 6 4}$ | 0.0088 | $\mathbf{1 2 6 4}$ | 0.0784 | $\mathbf{2 2 6 4}$ | 0.0000 |
| $\mathbf{2 6 5}$ | 0.0115 | $\mathbf{1 2 6 5}$ | 0.0945 | $\mathbf{2 2 6 5}$ | 0.0000 |
| $\mathbf{2 6 6}$ | 0.0286 | $\mathbf{1 2 6 6}$ | 0.0994 | $\mathbf{2 2 6 6}$ | 0.0584 |
| $\mathbf{2 6 7}$ | 0.0037 | $\mathbf{1 2 6 7}$ | 0.0469 | $\mathbf{2 2 6 7}$ | 0.0173 |
| $\mathbf{2 6 8}$ | 0.0000 | $\mathbf{1 2 6 8}$ | 0.0261 | $\mathbf{2 2 6 8}$ | 0.0188 |
| $\mathbf{2 6 9}$ | 0.0000 | $\mathbf{1 2 6 9}$ | 0.0176 | $\mathbf{2 2 6 9}$ | 0.0493 |
| $\mathbf{2 7 0}$ | 0.0000 | $\mathbf{1 2 7 0}$ | 0.0220 | $\mathbf{2 2 7 0}$ | 0.0359 |
| $\mathbf{2 7 1}$ | 0.0000 | $\mathbf{1 2 7 1}$ | 0.0173 | $\mathbf{2 2 7 1}$ | 0.0120 |
| $\mathbf{2 7 2}$ | 0.0117 | $\mathbf{1 2 7 2}$ | 0.0149 | $\mathbf{2 2 7 2}$ | 0.0293 |
| $\mathbf{2 7 3}$ | 0.0293 | $\mathbf{1 2 7 3}$ | 0.0444 | $\mathbf{2 2 7 3}$ | 0.0562 |
| $\mathbf{2 7 4}$ | 0.0234 | $\mathbf{1 2 7 4}$ | 0.0066 | $\mathbf{2 2 7 4}$ | 0.0335 |
| $\mathbf{2 7 5}$ | 0.0266 | $\mathbf{1 2 7 5}$ | 0.0000 | $\mathbf{2 2 7 5}$ | 0.0300 |
| $\mathbf{2 7 6}$ | 0.0134 | $\mathbf{1 2 7 6}$ | 0.0000 | $\mathbf{2 2 7 6}$ | 0.0234 |
| $\mathbf{2 7 7}$ | 0.0005 | $\mathbf{1 2 7 7}$ | 0.0000 | $\mathbf{2 2 7 7}$ | 0.0066 |
| $\mathbf{2 7 8}$ | 0.0000 | $\mathbf{1 2 7 8}$ | 0.0000 | $\mathbf{2 2 7 8}$ | 0.0000 |
| $\mathbf{2 7 9}$ | 0.0000 | $\mathbf{1 2 7 9}$ | 0.0000 | $\mathbf{2 2 7 9}$ | 0.0000 |
| $\mathbf{2 8 0}$ | 0.0000 | $\mathbf{1 2 8 0}$ | 0.0000 | $\mathbf{2 2 8 0}$ | 0.0000 |
| $\mathbf{2 8 1}$ | 0.0000 | $\mathbf{1 2 8 1}$ | 0.0000 | $\mathbf{2 2 8 1}$ | 0.0000 |
| $\mathbf{2 8 2}$ | 0.0000 | $\mathbf{1 2 8 2}$ | 0.0000 | $\mathbf{2 2 8 2}$ | 0.0000 |
| $\mathbf{2 8 3}$ | 0.0000 | $\mathbf{1 2 8 3}$ | 0.0000 | $\mathbf{2 2 8 3}$ | 0.0000 |
| $\mathbf{2 8 4}$ | 0.0000 | $\mathbf{1 2 8 4}$ | 0.0000 | $\mathbf{2 2 8 4}$ | 0.0000 |
| $\mathbf{2 8 5}$ | 0.0000 | $\mathbf{1 2 8 5}$ | 0.0000 | $\mathbf{2 2 8 5}$ | 0.0000 |
| $\mathbf{2 8 6}$ | 0.0000 | $\mathbf{1 2 8 6}$ | 0.0000 | $\mathbf{2 2 8 6}$ | 0.0000 |
| $\mathbf{2 8 7}$ | 0.0000 | $\mathbf{1 2 8 7}$ | 0.0000 | $\mathbf{2 2 8 7}$ | 0.0000 |
| $\mathbf{2 8 8}$ | 0.0000 | $\mathbf{1 2 8 8}$ | 0.0000 | $\mathbf{2 2 8 8}$ | 0.0000 |
| $\mathbf{2 8 9}$ | 0.0000 | $\mathbf{1 2 8 9}$ | 0.0000 | $\mathbf{2 2 8 9}$ | 0.0000 |
| $\mathbf{2 9 0}$ | 0.0000 | $\mathbf{1 2 9 0}$ | 0.0000 | $\mathbf{2 2 9 0}$ | 0.0000 |
| $\mathbf{2 9 1}$ | 0.0000 | $\mathbf{1 2 9 1}$ | 0.0000 | $\mathbf{2 2 9 1}$ | 0.0000 |
| $\mathbf{2 9 2}$ | 0.0000 | $\mathbf{1 2 9 2}$ | 0.0000 | $\mathbf{2 2 9 2}$ | 0.0000 |
| $\mathbf{2 9 3}$ | 0.0000 | $\mathbf{1 2 9 3}$ | 0.0000 | $\mathbf{2 2 9 3}$ | 0.0000 |
| $\mathbf{2 9 4}$ | 0.0000 | $\mathbf{1 2 9 4}$ | 0.0000 | $\mathbf{2 2 9 4}$ | 0.0000 |
| $\mathbf{2 9 5}$ | 0.0000 | $\mathbf{1 2 9 5}$ | 0.0000 | $\mathbf{2 2 9 5}$ | 0.0000 |


| $\mathbf{2 9 6}$ | 0.0000 | $\mathbf{1 2 9 6}$ | 0.0000 | $\mathbf{2 2 9 6}$ | 0.0000 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{2 9 7}$ | 0.0000 | $\mathbf{1 2 9 7}$ | 0.0000 | $\mathbf{2 2 9 7}$ | 0.0000 |
| $\mathbf{2 9 8}$ | 0.0000 | $\mathbf{1 2 9 8}$ | 0.0000 | $\mathbf{2 2 9 8}$ | 0.0000 |
| $\mathbf{2 9 9}$ | 0.0000 | $\mathbf{1 2 9 9}$ | 0.0000 | $\mathbf{2 2 9 9}$ | 0.0000 |
| $\mathbf{3 0 0}$ | 0.0000 | $\mathbf{1 3 0 0}$ | 0.0000 | $\mathbf{2 3 0 0}$ | 0.0000 |
| $\mathbf{3 0 1}$ | 0.0000 | $\mathbf{1 3 0 1}$ | 0.0000 | $\mathbf{2 3 0 1}$ | 0.0000 |
| $\mathbf{3 0 2}$ | 0.0005 | $\mathbf{1 3 0 2}$ | 0.0000 | $\mathbf{2 3 0 2}$ | 0.0000 |
| $\mathbf{3 0 3}$ | 0.0007 | $\mathbf{1 3 0 3}$ | 0.0000 | $\mathbf{2 3 0 3}$ | 0.0000 |
| $\mathbf{3 0 4}$ | 0.0000 | $\mathbf{1 3 0 4}$ | 0.0000 | $\mathbf{2 3 0 4}$ | 0.0000 |
| $\mathbf{3 0 5}$ | 0.0000 | $\mathbf{1 3 0 5}$ | 0.0000 | $\mathbf{2 3 0 5}$ | 0.0000 |
| $\mathbf{3 0 6}$ | 0.0000 | $\mathbf{1 3 0 6}$ | 0.0000 | $\mathbf{2 3 0 6}$ | 0.0000 |
| $\mathbf{3 0 7}$ | 0.0000 | $\mathbf{1 3 0 7}$ | 0.0000 | $\mathbf{2 3 0 7}$ | 0.0000 |
| $\mathbf{3 0 8}$ | 0.0000 | $\mathbf{1 3 0 8}$ | 0.0000 | $\mathbf{2 3 0 8}$ | 0.0000 |
| $\mathbf{3 0 9}$ | 0.0000 | $\mathbf{1 3 0 9}$ | 0.0000 | $\mathbf{2 3 0 9}$ | 0.0000 |
| $\mathbf{3 1 0}$ | 0.0000 | $\mathbf{1 3 1 0}$ | 0.0000 | $\mathbf{2 3 1 0}$ | 0.0000 |
| $\mathbf{3 1 1}$ | 0.0000 | $\mathbf{1 3 1 1}$ | 0.0000 | $\mathbf{2 3 1 1}$ | 0.0000 |
| $\mathbf{3 1 2}$ | 0.0000 | $\mathbf{1 3 1 2}$ | 0.0000 | $\mathbf{2 3 1 2}$ | 0.0000 |
| $\mathbf{3 1 3}$ | 0.0000 | $\mathbf{1 3 1 3}$ | 0.0000 | $\mathbf{2 3 1 3}$ | 0.0000 |
| $\mathbf{3 1 4}$ | 0.0000 | $\mathbf{1 3 1 4}$ | 0.0000 | $\mathbf{2 3 1 4}$ | 0.0000 |
| $\mathbf{3 1 5}$ | 0.0000 | $\mathbf{1 3 1 5}$ | 0.0000 | $\mathbf{2 3 1 5}$ | 0.0000 |
| $\mathbf{3 1 6}$ | 0.0000 | $\mathbf{1 3 1 6}$ | 0.0000 | $\mathbf{2 3 1 6}$ | 0.0000 |
| $\mathbf{3 1 7}$ | 0.0000 | $\mathbf{1 3 1 7}$ | 0.0000 | $\mathbf{2 3 1 7}$ | 0.0000 |
| $\mathbf{3 1 8}$ | 0.0000 | $\mathbf{1 3 1 8}$ | 0.0000 | $\mathbf{2 3 1 8}$ | 0.0000 |
| $\mathbf{3 1 9}$ | 0.0000 | $\mathbf{1 3 1 9}$ | 0.0000 | $\mathbf{2 3 1 9}$ | 0.0000 |
| $\mathbf{3 2 0}$ | 0.0000 | $\mathbf{1 3 2 0}$ | 0.0000 | $\mathbf{2 3 2 0}$ | 0.0000 |
| $\mathbf{3 2 1}$ | 0.0186 | $\mathbf{1 3 2 1}$ | 0.0000 | $\mathbf{2 3 2 1}$ | 0.0017 |
| $\mathbf{3 2 2}$ | 0.0073 | $\mathbf{1 3 2 2}$ | 0.0000 | $\mathbf{2 3 2 2}$ | 0.0007 |
| $\mathbf{3 2 3}$ | 0.0112 | $\mathbf{1 3 2 3}$ | 0.0000 | $\mathbf{2 3 2 3}$ | 0.0010 |
| $\mathbf{3 2 4}$ | 0.0000 | $\mathbf{1 3 2 4}$ | 0.0076 | $\mathbf{2 3 2 4}$ | 0.0264 |
| $\mathbf{3 2 5}$ | 0.0000 | $\mathbf{1 3 2 5}$ | 0.0361 | $\mathbf{2 3 2 5}$ | 0.0125 |
| $\mathbf{3 2 6}$ | 0.0000 | $\mathbf{1 3 2 6}$ | 0.0823 | $\mathbf{2 3 2 6}$ | 0.0630 |
| $\mathbf{3 2 7}$ | 0.0000 | $\mathbf{1 3 2 7}$ | 0.0596 | $\mathbf{2 3 2 7}$ | 0.0000 |
| $\mathbf{3 2 8}$ | 0.0000 | $\mathbf{1 3 2 8}$ | 0.0327 | $\mathbf{2 3 2 8}$ | 0.0281 |
| $\mathbf{3 2 9}$ | 0.0000 | $\mathbf{1 3 2 9}$ | 0.0342 | $\mathbf{2 3 2 9}$ | 0.0000 |
| $\mathbf{3 3 0}$ | 0.0000 | $\mathbf{1 3 3 0}$ | 0.0000 | $\mathbf{2 3 3 0}$ | 0.0259 |
| $\mathbf{3 3 1}$ | 0.0002 | $\mathbf{1 3 3 1}$ | 0.0005 | $\mathbf{2 3 3 1}$ | 0.0256 |
| $\mathbf{3 3 2}$ | 0.0093 | $\mathbf{1 3 3 2}$ | 0.0955 | $\mathbf{2 3 3 2}$ | 0.0164 |
| $\mathbf{3 3 3}$ | 0.0090 | $\mathbf{1 3 3 3}$ | 0.0413 | $\mathbf{2 3 3 3}$ | 0.1140 |
| $\mathbf{3 3 4}$ | 0.0093 | $\mathbf{1 3 3 4}$ | 0.0320 | $\mathbf{2 3 3 4}$ | 0.0176 |
| $\mathbf{3 3 5}$ | 0.0017 | $\mathbf{1 3 3 5}$ | 0.0989 | $\mathbf{2 3 3 5}$ | 0.0308 |


| $\mathbf{3 3 6}$ | 0.0000 | $\mathbf{1 3 3 6}$ | 0.0486 | $\mathbf{2 3 3 6}$ | 0.0000 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{3 3 7}$ | 0.0000 | $\mathbf{1 3 3 7}$ | 0.0147 | $\mathbf{2 3 3 7}$ | 0.0000 |
| $\mathbf{3 3 8}$ | 0.0000 | $\mathbf{1 3 3 8}$ | 0.0425 | $\mathbf{2 3 3 8}$ | 0.0000 |
| $\mathbf{3 3 9}$ | 0.0000 | $\mathbf{1 3 3 9}$ | 0.0022 | $\mathbf{2 3 3 9}$ | 0.0000 |
| $\mathbf{3 4 0}$ | 0.0002 | $\mathbf{1 3 4 0}$ | 0.0103 | $\mathbf{2 3 4 0}$ | 0.0000 |
| $\mathbf{3 4 1}$ | 0.0137 | $\mathbf{1 3 4 1}$ | 0.0833 | $\mathbf{2 3 4 1}$ | 0.0000 |
| $\mathbf{3 4 2}$ | 0.0173 | $\mathbf{1 3 4 2}$ | 0.0386 | $\mathbf{2 3 4 2}$ | 0.0000 |
| $\mathbf{3 4 3}$ | 0.0581 | $\mathbf{1 3 4 3}$ | 0.1160 | $\mathbf{2 3 4 3}$ | 0.0000 |
| $\mathbf{3 4 4}$ | 0.0574 | $\mathbf{1 3 4 4}$ | 0.0427 | $\mathbf{2 3 4 4}$ | 0.0000 |
| $\mathbf{3 4 5}$ | 0.0466 | $\mathbf{1 3 4 5}$ | 0.0969 | $\mathbf{2 3 4 5}$ | 0.0000 |
| $\mathbf{3 4 6}$ | 0.0269 | $\mathbf{1 3 4 6}$ | 0.0684 | $\mathbf{2 3 4 6}$ | 0.0000 |
| $\mathbf{3 4 7}$ | 0.0295 | $\mathbf{1 3 4 7}$ | 0.0513 | $\mathbf{2 3 4 7}$ | 0.0000 |
| $\mathbf{3 4 8}$ | 0.0557 | $\mathbf{1 3 4 8}$ | 0.0252 | $\mathbf{2 3 4 8}$ | 0.0000 |
| $\mathbf{3 4 9}$ | 0.0232 | $\mathbf{1 3 4 9}$ | 0.0288 | $\mathbf{2 3 4 9}$ | 0.0000 |
| $\mathbf{3 5 0}$ | 0.0049 | $\mathbf{1 3 5 0}$ | 0.0046 | $\mathbf{2 3 5 0}$ | 0.0000 |
| $\mathbf{3 5 1}$ | 0.0339 | $\mathbf{1 3 5 1}$ | 0.0000 | $\mathbf{2 3 5 1}$ | 0.0000 |
| $\mathbf{3 5 2}$ | 0.0203 | $\mathbf{1 3 5 2}$ | 0.0032 | $\mathbf{2 3 5 2}$ | 0.0000 |
| $\mathbf{3 5 3}$ | 0.0584 | $\mathbf{1 3 5 3}$ | 0.0716 | $\mathbf{2 3 5 3}$ | 0.0000 |
| $\mathbf{3 5 4}$ | 0.0166 | $\mathbf{1 3 5 4}$ | 0.0313 | $\mathbf{2 3 5 4}$ | 0.0000 |
| $\mathbf{3 5 5}$ | 0.0339 | $\mathbf{1 3 5 5}$ | 0.0513 | $\mathbf{2 3 5 5}$ | 0.0000 |
| $\mathbf{3 5 6}$ | 0.0002 | $\mathbf{1 3 5 6}$ | 0.0593 | $\mathbf{2 3 5 6}$ | 0.0000 |
| $\mathbf{3 5 7}$ | 0.0105 | $\mathbf{1 3 5 7}$ | 0.0054 | $\mathbf{2 3 5 7}$ | 0.0000 |
| $\mathbf{3 5 8}$ | 0.0181 | $\mathbf{1 3 5 8}$ | 0.0156 | $\mathbf{2 3 5 8}$ | 0.0000 |
| $\mathbf{3 5 9}$ | 0.0110 | $\mathbf{1 3 5 9}$ | 0.0371 | $\mathbf{2 3 5 9}$ | 0.0000 |
| $\mathbf{3 6 0}$ | 0.0242 | $\mathbf{1 3 6 0}$ | 0.0325 | $\mathbf{2 3 6 0}$ | 0.0000 |
| $\mathbf{3 6 1}$ | 0.0044 | $\mathbf{1 3 6 1}$ | 0.0168 | $\mathbf{2 3 6 1}$ | 0.0000 |
| $\mathbf{3 6 2}$ | 0.0161 | $\mathbf{1 3 6 2}$ | 0.0576 | $\mathbf{2 3 6 2}$ | 0.0000 |
| $\mathbf{3 6 3}$ | 0.0044 | $\mathbf{1 3 6 3}$ | 0.0371 | $\mathbf{2 3 6 3}$ | 0.0000 |
| $\mathbf{3 6 4}$ | 0.0239 | $\mathbf{1 3 6 4}$ | 0.0725 | $\mathbf{2 3 6 4}$ | 0.0000 |
| $\mathbf{3 6 5}$ | 0.0044 | $\mathbf{1 3 6 5}$ | 0.0647 | $\mathbf{2 3 6 5}$ | 0.0000 |
| $\mathbf{3 6 6}$ | 0.0000 | $\mathbf{1 3 6 6}$ | 0.0540 | $\mathbf{2 3 6 6}$ | 0.0264 |
| $\mathbf{3 6 7}$ | 0.0000 | $\mathbf{1 3 6 7}$ | 0.0078 | $\mathbf{2 3 6 7}$ | 0.0059 |
| $\mathbf{3 6 8}$ | 0.0000 | $\mathbf{1 3 6 8}$ | 0.0000 | $\mathbf{2 3 6 8}$ | 0.0000 |
| $\mathbf{3 6 9}$ | 0.0000 | $\mathbf{1 3 6 9}$ | 0.0071 | $\mathbf{2 3 6 9}$ | 0.0000 |
| $\mathbf{3 7 0}$ | 0.0000 | $\mathbf{1 3 7 0}$ | 0.0403 | $\mathbf{2 3 7 0}$ | 0.0046 |
| $\mathbf{3 7 1}$ | 0.0037 | $\mathbf{1 3 7 1}$ | 0.0164 | $\mathbf{2 3 7 1}$ | 0.0161 |
| $\mathbf{3 7 2}$ | 0.0120 | $\mathbf{1 3 7 2}$ | 0.0459 | $\mathbf{2 3 7 2}$ | 0.0159 |
| $\mathbf{3 7 3}$ | 0.0227 | $\mathbf{1 3 7 3}$ | 0.0420 | $\mathbf{2 3 7 3}$ | 0.0342 |
| $\mathbf{3 7 4}$ | 0.0134 | $\mathbf{1 3 7 4}$ | 0.0305 | $\mathbf{2 3 7 4}$ | 0.0188 |
| $\mathbf{3 7 5}$ | 0.0151 | $\mathbf{1 3 7 5}$ | 0.0364 | $\mathbf{2 3 7 5}$ | 0.0176 |
|  |  |  |  |  |  |


| $\mathbf{3 7 6}$ | 0.0093 | $\mathbf{1 3 7 6}$ | 0.0144 | $\mathbf{2 3 7 6}$ | 0.0105 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{3 7 7}$ | 0.0000 | $\mathbf{1 3 7 7}$ | 0.0012 | $\mathbf{2 3 7 7}$ | 0.0007 |
| $\mathbf{3 7 8}$ | 0.0000 | $\mathbf{1 3 7 8}$ | 0.0000 | $\mathbf{2 3 7 8}$ | 0.0000 |
| $\mathbf{3 7 9}$ | 0.0000 | $\mathbf{1 3 7 9}$ | 0.0000 | $\mathbf{2 3 7 9}$ | 0.0000 |
| $\mathbf{3 8 0}$ | 0.0000 | $\mathbf{1 3 8 0}$ | 0.0000 | $\mathbf{2 3 8 0}$ | 0.0000 |
| $\mathbf{3 8 1}$ | 0.0000 | $\mathbf{1 3 8 1}$ | 0.0000 | $\mathbf{2 3 8 1}$ | 0.0000 |
| $\mathbf{3 8 2}$ | 0.0000 | $\mathbf{1 3 8 2}$ | 0.0000 | $\mathbf{2 3 8 2}$ | 0.0000 |
| $\mathbf{3 8 3}$ | 0.0000 | $\mathbf{1 3 8 3}$ | 0.0000 | $\mathbf{2 3 8 3}$ | 0.0000 |
| $\mathbf{3 8 4}$ | 0.0000 | $\mathbf{1 3 8 4}$ | 0.0000 | $\mathbf{2 3 8 4}$ | 0.0000 |
| $\mathbf{3 8 5}$ | 0.0000 | $\mathbf{1 3 8 5}$ | 0.0000 | $\mathbf{2 3 8 5}$ | 0.0000 |
| $\mathbf{3 8 6}$ | 0.0000 | $\mathbf{1 3 8 6}$ | 0.0000 | $\mathbf{2 3 8 6}$ | 0.0000 |
| $\mathbf{3 8 7}$ | 0.0000 | $\mathbf{1 3 8 7}$ | 0.0000 | $\mathbf{2 3 8 7}$ | 0.0000 |
| $\mathbf{3 8 8}$ | 0.0000 | $\mathbf{1 3 8 8}$ | 0.0000 | $\mathbf{2 3 8 8}$ | 0.0000 |
| $\mathbf{3 8 9}$ | 0.0000 | $\mathbf{1 3 8 9}$ | 0.0000 | $\mathbf{2 3 8 9}$ | 0.0000 |
| $\mathbf{3 9 0}$ | 0.0000 | $\mathbf{1 3 9 0}$ | 0.0000 | $\mathbf{2 3 9 0}$ | 0.0000 |
| $\mathbf{3 9 1}$ | 0.0000 | $\mathbf{1 3 9 1}$ | 0.0000 | $\mathbf{2 3 9 1}$ | 0.0000 |
| $\mathbf{3 9 2}$ | 0.0000 | $\mathbf{1 3 9 2}$ | 0.0000 | $\mathbf{2 3 9 2}$ | 0.0000 |
| $\mathbf{3 9 3}$ | 0.0000 | $\mathbf{1 3 9 3}$ | 0.0000 | $\mathbf{2 3 9 3}$ | 0.0000 |
| $\mathbf{3 9 4}$ | 0.0000 | $\mathbf{1 3 9 4}$ | 0.0000 | $\mathbf{2 3 9 4}$ | 0.0000 |
| $\mathbf{3 9 5}$ | 0.0000 | $\mathbf{1 3 9 5}$ | 0.0000 | $\mathbf{2 3 9 5}$ | 0.0000 |
| $\mathbf{3 9 6}$ | 0.0000 | $\mathbf{1 3 9 6}$ | 0.0000 | $\mathbf{2 3 9 6}$ | 0.0000 |
| $\mathbf{3 9 7}$ | 0.0000 | $\mathbf{1 3 9 7}$ | 0.0000 | $\mathbf{2 3 9 7}$ | 0.0000 |
| $\mathbf{3 9 8}$ | 0.0000 | $\mathbf{1 3 9 8}$ | 0.0000 | $\mathbf{2 3 9 8}$ | 0.0000 |
| $\mathbf{3 9 9}$ | 0.0000 | $\mathbf{1 3 9 9}$ | 0.0000 | $\mathbf{2 3 9 9}$ | 0.0000 |
| $\mathbf{4 0 0}$ | 0.0000 | $\mathbf{1 4 0 0}$ | 0.0000 | $\mathbf{2 4 0 0}$ | 0.0000 |
| $\mathbf{4 0 1}$ | 0.0000 | $\mathbf{1 4 0 1}$ | 0.0000 | $\mathbf{2 4 0 1}$ | 0.0000 |
| $\mathbf{4 0 2}$ | 0.0000 | $\mathbf{1 4 0 2}$ | 0.0000 | $\mathbf{2 4 0 2}$ | 0.0000 |
| $\mathbf{4 0 3}$ | 0.0000 | $\mathbf{1 4 0 3}$ | 0.0000 | $\mathbf{2 4 0 3}$ | 0.0000 |
| $\mathbf{4 0 4}$ | 0.0000 | $\mathbf{1 4 0 4}$ | 0.0000 | $\mathbf{2 4 0 4}$ | 0.0000 |
| $\mathbf{4 0 5}$ | 0.0000 | $\mathbf{1 4 0 5}$ | 0.0000 | $\mathbf{2 4 0 5}$ | 0.0000 |
| $\mathbf{4 0 6}$ | 0.0000 | $\mathbf{1 4 0 6}$ | 0.0000 | $\mathbf{2 4 0 6}$ | 0.0000 |
| $\mathbf{4 0 7}$ | 0.0000 | $\mathbf{1 4 0 7}$ | 0.0000 | $\mathbf{2 4 0 7}$ | 0.0010 |
| $\mathbf{4 0 8}$ | 0.0000 | $\mathbf{1 4 0 8}$ | 0.0000 | $\mathbf{2 4 0 8}$ | 0.0000 |
| $\mathbf{4 0 9}$ | 0.0000 | $\mathbf{1 4 0 9}$ | 0.0000 | $\mathbf{2 4 0 9}$ | 0.0000 |
| $\mathbf{4 1 0}$ | 0.0000 | $\mathbf{1 4 1 0}$ | 0.0000 | $\mathbf{2 4 1 0}$ | 0.0000 |
| $\mathbf{4 1 1}$ | 0.0000 | $\mathbf{1 4 1 1}$ | 0.0000 | $\mathbf{2 4 1 1}$ | 0.0000 |
| $\mathbf{4 1 2}$ | 0.0000 | $\mathbf{1 4 1 2}$ | 0.0000 | $\mathbf{2 4 1 2}$ | 0.0000 |
| $\mathbf{4 1 3}$ | 0.0000 | $\mathbf{1 4 1 3}$ | 0.0000 | $\mathbf{2 4 1 3}$ | 0.0000 |
| $\mathbf{4 1 4}$ | 0.0000 | $\mathbf{1 4 1 4}$ | 0.0000 | $\mathbf{2 4 1 4}$ | 0.0000 |
| $\mathbf{4 1 5}$ | 0.0000 | $\mathbf{1 4 1 5}$ | 0.0000 | $\mathbf{2 4 1 5}$ | 0.0000 |
|  |  |  |  |  |  |


