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SkipPLUS: Skip the First Few Layers to Better Explain Vision Transformers

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Abstract

Despite their remarkable performance, the explainability of Vision Transformers (ViTs) remains a challenge. While forward attention-based token attribution techniques have become popular in text processing, their suitability for ViTs hasn't been extensively explored. In this paper, we compare these methods against state-of-the-art input attribution methods from the Vision literature, revealing their limitations due to improper aggregation of information across layers. To address this, we introduce two general techniques, PLUS and SkipPLUS, that can be composed with any input attribution method to more effectively aggregate information across layers while handling noisy layers. Through comprehensive and quantitative evaluations of faithfulness and human interpretability on a variety of ViT architectures and datasets, we demonstrate the effectiveness of PLUS and SkipPLUS, establishing a new state-of-the-art in white-box token attribution. We conclude with a comparative analysis highlighting the strengths and weaknesses of the best versions of all the studied methods. The code used in this paper is freely available at https://github.com/NightMachinery/ SkipPLUS-CVPR-2024.

1. Introduction

Transformers currently dominate various NLP tasks and are gaining significant popularity in the field of computer vision [20, 23, 53, 57, 71]. Despite their remarkable success, a crucial challenge remains in comprehending their inner workings, which poses risks in real-world deployments. Consequently, there is an increasing demand for research that explains the outputs of Transformers [15, 41, 48, 60].

Input attribution methods are techniques designed to quantify the influence of individual input features, or groups



Figure 1. This figure presents a qualitative comparison of the composition of the proposed SkipPLUS method with the Forward Attention-Based Token Attribution technique DecompX, using the EVA Large model. Brighter shades signify an increased positive contribution of features towards the prediction of the target class. The results illustrate that DecompX-SkipPLUS effectively concentrates on the target class ("Newt" in this image) while minimizing noise. In contrast, GenAtt, the previous state-of-the-art method, exhibits suboptimal performance on EVA Large, falling behind baselines such as GradCAM. For additional qualitative examples, including multi-class instances, refer to Figs. 5 and 6, as well as the appendices.

of them, on a model's output [6, 38, 43, 44, 61, 68, 69, 80]. Input attribution methods can assist in understanding a model's decision locally for a single input considered in isolation. They also act as foundational elements for more advanced explanation techniques. For instance, in concept-based explanation methods like CRAFT [25], attribution methods are employed for two main purposes: to quantify the impact of each activated concept and to identify the specific input features responsible for activating these concepts.

Early works used the raw self-attention weights of the last layer as a token attribution map [8, 11, 32]. Recent studies have questioned the reliability of this approach, given

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Figure 2. Starting DecompX from Different Layers

that self-attention is only a small part of a Transformer block [15, 35, 64, 75]. Forward Attention-Based Token Attribution methods [1, 26–28, 47] try to address this issue by incorporating other components of the block. These methods have been primarily developed and evaluated on text Transformers and their effectiveness in Vision Transformers has not been thoroughly investigated.

In this paper, we conduct a comprehensive study comparing Forward Attention-Based Token Attribution methods against popular interpretation techniques used in the Vision literature. Our findings reveal that, in their original formulation, Forward Attention-Based Token Attribution methods do not perform well for Vision Transformers, mainly due to their improper aggregation of information across layers.

To address this limitation, we propose PLUS and Skip-PLUS, simple techniques that can be applied to a wide range of input attribution methods, without imposing any specific prerequisites. We perform extensive quantitative evaluations on a variety of ViT architectures and datasets to assess the faithfulness and human interpretability of the proposed method. Our results show that composing Skip-PLUS with recent text-based interpretation techniques can significantly enhance their performance, surpassing all the widely-used techniques for interpreting vision models. Encouraged by this success and the composability of these techniques, we compose PLUS and SkipPLUS with other attribution methods. This integration enhances the effectiveness of many traditional methods without compromising performance when it proves unhelpful. (See Fig. 4 and Sec. C in the appendices for further details.)

