# Multiplexity of Human Brain Oscillations as a Personal Brain Signature 

Abbreviated Title: A Personalized Multiplex Human Brain Signature

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## 1. Hidden Markov Modeling

Baum-Welch algorithm finds values for HMM parameters that best fit the observed data. For training we need:

- sequence of observations $\mathrm{O}_{1}, \mathrm{O}_{2}, \ldots, \mathrm{O}_{\mathrm{n}}$
- sequence of hidden states for these observations $S_{1}, S_{2}, \ldots, S_{n}$

Algorithm tries to estimate transition matrix $A$ and emission matrix $B$ using values of $O$ and $S$. Since, we don't known the O and S , we assigned a random initial guess of their values. Then, the algorithm iterates using the training $\mathrm{DoCM}^{\text {ts }}$ and re-calculate both O and S matrices till the convergence of the algorithm.

## Expectation maximization

Baum-Welch algorithm is using expectation maximization (EM) approach to find values for $A$ and $B$.

1. Initialize $A$ and $B$ with some initial values (done only once)
2. Then, the algorithm estimates latent variables $\xi_{i j}(t)$ and $\gamma_{i}(t)$ using $A, B, O$ and $S$. This step estimates how much each transition and emission has been employed. This is called the 'estimation step'.
3. Then, the algorithm maximizes $A$ and $B$ matrices employing estimations (latent variables) from previous steps. This is called the 'maximization step'
4. The procedure continues until its convergence

## Initial equations

For the estimation of $A$ and $B$ matrices, we used the following formulas (source):

1. $A=a_{i j}$ (probability of transition from hidden state $i$ to hidden state $j$ )= expected number of transitions from hidden state i to state $\mathrm{j} /$ expected number of transition from hidden state i
2. $B=b_{j k}$ (probability of observing observation $O_{k}$ in hidden state $j$ )= expected number of times model is in hidden state j and we observe $\mathrm{O}_{\mathrm{k}}$ / expected number of times in hidden state j

The probability $\mathrm{a}_{\mathrm{ij}}$ could be defined as the probability of being in hidden state i at time t and in hidden state j at time $t+1$, given the observation sequence $O$ and the model (source). The described procedure can be graphically showed as follows:


S1. Current step probability with forward, backward and emission probability

In the graph we are at time t , we know probability that we are at the current hidden state $S_{i}\left(\right.$ this is forward probability $\left.\alpha_{i}(t)\right)$, we know hidden probabilities going from hidden state $S_{j}$ to the end of the sequence using backward probabilities $\beta_{i_{+1}}(t)$. We want to get probability of going from $S_{i}$ to $S_{j}$ and given that we have observed $O_{t+1}$ in $S_{j}$ at $t+1$.

Here we'll make use of latent variables $\xi_{\mathrm{ij}}(\mathrm{t})$ and $\gamma_{i}(\mathrm{t})$ :

- $\xi_{\mathrm{ij}}(\mathrm{t})$-probability of transition from hidden state i to hidden state j at time t given observations:

$$
\begin{equation*}
\left.\varepsilon_{i j}(t)=\right) P\left(X_{t}=i, X_{t+1}=j \mid Y, \Theta\right)=\frac{P\left(X_{t}=i, X_{t+1}=j, Y \mid \Theta\right)}{P(Y \mid \Theta)}=\frac{\alpha_{i}(t) a_{i j} b_{j}\left(O_{t+1}\right) \beta_{j}(t+1)}{\sum_{i=1}^{M} \sum_{j=1}^{M} \alpha_{i}(t) a_{i j} b_{j}\left(O_{t+1}\right) \beta_{j}(t+1)} \tag{1}
\end{equation*}
$$

Note that denominator $\mathrm{P}(\mathrm{O} \mid \Theta)$ means probability of the observation sequence O by any path given the model $\Theta$. $\xi_{\mathrm{ij}}(\mathrm{t})$ is defined for time t only. We have to sum over all time-steps to get the total joint probability for all the transitions from hidden state i to hidden state j (calculate $a_{i j}$ ). This will be our numerator of the equation of $a_{\mathrm{ij}}$. For denominator we could use marginal probability which means the probability of being in state $i$ at time $t$, whole equation has the following form:

$$
\begin{equation*}
a_{i j}=\frac{\sum_{t=1}^{T-1} \varepsilon_{i j}(t)}{\sum_{t=1}^{T-1} \sum_{j=1}^{M} \varepsilon_{i j}(t)} \tag{2}
\end{equation*}
$$