| $\mathbf{4 1 6}$ | 0.0000 | $\mathbf{1 4 1 6}$ | 0.0000 | $\mathbf{2 4 1 6}$ | 0.0000 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{4 1 7}$ | 0.0000 | $\mathbf{1 4 1 7}$ | 0.0000 | $\mathbf{2 4 1 7}$ | 0.0000 |
| $\mathbf{4 1 8}$ | 0.0000 | $\mathbf{1 4 1 8}$ | 0.0000 | $\mathbf{2 4 1 8}$ | 0.0000 |
| $\mathbf{4 1 9}$ | 0.0000 | $\mathbf{1 4 1 9}$ | 0.0000 | $\mathbf{2 4 1 9}$ | 0.0000 |
| $\mathbf{4 2 0}$ | 0.0000 | $\mathbf{1 4 2 0}$ | 0.0000 | $\mathbf{2 4 2 0}$ | 0.0000 |
| $\mathbf{4 2 1}$ | 0.0000 | $\mathbf{1 4 2 1}$ | 0.0000 | $\mathbf{2 4 2 1}$ | 0.0000 |
| $\mathbf{4 2 2}$ | 0.0000 | $\mathbf{1 4 2 2}$ | 0.0000 | $\mathbf{2 4 2 2}$ | 0.0000 |
| $\mathbf{4 2 3}$ | 0.0000 | $\mathbf{1 4 2 3}$ | 0.0115 | $\mathbf{2 4 2 3}$ | 0.0000 |
| $\mathbf{4 2 4}$ | 0.0000 | $\mathbf{1 4 2 4}$ | 0.0203 | $\mathbf{2 4 2 4}$ | 0.0000 |
| $\mathbf{4 2 5}$ | 0.0000 | $\mathbf{1 4 2 5}$ | 0.0176 | $\mathbf{2 4 2 5}$ | 0.0000 |
| $\mathbf{4 2 6}$ | 0.0000 | $\mathbf{1 4 2 6}$ | 0.0120 | $\mathbf{2 4 2 6}$ | 0.0000 |
| $\mathbf{4 2 7}$ | 0.0364 | $\mathbf{1 4 2 7}$ | 0.0098 | $\mathbf{2 4 2 7}$ | 0.0000 |
| $\mathbf{4 2 8}$ | 0.0112 | $\mathbf{1 4 2 8}$ | 0.0134 | $\mathbf{2 4 2 8}$ | 0.0000 |
| $\mathbf{4 2 9}$ | 0.0398 | $\mathbf{1 4 2 9}$ | 0.0076 | $\mathbf{2 4 2 9}$ | 0.0491 |
| $\mathbf{4 3 0}$ | 0.0005 | $\mathbf{1 4 3 0}$ | 0.0125 | $\mathbf{2 4 3 0}$ | 0.0000 |
| $\mathbf{4 3 1}$ | 0.0105 | $\mathbf{1 4 3 1}$ | 0.0139 | $\mathbf{2 4 3 1}$ | 0.0000 |
| $\mathbf{4 3 2}$ | 0.0156 | $\mathbf{1 4 3 2}$ | 0.0200 | $\mathbf{2 4 3 2}$ | 0.0000 |
| $\mathbf{4 3 3}$ | 0.0447 | $\mathbf{1 4 3 3}$ | 0.0271 | $\mathbf{2 4 3 3}$ | 0.0398 |
| $\mathbf{4 3 4}$ | 0.0779 | $\mathbf{1 4 3 4}$ | 0.0447 | $\mathbf{2 4 3 4}$ | 0.0112 |
| $\mathbf{4 3 5}$ | 0.0816 | $\mathbf{1 4 3 5}$ | 0.0405 | $\mathbf{2 4 3 5}$ | 0.0000 |
| $\mathbf{4 3 6}$ | 0.0579 | $\mathbf{1 4 3 6}$ | 0.0408 | $\mathbf{2 4 3 6}$ | 0.0000 |
| $\mathbf{4 3 7}$ | 0.0728 | $\mathbf{1 4 3 7}$ | 0.0222 | $\mathbf{2 4 3 7}$ | 0.0000 |
| $\mathbf{4 3 8}$ | 0.0027 | $\mathbf{1 4 3 8}$ | 0.0269 | $\mathbf{2 4 3 8}$ | 0.0000 |
| $\mathbf{4 3 9}$ | 0.0000 | $\mathbf{1 4 3 9}$ | 0.0037 | $\mathbf{2 4 3 9}$ | 0.0000 |
| $\mathbf{4 4 0}$ | 0.0000 | $\mathbf{1 4 4 0}$ | 0.0200 | $\mathbf{2 4 4 0}$ | 0.0000 |
| $\mathbf{4 4 1}$ | 0.0000 | $\mathbf{1 4 4 1}$ | 0.0664 | $\mathbf{2 4 4 1}$ | 0.0000 |
| $\mathbf{4 4 2}$ | 0.0000 | $\mathbf{1 4 4 2}$ | 0.0808 | $\mathbf{2 4 4 2}$ | 0.0000 |
| $\mathbf{4 4 3}$ | 0.0364 | $\mathbf{1 4 4 3}$ | 0.0608 | $\mathbf{2 4 4 3}$ | 0.0000 |
| $\mathbf{4 4 4}$ | 0.0217 | $\mathbf{1 4 4 4}$ | 0.0730 | $\mathbf{2 4 4 4}$ | 0.0000 |
| $\mathbf{4 4 5}$ | 0.0303 | $\mathbf{1 4 4 5}$ | 0.0611 | $\mathbf{2 4 4 5}$ | 0.0000 |
| $\mathbf{4 4 6}$ | 0.0442 | $\mathbf{1 4 4 6}$ | 0.0391 | $\mathbf{2 4 4 6}$ | 0.0000 |
| $\mathbf{4 4 7}$ | 0.0198 | $\mathbf{1 4 4 7}$ | 0.0198 | $\mathbf{2 4 4 7}$ | 0.0000 |
| $\mathbf{4 4 8}$ | 0.0911 | $\mathbf{1 4 4 8}$ | 0.0596 | $\mathbf{2 4 4 8}$ | 0.0000 |
| $\mathbf{4 4 9}$ | 0.0559 | $\mathbf{1 4 4 9}$ | 0.0230 | $\mathbf{2 4 4 9}$ | 0.0000 |
| $\mathbf{4 5 0}$ | 0.1287 | $\mathbf{1 4 5 0}$ | 0.0276 | $\mathbf{2 4 5 0}$ | 0.0000 |
| $\mathbf{4 5 1}$ | 0.0501 | $\mathbf{1 4 5 1}$ | 0.0317 | $\mathbf{2 4 5 1}$ | 0.0000 |
| $\mathbf{4 5 2}$ | 0.0186 | $\mathbf{1 4 5 2}$ | 0.0000 | $\mathbf{2 4 5 2}$ | 0.0000 |
| $\mathbf{4 5 3}$ | 0.0987 | $\mathbf{1 4 5 3}$ | 0.0484 | $\mathbf{2 4 5 3}$ | 0.0000 |
| $\mathbf{4 5 4}$ | 0.0361 | $\mathbf{1 4 5 4}$ | 0.0413 | $\mathbf{2 4 5 4}$ | 0.0000 |
| $\mathbf{4 5 5}$ | 0.0427 | $\mathbf{1 4 5 5}$ | 0.1045 | $\mathbf{2 4 5 5}$ | 0.0000 |


| $\mathbf{4 5 6}$ | 0.0335 | $\mathbf{1 4 5 6}$ | 0.0650 | $\mathbf{2 4 5 6}$ | 0.0000 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{4 5 7}$ | 0.0032 | $\mathbf{1 4 5 7}$ | 0.0759 | $\mathbf{2 4 5 7}$ | 0.0000 |
| $\mathbf{4 5 8}$ | 0.0071 | $\mathbf{1 4 5 8}$ | 0.0618 | $\mathbf{2 4 5 8}$ | 0.0000 |
| $\mathbf{4 5 9}$ | 0.0342 | $\mathbf{1 4 5 9}$ | 0.0571 | $\mathbf{2 4 5 9}$ | 0.0000 |
| $\mathbf{4 6 0}$ | 0.0186 | $\mathbf{1 4 6 0}$ | 0.0759 | $\mathbf{2 4 6 0}$ | 0.0010 |
| $\mathbf{4 6 1}$ | 0.0562 | $\mathbf{1 4 6 1}$ | 0.0400 | $\mathbf{2 4 6 1}$ | 0.0000 |
| $\mathbf{4 6 2}$ | 0.0447 | $\mathbf{1 4 6 2}$ | 0.0672 | $\mathbf{2 4 6 2}$ | 0.0000 |
| $\mathbf{4 6 3}$ | 0.0264 | $\mathbf{1 4 6 3}$ | 0.0723 | $\mathbf{2 4 6 3}$ | 0.0000 |
| $\mathbf{4 6 4}$ | 0.0408 | $\mathbf{1 4 6 4}$ | 0.0310 | $\mathbf{2 4 6 4}$ | 0.0000 |
| $\mathbf{4 6 5}$ | 0.0215 | $\mathbf{1 4 6 5}$ | 0.0310 | $\mathbf{2 4 6 5}$ | 0.0000 |
| $\mathbf{4 6 6}$ | 0.0066 | $\mathbf{1 4 6 6}$ | 0.0188 | $\mathbf{2 4 6 6}$ | 0.0339 |
| $\mathbf{4 6 7}$ | 0.0147 | $\mathbf{1 4 6 7}$ | 0.0000 | $\mathbf{2 4 6 7}$ | 0.0327 |
| $\mathbf{4 6 8}$ | 0.0125 | $\mathbf{1 4 6 8}$ | 0.0000 | $\mathbf{2 4 6 8}$ | 0.0217 |
| $\mathbf{4 6 9}$ | 0.0103 | $\mathbf{1 4 6 9}$ | 0.0000 | $\mathbf{2 4 6 9}$ | 0.0464 |
| $\mathbf{4 7 0}$ | 0.0000 | $\mathbf{1 4 7 0}$ | 0.0000 | $\mathbf{2 4 7 0}$ | 0.0000 |
| $\mathbf{4 7 1}$ | 0.0000 | $\mathbf{1 4 7 1}$ | 0.0000 | $\mathbf{2 4 7 1}$ | 0.0256 |
| $\mathbf{4 7 2}$ | 0.0000 | $\mathbf{1 4 7 2}$ | 0.0078 | $\mathbf{2 4 7 2}$ | 0.0427 |
| $\mathbf{4 7 3}$ | 0.0000 | $\mathbf{1 4 7 3}$ | 0.0383 | $\mathbf{2 4 7 3}$ | 0.0515 |
| $\mathbf{4 7 4}$ | 0.0000 | $\mathbf{1 4 7 4}$ | 0.0154 | $\mathbf{2 4 7 4}$ | 0.0291 |
| $\mathbf{4 7 5}$ | 0.0000 | $\mathbf{1 4 7 5}$ | 0.0188 | $\mathbf{2 4 7 5}$ | 0.0320 |
| $\mathbf{4 7 6}$ | 0.0000 | $\mathbf{1 4 7 6}$ | 0.0142 | $\mathbf{2 4 7 6}$ | 0.0232 |
| $\mathbf{4 7 7}$ | 0.0000 | $\mathbf{1 4 7 7}$ | 0.0017 | $\mathbf{2 4 7 7}$ | 0.0066 |
| $\mathbf{4 7 8}$ | 0.0000 | $\mathbf{1 4 7 8}$ | 0.0000 | $\mathbf{2 4 7 8}$ | 0.0000 |
| $\mathbf{4 7 9}$ | 0.0000 | $\mathbf{1 4 7 9}$ | 0.0000 | $\mathbf{2 4 7 9}$ | 0.0000 |
| $\mathbf{4 8 0}$ | 0.0000 | $\mathbf{1 4 8 0}$ | 0.0000 | $\mathbf{2 4 8 0}$ | 0.0000 |
| $\mathbf{4 8 1}$ | 0.0000 | $\mathbf{1 4 8 1}$ | 0.0000 | $\mathbf{2 4 8 1}$ | 0.0000 |
| $\mathbf{4 8 2}$ | 0.0000 | $\mathbf{1 4 8 2}$ | 0.0000 | $\mathbf{2 4 8 2}$ | 0.0000 |
| $\mathbf{4 8 3}$ | 0.0000 | $\mathbf{1 4 8 3}$ | 0.0000 | $\mathbf{2 4 8 3}$ | 0.0000 |
| $\mathbf{4 8 4}$ | 0.0000 | $\mathbf{1 4 8 4}$ | 0.0000 | $\mathbf{2 4 8 4}$ | 0.0000 |
| $\mathbf{4 8 5}$ | 0.0000 | $\mathbf{1 4 8 5}$ | 0.0000 | $\mathbf{2 4 8 5}$ | 0.0000 |
| $\mathbf{4 8 6}$ | 0.0000 | $\mathbf{1 4 8 6}$ | 0.0000 | $\mathbf{2 4 8 6}$ | 0.0000 |
| $\mathbf{4 8 7}$ | 0.0000 | $\mathbf{1 4 8 7}$ | 0.0000 | $\mathbf{2 4 8 7}$ | 0.0000 |
| $\mathbf{4 8 8}$ | 0.0000 | $\mathbf{1 4 8 8}$ | 0.0000 | $\mathbf{2 4 8 8}$ | 0.0000 |
| $\mathbf{4 8 9}$ | 0.0000 | $\mathbf{1 4 8 9}$ | 0.0000 | $\mathbf{2 4 8 9}$ | 0.0000 |
| $\mathbf{4 9 0}$ | 0.0000 | $\mathbf{1 4 9 0}$ | 0.0000 | $\mathbf{2 4 9 0}$ | 0.0000 |
| $\mathbf{4 9 1}$ | 0.0000 | $\mathbf{1 4 9 1}$ | 0.0000 | $\mathbf{2 4 9 1}$ | 0.0000 |
| $\mathbf{4 9 2}$ | 0.0000 | $\mathbf{1 4 9 2}$ | 0.0000 | $\mathbf{2 4 9 2}$ | 0.0000 |
| $\mathbf{4 9 3}$ | 0.0000 | $\mathbf{1 4 9 3}$ | 0.0000 | $\mathbf{2 4 9 3}$ | 0.0000 |
| $\mathbf{4 9 4}$ | 0.0000 | $\mathbf{1 4 9 4}$ | 0.0000 | $\mathbf{2 4 9 4}$ | 0.0000 |
| $\mathbf{4 9 5}$ | 0.0000 | $\mathbf{1 4 9 5}$ | 0.0000 | $\mathbf{2 4 9 5}$ | 0.0000 |


| $\mathbf{4 9 6}$ | 0.0000 | $\mathbf{1 4 9 6}$ | 0.0000 | $\mathbf{2 4 9 6}$ | 0.0000 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{4 9 7}$ | 0.0000 | $\mathbf{1 4 9 7}$ | 0.0000 | $\mathbf{2 4 9 7}$ | 0.0000 |
| $\mathbf{4 9 8}$ | 0.0000 | $\mathbf{1 4 9 8}$ | 0.0000 | $\mathbf{2 4 9 8}$ | 0.0000 |
| $\mathbf{4 9 9}$ | 0.0000 | $\mathbf{1 4 9 9}$ | 0.0000 | $\mathbf{2 4 9 9}$ | 0.0000 |
| $\mathbf{5 0 0}$ | 0.0000 | $\mathbf{1 5 0 0}$ | 0.0000 | $\mathbf{2 5 0 0}$ | 0.0000 |
| $\mathbf{5 0 1}$ | 0.0000 | $\mathbf{1 5 0 1}$ | 0.0000 | $\mathbf{2 5 0 1}$ | 0.0000 |
| $\mathbf{5 0 2}$ | 0.0000 | $\mathbf{1 5 0 2}$ | 0.0000 | $\mathbf{2 5 0 2}$ | 0.0000 |
| $\mathbf{5 0 3}$ | 0.0000 | $\mathbf{1 5 0 3}$ | 0.0000 | $\mathbf{2 5 0 3}$ | 0.0000 |
| $\mathbf{5 0 4}$ | 0.0000 | $\mathbf{1 5 0 4}$ | 0.0000 | $\mathbf{2 5 0 4}$ | 0.0000 |
| $\mathbf{5 0 5}$ | 0.0000 | $\mathbf{1 5 0 5}$ | 0.0000 | $\mathbf{2 5 0 5}$ | 0.0000 |
| $\mathbf{5 0 6}$ | 0.0000 | $\mathbf{1 5 0 6}$ | 0.0000 | $\mathbf{2 5 0 6}$ | 0.0000 |
| $\mathbf{5 0 7}$ | 0.0000 | $\mathbf{1 5 0 7}$ | 0.0000 | $\mathbf{2 5 0 7}$ | 0.0000 |
| $\mathbf{5 0 8}$ | 0.0000 | $\mathbf{1 5 0 8}$ | 0.0000 | $\mathbf{2 5 0 8}$ | 0.0000 |
| $\mathbf{5 0 9}$ | 0.0000 | $\mathbf{1 5 0 9}$ | 0.0000 | $\mathbf{2 5 0 9}$ | 0.0000 |
| $\mathbf{5 1 0}$ | 0.0000 | $\mathbf{1 5 1 0}$ | 0.0000 | $\mathbf{2 5 1 0}$ | 0.0000 |
| $\mathbf{5 1 1}$ | 0.0000 | $\mathbf{1 5 1 1}$ | 0.0000 | $\mathbf{2 5 1 1}$ | 0.0000 |
| $\mathbf{5 1 2}$ | 0.0000 | $\mathbf{1 5 1 2}$ | 0.0000 | $\mathbf{2 5 1 2}$ | 0.0000 |
| $\mathbf{5 1 3}$ | 0.0000 | $\mathbf{1 5 1 3}$ | 0.0000 | $\mathbf{2 5 1 3}$ | 0.0242 |
| $\mathbf{5 1 4}$ | 0.0000 | $\mathbf{1 5 1 4}$ | 0.0000 | $\mathbf{2 5 1 4}$ | 0.0266 |
| $\mathbf{5 1 5}$ | 0.0000 | $\mathbf{1 5 1 5}$ | 0.0000 | $\mathbf{2 5 1 5}$ | 0.0195 |
| $\mathbf{5 1 6}$ | 0.0000 | $\mathbf{1 5 1 6}$ | 0.0000 | $\mathbf{2 5 1 6}$ | 0.0332 |
| $\mathbf{5 1 7}$ | 0.0000 | $\mathbf{1 5 1 7}$ | 0.0000 | $\mathbf{2 5 1 7}$ | 0.0000 |
| $\mathbf{5 1 8}$ | 0.0000 | $\mathbf{1 5 1 8}$ | 0.0000 | $\mathbf{2 5 1 8}$ | 0.0000 |
| $\mathbf{5 1 9}$ | 0.0000 | $\mathbf{1 5 1 9}$ | 0.0000 | $\mathbf{2 5 1 9}$ | 0.0000 |
| $\mathbf{5 2 0}$ | 0.0000 | $\mathbf{1 5 2 0}$ | 0.0000 | $\mathbf{2 5 2 0}$ | 0.0137 |
| $\mathbf{5 2 1}$ | 0.0000 | $\mathbf{1 5 2 1}$ | 0.0000 | $\mathbf{2 5 2 1}$ | 0.0349 |
| $\mathbf{5 2 2}$ | 0.0000 | $\mathbf{1 5 2 2}$ | 0.0000 | $\mathbf{2 5 2 2}$ | 0.0068 |
| $\mathbf{5 2 3}$ | 0.0000 | $\mathbf{1 5 2 3}$ | 0.0044 | $\mathbf{2 5 2 3}$ | 0.0000 |
| $\mathbf{5 2 4}$ | 0.0000 | $\mathbf{1 5 2 4}$ | 0.0325 | $\mathbf{2 5 2 4}$ | 0.0000 |
| $\mathbf{5 2 5}$ | 0.0000 | $\mathbf{1 5 2 5}$ | 0.1309 | $\mathbf{2 5 2 5}$ | 0.0000 |
| $\mathbf{5 2 6}$ | 0.0000 | $\mathbf{1 5 2 6}$ | 0.0906 | $\mathbf{2 5 2 6}$ | 0.0000 |
| $\mathbf{5 2 7}$ | 0.0000 | $\mathbf{1 5 2 7}$ | 0.0999 | $\mathbf{2 5 2 7}$ | 0.0288 |
| $\mathbf{5 2 8}$ | 0.0000 | $\mathbf{1 5 2 8}$ | 0.0430 | $\mathbf{2 5 2 8}$ | 0.0190 |
| $\mathbf{5 2 9}$ | 0.0000 | $\mathbf{1 5 2 9}$ | 0.0298 | $\mathbf{2 5 2 9}$ | 0.0466 |
| $\mathbf{5 3 0}$ | 0.0000 | $\mathbf{1 5 3 0}$ | 0.1197 | $\mathbf{2 5 3 0}$ | 0.0926 |
| $\mathbf{5 3 1}$ | 0.0220 | $\mathbf{1 5 3 1}$ | 0.0313 | $\mathbf{2 5 3 1}$ | 0.0894 |
| $\mathbf{5 3 2}$ | 0.0584 | $\mathbf{1 5 3 2}$ | 0.0442 | $\mathbf{2 5 3 2}$ | 0.0945 |
| $\mathbf{5 3 3}$ | 0.0669 | $\mathbf{1 5 3 3}$ | 0.0391 | $\mathbf{2 5 3 3}$ | 0.1238 |
| $\mathbf{5 3 4}$ | 0.0606 | $\mathbf{1 5 3 4}$ | 0.0195 | $\mathbf{2 5 3 4}$ | 0.0271 |
| $\mathbf{5 3 5}$ | 0.0190 | $\mathbf{1 5 3 5}$ | 0.0007 | $\mathbf{2 5 3 5}$ | 0.0000 |
|  |  |  |  |  |  |