Finally, we provide a comparative analysis of the best versions of all the studied methods, highlighting their strengths and weaknesses.

2. Related Work

Owing to space constraints, this section will briefly introduce only the most fundamental methods. A comprehensive overview of additional methods is provided in the appendix, detailed in Sec. E.

2.1. Gradient-Based Methods

Input×**Gradient (IxG).** IxG [2, 66, 67] multiplies the input values by their corresponding gradients. Let x_i be a spatial feature of the input, where $x_{i,j}$ represents the *j*-th channel of x_i . The Input×Gradient attribution for the spatial feature x_i with respect to the target class *c* is computed as follows, where y_c is the output of the model for the target class c:

Input×Gradient_i =
$$\sum_{i} \frac{\partial y_c}{\partial x_{i,j}} \cdot x_{i,j}$$
, (1)

2.2. Forward Attention-Based Token Attribution Methods

Rollout. Rollout [1] is a technique used to aggregate the attribution maps from different self-attention layers in Transformer models. While Rollout was originally developed for aggregating attention weights across layers, it can be applied to any attribution method that produces a 2D From-To attribution matrix for each layer. The Rollout method linearly multiplies the attribution maps from each layer.

Given the attribution map T_i at the *i*-th layer, the Rollout operation updates the accumulated attribution map R_i that has aggregated information up to the *i*-th layer. The update rule for the accumulated attribution map is as follows:

$$\mathbf{R}_0 = \mathbf{I}, \quad \mathbf{R}_{i+1} = (0.5\mathbf{I} + 0.5\overline{\mathbf{T}}_i)\mathbf{R}_i \tag{2}$$

where I is the identity matrix, and $\overline{\mathbf{T}}_i$ is the normalized attribution map of the *i*-th layer. The normalization ensures that the sum of each row in the attribution map is one, mirroring the behavior of attention weights. Some methods forgo the 0.5I term and/or the normalization step in the Rollout operation.

3. Methodology

3.1. Progressive Layer Unification Through Summation (PLUS)

Let f be a model with L layers (numbered from 0 to L-1), and A be an attribution method that takes a model and an input, and produces an attribution map. Given an input x_0 to the model, we define Progressive Layer Unification Through Summation (PLUS) as:

$$PLUS(f, A)(x_0) = \sum_{l=0}^{L-1} A(f_l)(x_l)$$
(3)

where f_l is the sub-network of f starting from layer l(and going until the end of the model), and x_l is the intermediate output of the model at layer l - 1 when the input is x_0 . Note that the layer numbers are zero-based, so f_0 is equivalent to the full model f. In essence, PLUS varies the start layer of the underlying attribution method A from the first to the last layer and aggregates the resulting attribution maps through summation.

3.2. SkipPLUS

SkipPLUS is a variant of PLUS that starts the aggregation from the middle layer instead of the first layer. Formally, let $m = \lceil \frac{L}{2} \rceil$ be the middle layer of the model f. Then, SkipPLUS is defined as:

$$SkipPLUS(f, A)(x_0) = \sum_{l=m}^{L-1} A(f_l)(x_l)$$
(4)

In other words, SkipPLUS skips the first m layers and only aggregates the attribution maps starting from the middle layer m.

For a discussion on the justification and insights behind these methods, refer to Sec. 5.1.

3.3. FullGrad+

FullGrad [70] extends the Input×Gradient (IxG) method [38] by computing attribution maps not only for the original input but also for each bias term in the network. The final attribution map is obtained by summing the IxG attribution map of the input with the bias attribution maps.