Denominator could be expressed differently and leads to a new latent variable $\gamma_{i}(t)$ :

$$
\begin{equation*}
\sum_{j=1}^{M} \varepsilon_{i j}(t)=\frac{\alpha_{i}(t) \beta_{i}(t)}{\sum_{i=1}^{M} \alpha_{i}(t) \beta_{i}(t)}=\gamma_{i}(t) \tag{3}
\end{equation*}
$$

$Y_{i}(t)$-probability at given state $i$ at time $t$ given observations. We can use it to calculate $a_{i j}$ (our previous formula for $\mathrm{a}_{\mathrm{ij}}$ is also valid):

$$
\begin{equation*}
a_{i j}=\frac{\sum_{t=1}^{T-1} \varepsilon_{i j}(t)}{\sum_{t=1}^{T-1} \gamma_{i}(t)} \tag{4}
\end{equation*}
$$

We can use $\gamma_{i}(t)$ to calculate $b_{j k}$ (which is the probability of a observation $\mathrm{O}_{\mathrm{k}}$ from the observations O given hidden state j):

$$
\begin{equation*}
b_{j k}=\frac{\sum_{t=1}^{T-1} 1_{O_{t}=k} \gamma_{i}(t)}{\sum_{t=1}^{T-1} \gamma_{i}(t)} \tag{5}
\end{equation*}
$$

Note that $1_{\mathrm{ot}=\mathrm{k}}$ is an indicator function which has value 1 , if observation $\mathrm{O}_{\mathrm{t}}$ belongs to class k and 0 if it doesn't.

## Expectations and maximization in HMM

Based on the aforementioned equations, we can calculate components separately under the form of EM approach. We have to follow these two steps:

- Calculate expected value of latent variables $\xi_{i j}(t)$ and $\gamma_{i}(t)$. One can either I initialize $A$ and $B$ randomly or use some previous knowledge if we have it. Here, we used the DoCM ${ }^{\text {ts }}$ for every subject's ROI from the scan session 1 to initialize A and B.
- Maximize values of $A$ and $B$ by using equations for $a_{i j}$ and $b_{j k}$. And go for a next round by using new $A$ and $B$ values for estimating $\xi_{i j}(t)$ and $\gamma_{i}(t)$.

We have only observations and we start with random guess (or if we have some more information we could use it). We estimate our latent variables which we'll be then used to maximize $A$ and $B$. At each step we get a better estimation for $A$ and $B$ until improvements are small and algorithm will converge.

## 2. Nodes to networks mapping

STable 1 tabulates the id, the full name of each brain area's, its name according to AAL (Rolls et al., 2015), the located lobe, the abbreviated name and also the corresponding network used in our study. Here, we used the first 90 areas excluding the cerebellum brain areas (91-116).

The Default Mode Network (DMN) involves the following brain areas :

|  | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 23 | 24 | 25 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 26 | 27 | 28 | 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 | 55 | 56 | 61 | 62 |  |
| 65 | 66 | 67 | 68 | 85 | 86 | 87 | 88 | 89 | 90 |  |  |  |  |  |  |  |  |

The Occipital (0) network involves the following brain areas:
4344454647484950515253545556

The Cingulo-Opercular (CO) network involves the following brain areas:
29,30 31,32, 77,78

The Sensory-Motor (SM) network involves the following brain areas:
1219205758

The Fronto-Parietal (FP) network involves the following brain areas:
1314151617183536596061626364656667686970

STable 1. The anatomical regions defined in each hemisphere and their label in the automated anatomical labeling atlas - AAL (Rolls et al., 2015). Odd/even numbers refer to the left/right homologue brain areas.