| $\mathbf{5 3 6}$ | 0.0107 | $\mathbf{1 5 3 6}$ | 0.0381 | $\mathbf{2 5 3 6}$ | 0.0000 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{5 3 7}$ | 0.0354 | $\mathbf{1 5 3 7}$ | 0.0173 | $\mathbf{2 5 3 7}$ | 0.0000 |
| $\mathbf{5 3 8}$ | 0.0286 | $\mathbf{1 5 3 8}$ | 0.0293 | $\mathbf{2 5 3 8}$ | 0.0000 |
| $\mathbf{5 3 9}$ | 0.0469 | $\mathbf{1 5 3 9}$ | 0.0061 | $\mathbf{2 5 3 9}$ | 0.0000 |
| $\mathbf{5 4 0}$ | 0.0598 | $\mathbf{1 5 4 0}$ | 0.0076 | $\mathbf{2 5 4 0}$ | 0.0000 |
| $\mathbf{5 4 1}$ | 0.0608 | $\mathbf{1 5 4 1}$ | 0.1031 | $\mathbf{2 5 4 1}$ | 0.0000 |
| $\mathbf{5 4 2}$ | 0.0369 | $\mathbf{1 5 4 2}$ | 0.0444 | $\mathbf{2 5 4 2}$ | 0.0000 |
| $\mathbf{5 4 3}$ | 0.0095 | $\mathbf{1 5 4 3}$ | 0.1739 | $\mathbf{2 5 4 3}$ | 0.0000 |
| $\mathbf{5 4 4}$ | 0.0000 | $\mathbf{1 5 4 4}$ | 0.0344 | $\mathbf{2 5 4 4}$ | 0.0000 |
| $\mathbf{5 4 5}$ | 0.0000 | $\mathbf{1 5 4 5}$ | 0.0630 | $\mathbf{2 5 4 5}$ | 0.0000 |
| $\mathbf{5 4 6}$ | 0.0000 | $\mathbf{1 5 4 6}$ | 0.0647 | $\mathbf{2 5 4 6}$ | 0.0000 |
| $\mathbf{5 4 7}$ | 0.0000 | $\mathbf{1 5 4 7}$ | 0.0708 | $\mathbf{2 5 4 7}$ | 0.0137 |
| $\mathbf{5 4 8}$ | 0.0000 | $\mathbf{1 5 4 8}$ | 0.0737 | $\mathbf{2 5 4 8}$ | 0.0000 |
| $\mathbf{5 4 9}$ | 0.0000 | $\mathbf{1 5 4 9}$ | 0.0913 | $\mathbf{2 5 4 9}$ | 0.0000 |
| $\mathbf{5 5 0}$ | 0.0000 | $\mathbf{1 5 5 0}$ | 0.0540 | $\mathbf{2 5 5 0}$ | 0.0000 |
| $\mathbf{5 5 1}$ | 0.0000 | $\mathbf{1 5 5 1}$ | 0.0542 | $\mathbf{2 5 5 1}$ | 0.0332 |
| $\mathbf{5 5 2}$ | 0.0000 | $\mathbf{1 5 5 2}$ | 0.0181 | $\mathbf{2 5 5 2}$ | 0.0195 |
| $\mathbf{5 5 3}$ | 0.0488 | $\mathbf{1 5 5 3}$ | 0.0466 | $\mathbf{2 5 5 3}$ | 0.0266 |
| $\mathbf{5 5 4}$ | 0.0249 | $\mathbf{1 5 5 4}$ | 0.1177 | $\mathbf{2 5 5 4}$ | 0.0242 |
| $\mathbf{5 5 5}$ | 0.0471 | $\mathbf{1 5 5 5}$ | 0.0657 | $\mathbf{2 5 5 5}$ | 0.0000 |
| $\mathbf{5 5 6}$ | 0.0093 | $\mathbf{1 5 5 6}$ | 0.0432 | $\mathbf{2 5 5 6}$ | 0.0000 |
| $\mathbf{5 5 7}$ | 0.0107 | $\mathbf{1 5 5 7}$ | 0.1140 | $\mathbf{2 5 5 7}$ | 0.0000 |
| $\mathbf{5 5 8}$ | 0.0103 | $\mathbf{1 5 5 8}$ | 0.0879 | $\mathbf{2 5 5 8}$ | 0.0000 |
| $\mathbf{5 5 9}$ | 0.0000 | $\mathbf{1 5 5 9}$ | 0.0369 | $\mathbf{2 5 5 9}$ | 0.0000 |
| $\mathbf{5 6 0}$ | 0.0039 | $\mathbf{1 5 6 0}$ | 0.0510 | $\mathbf{2 5 6 0}$ | 0.0000 |
| $\mathbf{5 6 1}$ | 0.0110 | $\mathbf{1 5 6 1}$ | 0.1074 | $\mathbf{2 5 6 1}$ | 0.0000 |
| $\mathbf{5 6 2}$ | 0.0230 | $\mathbf{1 5 6 2}$ | 0.0440 | $\mathbf{2 5 6 2}$ | 0.0000 |
| $\mathbf{5 6 3}$ | 0.0210 | $\mathbf{1 5 6 3}$ | 0.0579 | $\mathbf{2 5 6 3}$ | 0.0000 |
| $\mathbf{5 6 4}$ | 0.0242 | $\mathbf{1 5 6 4}$ | 0.0391 | $\mathbf{2 5 6 4}$ | 0.0000 |
| $\mathbf{5 6 5}$ | 0.0352 | $\mathbf{1 5 6 5}$ | 0.0198 | $\mathbf{2 5 6 5}$ | 0.0000 |
| $\mathbf{5 6 6}$ | 0.0181 | $\mathbf{1 5 6 6}$ | 0.0708 | $\mathbf{2 5 6 6}$ | 0.0642 |
| $\mathbf{5 6 7}$ | 0.0090 | $\mathbf{1 5 6 7}$ | 0.0598 | $\mathbf{2 5 6 7}$ | 0.0171 |
| $\mathbf{5 6 8}$ | 0.0083 | $\mathbf{1 5 6 8}$ | 0.0464 | $\mathbf{2 5 6 8}$ | 0.0242 |
| $\mathbf{5 6 9}$ | 0.0129 | $\mathbf{1 5 6 9}$ | 0.0574 | $\mathbf{2 5 6 9}$ | 0.0217 |
| $\mathbf{5 7 0}$ | 0.0132 | $\mathbf{1 5 7 0}$ | 0.0496 | $\mathbf{2 5 7 0}$ | 0.0276 |
| $\mathbf{5 7 1}$ | 0.0210 | $\mathbf{1 5 7 1}$ | 0.0488 | $\mathbf{2 5 7 1}$ | 0.0137 |
| $\mathbf{5 7 2}$ | 0.0076 | $\mathbf{1 5 7 2}$ | 0.0147 | $\mathbf{2 5 7 2}$ | 0.0227 |
| $\mathbf{5 7 3}$ | 0.0168 | $\mathbf{1 5 7 3}$ | 0.0017 | $\mathbf{2 5 7 3}$ | 0.0444 |
| $\mathbf{5 7 4}$ | 0.0107 | $\mathbf{1 5 7 4}$ | 0.0000 | $\mathbf{2 5 7 4}$ | 0.0237 |
| $\mathbf{5 7 5}$ | 0.0129 | $\mathbf{1 5 7 5}$ | 0.0000 | $\mathbf{2 5 7 5}$ | 0.0208 |
|  |  |  |  |  |  |


| $\mathbf{5 7 6}$ | 0.0037 | $\mathbf{1 5 7 6}$ | 0.0000 | $\mathbf{2 5 7 6}$ | 0.0154 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{5 7 7}$ | 0.0000 | $\mathbf{1 5 7 7}$ | 0.0000 | $\mathbf{2 5 7 7}$ | 0.0063 |
| $\mathbf{5 7 8}$ | 0.0000 | $\mathbf{1 5 7 8}$ | 0.0000 | $\mathbf{2 5 7 8}$ | 0.0000 |
| $\mathbf{5 7 9}$ | 0.0000 | $\mathbf{1 5 7 9}$ | 0.0000 | $\mathbf{2 5 7 9}$ | 0.0000 |
| $\mathbf{5 8 0}$ | 0.0000 | $\mathbf{1 5 8 0}$ | 0.0000 | $\mathbf{2 5 8 0}$ | 0.0000 |
| $\mathbf{5 8 1}$ | 0.0000 | $\mathbf{1 5 8 1}$ | 0.0000 | $\mathbf{2 5 8 1}$ | 0.0000 |
| $\mathbf{5 8 2}$ | 0.0000 | $\mathbf{1 5 8 2}$ | 0.0000 | $\mathbf{2 5 8 2}$ | 0.0000 |
| $\mathbf{5 8 3}$ | 0.0000 | $\mathbf{1 5 8 3}$ | 0.0000 | $\mathbf{2 5 8 3}$ | 0.0000 |
| $\mathbf{5 8 4}$ | 0.0000 | $\mathbf{1 5 8 4}$ | 0.0000 | $\mathbf{2 5 8 4}$ | 0.0000 |
| $\mathbf{5 8 5}$ | 0.0000 | $\mathbf{1 5 8 5}$ | 0.0000 | $\mathbf{2 5 8 5}$ | 0.0000 |
| $\mathbf{5 8 6}$ | 0.0000 | $\mathbf{1 5 8 6}$ | 0.0000 | $\mathbf{2 5 8 6}$ | 0.0000 |
| $\mathbf{5 8 7}$ | 0.0000 | $\mathbf{1 5 8 7}$ | 0.0000 | $\mathbf{2 5 8 7}$ | 0.0000 |
| $\mathbf{5 8 8}$ | 0.0000 | $\mathbf{1 5 8 8}$ | 0.0000 | $\mathbf{2 5 8 8}$ | 0.0000 |
| $\mathbf{5 8 9}$ | 0.0000 | $\mathbf{1 5 8 9}$ | 0.0000 | $\mathbf{2 5 8 9}$ | 0.0000 |
| $\mathbf{5 9 0}$ | 0.0000 | $\mathbf{1 5 9 0}$ | 0.0000 | $\mathbf{2 5 9 0}$ | 0.0000 |
| $\mathbf{5 9 1}$ | 0.0000 | $\mathbf{1 5 9 1}$ | 0.0000 | $\mathbf{2 5 9 1}$ | 0.0000 |
| $\mathbf{5 9 2}$ | 0.0000 | $\mathbf{1 5 9 2}$ | 0.0000 | $\mathbf{2 5 9 2}$ | 0.0000 |
| $\mathbf{5 9 3}$ | 0.0000 | $\mathbf{1 5 9 3}$ | 0.0000 | $\mathbf{2 5 9 3}$ | 0.0000 |
| $\mathbf{5 9 4}$ | 0.0000 | $\mathbf{1 5 9 4}$ | 0.0000 | $\mathbf{2 5 9 4}$ | 0.0000 |
| $\mathbf{5 9 5}$ | 0.0000 | $\mathbf{1 5 9 5}$ | 0.0000 | $\mathbf{2 5 9 5}$ | 0.0000 |
| $\mathbf{5 9 6}$ | 0.0000 | $\mathbf{1 5 9 6}$ | 0.0000 | $\mathbf{2 5 9 6}$ | 0.0000 |
| $\mathbf{5 9 7}$ | 0.0000 | $\mathbf{1 5 9 7}$ | 0.0000 | $\mathbf{2 5 9 7}$ | 0.0000 |
| $\mathbf{5 9 8}$ | 0.0000 | $\mathbf{1 5 9 8}$ | 0.0000 | $\mathbf{2 5 9 8}$ | 0.0000 |
| $\mathbf{5 9 9}$ | 0.0000 | $\mathbf{1 5 9 9}$ | 0.0000 | $\mathbf{2 5 9 9}$ | 0.0000 |
| $\mathbf{6 0 0}$ | 0.0000 | $\mathbf{1 6 0 0}$ | 0.0000 | $\mathbf{2 6 0 0}$ | 0.0000 |
| $\mathbf{6 0 1}$ | 0.0000 | $\mathbf{1 6 0 1}$ | 0.0000 | $\mathbf{2 6 0 1}$ | 0.0000 |
| $\mathbf{6 0 2}$ | 0.0000 | $\mathbf{1 6 0 2}$ | 0.0000 | $\mathbf{2 6 0 2}$ | 0.0000 |
| $\mathbf{6 0 3}$ | 0.0000 | $\mathbf{1 6 0 3}$ | 0.0000 | $\mathbf{2 6 0 3}$ | 0.0000 |
| $\mathbf{6 0 4}$ | 0.0000 | $\mathbf{1 6 0 4}$ | 0.0000 | $\mathbf{2 6 0 4}$ | 0.0000 |
| $\mathbf{6 0 5}$ | 0.0000 | $\mathbf{1 6 0 5}$ | 0.0000 | $\mathbf{2 6 0 5}$ | 0.0000 |
| $\mathbf{6 0 6}$ | 0.0000 | $\mathbf{1 6 0 6}$ | 0.0000 | $\mathbf{2 6 0 6}$ | 0.0000 |
| $\mathbf{6 0 7}$ | 0.0000 | $\mathbf{1 6 0 7}$ | 0.0000 | $\mathbf{2 6 0 7}$ | 0.0000 |
| $\mathbf{6 0 8}$ | 0.0000 | $\mathbf{1 6 0 8}$ | 0.0000 | $\mathbf{2 6 0 8}$ | 0.0000 |
| $\mathbf{6 0 9}$ | 0.0000 | $\mathbf{1 6 0 9}$ | 0.0000 | $\mathbf{2 6 0 9}$ | 0.0000 |
| $\mathbf{6 1 0}$ | 0.0000 | $\mathbf{1 6 1 0}$ | 0.0000 | $\mathbf{2 6 1 0}$ | 0.0000 |
| $\mathbf{6 1 1}$ | 0.0000 | $\mathbf{1 6 1 1}$ | 0.0000 | $\mathbf{2 6 1 1}$ | 0.0000 |
| $\mathbf{6 1 2}$ | 0.0000 | $\mathbf{1 6 1 2}$ | 0.0000 | $\mathbf{2 6 1 2}$ | 0.0000 |
| $\mathbf{6 1 3}$ | 0.0000 | $\mathbf{1 6 1 3}$ | 0.0000 | $\mathbf{2 6 1 3}$ | 0.0000 |
| $\mathbf{6 1 4}$ | 0.0000 | $\mathbf{1 6 1 4}$ | 0.0000 | $\mathbf{2 6 1 4}$ | 0.0000 |
| $\mathbf{6 1 5}$ | 0.0000 | $\mathbf{1 6 1 5}$ | 0.0000 | $\mathbf{2 6 1 5}$ | 0.0000 |
|  |  |  |  |  |  |


| $\mathbf{6 1 6}$ | 0.0000 | $\mathbf{1 6 1 6}$ | 0.0000 | $\mathbf{2 6 1 6}$ | 0.0000 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{6 1 7}$ | 0.0000 | $\mathbf{1 6 1 7}$ | 0.0000 | $\mathbf{2 6 1 7}$ | 0.0000 |
| $\mathbf{6 1 8}$ | 0.0000 | $\mathbf{1 6 1 8}$ | 0.0000 | $\mathbf{2 6 1 8}$ | 0.0159 |
| $\mathbf{6 1 9}$ | 0.0000 | $\mathbf{1 6 1 9}$ | 0.0000 | $\mathbf{2 6 1 9}$ | 0.0371 |
| $\mathbf{6 2 0}$ | 0.0000 | $\mathbf{1 6 2 0}$ | 0.0000 | $\mathbf{2 6 2 0}$ | 0.0227 |
| $\mathbf{6 2 1}$ | 0.0039 | $\mathbf{1 6 2 1}$ | 0.0000 | $\mathbf{2 6 2 1}$ | 0.0000 |
| $\mathbf{6 2 2}$ | 0.0017 | $\mathbf{1 6 2 2}$ | 0.0000 | $\mathbf{2 6 2 2}$ | 0.0315 |
| $\mathbf{6 2 3}$ | 0.0051 | $\mathbf{1 6 2 3}$ | 0.0000 | $\mathbf{2 6 2 3}$ | 0.0000 |
| $\mathbf{6 2 4}$ | 0.0000 | $\mathbf{1 6 2 4}$ | 0.0000 | $\mathbf{2 6 2 4}$ | 0.0051 |
| $\mathbf{6 2 5}$ | 0.0000 | $\mathbf{1 6 2 5}$ | 0.0000 | $\mathbf{2 6 2 5}$ | 0.0066 |
| $\mathbf{6 2 6}$ | 0.0000 | $\mathbf{1 6 2 6}$ | 0.0120 | $\mathbf{2 6 2 6}$ | 0.0000 |
| $\mathbf{6 2 7}$ | 0.0000 | $\mathbf{1 6 2 7}$ | 0.0400 | $\mathbf{2 6 2 7}$ | 0.0000 |
| $\mathbf{6 2 8}$ | 0.0015 | $\mathbf{1 6 2 8}$ | 0.0799 | $\mathbf{2 6 2 8}$ | 0.0068 |
| $\mathbf{6 2 9}$ | 0.1343 | $\mathbf{1 6 2 9}$ | 0.0674 | $\mathbf{2 6 2 9}$ | 0.0000 |
| $\mathbf{6 3 0}$ | 0.0725 | $\mathbf{1 6 3 0}$ | 0.0320 | $\mathbf{2 6 3 0}$ | 0.0476 |
| $\mathbf{6 3 1}$ | 0.0974 | $\mathbf{1 6 3 1}$ | 0.0833 | $\mathbf{2 6 3 1}$ | 0.0000 |
| $\mathbf{6 3 2}$ | 0.0872 | $\mathbf{1 6 3 2}$ | 0.0105 | $\mathbf{2 6 3 2}$ | 0.0449 |
| $\mathbf{6 3 3}$ | 0.0000 | $\mathbf{1 6 3 3}$ | 0.0435 | $\mathbf{2 6 3 3}$ | 0.0198 |
| $\mathbf{6 3 4}$ | 0.0000 | $\mathbf{1 6 3 4}$ | 0.0063 | $\mathbf{2 6 3 4}$ | 0.0000 |
| $\mathbf{6 3 5}$ | 0.0469 | $\mathbf{1 6 3 5}$ | 0.0737 | $\mathbf{2 6 3 5}$ | 0.0000 |
| $\mathbf{6 3 6}$ | 0.0095 | $\mathbf{1 6 3 6}$ | 0.0637 | $\mathbf{2 6 3 6}$ | 0.0000 |
| $\mathbf{6 3 7}$ | 0.0505 | $\mathbf{1 6 3 7}$ | 0.0476 | $\mathbf{2 6 3 7}$ | 0.0000 |
| $\mathbf{6 3 8}$ | 0.0000 | $\mathbf{1 6 3 8}$ | 0.0569 | $\mathbf{2 6 3 8}$ | 0.0000 |
| $\mathbf{6 3 9}$ | 0.0000 | $\mathbf{1 6 3 9}$ | 0.0095 | $\mathbf{2 6 3 9}$ | 0.0000 |
| $\mathbf{6 4 0}$ | 0.0000 | $\mathbf{1 6 4 0}$ | 0.0000 | $\mathbf{2 6 4 0}$ | 0.0000 |
| $\mathbf{6 4 1}$ | 0.0015 | $\mathbf{1 6 4 1}$ | 0.0481 | $\mathbf{2 6 4 1}$ | 0.0000 |
| $\mathbf{6 4 2}$ | 0.0339 | $\mathbf{1 6 4 2}$ | 0.0408 | $\mathbf{2 6 4 2}$ | 0.0000 |
| $\mathbf{6 4 3}$ | 0.1170 | $\mathbf{1 6 4 3}$ | 0.0781 | $\mathbf{2 6 4 3}$ | 0.0000 |
| $\mathbf{6 4 4}$ | 0.0608 | $\mathbf{1 6 4 4}$ | 0.0410 | $\mathbf{2 6 4 4}$ | 0.0000 |
| $\mathbf{6 4 5}$ | 0.0818 | $\mathbf{1 6 4 5}$ | 0.0332 | $\mathbf{2 6 4 5}$ | 0.0000 |
| $\mathbf{6 4 6}$ | 0.1143 | $\mathbf{1 6 4 6}$ | 0.0823 | $\mathbf{2 6 4 6}$ | 0.0000 |
| $\mathbf{6 4 7}$ | 0.0430 | $\mathbf{1 6 4 7}$ | 0.0523 | $\mathbf{2 6 4 7}$ | 0.0227 |
| $\mathbf{6 4 8}$ | 0.0090 | $\mathbf{1 6 4 8}$ | 0.0186 | $\mathbf{2 6 4 8}$ | 0.0371 |
| $\mathbf{6 4 9}$ | 0.0259 | $\mathbf{1 6 4 9}$ | 0.0327 | $\mathbf{2 6 4 9}$ | 0.0159 |
| $\mathbf{6 5 0}$ | 0.0247 | $\mathbf{1 6 5 0}$ | 0.0230 | $\mathbf{2 6 5 0}$ | 0.0000 |
| $\mathbf{6 5 1}$ | 0.0706 | $\mathbf{1 6 5 1}$ | 0.0183 | $\mathbf{2 6 5 1}$ | 0.0000 |
| $\mathbf{6 5 2}$ | 0.0298 | $\mathbf{1 6 5 2}$ | 0.0186 | $\mathbf{2 6 5 2}$ | 0.0000 |
| $\mathbf{6 5 3}$ | 0.0708 | $\mathbf{1 6 5 3}$ | 0.0864 | $\mathbf{2 6 5 3}$ | 0.0000 |
| $\mathbf{6 5 4}$ | 0.0698 | $\mathbf{1 6 5 4}$ | 0.1050 | $\mathbf{2 6 5 4}$ | 0.0000 |
| $\mathbf{6 5 5}$ | 0.0679 | $\mathbf{1 6 5 5}$ | 0.0703 | $\mathbf{2 6 5 5}$ | 0.0000 |
|  |  |  |  |  |  |


| $\mathbf{6 5 6}$ | 0.0418 | $\mathbf{1 6 5 6}$ | 0.0908 | $\mathbf{2 6 5 6}$ | 0.0000 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{6 5 7}$ | 0.0398 | $\mathbf{1 6 5 7}$ | 0.0733 | $\mathbf{2 6 5 7}$ | 0.0000 |
| $\mathbf{6 5 8}$ | 0.0510 | $\mathbf{1 6 5 8}$ | 0.0259 | $\mathbf{2 6 5 8}$ | 0.0000 |
| $\mathbf{6 5 9}$ | 0.0647 | $\mathbf{1 6 5 9}$ | 0.0586 | $\mathbf{2 6 5 9}$ | 0.0000 |
| $\mathbf{6 6 0}$ | 0.0623 | $\mathbf{1 6 6 0}$ | 0.0503 | $\mathbf{2 6 6 0}$ | 0.0000 |
| $\mathbf{6 6 1}$ | 0.0435 | $\mathbf{1 6 6 1}$ | 0.0330 | $\mathbf{2 6 6 1}$ | 0.0000 |
| $\mathbf{6 6 2}$ | 0.0926 | $\mathbf{1 6 6 2}$ | 0.0520 | $\mathbf{2 6 6 2}$ | 0.0000 |
| $\mathbf{6 6 3}$ | 0.0188 | $\mathbf{1 6 6 3}$ | 0.0344 | $\mathbf{2 6 6 3}$ | 0.0000 |
| $\mathbf{6 6 4}$ | 0.0215 | $\mathbf{1 6 6 4}$ | 0.0181 | $\mathbf{2 6 6 4}$ | 0.0000 |
| $\mathbf{6 6 5}$ | 0.0068 | $\mathbf{1 6 6 5}$ | 0.0347 | $\mathbf{2 6 6 5}$ | 0.0000 |
| $\mathbf{6 6 6}$ | 0.0071 | $\mathbf{1 6 6 6}$ | 0.0227 | $\mathbf{2 6 6 6}$ | 0.0562 |
| $\mathbf{6 6 7}$ | 0.0215 | $\mathbf{1 6 6 7}$ | 0.0274 | $\mathbf{2 6 6 7}$ | 0.0457 |
| $\mathbf{6 6 8}$ | 0.0105 | $\mathbf{1 6 6 8}$ | 0.0078 | $\mathbf{2 6 6 8}$ | 0.0291 |
| $\mathbf{6 6 9}$ | 0.0200 | $\mathbf{1 6 6 9}$ | 0.0088 | $\mathbf{2 6 6 9}$ | 0.0479 |
| $\mathbf{6 7 0}$ | 0.0098 | $\mathbf{1 6 7 0}$ | 0.0217 | $\mathbf{2 6 7 0}$ | 0.0879 |
| $\mathbf{6 7 1}$ | 0.0010 | $\mathbf{1 6 7 1}$ | 0.0274 | $\mathbf{2 6 7 1}$ | 0.0276 |
| $\mathbf{6 7 2}$ | 0.0078 | $\mathbf{1 6 7 2}$ | 0.0274 | $\mathbf{2 6 7 2}$ | 0.0513 |
| $\mathbf{6 7 3}$ | 0.0274 | $\mathbf{1 6 7 3}$ | 0.0361 | $\mathbf{2 6 7 3}$ | 0.0505 |
| $\mathbf{6 7 4}$ | 0.0144 | $\mathbf{1 6 7 4}$ | 0.0190 | $\mathbf{2 6 7 4}$ | 0.0151 |
| $\mathbf{6 7 5}$ | 0.0161 | $\mathbf{1 6 7 5}$ | 0.0166 | $\mathbf{2 6 7 5}$ | 0.0168 |
| $\mathbf{6 7 6}$ | 0.0186 | $\mathbf{1 6 7 6}$ | 0.0120 | $\mathbf{2 6 7 6}$ | 0.0137 |
| $\mathbf{6 7 7}$ | 0.0044 | $\mathbf{1 6 7 7}$ | 0.0005 | $\mathbf{2 6 7 7}$ | 0.0007 |
| $\mathbf{6 7 8}$ | 0.0000 | $\mathbf{1 6 7 8}$ | 0.0000 | $\mathbf{2 6 7 8}$ | 0.0000 |
| $\mathbf{6 7 9}$ | 0.0000 | $\mathbf{1 6 7 9}$ | 0.0000 | $\mathbf{2 6 7 9}$ | 0.0000 |
| $\mathbf{6 8 0}$ | 0.0000 | $\mathbf{1 6 8 0}$ | 0.0000 | $\mathbf{2 6 8 0}$ | 0.0000 |
| $\mathbf{6 8 1}$ | 0.0000 | $\mathbf{1 6 8 1}$ | 0.0000 | $\mathbf{2 6 8 1}$ | 0.0000 |
| $\mathbf{6 8 2}$ | 0.0000 | $\mathbf{1 6 8 2}$ | 0.0000 | $\mathbf{2 6 8 2}$ | 0.0000 |
| $\mathbf{6 8 3}$ | 0.0000 | $\mathbf{1 6 8 3}$ | 0.0000 | $\mathbf{2 6 8 3}$ | 0.0000 |
| $\mathbf{6 8 4}$ | 0.0000 | $\mathbf{1 6 8 4}$ | 0.0000 | $\mathbf{2 6 8 4}$ | 0.0000 |
| $\mathbf{6 8 5}$ | 0.0000 | $\mathbf{1 6 8 5}$ | 0.0000 | $\mathbf{2 6 8 5}$ | 0.0000 |
| $\mathbf{6 8 6}$ | 0.0000 | $\mathbf{1 6 8 6}$ | 0.0000 | $\mathbf{2 6 8 6}$ | 0.0000 |
| $\mathbf{6 8 7}$ | 0.0000 | $\mathbf{1 6 8 7}$ | 0.0000 | $\mathbf{2 6 8 7}$ | 0.0000 |
| $\mathbf{6 8 8}$ | 0.0000 | $\mathbf{1 6 8 8}$ | 0.0000 | $\mathbf{2 6 8 8}$ | 0.0000 |
| $\mathbf{6 8 9}$ | 0.0000 | $\mathbf{1 6 8 9}$ | 0.0000 | $\mathbf{2 6 8 9}$ | 0.0000 |
| $\mathbf{6 9 0}$ | 0.0000 | $\mathbf{1 6 9 0}$ | 0.0000 | $\mathbf{2 6 9 0}$ | 0.0000 |
| $\mathbf{6 9 1}$ | 0.0000 | $\mathbf{1 6 9 1}$ | 0.0000 | $\mathbf{2 6 9 1}$ | 0.0000 |
| $\mathbf{6 9 2}$ | 0.0000 | $\mathbf{1 6 9 2}$ | 0.0000 | $\mathbf{2 6 9 2}$ | 0.0000 |
| $\mathbf{6 9 3}$ | 0.0000 | $\mathbf{1 6 9 3}$ | 0.0000 | $\mathbf{2 6 9 3}$ | 0.0000 |
| $\mathbf{6 9 4}$ | 0.0000 | $\mathbf{1 6 9 4}$ | 0.0000 | $\mathbf{2 6 9 4}$ | 0.0000 |
| $\mathbf{6 9 5}$ | 0.0000 | $\mathbf{1 6 9 5}$ | 0.0000 | $\mathbf{2 6 9 5}$ | 0.0000 |
|  |  |  |  |  |  |