Directly applying PLUS or SkipPLUS on FullGrad would lead to multiple sums of the bias attribution maps of the later layers, as the bias attribution maps of layer lalso appears in FullGrad (f_k) for k less than l. To avoid this repetition, we define FullGrad+ as follows:

FullGrad+
$$\circ$$
 PLUS $(f)(x_0) =$

$$\sum_{l=0}^{L-1} \operatorname{IxG}(f_l)(x_l) + \sum_{l=0}^{L-1} \sum_{b \in B_l} \operatorname{IxG}(f_b)(b) \quad (5)$$

FullGrad+
$$\circ$$
 SkipPLUS $(f)(x_0) =$

$$\sum_{l=m}^{L-1} \text{IxG}(f_l)(x_l) + \sum_{l=m}^{L-1} \sum_{b \in B_l} \text{IxG}(f_b)(b)$$
 (6)

where $IxG(f_l)(x_l)$ is the Input×Gradient attribution map of the sub-network f_l with input x_l , and $IxG(f_b)(b)$ is the Input×Gradient attribution map of the sub-network f_b with a bias term b from layer l as the input. f_b is the sub-network of f starting from the bias term b and going until the end of the model. B_l denotes the set of all bias terms in layer l. FullGrad+ aggregates the input attribution maps of each layer along with the attribution maps of all bias terms in each layer, ensuring no repetition occurs. Refer to Fig. 10 (in the appendices) for a quantitative evaluation of Full-Grad+ versus FullGrad, and Fig. 6 for a qualitative comparison.

3.4. Special Cases of PLUS in Prior Work

The methods described below can be viewed as special cases of PLUS, where PLUS is composed with a previously existing method.

GradSAM. GradSAM [4] is equivalent to composing GenAtt [10] with PLUS, instead of using Rollout. (cf. Fig. 9 in the appendices)

CAT. Class Activation Tokens [56] is equivalent to $IxG \circ PLUS$. (cf. Fig. 11 in the appendices)

AttCAT. We can define an attention-enhanced variant of IxG, AttIxG, by multiplying IxG with AttnFrom:

$$\mathtt{AttnFrom}_j = rac{1}{H imes N} \sum_{h=1}^{H:=\mathtt{Heads}} \sum_{i=1}^{N:=\mathtt{Tokens}} \mathtt{Raw} \mathtt{Attn}_{h,i,j}$$

Note that attention weights have three dimensions: heads, to, from.

Attentive Class Activation Tokens [56, AttCAT] would then be equivalent to AttIxGoPLUS. (cf. Fig. 11 in the appendices)

LayerCAM. LayerCAM [36] was introduced for ReLU CNN networks, where it is equivalent to applying a normalization process on the layer-wise attribution maps obtained from GradCAMElementWise [31], followed by the PLUS aggregation method. The normalization step is proposed because earlier layers tend to have smaller attribution maps compared to later layers. By normalizing the maps, LayerCAM ensures that each layer contributes more equally to the final attribution map. However, this approach is not suitable for ViTs, as we explicitly want to avoid giving earlier layers the same impact on the final attribution map as later layers (cf. Fig. 2, also supported by our preliminary quantitative evaluations).

4. Experimental Setup

4.1. Faithfulness Evaluation Metrics

Modern literature favors evaluations for input attribution methods that are collectively called faithfulness, which intuitively measures how well the attribution scores reflect the true contribution of each input feature to the target output. Although several metrics have been proposed to quantify faithfulness, we adopt the most comprehensive approach, which involves computing the area under the curve (AUC) for the deletion and insertion operations, considering the changes in accuracy and the target probability [14, 27, 47, 50]. The deletion accuracy curve is obtained by progressively removing input features in order of decreasing attribution scores and measuring the model's accuracy at each step. A faithful attribution method should result in a steep drop in performance as the most important features are removed first. The deletion accuracy scores are normalized using the formula 100-x, where x is the original score, so that higher scores always indicate better performance.

Similarly, the deletion AOPC curve is generated by gradually removing input features in order of decreasing attribution scores and evaluating the change in the target output probability at each step. A faithful attribution method should lead to a rapid decrease in the target probability as the most important features are removed first.

Conversely, the insertion accuracy curve is generated by gradually adding input features in order of decreasing attribution scores and evaluating the model's performance at each step. A faithful attribution method should lead to a rapid increase in performance as the most important features are added first. Sec. A.1 in the appendices explains these metrics in more detail.