| ID | Region Description | AAL | Lobe | Abbreviation |
| :---: | :---: | :---: | :---: | :---: |
| 1,2 | Precentral gyrus | Precentral | Sensorimotor | PreCG |
| 3,4 | Superior frontal gyrus, dorsolateral | Frontal Sup | Frontal | SFG |
| 5,6 | Superior frontal gyrus, orbital | Frontal_Sup_Orb | Frontal | SForb |
| 7,8 | Middle frontal gyrus | Front_Mid | Frontal | FMid |
| 9,10 | Middle frontal gyrus, orbital | Front_Mid_Orb | Frontal | FMorb |
| 11,12 | Inferior frontal gyrus, opercular | Front_Inf_Oper | Frontal | IFoper |
| 13,14 | Inferior frontal gyrus, triangular | Front Inf_Tri | Frontal | IFtri |
| 15,16 | Inferior frontal gyrus, orbital | Front_Inf_Orb | Frontal | IForb |
| 17,18 | Rolandic operculum | Rol_Öper | Frontal | Roloper |
| 19,20 | Supplementary motor area | Supp_motor_Area | Sensorimotor | SMA |
| 21,22 | Olfactory cortex | Olfactory | Frontal | OLF |
| 23,24 | Superior frontal gyrus, medial | Frontal_Sup_Med | Frontal | SFGmedial |
| 25,26 | Superior frontal gyrus, medial orbital | Frontal_Med_Orb | Frontal | PFCventmed |
| 27,28 | Gyrus rectus | Rectus | Frontal | REC |
| 29,30 | Insula | Insula | Subcortical | INS |
| 31,32 | Cingulate gyrus, anterior part | Cingulate_Ant | Frontal | ACC |
| 33,34 | Cingulate gyrus, mid part | Cingulate_Mid | Frontal | MCC |
| 35,36 | Cingulate gyurs, posterior part | Cingulate_Post | Parietal | PCC |
| 37,38 | Hippocampus | Hippocampus | Temporal | HIP |
| 39,40 | Parahippocampal Gyrus | Parahippocampal | Temporal | PHG |
| 41,42 | Amygdala | Amygdala | Subcortical | AMYG |
| 43,44 | Calcarine fissure and surrounding cortex (V1) | Calcarine | Occipital | V1 |
| 45,46 | Cuneus | Cuneus | Occipital | CUN |
| 47,48 | Lingual | Lingual | Occipital | LING |
| 49,50 | Superior Occipital Gyrus | Occipital_Sup | Occipital | SOG |
| 51,52 | Middle Occipital Gyrus | Occipital_Mid | Occipital | MOG |
| 53,54 | Inferior Occipital Gyrus | Occipital_Inf | Occipital | IOG |
| 55,56 | Fusiform Gyrus | Fusiform | Occipital | FFG |
| 57,58 | Postcentral Gyrus | Postcentral | Sensorimotor | PoCG |
| 59,60 | Superior parietal Gyrus | Parietal_Sup | Parietal | SPG |
| 61,62 | Inferior parietal Gyrus | Parietal_Inf | Parietal | IPG |
| 63,64 | Supramarginal Gyrus | Supramarginal | Parietal | SMG |
| 65,66 | Angular Gyrus | Angular | Parietal | ANG |
| 67,68 | Precuneus | Precuneus | Parietal | PCUN |
| 69,70 | Paracentral Lobule | Paracentral_Lobule | Parietal | PCL |
| 71,72 | Caudate nucleus | Caudate | Subcortical | CAU |
| 73,74 | Lenticular nucleus, Putamen | Putamen | Subcortical | PUT |
| 75,76 | Lenticular nucleus, |  |  |  |
|  | Pallidum | Pallidum | Subcortical | PAL |
| 77,78 | Thalamus | Thalamus | Subcortical | THA |
| 79,80 | Heschl's Gyrus | Heschl | Temporal | HES |
| 81,82 | Superior Temporal Gyrus | Temporal_Sup | Temporal | STG |
| 83,84 | Temporal Pole |  |  |  |
|  | Superior Temporal Gyrus | Temporal_Pole_Sup | p Temporal | TPOsup |

85,86 Middle Temporal Gyrus
87,88 Temporal Pole
Middle Temporal Gyrus
89,90 Inferior Temporal Gyrus

| Temporal_Mid | Temporal | MTG |
| :--- | :--- | :--- |
| Temporal_Pole_Mid | Temporal | TPOmid |
| Temporal_Inf | Temporal | ITG |

## References

1. Rolls, E. T., Joliot, M., and Tzourio-Mazoyer, N. (2015). Implementation of a new parcellation of the orbitofrontal cortex in the automated anatomical labeling atlas. Neuroimage 122, 1-5. doi: 10.1016/j.neuroimage.2015.07.075