| $\mathbf{6 9 6}$ | 0.0000 | $\mathbf{1 6 9 6}$ | 0.0000 | $\mathbf{2 6 9 6}$ | 0.0000 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{6 9 7}$ | 0.0000 | $\mathbf{1 6 9 7}$ | 0.0000 | $\mathbf{2 6 9 7}$ | 0.0000 |
| $\mathbf{6 9 8}$ | 0.0000 | $\mathbf{1 6 9 8}$ | 0.0000 | $\mathbf{2 6 9 8}$ | 0.0000 |
| $\mathbf{6 9 9}$ | 0.0000 | $\mathbf{1 6 9 9}$ | 0.0000 | $\mathbf{2 6 9 9}$ | 0.0000 |
| $\mathbf{7 0 0}$ | 0.0000 | $\mathbf{1 7 0 0}$ | 0.0000 | $\mathbf{2 7 0 0}$ | 0.0000 |
| $\mathbf{7 0 1}$ | 0.0000 | $\mathbf{1 7 0 1}$ | 0.0000 | $\mathbf{2 7 0 1}$ | 0.0000 |
| $\mathbf{7 0 2}$ | 0.0000 | $\mathbf{1 7 0 2}$ | 0.0000 | $\mathbf{2 7 0 2}$ | 0.0000 |
| $\mathbf{7 0 3}$ | 0.0000 | $\mathbf{1 7 0 3}$ | 0.0000 | $\mathbf{2 7 0 3}$ | 0.0000 |
| $\mathbf{7 0 4}$ | 0.0000 | $\mathbf{1 7 0 4}$ | 0.0000 | $\mathbf{2 7 0 4}$ | 0.0000 |
| $\mathbf{7 0 5}$ | 0.0000 | $\mathbf{1 7 0 5}$ | 0.0000 | $\mathbf{2 7 0 5}$ | 0.0000 |
| $\mathbf{7 0 6}$ | 0.0000 | $\mathbf{1 7 0 6}$ | 0.0000 | $\mathbf{2 7 0 6}$ | 0.0000 |
| $\mathbf{7 0 7}$ | 0.0000 | $\mathbf{1 7 0 7}$ | 0.0000 | $\mathbf{2 7 0 7}$ | 0.0000 |
| $\mathbf{7 0 8}$ | 0.0000 | $\mathbf{1 7 0 8}$ | 0.0000 | $\mathbf{2 7 0 8}$ | 0.0000 |
| $\mathbf{7 0 9}$ | 0.0000 | $\mathbf{1 7 0 9}$ | 0.0000 | $\mathbf{2 7 0 9}$ | 0.0000 |
| $\mathbf{7 1 0}$ | 0.0000 | $\mathbf{1 7 1 0}$ | 0.0000 | $\mathbf{2 7 1 0}$ | 0.0000 |
| $\mathbf{7 1 1}$ | 0.0000 | $\mathbf{1 7 1 1}$ | 0.0000 | $\mathbf{2 7 1 1}$ | 0.0000 |
| $\mathbf{7 1 2}$ | 0.0000 | $\mathbf{1 7 1 2}$ | 0.0000 | $\mathbf{2 7 1 2}$ | 0.0000 |
| $\mathbf{7 1 3}$ | 0.0000 | $\mathbf{1 7 1 3}$ | 0.0000 | $\mathbf{2 7 1 3}$ | 0.0000 |
| $\mathbf{7 1 4}$ | 0.0000 | $\mathbf{1 7 1 4}$ | 0.0000 | $\mathbf{2 7 1 4}$ | 0.0000 |
| $\mathbf{7 1 5}$ | 0.0000 | $\mathbf{1 7 1 5}$ | 0.0000 | $\mathbf{2 7 1 5}$ | 0.0000 |
| $\mathbf{7 1 6}$ | 0.0000 | $\mathbf{1 7 1 6}$ | 0.0000 | $\mathbf{2 7 1 6}$ | 0.0000 |
| $\mathbf{7 1 7}$ | 0.0000 | $\mathbf{1 7 1 7}$ | 0.0286 | $\mathbf{2 7 1 7}$ | 0.0000 |
| $\mathbf{7 1 8}$ | 0.0000 | $\mathbf{1 7 1 8}$ | 0.0181 | $\mathbf{2 7 1 8}$ | 0.0000 |
| $\mathbf{7 1 9}$ | 0.0000 | $\mathbf{1 7 1 9}$ | 0.0230 | $\mathbf{2 7 1 9}$ | 0.0000 |
| $\mathbf{7 2 0}$ | 0.0000 | $\mathbf{1 7 2 0}$ | 0.0220 | $\mathbf{2 7 2 0}$ | 0.0000 |
| $\mathbf{7 2 1}$ | 0.0000 | $\mathbf{1 7 2 1}$ | 0.0056 | $\mathbf{2 7 2 1}$ | 0.0000 |
| $\mathbf{7 2 2}$ | 0.0000 | $\mathbf{1 7 2 2}$ | 0.0093 | $\mathbf{2 7 2 2}$ | 0.0000 |
| $\mathbf{7 2 3}$ | 0.0000 | $\mathbf{1 7 2 3}$ | 0.0122 | $\mathbf{2 7 2 3}$ | 0.0000 |
| $\mathbf{7 2 4}$ | 0.0000 | $\mathbf{1 7 2 4}$ | 0.0059 | $\mathbf{2 7 2 4}$ | 0.0000 |
| $\mathbf{7 2 5}$ | 0.0000 | $\mathbf{1 7 2 5}$ | 0.0000 | $\mathbf{2 7 2 5}$ | 0.0000 |
| $\mathbf{7 2 6}$ | 0.0000 | $\mathbf{1 7 2 6}$ | 0.0000 | $\mathbf{2 7 2 6}$ | 0.0000 |
| $\mathbf{7 2 7}$ | 0.0000 | $\mathbf{1 7 2 7}$ | 0.0000 | $\mathbf{2 7 2 7}$ | 0.0906 |
| $\mathbf{7 2 8}$ | 0.0000 | $\mathbf{1 7 2 8}$ | 0.0000 | $\mathbf{2 7 2 8}$ | 0.0354 |
| $\mathbf{7 2 9}$ | 0.0000 | $\mathbf{1 7 2 9}$ | 0.0535 | $\mathbf{2 7 2 9}$ | 0.0632 |
| $\mathbf{7 3 0}$ | 0.0000 | $\mathbf{1 7 3 0}$ | 0.0134 | $\mathbf{2 7 3 0}$ | 0.0960 |
| $\mathbf{7 3 1}$ | 0.0012 | $\mathbf{1 7 3 1}$ | 0.1106 | $\mathbf{2 7 3 1}$ | 0.0484 |
| $\mathbf{7 3 2}$ | 0.0249 | $\mathbf{1 7 3 2}$ | 0.0281 | $\mathbf{2 7 3 2}$ | 0.0459 |
| $\mathbf{7 3 3}$ | 0.0139 | $\mathbf{1 7 3 3}$ | 0.0476 | $\mathbf{2 7 3 3}$ | 0.0625 |
| $\mathbf{7 3 4}$ | 0.0225 | $\mathbf{1 7 3 4}$ | 0.0024 | $\mathbf{2 7 3 4}$ | 0.0422 |
| $\mathbf{7 3 5}$ | 0.0254 | $\mathbf{1 7 3 5}$ | 0.0000 | $\mathbf{2 7 3 5}$ | 0.0706 |


| $\mathbf{7 3 6}$ | 0.0242 | $\mathbf{1 7 3 6}$ | 0.0000 | $\mathbf{2 7 3 6}$ | 0.0000 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{7 3 7}$ | 0.0205 | $\mathbf{1 7 3 7}$ | 0.0364 | $\mathbf{2 7 3 7}$ | 0.0000 |
| $\mathbf{7 3 8}$ | 0.0860 | $\mathbf{1 7 3 8}$ | 0.0200 | $\mathbf{2 7 3 8}$ | 0.0000 |
| $\mathbf{7 3 9}$ | 0.0298 | $\mathbf{1 7 3 9}$ | 0.0386 | $\mathbf{2 7 3 9}$ | 0.0000 |
| $\mathbf{7 4 0}$ | 0.0657 | $\mathbf{1 7 4 0}$ | 0.0567 | $\mathbf{2 7 4 0}$ | 0.0000 |
| $\mathbf{7 4 1}$ | 0.0352 | $\mathbf{1 7 4 1}$ | 0.0747 | $\mathbf{2 7 4 1}$ | 0.0000 |
| $\mathbf{7 4 2}$ | 0.0068 | $\mathbf{1 7 4 2}$ | 0.0537 | $\mathbf{2 7 4 2}$ | 0.0000 |
| $\mathbf{7 4 3}$ | 0.0806 | $\mathbf{1 7 4 3}$ | 0.1426 | $\mathbf{2 7 4 3}$ | 0.0000 |
| $\mathbf{7 4 4}$ | 0.0657 | $\mathbf{1 7 4 4}$ | 0.0476 | $\mathbf{2 7 4 4}$ | 0.0000 |
| $\mathbf{7 4 5}$ | 0.0708 | $\mathbf{1 7 4 5}$ | 0.0713 | $\mathbf{2 7 4 5}$ | 0.0000 |
| $\mathbf{7 4 6}$ | 0.1243 | $\mathbf{1 7 4 6}$ | 0.0281 | $\mathbf{2 7 4 6}$ | 0.0000 |
| $\mathbf{7 4 7}$ | 0.1314 | $\mathbf{1 7 4 7}$ | 0.0674 | $\mathbf{2 7 4 7}$ | 0.0000 |
| $\mathbf{7 4 8}$ | 0.1094 | $\mathbf{1 7 4 8}$ | 0.0559 | $\mathbf{2 7 4 8}$ | 0.0000 |
| $\mathbf{7 4 9}$ | 0.0777 | $\mathbf{1 7 4 9}$ | 0.0650 | $\mathbf{2 7 4 9}$ | 0.0000 |
| $\mathbf{7 5 0}$ | 0.0571 | $\mathbf{1 7 5 0}$ | 0.0298 | $\mathbf{2 7 5 0}$ | 0.0000 |
| $\mathbf{7 5 1}$ | 0.0591 | $\mathbf{1 7 5 1}$ | 0.0073 | $\mathbf{2 7 5 1}$ | 0.0000 |
| $\mathbf{7 5 2}$ | 0.0232 | $\mathbf{1 7 5 2}$ | 0.0200 | $\mathbf{2 7 5 2}$ | 0.0000 |
| $\mathbf{7 5 3}$ | 0.0676 | $\mathbf{1 7 5 3}$ | 0.0313 | $\mathbf{2 7 5 3}$ | 0.0000 |
| $\mathbf{7 5 4}$ | 0.0425 | $\mathbf{1 7 5 4}$ | 0.0662 | $\mathbf{2 7 5 4}$ | 0.0000 |
| $\mathbf{7 5 5}$ | 0.0462 | $\mathbf{1 7 5 5}$ | 0.1045 | $\mathbf{2 7 5 5}$ | 0.0000 |
| $\mathbf{7 5 6}$ | 0.0210 | $\mathbf{1 7 5 6}$ | 0.0518 | $\mathbf{2 7 5 6}$ | 0.0000 |
| $\mathbf{7 5 7}$ | 0.0332 | $\mathbf{1 7 5 7}$ | 0.0581 | $\mathbf{2 7 5 7}$ | 0.0000 |
| $\mathbf{7 5 8}$ | 0.0107 | $\mathbf{1 7 5 8}$ | 0.0247 | $\mathbf{2 7 5 8}$ | 0.0000 |
| $\mathbf{7 5 9}$ | 0.0000 | $\mathbf{1 7 5 9}$ | 0.0308 | $\mathbf{2 7 5 9}$ | 0.0000 |
| $\mathbf{7 6 0}$ | 0.0000 | $\mathbf{1 7 6 0}$ | 0.0325 | $\mathbf{2 7 6 0}$ | 0.0000 |
| $\mathbf{7 6 1}$ | 0.0010 | $\mathbf{1 7 6 1}$ | 0.0234 | $\mathbf{2 7 6 1}$ | 0.0000 |
| $\mathbf{7 6 2}$ | 0.0217 | $\mathbf{1 7 6 2}$ | 0.0447 | $\mathbf{2 7 6 2}$ | 0.0000 |
| $\mathbf{7 6 3}$ | 0.0545 | $\mathbf{1 7 6 3}$ | 0.0383 | $\mathbf{2 7 6 3}$ | 0.0000 |
| $\mathbf{7 6 4}$ | 0.0379 | $\mathbf{1 7 6 4}$ | 0.0203 | $\mathbf{2 7 6 4}$ | 0.0000 |
| $\mathbf{7 6 5}$ | 0.0632 | $\mathbf{1 7 6 5}$ | 0.0339 | $\mathbf{2 7 6 5}$ | 0.0000 |
| $\mathbf{7 6 6}$ | 0.0542 | $\mathbf{1 7 6 6}$ | 0.0227 | $\mathbf{2 7 6 6}$ | 0.0457 |
| $\mathbf{7 6 7}$ | 0.0056 | $\mathbf{1 7 6 7}$ | 0.0393 | $\mathbf{2 7 6 7}$ | 0.0569 |
| $\mathbf{7 6 8}$ | 0.0000 | $\mathbf{1 7 6 8}$ | 0.0166 | $\mathbf{2 7 6 8}$ | 0.0317 |
| $\mathbf{7 6 9}$ | 0.0066 | $\mathbf{1 7 6 9}$ | 0.0100 | $\mathbf{2 7 6 9}$ | 0.0552 |
| $\mathbf{7 7 0}$ | 0.0212 | $\mathbf{1 7 7 0}$ | 0.0000 | $\mathbf{2 7 7 0}$ | 0.0708 |
| $\mathbf{7 7 1}$ | 0.0078 | $\mathbf{1 7 7 1}$ | 0.0000 | $\mathbf{2 7 7 1}$ | 0.0161 |
| $\mathbf{7 7 2}$ | 0.0168 | $\mathbf{1 7 7 2}$ | 0.0078 | $\mathbf{2 7 7 2}$ | 0.0327 |
| $\mathbf{7 7 3}$ | 0.0095 | $\mathbf{1 7 7 3}$ | 0.0195 | $\mathbf{2 7 7 3}$ | 0.0784 |
| $\mathbf{7 7 4}$ | 0.0000 | $\mathbf{1 7 7 4}$ | 0.0112 | $\mathbf{2 7 7 4}$ | 0.0271 |
| $\mathbf{7 7 5}$ | 0.0000 | $\mathbf{1 7 7 5}$ | 0.0186 | $\mathbf{2 7 7 5}$ | 0.0315 |


| $\mathbf{7 7 6}$ | 0.0000 | $\mathbf{1 7 7 6}$ | 0.0147 | $\mathbf{2 7 7 6}$ | 0.0388 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{7 7 7}$ | 0.0000 | $\mathbf{1 7 7 7}$ | 0.0032 | $\mathbf{2 7 7 7}$ | 0.0073 |
| $\mathbf{7 7 8}$ | 0.0000 | $\mathbf{1 7 7 8}$ | 0.0000 | $\mathbf{2 7 7 8}$ | 0.0000 |
| $\mathbf{7 7 9}$ | 0.0000 | $\mathbf{1 7 7 9}$ | 0.0000 | $\mathbf{2 7 7 9}$ | 0.0000 |
| $\mathbf{7 8 0}$ | 0.0000 | $\mathbf{1 7 8 0}$ | 0.0000 | $\mathbf{2 7 8 0}$ | 0.0000 |
| $\mathbf{7 8 1}$ | 0.0000 | $\mathbf{1 7 8 1}$ | 0.0000 | $\mathbf{2 7 8 1}$ | 0.0000 |
| $\mathbf{7 8 2}$ | 0.0000 | $\mathbf{1 7 8 2}$ | 0.0000 | $\mathbf{2 7 8 2}$ | 0.0000 |
| $\mathbf{7 8 3}$ | 0.0000 | $\mathbf{1 7 8 3}$ | 0.0000 | $\mathbf{2 7 8 3}$ | 0.0000 |
| $\mathbf{7 8 4}$ | 0.0000 | $\mathbf{1 7 8 4}$ | 0.0000 | $\mathbf{2 7 8 4}$ | 0.0000 |
| $\mathbf{7 8 5}$ | 0.0000 | $\mathbf{1 7 8 5}$ | 0.0000 | $\mathbf{2 7 8 5}$ | 0.0000 |
| $\mathbf{7 8 6}$ | 0.0000 | $\mathbf{1 7 8 6}$ | 0.0000 | $\mathbf{2 7 8 6}$ | 0.0000 |
| $\mathbf{7 8 7}$ | 0.0000 | $\mathbf{1 7 8 7}$ | 0.0000 | $\mathbf{2 7 8 7}$ | 0.0000 |
| $\mathbf{7 8 8}$ | 0.0000 | $\mathbf{1 7 8 8}$ | 0.0000 | $\mathbf{2 7 8 8}$ | 0.0000 |
| $\mathbf{7 8 9}$ | 0.0000 | $\mathbf{1 7 8 9}$ | 0.0000 | $\mathbf{2 7 8 9}$ | 0.0000 |
| $\mathbf{7 9 0}$ | 0.0000 | $\mathbf{1 7 9 0}$ | 0.0000 | $\mathbf{2 7 9 0}$ | 0.0000 |
| $\mathbf{7 9 1}$ | 0.0000 | $\mathbf{1 7 9 1}$ | 0.0000 | $\mathbf{2 7 9 1}$ | 0.0000 |
| $\mathbf{7 9 2}$ | 0.0000 | $\mathbf{1 7 9 2}$ | 0.0000 | $\mathbf{2 7 9 2}$ | 0.0000 |
| $\mathbf{7 9 3}$ | 0.0000 | $\mathbf{1 7 9 3}$ | 0.0000 | $\mathbf{2 7 9 3}$ | 0.0000 |
| $\mathbf{7 9 4}$ | 0.0000 | $\mathbf{1 7 9 4}$ | 0.0000 | $\mathbf{2 7 9 4}$ | 0.0000 |
| $\mathbf{7 9 5}$ | 0.0000 | $\mathbf{1 7 9 5}$ | 0.0000 | $\mathbf{2 7 9 5}$ | 0.0000 |
| $\mathbf{7 9 6}$ | 0.0000 | $\mathbf{1 7 9 6}$ | 0.0000 | $\mathbf{2 7 9 6}$ | 0.0000 |
| $\mathbf{7 9 7}$ | 0.0000 | $\mathbf{1 7 9 7}$ | 0.0000 | $\mathbf{2 7 9 7}$ | 0.0000 |
| $\mathbf{7 9 8}$ | 0.0000 | $\mathbf{1 7 9 8}$ | 0.0000 | $\mathbf{2 7 9 8}$ | 0.0000 |
| $\mathbf{7 9 9}$ | 0.0000 | $\mathbf{1 7 9 9}$ | 0.0000 | $\mathbf{2 7 9 9}$ | 0.0000 |
| $\mathbf{8 0 0}$ | 0.0000 | $\mathbf{1 8 0 0}$ | 0.0000 | $\mathbf{2 8 0 0}$ | 0.0000 |
| $\mathbf{8 0 1}$ | 0.0000 | $\mathbf{1 8 0 1}$ | 0.0000 | $\mathbf{2 8 0 1}$ | 0.0000 |
| $\mathbf{8 0 2}$ | 0.0000 | $\mathbf{1 8 0 2}$ | 0.0000 | $\mathbf{2 8 0 2}$ | 0.0000 |
| $\mathbf{8 0 3}$ | 0.0000 | $\mathbf{1 8 0 3}$ | 0.0000 | $\mathbf{2 8 0 3}$ | 0.0000 |
| $\mathbf{8 0 4}$ | 0.0000 | $\mathbf{1 8 0 4}$ | 0.0000 | $\mathbf{2 8 0 4}$ | 0.0000 |
| $\mathbf{8 0 5}$ | 0.0000 | $\mathbf{1 8 0 5}$ | 0.0000 | $\mathbf{2 8 0 5}$ | 0.0000 |
| $\mathbf{8 0 6}$ | 0.0000 | $\mathbf{1 8 0 6}$ | 0.0000 | $\mathbf{2 8 0 6}$ | 0.0000 |
| $\mathbf{8 0 7}$ | 0.0000 | $\mathbf{1 8 0 7}$ | 0.0000 | $\mathbf{2 8 0 7}$ | 0.0000 |
| $\mathbf{8 0 8}$ | 0.0000 | $\mathbf{1 8 0 8}$ | 0.0000 | $\mathbf{2 8 0 8}$ | 0.0000 |
| $\mathbf{8 0 9}$ | 0.0000 | $\mathbf{1 8 0 9}$ | 0.0000 | $\mathbf{2 8 0 9}$ | 0.0000 |
| $\mathbf{8 1 0}$ | 0.0000 | $\mathbf{1 8 1 0}$ | 0.0000 | $\mathbf{2 8 1 0}$ | 0.0000 |
| $\mathbf{8 1 1}$ | 0.0000 | $\mathbf{1 8 1 1}$ | 0.0000 | $\mathbf{2 8 1 1}$ | 0.0000 |
| $\mathbf{8 1 2}$ | 0.0000 | $\mathbf{1 8 1 2}$ | 0.0000 | $\mathbf{2 8 1 2}$ | 0.0000 |
| $\mathbf{8 1 3}$ | 0.0000 | $\mathbf{1 8 1 3}$ | 0.0000 | $\mathbf{2 8 1 3}$ | 0.0000 |
| $\mathbf{8 1 4}$ | 0.0000 | $\mathbf{1 8 1 4}$ | 0.0000 | $\mathbf{2 8 1 4}$ | 0.0000 |
| $\mathbf{8 1 5}$ | 0.0000 | $\mathbf{1 8 1 5}$ | 0.0000 | $\mathbf{2 8 1 5}$ | 0.0000 |
|  |  |  |  |  |  |