True Token Masking. Instead of simply overlaying a color mask, we choose to completely exclude the masked patches from the model's input [16]. At the same time, we preserve accurate positional encodings for the unmasked patches. (cf. Sec. A.2 in the appendices)

4.2. Human Interpretability Evaluation

Although lacking a strong theoretical justification, human interpretability evaluations serve as effective sanity checks and provide a quantitative measure that aligns with intuitive inferences drawn from qualitative examples of attribution methods. Following the zero-shot segmentation setup proposed by [11], we report the Average Precision (AP) metric. This evaluation requires a dataset with ground truth labels for the target class. Notably, AP is invariant to shift and scale transformations, mirroring the properties of our faithfulness metrics.

4.3. Models, Task, and Datasets

We assess three models on two datasets. First, we employ EVA Large (Patch Size 14) [23], a top-performing ViT model in the timm library [76], pretrained on image-text reconstruction and finetuned on ImageNet [18]. Second, we use ViT Base (Patch Size 8) [20], pretrained and finetuned on ImageNet, choosing a model size (Base) and a patch size (8) to maximally differ from our previous choice of EVA

Large (Patch Size 14); this aligns with prior work [11, 78] that evaluate attribution methods on the vanilla ViT. Third, following [16], we use MURA ViT Base (Patch 16), trained on the MURA dataset. MURA [58] contains bone X-rays labeled as normal or abnormal.

All models serve as image classifiers, and the attribution target is set to the ground truth label for a better assessment of class discriminativity [11]. We use ImageNet due to its prevalence in prior work, the availability of high-quality ViT finetunes in timm, and its challenging 1000-class setting. We randomly select 5000 images from the ImageNet-1k validation set and 2000 images from the MURA training set, using fixed seeds for reproducibility.

For segmentation evaluations, we use ImageNet-S [30] ground truth segmentation maps, which encompasses 919 distinct classes, with a random subset of 5000 images from the validation set. The target is set to the class with the largest area in the ground truth segmentation map. Token attribution methods generate token-level rather than pixel-level maps. Consequently, we apply nearest interpolation to upscale these token-level maps to pixel-level.

5. Results

5.1. Justification for PLUS and SkipPLUS

Fig. 3 shows that Forward Attention-Based Token Attribution methods, most of which use Rollout, are not competitive with the previous SOTA in ViT-specific attribution methods. This underperformance can be partially attributed to the vanishing attributions problem, which arises from the multiplication of small numbers in each layer, resulting in nearly zero values in the final aggregated output.

The severity of the vanishing attributions problem varies depending on the combination of the model and the attribution method used. For example, ALTI-Rollout [27] suffers from severe vanishing attributions on ViT Base due to the presence of ReLU operations in the layer-wise maps, resulting in almost all-zero attribution maps (Fig. 5) and performance worse than the random baseline. However, it performs competitively on EVA Large. GlobEnc-Rollout [45], which does not involve ReLU operations, avoids vanishing attributions on ViT Base but exhibits the issue on EVA Large (cf. D.2 in the appendices). Other Rollout-based methods, such as GenAtt [10], do not encounter the vanishing attributions problem on any of the evaluated models.

DecompX [47], a successor to older methods such as GlobEnc and ALTI, does not need to produce layer-wise attribution maps and aggregate them separately. However, Fig. 2 shows that when DecompX starts from the initial layers and propagates attribution scores to the end of the network, it results in noisy attribution maps. Simply starting later can significantly boost the performance, but choosing this optimal layer can be challenging. As many leading

EVA2 and EVA Giant outperform EVA Large, but our fork of timm did not support them. We also lacked the resources for evaluating on the Giant variants. (cf. https://github.com/huggingface/ pytorch-image-models/blob/main/results/resultsimagenet-real.csv)

Transformer-specific methods (e.g., GenAtt) aggregate information across multiple layers using Rollout, one might be tempted to use Rollout on DecompX. However, this is not (naively) possible, as Rollout requires a 2D From-To attribution matrix for each layer, while DecompX simply produces a 1D From-Target vector with a single target.