| $\mathbf{8 1 6}$ | 0.0039 | $\mathbf{1 8 1 6}$ | 0.0000 | $\mathbf{2 8 1 6}$ | 0.0000 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{8 1 7}$ | 0.0098 | $\mathbf{1 8 1 7}$ | 0.0000 | $\mathbf{2 8 1 7}$ | 0.0000 |
| $\mathbf{8 1 8}$ | 0.0051 | $\mathbf{1 8 1 8}$ | 0.0000 | $\mathbf{2 8 1 8}$ | 0.0000 |
| $\mathbf{8 1 9}$ | 0.0068 | $\mathbf{1 8 1 9}$ | 0.0000 | $\mathbf{2 8 1 9}$ | 0.0000 |
| $\mathbf{8 2 0}$ | 0.0000 | $\mathbf{1 8 2 0}$ | 0.0000 | $\mathbf{2 8 2 0}$ | 0.0000 |
| $\mathbf{8 2 1}$ | 0.0000 | $\mathbf{1 8 2 1}$ | 0.0000 | $\mathbf{2 8 2 1}$ | 0.0000 |
| $\mathbf{8 2 2}$ | 0.0000 | $\mathbf{1 8 2 2}$ | 0.0000 | $\mathbf{2 8 2 2}$ | 0.0000 |
| $\mathbf{8 2 3}$ | 0.0313 | $\mathbf{1 8 2 3}$ | 0.0000 | $\mathbf{2 8 2 3}$ | 0.0000 |
| $\mathbf{8 2 4}$ | 0.0168 | $\mathbf{1 8 2 4}$ | 0.0000 | $\mathbf{2 8 2 4}$ | 0.0000 |
| $\mathbf{8 2 5}$ | 0.0230 | $\mathbf{1 8 2 5}$ | 0.0498 | $\mathbf{2 8 2 5}$ | 0.0000 |
| $\mathbf{8 2 6}$ | 0.0063 | $\mathbf{1 8 2 6}$ | 0.0237 | $\mathbf{2 8 2 6}$ | 0.0000 |
| $\mathbf{8 2 7}$ | 0.0242 | $\mathbf{1 8 2 7}$ | 0.0684 | $\mathbf{2 8 2 7}$ | 0.0000 |
| $\mathbf{8 2 8}$ | 0.0117 | $\mathbf{1 8 2 8}$ | 0.0256 | $\mathbf{2 8 2 8}$ | 0.0244 |
| $\mathbf{8 2 9}$ | 0.0781 | $\mathbf{1 8 2 9}$ | 0.0757 | $\mathbf{2 8 2 9}$ | 0.0000 |
| $\mathbf{8 3 0}$ | 0.0115 | $\mathbf{1 8 3 0}$ | 0.0618 | $\mathbf{2 8 3 0}$ | 0.0293 |
| $\mathbf{8 3 1}$ | 0.0515 | $\mathbf{1 8 3 1}$ | 0.0654 | $\mathbf{2 8 3 1}$ | 0.0000 |
| $\mathbf{8 3 2}$ | 0.0256 | $\mathbf{1 8 3 2}$ | 0.0449 | $\mathbf{2 8 3 2}$ | 0.0000 |
| $\mathbf{8 3 3}$ | 0.0217 | $\mathbf{1 8 3 3}$ | 0.0950 | $\mathbf{2 8 3 3}$ | 0.0491 |
| $\mathbf{8 3 4}$ | 0.0205 | $\mathbf{1 8 3 4}$ | 0.0369 | $\mathbf{2 8 3 4}$ | 0.0493 |
| $\mathbf{8 3 5}$ | 0.0288 | $\mathbf{1 8 3 5}$ | 0.0000 | $\mathbf{2 8 3 5}$ | 0.1380 |
| $\mathbf{8 3 6}$ | 0.0000 | $\mathbf{1 8 3 6}$ | 0.0000 | $\mathbf{2 8 3 6}$ | 0.0000 |
| $\mathbf{8 3 7}$ | 0.0000 | $\mathbf{1 8 3 7}$ | 0.0000 | $\mathbf{2 8 3 7}$ | 0.0000 |
| $\mathbf{8 3 8}$ | 0.0181 | $\mathbf{1 8 3 8}$ | 0.0000 | $\mathbf{2 8 3 8}$ | 0.0000 |
| $\mathbf{8 3 9}$ | 0.0488 | $\mathbf{1 8 3 9}$ | 0.0000 | $\mathbf{2 8 3 9}$ | 0.0000 |
| $\mathbf{8 4 0}$ | 0.0308 | $\mathbf{1 8 4 0}$ | 0.0000 | $\mathbf{2 8 4 0}$ | 0.0000 |
| $\mathbf{8 4 1}$ | 0.0640 | $\mathbf{1 8 4 1}$ | 0.0000 | $\mathbf{2 8 4 1}$ | 0.0000 |
| $\mathbf{8 4 2}$ | 0.0000 | $\mathbf{1 8 4 2}$ | 0.0000 | $\mathbf{2 8 4 2}$ | 0.0000 |
| $\mathbf{8 4 3}$ | 0.0063 | $\mathbf{1 8 4 3}$ | 0.0000 | $\mathbf{2 8 4 3}$ | 0.0000 |
| $\mathbf{8 4 4}$ | 0.0129 | $\mathbf{1 8 4 4}$ | 0.0000 | $\mathbf{2 8 4 4}$ | 0.0000 |
| $\mathbf{8 4 5}$ | 0.0156 | $\mathbf{1 8 4 5}$ | 0.0000 | $\mathbf{2 8 4 5}$ | 0.0000 |
| $\mathbf{8 4 6}$ | 0.0037 | $\mathbf{1 8 4 6}$ | 0.0000 | $\mathbf{2 8 4 6}$ | 0.0000 |
| $\mathbf{8 4 7}$ | 0.0606 | $\mathbf{1 8 4 7}$ | 0.0000 | $\mathbf{2 8 4 7}$ | 0.0000 |
| $\mathbf{8 4 8}$ | 0.0261 | $\mathbf{1 8 4 8}$ | 0.0000 | $\mathbf{2 8 4 8}$ | 0.0000 |
| $\mathbf{8 4 9}$ | 0.0364 | $\mathbf{1 8 4 9}$ | 0.0000 | $\mathbf{2 8 4 9}$ | 0.0000 |
| $\mathbf{8 5 0}$ | 0.0000 | $\mathbf{1 8 5 0}$ | 0.0000 | $\mathbf{2 8 5 0}$ | 0.0000 |
| $\mathbf{8 5 1}$ | 0.0000 | $\mathbf{1 8 5 1}$ | 0.0000 | $\mathbf{2 8 5 1}$ | 0.0000 |
| $\mathbf{8 5 2}$ | 0.0000 | $\mathbf{1 8 5 2}$ | 0.0000 | $\mathbf{2 8 5 2}$ | 0.0000 |
| $\mathbf{8 5 3}$ | 0.0239 | $\mathbf{1 8 5 3}$ | 0.0000 | $\mathbf{2 8 5 3}$ | 0.0000 |
| $\mathbf{8 5 4}$ | 0.0227 | $\mathbf{1 8 5 4}$ | 0.0000 | $\mathbf{2 8 5 4}$ | 0.0000 |
| $\mathbf{8 5 5}$ | 0.0525 | $\mathbf{1 8 5 5}$ | 0.0000 | $\mathbf{2 8 5 5}$ | 0.0000 |
|  |  |  |  |  |  |


| $\mathbf{8 5 6}$ | 0.0103 | $\mathbf{1 8 5 6}$ | 0.0000 | $\mathbf{2 8 5 6}$ | 0.0000 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{8 5 7}$ | 0.0129 | $\mathbf{1 8 5 7}$ | 0.0000 | $\mathbf{2 8 5 7}$ | 0.0000 |
| $\mathbf{8 5 8}$ | 0.0112 | $\mathbf{1 8 5 8}$ | 0.0000 | $\mathbf{2 8 5 8}$ | 0.0000 |
| $\mathbf{8 5 9}$ | 0.0037 | $\mathbf{1 8 5 9}$ | 0.0000 | $\mathbf{2 8 5 9}$ | 0.0000 |
| $\mathbf{8 6 0}$ | 0.0364 | $\mathbf{1 8 6 0}$ | 0.0000 | $\mathbf{2 8 6 0}$ | 0.0000 |
| $\mathbf{8 6 1}$ | 0.0222 | $\mathbf{1 8 6 1}$ | 0.0000 | $\mathbf{2 8 6 1}$ | 0.0000 |
| $\mathbf{8 6 2}$ | 0.0349 | $\mathbf{1 8 6 2}$ | 0.0000 | $\mathbf{2 8 6 2}$ | 0.0000 |
| $\mathbf{8 6 3}$ | 0.0654 | $\mathbf{1 8 6 3}$ | 0.0000 | $\mathbf{2 8 6 3}$ | 0.0000 |
| $\mathbf{8 6 4}$ | 0.0217 | $\mathbf{1 8 6 4}$ | 0.0000 | $\mathbf{2 8 6 4}$ | 0.0000 |
| $\mathbf{8 6 5}$ | 0.0190 | $\mathbf{1 8 6 5}$ | 0.0000 | $\mathbf{2 8 6 5}$ | 0.0000 |
| $\mathbf{8 6 6}$ | 0.0237 | $\mathbf{1 8 6 6}$ | 0.0359 | $\mathbf{2 8 6 6}$ | 0.0603 |
| $\mathbf{8 6 7}$ | 0.0007 | $\mathbf{1 8 6 7}$ | 0.0044 | $\mathbf{2 8 6 7}$ | 0.0403 |
| $\mathbf{8 6 8}$ | 0.0000 | $\mathbf{1 8 6 8}$ | 0.0000 | $\mathbf{2 8 6 8}$ | 0.0186 |
| $\mathbf{8 6 9}$ | 0.0000 | $\mathbf{1 8 6 9}$ | 0.0000 | $\mathbf{2 8 6 9}$ | 0.0134 |
| $\mathbf{8 7 0}$ | 0.0000 | $\mathbf{1 8 7 0}$ | 0.0000 | $\mathbf{2 8 7 0}$ | 0.0166 |
| $\mathbf{8 7 1}$ | 0.0000 | $\mathbf{1 8 7 1}$ | 0.0000 | $\mathbf{2 8 7 1}$ | 0.0066 |
| $\mathbf{8 7 2}$ | 0.0046 | $\mathbf{1 8 7 2}$ | 0.0171 | $\mathbf{2 8 7 2}$ | 0.0078 |
| $\mathbf{8 7 3}$ | 0.0151 | $\mathbf{1 8 7 3}$ | 0.0755 | $\mathbf{2 8 7 3}$ | 0.0274 |
| $\mathbf{8 7 4}$ | 0.0178 | $\mathbf{1 8 7 4}$ | 0.0276 | $\mathbf{2 8 7 4}$ | 0.0200 |
| $\mathbf{8 7 5}$ | 0.0171 | $\mathbf{1 8 7 5}$ | 0.0366 | $\mathbf{2 8 7 5}$ | 0.0183 |
| $\mathbf{8 7 6}$ | 0.0098 | $\mathbf{1 8 7 6}$ | 0.0230 | $\mathbf{2 8 7 6}$ | 0.0164 |
| $\mathbf{8 7 7}$ | 0.0000 | $\mathbf{1 8 7 7}$ | 0.0085 | $\mathbf{2 8 7 7}$ | 0.0044 |
| $\mathbf{8 7 8}$ | 0.0000 | $\mathbf{1 8 7 8}$ | 0.0000 | $\mathbf{2 8 7 8}$ | 0.0000 |
| $\mathbf{8 7 9}$ | 0.0000 | $\mathbf{1 8 7 9}$ | 0.0000 | $\mathbf{2 8 7 9}$ | 0.0000 |
| $\mathbf{8 8 0}$ | 0.0000 | $\mathbf{1 8 8 0}$ | 0.0000 | $\mathbf{2 8 8 0}$ | 0.0000 |
| $\mathbf{8 8 1}$ | 0.0000 | $\mathbf{1 8 8 1}$ | 0.0000 | $\mathbf{2 8 8 1}$ | 0.0000 |
| $\mathbf{8 8 2}$ | 0.0000 | $\mathbf{1 8 8 2}$ | 0.0000 | $\mathbf{2 8 8 2}$ | 0.0000 |
| $\mathbf{8 8 3}$ | 0.0000 | $\mathbf{1 8 8 3}$ | 0.0000 | $\mathbf{2 8 8 3}$ | 0.0000 |
| $\mathbf{8 8 4}$ | 0.0000 | $\mathbf{1 8 8 4}$ | 0.0000 | $\mathbf{2 8 8 4}$ | 0.0000 |
| $\mathbf{8 8 5}$ | 0.0000 | $\mathbf{1 8 8 5}$ | 0.0000 | $\mathbf{2 8 8 5}$ | 0.0000 |
| $\mathbf{8 8 6}$ | 0.0000 | $\mathbf{1 8 8 6}$ | 0.0000 | $\mathbf{2 8 8 6}$ | 0.0000 |
| $\mathbf{8 8 7}$ | 0.0000 | $\mathbf{1 8 8 7}$ | 0.0000 | $\mathbf{2 8 8 7}$ | 0.0000 |
| $\mathbf{8 8 8}$ | 0.0000 | $\mathbf{1 8 8 8}$ | 0.0000 | $\mathbf{2 8 8 8}$ | 0.0000 |
| $\mathbf{8 8 9}$ | 0.0000 | $\mathbf{1 8 8 9}$ | 0.0000 | $\mathbf{2 8 8 9}$ | 0.0000 |
| $\mathbf{8 9 0}$ | 0.0000 | $\mathbf{1 8 9 0}$ | 0.0000 | $\mathbf{2 8 9 0}$ | 0.0000 |
| $\mathbf{8 9 1}$ | 0.0000 | $\mathbf{1 8 9 1}$ | 0.0000 | $\mathbf{2 8 9 1}$ | 0.0000 |
| $\mathbf{8 9 2}$ | 0.0000 | $\mathbf{1 8 9 2}$ | 0.0000 | $\mathbf{2 8 9 2}$ | 0.0000 |
| $\mathbf{8 9 3}$ | 0.0000 | $\mathbf{1 8 9 3}$ | 0.0000 | $\mathbf{2 8 9 3}$ | 0.0000 |
| $\mathbf{8 9 4}$ | 0.0000 | $\mathbf{1 8 9 4}$ | 0.0000 | $\mathbf{2 8 9 4}$ | 0.0000 |
| $\mathbf{8 9 5}$ | 0.0000 | $\mathbf{1 8 9 5}$ | 0.0000 | $\mathbf{2 8 9 5}$ | 0.0000 |
|  |  |  |  |  |  |


| $\mathbf{8 9 6}$ | 0.0000 | $\mathbf{1 8 9 6}$ | 0.0000 | $\mathbf{2 8 9 6}$ | 0.0000 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{8 9 7}$ | 0.0000 | $\mathbf{1 8 9 7}$ | 0.0000 | $\mathbf{2 8 9 7}$ | 0.0000 |
| $\mathbf{8 9 8}$ | 0.0000 | $\mathbf{1 8 9 8}$ | 0.0000 | $\mathbf{2 8 9 8}$ | 0.0000 |
| $\mathbf{8 9 9}$ | 0.0000 | $\mathbf{1 8 9 9}$ | 0.0000 | $\mathbf{2 8 9 9}$ | 0.0000 |
| $\mathbf{9 0 0}$ | 0.0000 | $\mathbf{1 9 0 0}$ | 0.0000 | $\mathbf{2 9 0 0}$ | 0.0000 |
| $\mathbf{9 0 1}$ | 0.0000 | $\mathbf{1 9 0 1}$ | 0.0000 | $\mathbf{2 9 0 1}$ | 0.0000 |
| $\mathbf{9 0 2}$ | 0.0000 | $\mathbf{1 9 0 2}$ | 0.0000 | $\mathbf{2 9 0 2}$ | 0.0000 |
| $\mathbf{9 0 3}$ | 0.0000 | $\mathbf{1 9 0 3}$ | 0.0000 | $\mathbf{2 9 0 3}$ | 0.0000 |
| $\mathbf{9 0 4}$ | 0.0000 | $\mathbf{1 9 0 4}$ | 0.0000 | $\mathbf{2 9 0 4}$ | 0.0000 |
| $\mathbf{9 0 5}$ | 0.0000 | $\mathbf{1 9 0 5}$ | 0.0000 | $\mathbf{2 9 0 5}$ | 0.0000 |
| $\mathbf{9 0 6}$ | 0.0000 | $\mathbf{1 9 0 6}$ | 0.0000 | $\mathbf{2 9 0 6}$ | 0.0000 |
| $\mathbf{9 0 7}$ | 0.0000 | $\mathbf{1 9 0 7}$ | 0.0000 | $\mathbf{2 9 0 7}$ | 0.0000 |
| $\mathbf{9 0 8}$ | 0.0000 | $\mathbf{1 9 0 8}$ | 0.0000 | $\mathbf{2 9 0 8}$ | 0.0000 |
| $\mathbf{9 0 9}$ | 0.0000 | $\mathbf{1 9 0 9}$ | 0.0000 | $\mathbf{2 9 0 9}$ | 0.0000 |
| $\mathbf{9 1 0}$ | 0.0000 | $\mathbf{1 9 1 0}$ | 0.0000 | $\mathbf{2 9 1 0}$ | 0.0000 |
| $\mathbf{9 1 1}$ | 0.0000 | $\mathbf{1 9 1 1}$ | 0.0000 | $\mathbf{2 9 1 1}$ | 0.0000 |
| $\mathbf{9 1 2}$ | 0.0000 | $\mathbf{1 9 1 2}$ | 0.0000 | $\mathbf{2 9 1 2}$ | 0.0000 |
| $\mathbf{9 1 3}$ | 0.0000 | $\mathbf{1 9 1 3}$ | 0.0000 | $\mathbf{2 9 1 3}$ | 0.0000 |
| $\mathbf{9 1 4}$ | 0.0000 | $\mathbf{1 9 1 4}$ | 0.0000 | $\mathbf{2 9 1 4}$ | 0.0000 |
| $\mathbf{9 1 5}$ | 0.0000 | $\mathbf{1 9 1 5}$ | 0.0000 | $\mathbf{2 9 1 5}$ | 0.0000 |
| $\mathbf{9 1 6}$ | 0.0000 | $\mathbf{1 9 1 6}$ | 0.0000 | $\mathbf{2 9 1 6}$ | 0.0000 |
| $\mathbf{9 1 7}$ | 0.0000 | $\mathbf{1 9 1 7}$ | 0.0000 | $\mathbf{2 9 1 7}$ | 0.0000 |
| $\mathbf{9 1 8}$ | 0.0000 | $\mathbf{1 9 1 8}$ | 0.0000 | $\mathbf{2 9 1 8}$ | 0.0000 |
| $\mathbf{9 1 9}$ | 0.0000 | $\mathbf{1 9 1 9}$ | 0.0000 | $\mathbf{2 9 1 9}$ | 0.0254 |
| $\mathbf{9 2 0}$ | 0.0000 | $\mathbf{1 9 2 0}$ | 0.0000 | $\mathbf{2 9 2 0}$ | 0.0339 |
| $\mathbf{9 2 1}$ | 0.0000 | $\mathbf{1 9 2 1}$ | 0.0000 | $\mathbf{2 9 2 1}$ | 0.0127 |
| $\mathbf{9 2 2}$ | 0.0000 | $\mathbf{1 9 2 2}$ | 0.0000 | $\mathbf{2 9 2 2}$ | 0.0442 |
| $\mathbf{9 2 3}$ | 0.0000 | $\mathbf{1 9 2 3}$ | 0.0000 | $\mathbf{2 9 2 3}$ | 0.0242 |
| $\mathbf{9 2 4}$ | 0.0000 | $\mathbf{1 9 2 4}$ | 0.0000 | $\mathbf{2 9 2 4}$ | 0.0059 |
| $\mathbf{9 2 5}$ | 0.0344 | $\mathbf{1 9 2 5}$ | 0.0000 | $\mathbf{2 9 2 5}$ | 0.0076 |
| $\mathbf{9 2 6}$ | 0.0593 | $\mathbf{1 9 2 6}$ | 0.0000 | $\mathbf{2 9 2 6}$ | 0.0369 |
| $\mathbf{9 2 7}$ | 0.0383 | $\mathbf{1 9 2 7}$ | 0.0000 | $\mathbf{2 9 2 7}$ | 0.0000 |
| $\mathbf{9 2 8}$ | 0.0437 | $\mathbf{1 9 2 8}$ | 0.0000 | $\mathbf{2 9 2 8}$ | 0.0466 |
| $\mathbf{9 2 9}$ | 0.0632 | $\mathbf{1 9 2 9}$ | 0.0000 | $\mathbf{2 9 2 9}$ | 0.0000 |
| $\mathbf{9 3 0}$ | 0.0696 | $\mathbf{1 9 3 0}$ | 0.0000 | $\mathbf{2 9 3 0}$ | 0.0449 |
| $\mathbf{9 3 1}$ | 0.0689 | $\mathbf{1 9 3 1}$ | 0.0000 | $\mathbf{2 9 3 1}$ | 0.0249 |
| $\mathbf{9 3 2}$ | 0.0327 | $\mathbf{1 9 3 2}$ | 0.0000 | $\mathbf{2 9 3 2}$ | 0.0278 |
| $\mathbf{9 3 3}$ | 0.0855 | $\mathbf{1 9 3 3}$ | 0.0591 | $\mathbf{2 9 3 3}$ | 0.0000 |
| $\mathbf{9 3 4}$ | 0.0208 | $\mathbf{1 9 3 4}$ | 0.0708 | $\mathbf{2 9 3 4}$ | 0.0000 |
| $\mathbf{9 3 5}$ | 0.0264 | $\mathbf{1 9 3 5}$ | 0.0249 | $\mathbf{2 9 3 5}$ | 0.0000 |
|  |  |  |  |  |  |


| $\mathbf{9 3 6}$ | 0.0269 | $\mathbf{1 9 3 6}$ | 0.0000 | $\mathbf{2 9 3 6}$ | 0.0000 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{9 3 7}$ | 0.0000 | $\mathbf{1 9 3 7}$ | 0.0000 | $\mathbf{2 9 3 7}$ | 0.0000 |
| $\mathbf{9 3 8}$ | 0.0000 | $\mathbf{1 9 3 8}$ | 0.0000 | $\mathbf{2 9 3 8}$ | 0.0000 |
| $\mathbf{9 3 9}$ | 0.1033 | $\mathbf{1 9 3 9}$ | 0.0000 | $\mathbf{2 9 3 9}$ | 0.0000 |
| $\mathbf{9 4 0}$ | 0.1375 | $\mathbf{1 9 4 0}$ | 0.0000 | $\mathbf{2 9 4 0}$ | 0.0000 |
| $\mathbf{9 4 1}$ | 0.1006 | $\mathbf{1 9 4 1}$ | 0.0000 | $\mathbf{2 9 4 1}$ | 0.0000 |
| $\mathbf{9 4 2}$ | 0.1114 | $\mathbf{1 9 4 2}$ | 0.0000 | $\mathbf{2 9 4 2}$ | 0.0000 |
| $\mathbf{9 4 3}$ | 0.1131 | $\mathbf{1 9 4 3}$ | 0.0000 | $\mathbf{2 9 4 3}$ | 0.0000 |
| $\mathbf{9 4 4}$ | 0.0708 | $\mathbf{1 9 4 4}$ | 0.0000 | $\mathbf{2 9 4 4}$ | 0.0000 |
| $\mathbf{9 4 5}$ | 0.0823 | $\mathbf{1 9 4 5}$ | 0.0000 | $\mathbf{2 9 4 5}$ | 0.0000 |
| $\mathbf{9 4 6}$ | 0.0659 | $\mathbf{1 9 4 6}$ | 0.0000 | $\mathbf{2 9 4 6}$ | 0.0000 |
| $\mathbf{9 4 7}$ | 0.0095 | $\mathbf{1 9 4 7}$ | 0.0000 | $\mathbf{2 9 4 7}$ | 0.0339 |
| $\mathbf{9 4 8}$ | 0.0142 | $\mathbf{1 9 4 8}$ | 0.0000 | $\mathbf{2 9 4 8}$ | 0.0254 |
| $\mathbf{9 4 9}$ | 0.0274 | $\mathbf{1 9 4 9}$ | 0.0000 | $\mathbf{2 9 4 9}$ | 0.0000 |
| $\mathbf{9 5 0}$ | 0.0315 | $\mathbf{1 9 5 0}$ | 0.0000 | $\mathbf{2 9 5 0}$ | 0.0000 |
| $\mathbf{9 5 1}$ | 0.0405 | $\mathbf{1 9 5 1}$ | 0.0000 | $\mathbf{2 9 5 1}$ | 0.0000 |
| $\mathbf{9 5 2}$ | 0.0520 | $\mathbf{1 9 5 2}$ | 0.0000 | $\mathbf{2 9 5 2}$ | 0.0000 |
| $\mathbf{9 5 3}$ | 0.1368 | $\mathbf{1 9 5 3}$ | 0.0000 | $\mathbf{2 9 5 3}$ | 0.0000 |
| $\mathbf{9 5 4}$ | 0.0611 | $\mathbf{1 9 5 4}$ | 0.0000 | $\mathbf{2 9 5 4}$ | 0.0000 |
| $\mathbf{9 5 5}$ | 0.0305 | $\mathbf{1 9 5 5}$ | 0.0000 | $\mathbf{2 9 5 5}$ | 0.0000 |
| $\mathbf{9 5 6}$ | 0.0376 | $\mathbf{1 9 5 6}$ | 0.0000 | $\mathbf{2 9 5 6}$ | 0.0000 |
| $\mathbf{9 5 7}$ | 0.0000 | $\mathbf{1 9 5 7}$ | 0.0000 | $\mathbf{2 9 5 7}$ | 0.0000 |
| $\mathbf{9 5 8}$ | 0.0132 | $\mathbf{1 9 5 8}$ | 0.0000 | $\mathbf{2 9 5 8}$ | 0.0000 |
| $\mathbf{9 5 9}$ | 0.0527 | $\mathbf{1 9 5 9}$ | 0.0000 | $\mathbf{2 9 5 9}$ | 0.0000 |
| $\mathbf{9 6 0}$ | 0.0882 | $\mathbf{1 9 6 0}$ | 0.0000 | $\mathbf{2 9 6 0}$ | 0.0000 |
| $\mathbf{9 6 1}$ | 0.0479 | $\mathbf{1 9 6 1}$ | 0.0000 | $\mathbf{2 9 6 1}$ | 0.0000 |
| $\mathbf{9 6 2}$ | 0.1319 | $\mathbf{1 9 6 2}$ | 0.0000 | $\mathbf{2 9 6 2}$ | 0.0000 |
| $\mathbf{9 6 3}$ | 0.1038 | $\mathbf{1 9 6 3}$ | 0.0000 | $\mathbf{2 9 6 3}$ | 0.0000 |
| $\mathbf{9 6 4}$ | 0.0266 | $\mathbf{1 9 6 4}$ | 0.0000 | $\mathbf{2 9 6 4}$ | 0.0000 |
| $\mathbf{9 6 5}$ | 0.0366 | $\mathbf{1 9 6 5}$ | 0.0000 | $\mathbf{2 9 6 5}$ | 0.0000 |
| $\mathbf{9 6 6}$ | 0.0171 | $\mathbf{1 9 6 6}$ | 0.0000 | $\mathbf{2 9 6 6}$ | 0.0625 |
| $\mathbf{9 6 7}$ | 0.0000 | $\mathbf{1 9 6 7}$ | 0.0000 | $\mathbf{2 9 6 7}$ | 0.0339 |
| $\mathbf{9 6 8}$ | 0.0000 | $\mathbf{1 9 6 8}$ | 0.0000 | $\mathbf{2 9 6 8}$ | 0.0320 |
| $\mathbf{9 6 9}$ | 0.0000 | $\mathbf{1 9 6 9}$ | 0.0000 | $\mathbf{2 9 6 9}$ | 0.0234 |
| $\mathbf{9 7 0}$ | 0.0000 | $\mathbf{1 9 7 0}$ | 0.0000 | $\mathbf{2 9 7 0}$ | 0.0210 |
| $\mathbf{9 7 1}$ | 0.0000 | $\mathbf{1 9 7 1}$ | 0.0134 | $\mathbf{2 9 7 1}$ | 0.0359 |
| $\mathbf{9 7 2}$ | 0.0081 | $\mathbf{1 9 7 2}$ | 0.0244 | $\mathbf{2 9 7 2}$ | 0.0400 |
| $\mathbf{9 7 3}$ | 0.0195 | $\mathbf{1 9 7 3}$ | 0.0339 | $\mathbf{2 9 7 3}$ | 0.0447 |
| $\mathbf{9 7 4}$ | 0.0222 | $\mathbf{1 9 7 4}$ | 0.0354 | $\mathbf{2 9 7 4}$ | 0.0554 |
| $\mathbf{9 7 5}$ | 0.0203 | $\mathbf{1 9 7 5}$ | 0.0230 | $\mathbf{2 9 7 5}$ | 0.0310 |


| $\mathbf{9 7 6}$ | 0.0149 | $\mathbf{1 9 7 6}$ | 0.0168 | $\mathbf{2 9 7 6}$ | 0.0103 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{9 7 7}$ | 0.0039 | $\mathbf{1 9 7 7}$ | 0.0034 | $\mathbf{2 9 7 7}$ | 0.0000 |
| $\mathbf{9 7 8}$ | 0.0000 | $\mathbf{1 9 7 8}$ | 0.0000 | $\mathbf{2 9 7 8}$ | 0.0000 |
| $\mathbf{9 7 9}$ | 0.0000 | $\mathbf{1 9 7 9}$ | 0.0000 | $\mathbf{2 9 7 9}$ | 0.0000 |
| $\mathbf{9 8 0}$ | 0.0000 | $\mathbf{1 9 8 0}$ | 0.0000 | $\mathbf{2 9 8 0}$ | 0.0000 |
| $\mathbf{9 8 1}$ | 0.0000 | $\mathbf{1 9 8 1}$ | 0.0000 | $\mathbf{2 9 8 1}$ | 0.0000 |
| $\mathbf{9 8 2}$ | 0.0000 | $\mathbf{1 9 8 2}$ | 0.0000 | $\mathbf{2 9 8 2}$ | 0.0000 |
| $\mathbf{9 8 3}$ | 0.0000 | $\mathbf{1 9 8 3}$ | 0.0000 | $\mathbf{2 9 8 3}$ | 0.0000 |
| $\mathbf{9 8 4}$ | 0.0000 | $\mathbf{1 9 8 4}$ | 0.0000 | $\mathbf{2 9 8 4}$ | 0.0000 |
| $\mathbf{9 8 5}$ | 0.0000 | $\mathbf{1 9 8 5}$ | 0.0000 | $\mathbf{2 9 8 5}$ | 0.0000 |
| $\mathbf{9 8 6}$ | 0.0000 | $\mathbf{1 9 8 6}$ | 0.0000 | $\mathbf{2 9 8 6}$ | 0.0000 |
| $\mathbf{9 8 7}$ | 0.0000 | $\mathbf{1 9 8 7}$ | 0.0000 | $\mathbf{2 9 8 7}$ | 0.0000 |
| $\mathbf{9 8 8}$ | 0.0000 | $\mathbf{1 9 8 8}$ | 0.0000 | $\mathbf{2 9 8 8}$ | 0.0000 |
| $\mathbf{9 8 9}$ | 0.0000 | $\mathbf{1 9 8 9}$ | 0.0000 | $\mathbf{2 9 8 9}$ | 0.0000 |
| $\mathbf{9 9 0}$ | 0.0000 | $\mathbf{1 9 9 0}$ | 0.0000 | $\mathbf{2 9 9 0}$ | 0.0000 |
| $\mathbf{9 9 1}$ | 0.0000 | $\mathbf{1 9 9 1}$ | 0.0000 | $\mathbf{2 9 9 1}$ | 0.0000 |
| $\mathbf{9 9 2}$ | 0.0000 | $\mathbf{1 9 9 2}$ | 0.0000 | $\mathbf{2 9 9 2}$ | 0.0000 |
| $\mathbf{9 9 3}$ | 0.0000 | $\mathbf{1 9 9 3}$ | 0.0000 | $\mathbf{2 9 9 3}$ | 0.0000 |
| $\mathbf{9 9 4}$ | 0.0000 | $\mathbf{1 9 9 4}$ | 0.0000 | $\mathbf{2 9 9 4}$ | 0.0000 |
| $\mathbf{9 9 5}$ | 0.0000 | $\mathbf{1 9 9 5}$ | 0.0000 | $\mathbf{2 9 9 5}$ | 0.0000 |
| $\mathbf{9 9 6}$ | 0.0000 | $\mathbf{1 9 9 6}$ | 0.0000 | $\mathbf{2 9 9 6}$ | 0.0000 |
| $\mathbf{9 9 7}$ | 0.0000 | $\mathbf{1 9 9 7}$ | 0.0000 | $\mathbf{2 9 9 7}$ | 0.0000 |
| $\mathbf{9 9 8}$ | 0.0000 | $\mathbf{1 9 9 8}$ | 0.0000 | $\mathbf{2 9 9 8}$ | 0.0000 |
| $\mathbf{9 9 9}$ | 0.0000 | $\mathbf{1 9 9 9}$ | 0.0000 | $\mathbf{2 9 9 9}$ | 0.0000 |
| $\mathbf{1 0 0 0}$ | 0.0000 | $\mathbf{2 0 0 0}$ | 0.0000 | $\mathbf{3 0 0 0}$ | 0.0000 |
|  |  |  |  |  |  |

### 1.7 Regression Convolutional Neural Network (RCNN)

clc;
clear;
close all;
for $\mathrm{c}=1: 1$
$\mathrm{SD}=3 ;$

ILR $=0.01$;
$\mathrm{M}=0.8 ;$
$\mathrm{R}=1 \mathrm{e}-10 ;$

## \%Load and Explore Image Data

ArtificialPorosityImagesDatasetPath $=$ fullfile('/nfshome','store02','users','c.c 1881324','Documents','MATLAB','3000 Slices','*.jpg');
[XTraining,YTrainingPoP,XValidation, YV alidationPoP,XTesting, $\mathrm{YTestingPoP]} \mathrm{=}$ loadAPIData(ArtificialPorosityImagesDatasetPath);

## \%Specify Convolutional Neural Network Architecture

imageSize $=[650630$ 3];
layersPoP $=[$
imageInputLayer(imageSize)
convBlock(5,8, SD(c))
averagePooling2dLayer(4,'Stride',4)
convBlock(5,16, SD(c))
averagePooling2dLayer(4,'Stride',4)

```
convBlock(5,32,SD(c))
```

averagePooling2dLayer(4,'Stride',4)
convBlock(5,64, SD(c))
averagePooling2dLayer(4,'Stride',4)
convBlock(5,128, SD(c))
fullyConnectedLayer(1)
regressionLayer];
miniBatchSize $=64$;
validationFrequency $=$ floor $(1800 /$ miniBatchSize $)$;
optionsPoP $=$ trainingOptions('sgdm', $\ldots$
'InitialLearnRate', ILR(c), ...
'Momentum', M(c), ...
'L2Regularization', R(c), ...
'MaxEpochs',20, ...
'MiniBatchSize',miniBatchSize, ...
'ValidationFrequency',validationFrequency, ...
'ValidationData', $\{$ XValidation, YValidationPoP(:,1)\}, ...
'Shuffle','every-epoch', ...
'Plots','training-progress');

## \%Train Network using Training Data

netPoP = trainNetwork(XTraining,YTrainingPoP(:,1),layersPoP,optionsPoP);

## \%Predict Responses and Compute Accuracy and Error

PredictedTrainingPoP(:,c) = predict(netPoP,XTraining);
PredictedValidationPoP(:,c) = predict(netPoP,XValidation);
PredictedTestingPoP(:,c) = predict(netPoP,XTesting);

TrainingError $(:, \mathrm{c})=\mathrm{YTrainingPoP}(:, 1)-\operatorname{PredictedTrainingPoP(:,c);~}$
AbsoluteTrainingError(:,c) $=\operatorname{abs}($ TrainingError(:,c) $)$;
AverageTrainingError(:,c) $=\operatorname{sum}($ AbsoluteTrainingError(:,c))$) / 1800$;
numCorrectTrainingPoP(:,c) = sum(abs(TrainingError(:,(c))) < 0.05);
TrainingAccuracyPoP(:,c) $=($ numCorrectTrainingPoP(:,(c))/1800)*100;

ValidationError(:,c) = YValidationPoP(:,1) - PredictedValidationPoP(:,c);
AbsoluteValidationError(:,c) $=\operatorname{abs}($ ValidationError(:, c) $)$;
AverageValidationError(:,c) $=\operatorname{sum}($ AbsoluteValidationError(:, c) )/600;
numCorrectValidationPoP(:,c) $=\operatorname{sum}(\operatorname{abs}($ ValidationError(:,(c))) < 0.05);

ValidationAccuracyPoP(:,c) $=($ numCorrectValidationPoP(:,(c))/600)*100;

TestingError(:,c) = YTestingPoP(:,1) - PredictedTestingPoP(:,c);
AbsoluteTestingError(:,c) $=$ abs(TestingError(:,c));
AverageTestingError(:,c) = sum(AbsoluteTestingError(:,c))/600;
numCorrectTestingPoP(:,c) $=\operatorname{sum}(\operatorname{abs}($ TestingError(:,(c))) < 0.05);
TestingAccuracyPoP(:,c) = (numCorrectTestingPoP(:,(c))/600)*100;
end
function layers $=$ convBlock(FilterSize,NumberofFilters,SectionDepth)
layers $=[$
convolution2dLayer(FilterSize,NumberofFilters,'Padding','same')
batchNormalizationLayer
reluLayer];
layers $=$ repmat(layers,SectionDepth,1);
end
function [XTraining, YTrainingPoP,XValidation, YV alidationPoP,XTesting, $\mathrm{YTestingPoP]}$
$=$ loadAPIData(ArtificialPorosityImagesDatasetPath)
location $=\operatorname{dir}($ ArtificialPorosityImagesDatasetPath $)$;

Percent_of_Porosity = Actual_Percent_of_Porosity;

RN = [1834 9199352202897189132675210627254241690900154825962947505 18022706149264827931652726185917692022878564210964656623762163 51824968985221049219225192221620121121522191261761828777697571692 16421555542779471509982554138228692633413280129342262132727701575 2881926274925736952100128110522511754279578326561446237120922288 1097154514742649229312327872986745170618682685253912413021842838 8932409125934810954817142359108213876057292211134310306931201621 24516099919902413188121055836918092954191737414631083299322792052 5741873131811578631921287218351501716032622150181180456017832001 12621331100318818585252411191262327041141287321709200493551136 1511277718192333658294327201845116016761849288218894251848722738 2828154244817752007281016721987133513504281818129626152142170211 176772133152410281131163815542213895546107810584171567011340226 4633061712295118621231299185115222718140628641726174518821915955 734148818478882529235312692204192129716492165113728022182743333 20729802991563294222481753296419996102485177029187085915571694 88372311932681173421581453196015522318951677133454947827891749 2745143317051223680886490141724165416272917516194297879026162299 8325186192191197337113015181693345265719952462407437242222741617 843614105520971142386107512332476138510720747101559208419242329 13012662382235422052095274097810341896469258115476620819081079 13491369288026993017392317164425611088147015642670200312711902493 141615212352077158011722296158917791332482860219676532329371206 73814423036661777185220962765361134625625732116148167183182661 23361123419954741152296238445678126362316181420282507268818982432 14074581909236609586272725132352486191022282652158210822174972345 14812983149413332350234465529397714352536529483267245729252383 21536027881830153928748055612995182410561313945257824151648661 16742187297322492927158193322107062754155023681792401143528811951

42253168682229994062336645128628573329573572126478072412231176 700106510892375755100528432247116126841659719468158169110472355 24027602671948455107412902563122725172471245176287721662521916 81028781324154924148592151280314761033242721282817254021802218 25769243258552420202159191221831576180845327112837117730211811827 29351051238935228492275168121224972962155394623242272172927172175 20913451963143711689641837222715911630223314751105147226018202381 19793342464284028584841738520257427121258349114241961628489901742 2093254919373912643297718752666248126839622621237818113325311147 21788345186750118983531750145127902010822348247415319565901196 25671890280723642188662260417671947215610011788143811735561050207 2679582171758526562717611586138829441175290462388543248226731238 17911777217681607785120019351117269525758421908155832225715612012 226110621749650258718251611740248712015452239791402248622951317 42298912661110606261120982416242815217674271532274125243391933 26892253376101818971409138014221121638146020381300279715059131465 39358711792598131612218412594257212632147507439153784148526902310 19762460234726081360176220262515111836431314364641967175152615 29761556147385421851086192816862721205111502875559275913661678 280915922311713142719511121122137179617082328862108116461181828 81372516941510391765144517412914197521771945206617956241341780 20509325701472783634157316631993591956162232317282186548811612 1365255314802551243824541396153729217021810155563067291714902687 6471906175923871355102888237222911045200206421172610270318511636 688201410225979092558178411741632141602166844270217661868911042 1533220793011991489498236319541021289617786571356137820619682358 37720893828231328112916452090211119221665160028531464257712411415 69070312539432959649254289011236330483716511391292823056422614 711228011401264523289199426932552101318157767317943672429936467 1038116610611934198424524591572426255025681988275784725561746594 29454011608627685156516581680299436535179728271540144157716622734

482122514181877203925414621032539671919214426255022585992811537 1111198477754041687132627752292341182635159026920852982508742 285229065062024258126407207641119189526729601911240025217002292 1673111253297520409966082209187495016151424371128173022971579993 29922492130722779891239234326644472968220189221623006231790962606 2126430184633227692916127263292027291151211023601936273315782265 2052241152522219721236105919032701292201322851655225129925095327 27083072250514107122238662533198011072886183999239827191261222047 977118549299117132172286118151216198324882599153523813845281053 2268208011551230281520179312555237243125792890291239817431309480 2651269418851681398482194165761321701426282522224767928769542237 405872400804231271427991940270916415151871113108420621916156980 23262294519254717721285699776277221231833172794222713311135203 29243891260124926325112435259636816195814252392956118329402779 280134231410111419202126426912031186124781955676228125062565640 30517924515022812232291026022893113310067015992181914249326591008 56280196921212083252615261138295023391876118810232904216819861860 155139414291744279517682735336196519072716592161328141068131487 136136228132189216423912032122132970191422351782220242512541102 16471959274660441129314591623286826542891245027432824188613101982 35014392058240824302334527131129382677664584184223934792417778 120565227193991963684120332415742941208621221961226113226631805 10620692143217116751220453585632055223026456652002216757619921099 16349586321171102974922543215888331640259513922146110624898061069 20462751214518792787953751171822862432439128427471401178725521806 22522263880127717251704126724227131092139725001421216218401370 148612551251219729721594116313682629176360160720429427281444641 10809291221138973617611807732212196914822307246316181855982458 15461865947072538622207112735411066440150021182443283020539791305 1194266162214620751799201627841782212017520186372616697727621683 2955144794415172107110124369592426820625297438281152023315962456

88422417031108501275529001786311153896016313663471432299092827 7272887175429312516121838423011774254686116242761223615166818197 2027465132025201376249119086527965092544156221981557247916611013 2985274421337946482475541279193841467717762466240232711849052661 15072635196814366329654545342477739102419521667158777924122926 1372853491344100410778552124814580375208816371856431868276492987 975426711040704297519312407145054411265695212912219285529802269 146917321820541853163912702200994852168212281209740266516011780 50388113252446166298441828622420824136227661120290824807962742 47318781399356217625712570187199888216143406431588151019252961 298148722032792236253811147719851601981450353142029302912074335 10942597279128456817732752300016991801249022322922254825801643902 775101623493087091282125059348926312680301230177110632422842885 25301747211921351268107368228631100113611878128341109197717932768 121716882322143414042369260857284628351615151015724108724241964 2315985247838127520232289113923972794170215422692260023952154982 2590219913731354124727071544281929691411167125892705295316252240 292991192218232282316244466890410973728792157106026341383271248 19661932182158119571220125198924628185212264716160618848171457 1943103678651323741974200028167412091192926241468726222514952758 5781978207828212453276722151696224412297931760135315166015412377 1584396661813444258626782138185825019102627387278545225839761096 1330226625412029124313122179381236891727352267210595131514052820 156643457113151244135923961014152925602584161137926283289211498 26861252330231218936016791850236676390610543782630168516601997 1752821848401449219524982030510200625662406320845698145428222125 1148433147810351043874171267611642625869284214611027209414101204 3410173722468200837026827821616151420652320207013212491128090934 416178524047702619287113117891950471386261212401124109047226458 24952543184174159718321570633119220823428122982244919461866799 1278295898614486289201870894271529972057121327434129711072691342

1287123459156857574731017488301431128328574126922035461253764 294828273920431721124511438038254112238189429112202224611451948 223181923402392160423511256290746658318671012184411599874462149 150223672033652773285619491222104826911294251217556787225672102 98827632104202753371273713118661716529252895536423248429462308 62653014919721067100019310762527388966277115952998442221416891127 2963758280510201707272225881122717285015344451970583183623042774 20731452997287015833851930228786721025281010162919041817851102902 18010412978502298269821429131888183810217572832102528721361091 22762970798111317202282831230623901064121147116039652130205988 269714121466697926844116218541458409659111415472206164273017815 25692748161227241443991151816873653213129515301363149755513191381 1170104422782036247379512885045401367547940133714593721742148135 289413361207856260129671026253448511342483264628891159825591628 13042884114911692173111612082979243726962042383259326032335639 2313829201978921132667261811581596171944813742510139814553512208 13441527230915132273159329031224241924452966225798444327811731903 16022641282109839416661338247028412658928353382736622668292782 22428646001372952918213967418551246263829012582289218364082193 13061800221260728991701140116278319202626460163321691422612192270 11958962319889132192721278972489152854151913032564222917237151031 293328043431756123188711652866786792342267540907215027562171517 244734695225042433123712899814881619397135221602951722470572128 149314672034158597329368282780629110449514031440254518431375268 134717352518642370971114623792883774129283624401551169722161125 125727620633864381178180315361395124224673655009981057318182996 1417284514921085149620607122511364939233717981635291929052441808 4361971432166963127565187223021632165024612079260527864941191104 141319422773142341069410192723738719922056246911983542898718253 74616101408709572465846169823302674287610466811567395194424592099 58923562351504132216262455115674414024031392048885260972827232015

26131620768874751202100232577713292710140020682245326280617332131 214019962778195320252701695210819621736298824422535208924572251 2115115390122591900237320052442226687210342031228335526201571250 21142243499293228655332044223410094712255300451575544128002592 12921991294916644211412829204119182730791737255784128350818921653 238094124344498603141267565528392346276014282076899186914831180 2325415601414249913931891543212928673926441822753149981684912 10573682122731788225614841357961159133926552037923150623388001115 20492931348949283310326565427762161732150817151905275016751272 1503160575213902782826275129825912418121425022637240511912651528 18836672421197023034292385100769662120621535951750319200917111037 18122639206728441070148731232913511822137925231829432851222453 219020111523292311729092290189913778701456135861528396832525101 25141863264482320871710188075956802967213412762472241016708091103 23992700815240314791323232113081714190125221993273289127413831758 13023091656266927317321371496235718399832394114455310931902332 266023611215363849380579211297424941006197324237482505256286651 2503285962653797875144314302382182626502011716236528084621913390 176415121941185719612798192329158792847 927];

XTraining $=$ zeros $(650,630,3,1800)$;

YTrainingPoP = zeros(1800,1);
for $\mathrm{i}=1: 1800$

XTraining(:,:,:,i) = double(imread("S (" + RN(i) + ").jpg"));

YTrainingPoP(i,1) = Percent_of_Porosity(RN(i));
end

XValidation $=$ zeros $(650,630,3,600)$;
YValidationPoP $=\operatorname{zeros}(600,1)$;
for $\mathrm{i}=1801: 2400$

XValidation(:,:,:,i-1800) = double(imread("S (" + RN(i) + ").jpg"));

YValidationPoP(i-1800,1) = Percent_of_Porosity(RN(i));
end

XTesting $=$ zeros $(650,630,3,600)$;

YTestingPoP = zeros(600,1);
for $\mathrm{i}=2401: 3000$

XTesting(:,:,:,i-2400) = double(imread("S (" + RN(i) + ").jpg"));

YTestingPoP(i-2400,1) = Percent_of_Porosity(RN(i));
end
end
1.8 Bayesian Regression Convolutional Neural Network (BO-RCNN)
clc;
clear;
close all;

## \%Load and Explore Image Data

ArtificialPorosityImagesDatasetPath $=$ fullfile('/nfshome','store02','users','c.c1881324','Documents','MATLAB','3000 Slices','*.jpg');
[XTraining,YTrainingPoP,XValidation, YV , loadAPIData(ArtificialPorosityImagesDatasetPath);

## \%Define the Problem (Objective Function)

## ObjFcn =

makeObjFcn(XTraining, YTrainingPoP,XValidation, YValidationPoP,XTesting, YTesting PoP);
optimVars $=[$
optimizableVariable('SectionDepth',[1 3],'Type','integer')
optimizableVariable('InitialLearnRate',[0.01 0.012],'Transform','log')
optimizableVariable('Momentum',[0.8 0.98])
optimizableVariable('L2Regularization',[1e-10 1e-2],'Transform','log')];

## \%Optimize Variables

BayesObject $=$ bayesopt $($ ObjFcn,optimVars, $\ldots$
'MaxTime', $1 * 60 * 60, \ldots$
'IsObjectiveDeterministic',false, ...
'UseParallel',false);

```
function ObjFcn =
makeObjFcn(XTraining,YTrainingPoP,XValidation,YValidationPoP,XTesting,YTesting
PoP)
```

ObjFcn $=@$ ValidationErrorFunction;
function AverageValidationError = ValidationErrorFunction(optimVars)

## \%Specify Convolutional Neural Network Architecture

imageSize $=[650630$ 3];
layersPoP = [
imageInputLayer(imageSize)
convBlock(5,8, optimVars. SectionDepth)
averagePooling2dLayer(4,'Stride',4)
convBlock(5,16, optimVars. SectionDepth)
averagePooling2dLayer(4,'Stride',4)
convBlock(5,32, optimVars. SectionDepth)
averagePooling2dLayer(4,'Stride',4)
convBlock(5,64, optimVars. SectionDepth)
averagePooling2dLayer(4,'Stride',4)
convBlock(5,128, optimVars. SectionDepth)
fullyConnectedLayer(1)
regressionLayer];
miniBatchSize $=64$;
validationFrequency $=$ floor $(1800 /$ miniBatchSize $)$;
optionsPoP $=$ trainingOptions('sgdm', $\ldots$
'InitialLearnRate', optimVars.InitialLearnRate, ...
'Momentum', optimVars.Momentum, ...
'L2Regularization', optimVars.L2Regularization, ...
'MaxEpochs',20, ...
'MiniBatchSize',miniBatchSize, ...
'ValidationFrequency',validationFrequency, ...
'ValidationData', $\{$ XValidation, YValidationPoP(:,1) $\}, \ldots$
'Shuffle','every-epoch', ...
'Plots','training-progress');

## \%Train Network using Training Data

netPoP = trainNetwork(XTraining,YTrainingPoP(:,1),layersPoP,optionsPoP);

## \%Predict Responses and Compute Accuracy and Error

 $\mathrm{c}=1$;PredictedTrainingPoP(:,c) = predict(netPoP,XTraining);
PredictedValidationPoP(:,c) = predict(netPoP,XValidation);
PredictedTestingPoP(:,c) = predict(netPoP,XTesting);

TrainingError(:,c) = YTrainingPoP(:,1) - PredictedTrainingPoP(:,c);
AbsoluteTrainingError(:,c) $=\operatorname{abs}($ TrainingError(:,c) $)$;
AverageTrainingError(:,c) $=\operatorname{sum}($ AbsoluteTrainingError(:,c) $) / 1800$;
numCorrectTrainingPoP(:,c) = sum(abs(TrainingError(:,(c))) < 0.05);
TrainingAccuracyPoP(:,c) = (numCorrectTrainingPoP(:,(c))/1800)*100;

ValidationError(:, c) = YValidationPoP(:,1) - PredictedValidationPoP(:,c);
AbsoluteValidationError(:,c) = abs(ValidationError(:,c));

AverageValidationError(:,c) $=\operatorname{sum}($ AbsoluteValidationError(:, c) $) / 600$;
numCorrectValidationPoP(:,c) $=\operatorname{sum}(\operatorname{abs}(\operatorname{ValidationError}(:,(\mathrm{c})))$ < 0.05$)$;
ValidationAccuracyPoP(:,c) $=($ numCorrectValidationPoP(:,(c))/600)*100;

TestingError(:,c) = YTestingPoP(:,1) - PredictedTestingPoP(:,c);
AbsoluteTestingError(:,c) = abs(TestingError(:,c));

```
AverageTestingError(:,c) = sum(AbsoluteTestingError(:,c))/600;
numCorrectTestingPoP(:,c) = sum(abs(TestingError(:,(c))) < 0.05);
TestingAccuracyPoP(:,c) = (numCorrectTestingPoP(:,(c))/600)*100;
```

    end
    end
function layers $=\operatorname{convBlock}($ FilterSize,NumberofFilters,SectionDepth $)$
layers $=[$
convolution2dLayer(FilterSize,NumberofFilters,'Padding','same')
batchNormalizationLayer
reluLayer];
layers $=$ repmat(layers,SectionDepth,1);
end
function [XTraining, YTrainingPoP,XValidation, Y ValidationPoP,XTesting, YTestingPoP]
$=$ loadAPIData(ArtificialPorosityImagesDatasetPath)
location $=\operatorname{dir}($ ArtificialPorosityImagesDatasetPath $) ;$
Percent_of_Porosity = Actual_Percent_of_Porosity;

RN = 18349199352202897189132675210627254241690900154825962947505 18022706149264827931652726185917692022878564210964656623762163 51824968985221049219225192221620121121522191261761828777697571692 16421555542779471509982554138228692633413280129342262132727701575 2881926274925736952100128110522511754279578326561446237120922288 1097154514742649229312327872986745170618682685253912413021842838 8932409125934810954817142359108213876057292211134310306931201621 24516099919902413188121055836918092954191737414631083299322792052 5741873131811578631921287218351501716032622150181180456017832001 12621331100318818585252411191262327041141287321709200493551136 1511277718192333658294327201845116016761849288218894251848722738 2828154244817752007281016721987133513504281818129626152142170211 176772133152410281131163815542213895546107810584171567011340226 4633061712295118621231299185115222718140628641726174518821915955 734148818478882529235312692204192129716492165113728022182743333 20729802991563294222481753296419996102485177029187085915571694 88372311932681173421581453196015522318951677133454947827891749 2745143317051223680886490141724165416272917516194297879026162299 8325186192191197337113015181693345265719952462407437242222741617 843614105520971142386107512332476138510720747101559208419242329 13012662382235422052095274097810341896469258115476620819081079 13491369288026993017392317164425611088147015642670200312711902493 141615212352077158011722296158917791332482860219676532329371206 73814423036661777185220962765361134625625732116148167183182661 23361123419954741152296238445678126362316181420282507268818982432 14074581909236609586272725132352486191022282652158210822174972345 14812983149413332350234465529397714352536529483267245729252383 21536027881830153928748055612995182410561313945257824151648661 16742187297322492927158193322107062754155023681792401143528811951 42253168682229994062336645128628573329573572126478072412231176 700106510892375755100528432247116126841659719468158169110472355

24027602671948455107412902563122725172471245176287721662521916 81028781324154924148592151280314761033242721282817254021802218 25769243258552420202159191221831576180845327112837117730211811827 29351051238935228492275168121224972962155394623242272172927172175 20913451963143711689641837222715911630223314751105147226018202381 19793342464284028584841738520257427121258349114241961628489901742 2093254919373912643297718752666248126839622621237818113325311147 21788345186750118983531750145127902010822348247415319565901196 25671890280723642188662260417671947215610011788143811735561050207 2679582171758526562717611586138829441175290462388543248226731238 17911777217681607785120019351117269525758421908155832225715612012 226110621749650258718251611740248712015452239791402248622951317 42298912661110606261120982416242815217674271532274125243391933 26892253376101818971409138014221121638146020381300279715059131465 39358711792598131612218412594257212632147507439153784148526902310 19762460234726081360176220262515111836431314364641967175152615 29761556147385421851086192816862721205111502875559275913661678 280915922311713142719511121122137179617082328862108116461181828 81372516941510391765144517412914197521771945206617956241341780 20509325701472783634157316631993591956162232317282186548811612 1365255314802551243824541396153729217021810155563067291714902687 6471906175923871355102888237222911045200206421172610270318511636 688201410225979092558178411741632141602166844270217661868911042 1533220793011991489498236319541021289617786571356137820619682358 37720893828231328112916452090211119221665160028531464257712411415 69070312539432959649254289011236330483716511391292823056422614 711228011401264523289199426932552101318157767317943672429936467 1038116610611934198424524591572426255025681988275784725561746594 29454011608627685156516581680299436535179728271540144157716622734 482122514181877203925414621032539671919214426255022585992811537 1111198477754041687132627752292341182635159026920852982508742

285229065062024258126407207641119189526729601911240025217002292 1673111253297520409966082209187495016151424371128173022971579993 29922492130722779891239234326644472968220189221623006231790962606 2126430184633227692916127263292027291151211023601936273315782265 2052241152522219721236105919032701292201322851655225129925095327 27083072250514107122238662533198011072886183999239827191261222047 977118549299117132172286118151216198324882599153523813845281053 2268208011551230281520179312555237243125792890291239817431309480 2651269418851681398482194165761321701426282522224767928769542237 405872400804231271427991940270916415151871113108420621916156980 23262294519254717721285699776277221231833172794222713311135203 29243891260124926325112435259636816195814252392956118329402779 280134231410111419202126426912031186124781955676228125062565640 30517924515022812232291026022893113310067015992181914249326591008 56280196921212083252615261138295023391876118810232904216819861860 155139414291744279517682735336196519072716592161328141068131487 136136228132189216423912032122132970191422351782220242512541102 16471959274660441129314591623286826542891245027432824188613101982 35014392058240824302334527131129382677664584184223934792417778 120565227193991963684120332415742941208621221961226113226631805 10620692143217116751220453585632055223026456652002216757619921099 16349586321171102974922543215888331640259513922146110624898061069 20462751214518792787953751171822862432439128427471401178725521806 22522263880127717251704126724227131092139725001421216218401370 148612551251219729721594116313682629176360160720429427281444641 10809291221138973617611807732212196914822307246316181855982458 15461865947072538622207112735411066440150021182443283020539791305 1194266162214620751799201627841782212017520186372616697727621683 2955144794415172107110124369592426820625297438281152023315962456 88422417031108501275529001786311153896016313663471432299092827 7272887175429312516121838423011774254686116242761223615166818197

2027465132025201376249119086527965092544156221981557247916611013 2985274421337946482475541279193841467717762466240232711849052661 15072635196814366329654545342477739102419521667158777924122926 1372853491344100410778552124814580375208816371856431868276492987 975426711040704297519312407145054411265695212912219285529802269 146917321820541853163912702200994852168212281209740266516011780 50388113252446166298441828622420824136227661120290824807962742 47318781399356217625712570187199888216143406431588151019252961 298148722032792236253811147719851601981450353142029302912074335 10942597279128456817732752300016991801249022322922254825801643902 775101623493087091282125059348926312680301230177110632422842885 25301747211921351268107368228631100113611878128341109197717932768 121716882322143414042369260857284628351615151015724108724241964 2315985247838127520232289113923972794170215422692260023952154982 2590219913731354124727071544281929691411167125892705295316252240 292991192218232282316244466890410973728792157106026341383271248 19661932182158119571220125198924628185212264716160618848171457 1943103678651323741974200028167412091192926241468726222514952758 5781978207828212453276722151696224412297931760135315166015412377 1584396661813444258626782138185825019102627387278545225839761096 1330226625412029124313122179381236891727352267210595131514052820 156643457113151244135923961014152925602584161137926283289211498 26861252330231218936016791850236676390610543782630168516601997 1752821848401449219524982030510200625662406320845698145428222125 1148433147810351043874171267611642625869284214611027209414101204 3410173722468200837026827821616151420652320207013212491128090934 416178524047702619287113117891950471386261212401124109047226458 24952543184174159718321570633119220823428122982244919461866799 1278295898614486289201870894271529972057121327434129711072691342 1287123459156857574731017488301431128328574126922035461253764 294828273920431721124511438038254112238189429112202224611451948

223181923402392160423511256290746658318671012184411599874462149 150223672033652773285619491222104826911294251217556787225672102 98827632104202753371273713118661716529252895536423248429462308 62653014919721067100019310762527388966277115952998442221416891127 2963758280510201707272225881122717285015344451970583183623042774 20731452997287015833851930228786721025281010162919041817851102902 18010412978502298269821429131888183810217572832102528721361091 22762970798111317202282831230623901064121147116039652130205988 269714121466697926844116218541458409659111415472206164273017815 25692748161227241443991151816873653213129515301363149755513191381 1170104422782036247379512885045401367547940133714593721742148135 289413361207856260129671026253448511342483264628891159825591628 13042884114911692173111612082979243726962042383259326032335639 2313829201978921132667261811581596171944813742510139814553512208 13441527230915132273159329031224241924452966225798444327811731903 16022641282109839416661338247028412658928353382736622668292782 22428646001372952918213967418551246263829012582289218364082193 13061800221260728991701140116278319202626460163321691422612192270 11958962319889132192721278972489152854151913032564222917237151031 293328043431756123188711652866786792342267540907215027562171517 244734695225042433123712899814881619397135221602951722470572128 149314672034158597329368282780629110449514031440254518431375268 134717352518642370971114623792883774129283624401551169722161125 125727620633864381178180315361395124224673655009981057318182996 1417284514921085149620607122511364939233717981635291929052441808 4361971432166963127565187223021632165024612079260527864941191104 141319422773142341069410192723738719922056246911983542898718253 74616101408709572465846169823302674287610466811567395194424592099 58923562351504132216262455115674414024031392048885260972827232015 26131620768874751202100232577713292710140020682245326280617332131 214019962778195320252701695210819621736298824422535208924572251

2115115390122591900237320052442226687210342031228335526201571250 21142243499293228655332044223410094712255300451575544128002592 12921991294916644211412829204119182730791737255784128350818921653 238094124344498603141267565528392346276014282076899186914831180 2325415601414249913931891543212928673926441822753149981684912 10573682122731788225614841357961159133926552037923150623388001115 20492931348949283310326565427762161732150817151905275016751272 1503160575213902782826275129825912418121425022637240511912651528 18836672421197023034292385100769662120621535951750319200917111037 18122639206728441070148731232913511822137925231829432851222453 219020111523292311729092290189913778701456135861528396832525101 25141863264482320871710188075956802967213412762472241016708091103 23992700815240314791323232113081714190125221993273289127413831758 13023091656266927317321371496235718399832394114455310931902332 266023611215363849380579211297424941006197324237482505256286651 2503285962653797875144314302382182626502011716236528084621913390 $176415121941185719612798192329158792847927]$;

XTraining $=$ zeros $(650,630,3,1800)$;
YTrainingPoP $=\operatorname{zeros}(1800,1)$;
for $\mathrm{i}=1: 1800$
XTraining(:,:,:,i) = double(imread("S (" + RN(i) + ").jpg"));
YTrainingPoP(i,1) = Percent_of_Porosity(RN(i));
end

XValidation $=$ zeros $(650,630,3,600)$;
YValidationPoP $=\operatorname{zeros}(600,1)$;
for $\mathrm{i}=1801: 2400$

XValidation(:,:,:,i-1800) = double(imread("S (" + RN(i) + ").jpg"));

YValidationPoP(i-1800,1) = Percent_of_Porosity(RN(i));
end

XTesting $=$ zeros $(650,630,3,600)$;

YTestingPoP = zeros(600,1);
for $\mathrm{i}=2401: 3000$

XTesting(:,:,:,i-2400) = double(imread("S (" + RN(i) + ").jpg"));

YTestingPoP(i-2400,1) = Percent_of_Porosity(RN(i));
end
end
1.9 Bees Bayesian Regression Convolutional Neural Network (BA-BO-RCNN) clc;
clear;
close all;

## \%Load and Explore Image Data

ArtificialPorosityImagesDatasetPath $=$ fullfile('/nfshome','store02','users','c.c1881324','Documents','MATLAB','3000 Slices','*.jpg');
[XTraining,YTrainingPoP,XValidation, YV , loadAPIData(ArtificialPorosityImagesDatasetPath);
\%Define the Problem (Objective Function)
ObjFcn $=$
makeObjFcn(XTraining, YTrainingPoP,XValidation, YValidationPoP,XTesting, YTesting PoP);
nVar=6; \%Number of Weight Learning Rate Factors
VarSize=[1 nVar]; \%Matrix Size for Factors
VarMin=0.9; \%Lower Bound for Factors
VarMax=1.1; \% Upper Bound for Factors
\%Define Bees Algorithm Parameters
MaxIt=1; \%Maximum Number of Iterations
nScoutBee=4; \%Scout Bees
nSelectedSite=round $(0.5 *$ nScoutBee $)$; \%Selected Sites
nEliteSite=1; \%Selected Elite Sites
nSelectedSiteBee=round $(0.5 *$ nScoutBee $) ;$ \% Recruited Bees for Selected Sites nEliteSiteBee=2*nSelectedSiteBee; \%Recruited Bees for Elite Sites r=0.1*(VarMax-VarMin); \%Neighbourhood Radius rdamp $=0.95$; \%Neighbourhood Radius Damp Rate
\%Initialize Empty Bee Structure
empty_bee.Position=[];
empty_bee.Error=[];
\%Initialize Bees Array
bee=repmat(empty_bee,nScoutBee,1);

## \%Create New Solutions

for $\mathrm{i}=1$ :nScoutBee
bee(i).Position=unifrnd(VarMin,VarMax,VarSize);
bee(i).Error=ObjFcn(bee(i).Position);
end

## \%Sort the Solution

[ $\sim$, SortOrder]=sort([bee.Error]);
bee=bee(SortOrder);
\%Update Best Solution Ever Found
BestSol=bee(1);

## \%Create Array to Hold Best Error Values

LowestError=zeros(MaxIt,1);

## \%Create Bees Algorithm Main Loop

for $\mathrm{it}=1$ :MaxIt

## \%Elite Sites

for $\mathrm{i}=1$ :nEliteSite
bestnewbee.Error=inf;
for $\mathrm{j}=1$ :nEliteSiteBee
newbee.Position=PerformBeeDance(bee(i).Position,r);
newbee.Error=ObjFcn(newbee.Position);
if newbee.Error<bestnewbee.Error
bestnewbee=newbee;
end
end
if bestnewbee. Error<bee(i).Error bee(i)=bestnewbee;

> end
end

## \%Selected Non-Elite Sites

for $\mathrm{i}=\mathrm{nEliteSite}+1$ :nSelectedSite bestnewbee.Error=inf;
for $\mathrm{j}=1$ :nSelectedSiteBee newbee.Position=PerformBeeDance(bee(i).Position,r); newbee.Error=ObjFcn(newbee.Position); if newbee.Error<bestnewbee.Error bestnewbee=newbee; end

> end
if bestnewbee.Error<bee(i).Error bee(i)=bestnewbee;
end
end

## \% Non-Selected Sites

for $\mathrm{i}=\mathrm{nSelectedSite}+1$ :nScoutBee bee(i).Position=unifrnd(VarMin,VarMax,VarSize);

```
    bee(i).Error=ObjFcn(bee(i).Position);
    end
%Sort the Solution
[~, SortOrder]=sort([bee.Error]);
bee=bee(SortOrder);
%Update Best Solution Ever Found
BestSol=bee(1);
%Store Best Error Ever Found
LowestError(it)=BestSol.Error;
OptimalWeightLearningRateFactor=BestSol.Position;
```


## \%Display Iteration Information

$\operatorname{disp}([$ 'Iteration ' num2str(it) ': Lowest Error = ' num2str(LowestError(it))]);
\%Define Damp Neighborhood Radius
$\mathrm{r}=\mathrm{r}$ * rdamp;
end
\%Display the Results
figure;

```
%Make a Plot for Lowest Error
semilogy(LowestError,'LineWidth',2);
xlabel('Iteration');
ylabel('Lowest Error');
function ObjFcn =
makeObjFcn(XTraining,YTrainingPoP,XValidation,YValidationPoP,XTesting,YTesting
PoP)
```

ObjFcn $=@$ ValidationErrorFunction;
function AverageValidationError $=$
ValidationErrorFunction(OptimalWeightLearningRateFactor)

## \%Specify Convolutional Neural Network Architecture

imageSize $=[650630$ 3];
layersPoP = [
imageInputLayer(imageSize)
convBlock(5,8,3,OptimalWeightLearningRateFactor(1,1))
averagePooling2dLayer(4,'Stride',4)
averagePooling2dLayer(4,'Stride',4)
convBlock(5,32,3,OptimalWeightLearningRateFactor(1,3))
averagePooling2dLayer(4,'Stride',4)
convBlock(5,64,3,OptimalWeightLearningRateFactor(1,4))
averagePooling2dLayer(4,'Stride',4)
convBlock(5,128,3,OptimalWeightLearningRateFactor(1,5))
fullyConnectedLayer(1,'WeightLearnRateFactor',OptimalWeightLearningRateFactor(1,6) )
regressionLayer];
miniBatchSize $=64$;
validationFrequency $=$ floor(1800/miniBatchSize $)$;
optionsPoP $=$ trainingOptions('sgdm', $\ldots$
'InitialLearnRate', $0.011964, \ldots$
'Momentum', 0.90267, ...
'L2Regularization', 4.7995e-07, ...
'MaxEpochs',20, ...
'MiniBatchSize',miniBatchSize, ...
'ValidationFrequency',validationFrequency, ...
'ValidationData',\{XValidation,YValidationPoP(:,1)\}, ...
'Shuffle','every-epoch', ...
'Plots','training-progress');

## \%Train Network using Training Data

netPoP = trainNetwork(XTraining,YTrainingPoP(:,1),layersPoP,optionsPoP);
\%Predict Responses and Compute Accuracy and Error
$\mathrm{c}=1$;

PredictedTrainingPoP(:,c) = predict(netPoP,XTraining);
PredictedValidationPoP(:,c) = predict(netPoP,XValidation);
PredictedTestingPoP(:,c) = predict(netPoP,XTesting);

TrainingError(:,c) = YTrainingPoP(:,1) - PredictedTrainingPoP(:,c);
AbsoluteTrainingError(:,c) $=\operatorname{abs}($ TrainingError(:,c) $)$;
AverageTrainingError(:,c) = sum(AbsoluteTrainingError(:,c))/1800;
numCorrectTrainingPoP(:,c) = sum(abs(TrainingError(:,(c))) < 0.05);
TrainingAccuracyPoP(:,c) = (numCorrectTrainingPoP(:,(c))/1800)*100;

ValidationError(:,c) = YValidationPoP(:,1) - PredictedValidationPoP(:,c);
AbsoluteValidationError(:,c) = abs(ValidationError(:, c));

AverageValidationError(:,c) = sum(AbsoluteValidationError(:,c))/600;
numCorrectValidationPoP(:,c) $=\operatorname{sum}(\operatorname{abs}($ ValidationError(:,(c))) < 0.05);

ValidationAccuracyPoP(:,c) = (numCorrectValidationPoP(:,(c))/600)*100;

TestingError(:,c) = YTestingPoP(:,1) - PredictedTestingPoP(:,c);

AbsoluteTestingError(:,c) = abs(TestingError(:,c));
AverageTestingError(:,c) = sum(AbsoluteTestingError(:,c))/600;
numCorrectTestingPoP(:,c) = sum(abs(TestingError(:,(c))) < 0.05);

TestingAccuracyPoP(:,c) = (numCorrectTestingPoP(:,(c))/600)*100;
end
end

## \%Create Bees Dance Function

function $y=$ PerformBeeDance(ValidationErrorFunction,r)
nVar=numel(ValidationErrorFunction);
k=randi([1 nVar]);
$\mathrm{y}=$ ValidationErrorFunction;
$\mathrm{y}(\mathrm{k})=$ ValidationErrorFunction(k)+unifrnd(-r,r);
end
function layers $=$
convBlock(FilterSize,NumberofFilters,SectionDepth,OptimalWeightLearningRateFactor) layers $=[$
convolution2dLayer(FilterSize,NumberofFilters,'Padding','same','WeightLearnRateFactor' ,OptimalWeightLearningRateFactor) batchNormalizationLayer reluLayer];
layers $=$ repmat(layers,SectionDepth,1);
end
function [XTraining, YTrainingPoP,XValidation, YValidationPoP,XTesting, YTestingPoP]
$=$ loadAPIData(ArtificialPorosityImagesDatasetPath)
location $=\operatorname{dir}($ ArtificialPorosityImagesDatasetPath $) ;$

Percent_of_Porosity = Actual_Percent_of_Porosity;

RN = [1834 9199352202897189132675210627254241690900154825962947505 18022706149264827931652726185917692022878564210964656623762163 51824968985221049219225192221620121121522191261761828777697571692 16421555542779471509982554138228692633413280129342262132727701575 2881926274925736952100128110522511754279578326561446237120922288 1097154514742649229312327872986745170618682685253912413021842838 8932409125934810954817142359108213876057292211134310306931201621 24516099919902413188121055836918092954191737414631083299322792052

5741873131811578631921287218351501716032622150181180456017832001 12621331100318818585252411191262327041141287321709200493551136 1511277718192333658294327201845116016761849288218894251848722738 2828154244817752007281016721987133513504281818129626152142170211 176772133152410281131163815542213895546107810584171567011340226 4633061712295118621231299185115222718140628641726174518821915955 734148818478882529235312692204192129716492165113728022182743333 20729802991563294222481753296419996102485177029187085915571694 88372311932681173421581453196015522318951677133454947827891749 2745143317051223680886490141724165416272917516194297879026162299 8325186192191197337113015181693345265719952462407437242222741617 843614105520971142386107512332476138510720747101559208419242329 13012662382235422052095274097810341896469258115476620819081079 13491369288026993017392317164425611088147015642670200312711902493 141615212352077158011722296158917791332482860219676532329371206 73814423036661777185220962765361134625625732116148167183182661 23361123419954741152296238445678126362316181420282507268818982432 14074581909236609586272725132352486191022282652158210822174972345 14812983149413332350234465529397714352536529483267245729252383 21536027881830153928748055612995182410561313945257824151648661 16742187297322492927158193322107062754155023681792401143528811951 42253168682229994062336645128628573329573572126478072412231176 700106510892375755100528432247116126841659719468158169110472355 24027602671948455107412902563122725172471245176287721662521916 81028781324154924148592151280314761033242721282817254021802218 25769243258552420202159191221831576180845327112837117730211811827 29351051238935228492275168121224972962155394623242272172927172175 20913451963143711689641837222715911630223314751105147226018202381 19793342464284028584841738520257427121258349114241961628489901742 2093254919373912643297718752666248126839622621237818113325311147 21788345186750118983531750145127902010822348247415319565901196

25671890280723642188662260417671947215610011788143811735561050207 2679582171758526562717611586138829441175290462388543248226731238 17911777217681607785120019351117269525758421908155832225715612012 226110621749650258718251611740248712015452239791402248622951317 42298912661110606261120982416242815217674271532274125243391933 26892253376101818971409138014221121638146020381300279715059131465 39358711792598131612218412594257212632147507439153784148526902310 19762460234726081360176220262515111836431314364641967175152615 29761556147385421851086192816862721205111502875559275913661678 280915922311713142719511121122137179617082328862108116461181828 81372516941510391765144517412914197521771945206617956241341780 20509325701472783634157316631993591956162232317282186548811612 1365255314802551243824541396153729217021810155563067291714902687 6471906175923871355102888237222911045200206421172610270318511636 688201410225979092558178411741632141602166844270217661868911042 1533220793011991489498236319541021289617786571356137820619682358 37720893828231328112916452090211119221665160028531464257712411415 69070312539432959649254289011236330483716511391292823056422614 711228011401264523289199426932552101318157767317943672429936467 1038116610611934198424524591572426255025681988275784725561746594 29454011608627685156516581680299436535179728271540144157716622734 482122514181877203925414621032539671919214426255022585992811537 1111198477754041687132627752292341182635159026920852982508742 285229065062024258126407207641119189526729601911240025217002292 1673111253297520409966082209187495016151424371128173022971579993 29922492130722779891239234326644472968220189221623006231790962606 2126430184633227692916127263292027291151211023601936273315782265 2052241152522219721236105919032701292201322851655225129925095327 27083072250514107122238662533198011072886183999239827191261222047 977118549299117132172286118151216198324882599153523813845281053 2268208011551230281520179312555237243125792890291239817431309480

2651269418851681398482194165761321701426282522224767928769542237 405872400804231271427991940270916415151871113108420621916156980 23262294519254717721285699776277221231833172794222713311135203 29243891260124926325112435259636816195814252392956118329402779 280134231410111419202126426912031186124781955676228125062565640 30517924515022812232291026022893113310067015992181914249326591008 56280196921212083252615261138295023391876118810232904216819861860 155139414291744279517682735336196519072716592161328141068131487 136136228132189216423912032122132970191422351782220242512541102 16471959274660441129314591623286826542891245027432824188613101982 35014392058240824302334527131129382677664584184223934792417778 120565227193991963684120332415742941208621221961226113226631805 10620692143217116751220453585632055223026456652002216757619921099 16349586321171102974922543215888331640259513922146110624898061069 20462751214518792787953751171822862432439128427471401178725521806 22522263880127717251704126724227131092139725001421216218401370 148612551251219729721594116313682629176360160720429427281444641 10809291221138973617611807732212196914822307246316181855982458 15461865947072538622207112735411066440150021182443283020539791305 1194266162214620751799201627841782212017520186372616697727621683 2955144794415172107110124369592426820625297438281152023315962456 88422417031108501275529001786311153896016313663471432299092827 7272887175429312516121838423011774254686116242761223615166818197 2027465132025201376249119086527965092544156221981557247916611013 2985274421337946482475541279193841467717762466240232711849052661 15072635196814366329654545342477739102419521667158777924122926 1372853491344100410778552124814580375208816371856431868276492987 975426711040704297519312407145054411265695212912219285529802269 146917321820541853163912702200994852168212281209740266516011780 50388113252446166298441828622420824136227661120290824807962742 47318781399356217625712570187199888216143406431588151019252961

298148722032792236253811147719851601981450353142029302912074335 10942597279128456817732752300016991801249022322922254825801643902 775101623493087091282125059348926312680301230177110632422842885 25301747211921351268107368228631100113611878128341109197717932768 121716882322143414042369260857284628351615151015724108724241964 2315985247838127520232289113923972794170215422692260023952154982 2590219913731354124727071544281929691411167125892705295316252240 292991192218232282316244466890410973728792157106026341383271248 19661932182158119571220125198924628185212264716160618848171457 1943103678651323741974200028167412091192926241468726222514952758 5781978207828212453276722151696224412297931760135315166015412377 1584396661813444258626782138185825019102627387278545225839761096 1330226625412029124313122179381236891727352267210595131514052820 156643457113151244135923961014152925602584161137926283289211498 26861252330231218936016791850236676390610543782630168516601997 1752821848401449219524982030510200625662406320845698145428222125 1148433147810351043874171267611642625869284214611027209414101204 3410173722468200837026827821616151420652320207013212491128090934 416178524047702619287113117891950471386261212401124109047226458 24952543184174159718321570633119220823428122982244919461866799 1278295898614486289201870894271529972057121327434129711072691342 1287123459156857574731017488301431128328574126922035461253764 294828273920431721124511438038254112238189429112202224611451948 223181923402392160423511256290746658318671012184411599874462149 150223672033652773285619491222104826911294251217556787225672102 98827632104202753371273713118661716529252895536423248429462308 62653014919721067100019310762527388966277115952998442221416891127 2963758280510201707272225881122717285015344451970583183623042774 20731452997287015833851930228786721025281010162919041817851102902 18010412978502298269821429131888183810217572832102528721361091 22762970798111317202282831230623901064121147116039652130205988

269714121466697926844116218541458409659111415472206164273017815 25692748161227241443991151816873653213129515301363149755513191381 1170104422782036247379512885045401367547940133714593721742148135 289413361207856260129671026253448511342483264628891159825591628 13042884114911692173111612082979243726962042383259326032335639 2313829201978921132667261811581596171944813742510139814553512208 13441527230915132273159329031224241924452966225798444327811731903 16022641282109839416661338247028412658928353382736622668292782 22428646001372952918213967418551246263829012582289218364082193 13061800221260728991701140116278319202626460163321691422612192270 11958962319889132192721278972489152854151913032564222917237151031 293328043431756123188711652866786792342267540907215027562171517 244734695225042433123712899814881619397135221602951722470572128 149314672034158597329368282780629110449514031440254518431375268 134717352518642370971114623792883774129283624401551169722161125 125727620633864381178180315361395124224673655009981057318182996 1417284514921085149620607122511364939233717981635291929052441808 4361971432166963127565187223021632165024612079260527864941191104 141319422773142341069410192723738719922056246911983542898718253 74616101408709572465846169823302674287610466811567395194424592099 58923562351504132216262455115674414024031392048885260972827232015 26131620768874751202100232577713292710140020682245326280617332131 214019962778195320252701695210819621736298824422535208924572251 2115115390122591900237320052442226687210342031228335526201571250 21142243499293228655332044223410094712255300451575544128002592 12921991294916644211412829204119182730791737255784128350818921653 238094124344498603141267565528392346276014282076899186914831180 2325415601414249913931891543212928673926441822753149981684912 10573682122731788225614841357961159133926552037923150623388001115 20492931348949283310326565427762161732150817151905275016751272 1503160575213902782826275129825912418121425022637240511912651528

XTraining $=$ zeros $(650,630,3,1800)$;

YTrainingPoP = zeros(1800,1);
for $\mathrm{i}=1: 1800$

XTraining(:,:,:,i) = double(imread("S (" + RN(i) + ").jpg"));
YTrainingPoP(i,1) = Percent_of_Porosity(RN(i));
end

XValidation $=$ zeros $(650,630,3,600)$;

YValidationPoP $=\operatorname{zeros}(600,1)$;
for $\mathrm{i}=1801: 2400$

XValidation(:,:,:,i-1800) = double(imread("S (" + RN(i) + ").jpg"));
YValidationPoP(i-1800,1) = Percent_of_Porosity(RN(i));
end

XTesting $=$ zeros $(650,630,3,600)$;
$\mathrm{YTestingPoP}=\operatorname{zeros}(600,1)$;
for $\mathrm{i}=2401: 3000$

XTesting(:,,:,;,i-2400) = double(imread("S (" + RN(i) + ").jpg"));
YTestingPoP(i-2400,1) = Percent_of_Porosity(RN(i));
end
end

### 1.10 Bees Regression Convolutional Neural Network (BA-RCNN)

clc;
clear;
close all;

## \%Load and Explore Image Data

ArtificialPorosityImagesDatasetPath $=$ fullfile('/nfshome','store02','users','c.c1881324','Documents','MATLAB','3000 Slices','*.jpg');
[XTraining,YTrainingPoP,XValidation, YV alidationPoP,XTesting, $\mathrm{YTestingPoP]} \mathrm{=}$ loadAPIData(ArtificialPorosityImagesDatasetPath);
\%Define the Problem (Objective Function)
ObjFcn =
makeObjFcn(XTraining, YTrainingPoP,XValidation, YValidationPoP,XTesting, YTesting PoP);
nVar=4; \%Number of Variables
VarSize=[1 nVar]; \%Size of Variables
VarMin=[110.01 0.8 1e-10]; \%Lower Bound of Variables
VarMax=[30.012 0.98 1e-2]; \% Upper Bound of Variables
\%Define Bees Algorithm Parameters
MaxIt=1; \%Maximum Number of Iterations
nScoutBee=4; \%Scout Bees
nSelectedSite=round $(0.5 *$ nScoutBee $)$; \% Selected Sites
nEliteSite $=1$; \%Selected Elite Sites
nSelectedSiteBee=round $(0.5 *$ nScoutBee $)$; \% Recruited Bees for Selected Sites
nEliteSiteBee=2*nSelectedSiteBee; \%Recruited Bees for Elite Sites
r=0.1*(VarMax-VarMin); \%Neighbourhood Radius
rdamp $=0.95$; \% Neighbourhood Radius Damp Rate
\%Initialize Empty Bee Structure
empty_bee.Position=[];
empty_bee.Error=[];

## \%Initialize Bees Array

bee=repmat(empty_bee,nScoutBee,1);

## \%Create New Solutions

for $\mathrm{i}=1$ :nScoutBee bee(i).Position=unifrnd(VarMin,VarMax,VarSize); bee(i).Error=ObjFcn(bee(i).Position);
end
\%Sort the Solution
[ $\sim$, SortOrder]=sort([bee.Error]);
bee=bee(SortOrder);
\%Update Best Solution Ever Found

BestSol=bee(1);
\%Create Array to Hold Best Error Values

LowestError=zeros(MaxIt,1);

## \%Create Bees Algorithm Main Loop

for $\mathrm{it}=1$ :MaxIt

## \%Elite Sites

for $\mathrm{i}=1$ :nEliteSite bestnewbee.Error=inf;
for $\mathrm{j}=1$ :nEliteSiteBee newbee.Position=PerformBeeDance(bee(i).Position,r); newbee.Error=ObjFcn(newbee.Position); if newbee.Error<bestnewbee.Error bestnewbee=newbee;
end
end
if bestnewbee.Error<bee(i).Error bee(i)=bestnewbee;
end
end

## \%Selected Non-Elite Sites

for $\mathrm{i}=\mathrm{nEliteSite}+1$ :nSelectedSite
bestnewbee.Error=inf;
for $\mathrm{j}=1$ :nSelectedSiteBee newbee.Position=PerformBeeDance(bee(i).Position,r);

```
        newbee.Error=ObjFcn(newbee.Position);
        if newbee.Error<bestnewbee.Error
        bestnewbee=newbee;
        end
    end
    if bestnewbee.Error<bee(i).Error
        bee(i)=bestnewbee;
    end
end
%Non-Selected Sites
for i=nSelectedSite+1:nScoutBee
    bee(i).Position=unifrnd(VarMin,VarMax,VarSize);
    bee(i).Error=ObjFcn(bee(i).Position);
end
```

\%Sort the Solution
[ $\sim$, SortOrder]=sort([bee.Error]);
bee=bee(SortOrder);

# \%Store Best Error Ever Found <br> LowestError(it)=BestSol.Error; <br> OptimalSolution=BestSol.Position; 

## \%Display Iteration Information

disp(['Iteration ' num2str(it) ': Lowest Error = ' num2str(LowestError(it))]);
\%Define Damp Neighborhood Radius
$r=r$ * rdamp;
end
\%Display the Results
figure;
\%Make a Plot for Lowest Error
semilogy(LowestError,'LineWidth',2);
xlabel('Iteration');
ylabel('Lowest Error');
function $\mathrm{ObjFcn}=$
makeObjFcn(XTraining,YTrainingPoP,XValidation,YValidationPoP,XTesting,YTesting PoP)

```
ObjFcn = @ValidationErrorFunction;
    function AverageValidationError = ValidationErrorFunction(OptimalSolution)
```


## \%Specify Convolutional Neural Network Architecture

imageSize = [650 630 3];
layersPoP $=[$ imageInputLayer(imageSize)
convBlock(5,8, round(OptimalSolution(1,1)))
averagePooling2dLayer(4,'Stride',4)
$\operatorname{convBlock}(5,16$, round(OptimalSolution(1,1)))
averagePooling2dLayer(4,'Stride',4)
convBlock(5,32, round(OptimalSolution(1,1)))
averagePooling2dLayer(4,'Stride',4)
$\operatorname{convBlock}(5,64, \operatorname{round}($ OptimalSolution(1,1)))
averagePooling2dLayer(4,'Stride',4)
$\operatorname{convBlock}(5,128$, round(OptimalSolution(1,1)))
fullyConnectedLayer(1)
regressionLayer];
miniBatchSize $=64$;
validationFrequency $=$ floor $(1800 /$ miniBatchSize $)$;
optionsPoP = trainingOptions('sgdm', $\ldots$
'InitialLearnRate', OptimalSolution(1,2), ...
'Momentum', OptimalSolution(1,3), ...
'L2Regularization', OptimalSolution(1,4), ...
'MaxEpochs',20, ...
'MiniBatchSize',miniBatchSize, ...
'ValidationFrequency',validationFrequency, ...
'ValidationData',\{XValidation,YValidationPoP(:,1)\}, ...
'Shuffle','every-epoch', ...
'Plots','training-progress');

## \%Train Network using Training Data

netPoP = trainNetwork(XTraining,YTrainingPoP(:,1),layersPoP,optionsPoP);

```
\%Predict Responses and Compute Accuracy and Error
\(\mathrm{c}=1\);
```

PredictedTrainingPoP(:,c) = predict(netPoP,XTraining);
PredictedValidationPoP(:,c) = predict(netPoP,XValidation);

PredictedTestingPoP(:,c) = predict(netPoP,XTesting);

TrainingError(:,c) $=$ YTrainingPoP(:,1) - PredictedTrainingPoP(:,c);

AbsoluteTrainingError(:,c) = abs(TrainingError(:,c));
AverageTrainingError(:, c) $=\operatorname{sum}($ AbsoluteTrainingError(:, c) $) / 1800$;
numCorrectTrainingPoP(:,c) = sum(abs(TrainingError(:,(c))) < 0.05);
TrainingAccuracyPoP(:,c) = (numCorrectTrainingPoP(:,(c))/1800)*100;

ValidationError(:, c) = YValidationPoP(:,1) - PredictedValidationPoP(:,c);
AbsoluteValidationError(:,c) $=\operatorname{abs}($ ValidationError(:,c));

AverageValidationError(:,c) = sum(AbsoluteValidationError(:,c))/600;
numCorrectValidationPoP(:,c) $=\operatorname{sum}(\operatorname{abs}($ ValidationError(:,(c))) < 0.05);
ValidationAccuracyPoP(:,c) $=($ numCorrectValidationPoP(:,(c))/600)*100;

TestingError(:,c) = YTestingPoP(:,1) - PredictedTestingPoP(:,c);

AbsoluteTestingError(:,c) = abs(TestingError(:,c));
AverageTestingError(:,c) = sum(AbsoluteTestingError(:,c))/600;
numCorrectTestingPoP(:,c) = sum(abs(TestingError(:,(c))) < 0.05);

TestingAccuracyPoP(:,c) = (numCorrectTestingPoP(:,(c))/600)*100;

```
    end
end
```


## \%Create Bees Dance Function

```
function \(y=P e r f o r m B e e D a n c e(\) ValidationErrorFunction,r) nVar=numel(ValidationErrorFunction);
    k=randi([1 nVar]);
    y=ValidationErrorFunction;
    y(k)=ValidationErrorFunction(k)+unifrnd(-r,r);
end
function layers \(=\operatorname{convBlock}(\) FilterSize,NumberofFilters,SectionDepth \()\)
layers = [
    convolution2dLayer(FilterSize,NumberofFilters,'Padding','same')
    batchNormalizationLayer
    reluLayer];
layers = repmat(layers,SectionDepth,1);
end
```

function [XTraining, YTrainingPoP,XValidation, YV alidationPoP,XTesting, YTestingPoP] $=$ loadAPIData(ArtificialPorosityImagesDatasetPath)
location $=\operatorname{dir}($ ArtificialPorosityImagesDatasetPath $) ;$

Percent_of_Porosity = Actual_Percent_of_Porosity;

RN = $[18349199352202897189132675210627254241690900154825962947505$ 18022706149264827931652726185917692022878564210964656623762163 51824968985221049219225192221620121121522191261761828777697571692 16421555542779471509982554138228692633413280129342262132727701575 2881926274925736952100128110522511754279578326561446237120922288 1097154514742649229312327872986745170618682685253912413021842838 8932409125934810954817142359108213876057292211134310306931201621 24516099919902413188121055836918092954191737414631083299322792052 5741873131811578631921287218351501716032622150181180456017832001 12621331100318818585252411191262327041141287321709200493551136 1511277718192333658294327201845116016761849288218894251848722738 2828154244817752007281016721987133513504281818129626152142170211 176772133152410281131163815542213895546107810584171567011340226 4633061712295118621231299185115222718140628641726174518821915955 734148818478882529235312692204192129716492165113728022182743333 20729802991563294222481753296419996102485177029187085915571694 88372311932681173421581453196015522318951677133454947827891749 2745143317051223680886490141724165416272917516194297879026162299 8325186192191197337113015181693345265719952462407437242222741617 843614105520971142386107512332476138510720747101559208419242329 13012662382235422052095274097810341896469258115476620819081079 13491369288026993017392317164425611088147015642670200312711902493

141615212352077158011722296158917791332482860219676532329371206 73814423036661777185220962765361134625625732116148167183182661 23361123419954741152296238445678126362316181420282507268818982432 14074581909236609586272725132352486191022282652158210822174972345 14812983149413332350234465529397714352536529483267245729252383 21536027881830153928748055612995182410561313945257824151648661 16742187297322492927158193322107062754155023681792401143528811951 42253168682229994062336645128628573329573572126478072412231176 700106510892375755100528432247116126841659719468158169110472355 24027602671948455107412902563122725172471245176287721662521916 81028781324154924148592151280314761033242721282817254021802218 25769243258552420202159191221831576180845327112837117730211811827 29351051238935228492275168121224972962155394623242272172927172175 20913451963143711689641837222715911630223314751105147226018202381 19793342464284028584841738520257427121258349114241961628489901742 2093254919373912643297718752666248126839622621237818113325311147 21788345186750118983531750145127902010822348247415319565901196 25671890280723642188662260417671947215610011788143811735561050207 2679582171758526562717611586138829441175290462388543248226731238 17911777217681607785120019351117269525758421908155832225715612012 226110621749650258718251611740248712015452239791402248622951317 42298912661110606261120982416242815217674271532274125243391933 26892253376101818971409138014221121638146020381300279715059131465 39358711792598131612218412594257212632147507439153784148526902310 19762460234726081360176220262515111836431314364641967175152615 29761556147385421851086192816862721205111502875559275913661678 280915922311713142719511121122137179617082328862108116461181828 81372516941510391765144517412914197521771945206617956241341780 20509325701472783634157316631993591956162232317282186548811612 1365255314802551243824541396153729217021810155563067291714902687 6471906175923871355102888237222911045200206421172610270318511636

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20462751214518792787953751171822862432439128427471401178725521806 22522263880127717251704126724227131092139725001421216218401370 148612551251219729721594116313682629176360160720429427281444641 10809291221138973617611807732212196914822307246316181855982458 15461865947072538622207112735411066440150021182443283020539791305 1194266162214620751799201627841782212017520186372616697727621683 2955144794415172107110124369592426820625297438281152023315962456 88422417031108501275529001786311153896016313663471432299092827 7272887175429312516121838423011774254686116242761223615166818197 2027465132025201376249119086527965092544156221981557247916611013 2985274421337946482475541279193841467717762466240232711849052661 15072635196814366329654545342477739102419521667158777924122926 1372853491344100410778552124814580375208816371856431868276492987 975426711040704297519312407145054411265695212912219285529802269 146917321820541853163912702200994852168212281209740266516011780 50388113252446166298441828622420824136227661120290824807962742 47318781399356217625712570187199888216143406431588151019252961 298148722032792236253811147719851601981450353142029302912074335 10942597279128456817732752300016991801249022322922254825801643902 775101623493087091282125059348926312680301230177110632422842885 25301747211921351268107368228631100113611878128341109197717932768 121716882322143414042369260857284628351615151015724108724241964 2315985247838127520232289113923972794170215422692260023952154982 2590219913731354124727071544281929691411167125892705295316252240 292991192218232282316244466890410973728792157106026341383271248 19661932182158119571220125198924628185212264716160618848171457 1943103678651323741974200028167412091192926241468726222514952758 5781978207828212453276722151696224412297931760135315166015412377 1584396661813444258626782138185825019102627387278545225839761096 1330226625412029124313122179381236891727352267210595131514052820 156643457113151244135923961014152925602584161137926283289211498

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XTraining $=$ zeros $(650,630,3,1800)$;
YTrainingPoP = zeros(1800,1);
for $\mathrm{i}=1: 1800$

XTraining(:,:,:,i) = double(imread("S (" + RN(i) + ").jpg"));
YTrainingPoP(i,1) = Percent_of_Porosity(RN(i));
end

XValidation $=$ zeros $(650,630,3,600)$;

YValidationPoP $=\operatorname{zeros}(600,1)$;
for $\mathrm{i}=1801: 2400$
XValidation(:,:,:,i-1800) = double(imread("S (" + RN(i) + ").jpg"));
YValidationPoP(i-1800,1) = Percent_of_Porosity(RN(i));
end

XTesting $=$ zeros $(650,630,3,600)$;
YTestingPoP $=$ zeros $(600,1)$;
for $\mathrm{i}=2401: 3000$
XTesting(:,:,:,i-2400) = double(imread("S (" + RN(i) + ").jpg"));
YTestingPoP(i-2400,1) = Percent_of_Porosity(RN(i));
end
end

## Appendix 2: Curriculum Vitae

## Profile

Name: Nawaf Mohammad H Alamri

Date of Birth: 20/10/1992
Living area: Alrayyan Dist - Alharamain Road - Jeddah - Saudi Arabia - 23741
Mobile No: 07585697168
Email: alamrinm@cardiff.ac.uk
Nationality: Saudi Arabia

## Objective

I would like to focus my career on teaching, making research and consulting in industrial engineering cases by using the best practices in a creative way. I also aim to develop new skills and competence and acquire practical experience to be compatible with every changing work demand of the labour market

## Education

- Currently, I am studying PhD in Engineering in the field of in Mechanics, Material and Advanced Manufacturing at Cardiff University since 2019
- MSc. in Manufacturing Engineering Innovation and Management at Cardiff University with Merit Classification (2018-2020)
- MSc. in Industrial Engineering at King Abdulaziz University with a GPA 4.97 out of 5 (2016-2019)
- BSc. in Industrial Engineering at King Abdulaziz University with a GPA 4.97 out of 5 (2010-2015)
- I awarded Superior certificate in 2010-2011, 2011-2012, 2012-2013, and 20132014
- I graduated from high school in 2010 with Grade $\mathbf{9 9 . 9 5 \%}$


## Experience

- Currently, I am Teaching Assistant at King Abdulaziz University since 2017 and at Cardiff University since 2019
- 2 years of experience at supply chain department in Abdul Latif Jameel Group (2015-2017)
- Part time job in research and consulting institute at King Abdulaziz University (2013-2015)
- Students' representative in ABET evaluation meetings during the assessment visit
- Teaching assistant (Design of Experiments course) in Industrial Engineering department at King Abdulaziz University
- Grader in Introduction to Engineering Design course at King Abdulaziz University


## Training

- Entrepreneurship course at Al-Ahli Bank entitled How to start your small project (2013)
- Riyali course (Financial Literacy Program) at King Abdulaziz University (2013)
- English course at New Horizons institute (2010)


## Skills

- Developing and analysing Convolutional neural network models using MATLAB
- Developing and analysing neural network models using MATLAB
- Performing statistical analysis using Minitab
- Analyzing engineering experiments using Design-Expert
- Performing data mining using WEKA software
- Designing database system using oracle application
- Simulation and Animation using Arena Package
- Analysis of Supply Chain systems
- Conducting management self-assessment based on EFQM criteria
- Applications of project management tools \& techniques


## Projects

- Applying Deep Learning Algorithm to Achieve Automized Porosity Assessment for Additive Layer Manufacturing Process
Developing convolutional neural network and long short term memory algorithms to predict the percent of porosity in the finished selective laser melting parts achieving automized porosity assessment
- Applying Machine Learning Algorithm for a Milling Process Simulator for Process Modelling and Optimisation
Implementing neural network algorithm for a milling process simulator in order to model and optimize the process
- Water and Electricity Consumption Analysis using DEA and Regression Analysis: Future Prediction Considering Saudi Vision 2030

Identifying the relative efficiency of water consumption for the five main regions in Saudi Arabia and predicting the future consumption and production of the water and electricity considering strategy in Saudi Vision 2030

## - Research and Consultant Institute Project

Redesigning business process in this institute using simulation, design of experiment and operation Research to solve this problem

## - Ejector Pump Project

Applying response surface technique to find the best ejector pump for a system, the project was a part of joint work between King Abdulaziz University and Missouri University in USA

- Maintenance C-check Project

Simulating and optimizing the maintenance C-Check process at Saudi Airlines

- EFQM Project

Conducting management self-assessment based on EFQM criteria on research and consulting institute

## - Assembly Task Performance

Identifying the most influential factors on human body during assembly task performance

## - Database Project

Designing a reservation system for an airline company using oracle applications

## - Reaction Time Project

Identifying the most influential factors on human reaction time using Design of Experiments technique

## Voluntary Work

Member of the organizing committee of the eighth Engineering day (2014) at King Abdulaziz University (Leader of the team in charge of introducing Industrial Engineering field to junior students)

## References

- Prof. Seraj Y. Abed

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