These observations lead us to propose Progressive Layer Unification Through Summation (PLUS). PLUS involves varying the start layer of the underlying attribution method from the very first layer to the very last and aggregating the resultant attribution maps through summation. While PLUS successfully enhances the performance of Forward Attention-Based Token Attribution methods, surpassing previous white-box state-of-the-art methods from ViT and CNN literature, we might wonder what happens if we drop the noisy layers altogether from our aggregated output. We conduct evaluations dropping the starting layers one by one from the layers considered in PLUS (cf. Sec. B in the appendices). We see that two points emerge naturally to start the aggregation from: one is the very first layer, and the other is the middle layer. We name this latter variant SkipPLUS, which achieves state-of-the-art performance (cf. Fig. 4).

As PLUS and SkipPLUS have no constraints on the base attribution method they wrap around, we also evaluate their compositions with many other methods (cf. Sec. C in the appendices). This investigation leads to improving several methods. Notably, even when composing a method with PLUS does not help, it usually does not degrade performance considerably either. This makes PLUS and Skip-PLUS robust methods that can be used with other methods without thorough evaluations.

5.2. Comprehensive Benchmark of White-Box Attribution Methods on Vision Transformers

Having enhanced several underperforming and underrated methods, we now present a thorough and modern benchmark of the best versions of all the methods studied in Fig. 4. DecompXoSkipPLUS outperforms all other methods, including its original version DecompX, by a significant margin, except in the insertion faithfulness tests on EVA Large, where it remains competitive with the best method, AttIxGoPLUS. In general, the topperforming methods are compositions of PLUS and Skip-PLUS, with some even incorporating classic methods such as IxGoSkipPLUS.

Another interesting observation is the high performance of the random baseline on the insertion faithfulness tests, which signifies the robustness of Vision Transformers to random token omissions. In insertion tests, the goal is to insert patches so that the model reaches the correct target class faster; as the model is robust against random omissions, this happens quickly. However, the random baseline does not fare well in the deletion faithfulness tests. In deletion tests, the aim is to adversarially delete strategic tokens to change the model's decision. Here, the model's robustness acts against the random baseline.

In general, we observe a trade-off between insertion performance and deletion, and a positive correlation between deletion performance and segmentation performance (AP). This trade-off can also be seen when selecting which layers to drop from PLUS in Sec. C in the appendices. Prior work has also reported similar trade-offs [61]. However, a strong method such as DecompXoSkipPLUS manages to achieve almost optimal performance in all metrics, highlighting the possibility of attaining high performance despite the tradeoffs.

6. Conclusion

We conducted a comprehensive evaluation of white-box token attribution methods for Vision Transformers (ViTs). We compared Forward Attention-Based Token Attribution methods, originally developed for text Transformers, against state-of-the-art input attribution methods from the ViT and CNN literature. Our analysis revealed the limitations of these methods due to improper aggregation of information across layers.

To address these limitations, we introduced Progressive Layer Unification Through Summation (PLUS) and Skip-PLUS, two general techniques that can be combined with any input attribution method to more effectively aggregate information across layers while handling noisy layers. Through extensive quantitative evaluations of faithfulness and human interpretability on various ViT architectures and datasets, we demonstrated the effectiveness of PLUS and SkipPLUS. We also conducted thorough qualitative comparisons, including an analysis of multi-class qualitative examples to assess class discriminativity. Our comprehensive approach, combining quantitative and qualitative analyses, establishes a new state-of-the-art in white-box token attribution.

Future work could explore the application of these techniques to other domains (e.g., text Transformers) and investigate combining them with other explainability methods to further improve the interpretability of Transformers.

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Figure 3. Composing PLUS and SkipPLUS with Forward Attention-Based Token Attribution methods is helpful in increasing performance across all metrics. 6



Figure 4. Best versions of methods compared against each other. The axis hidden under the legend corresponds to Deletion Accuracy. (cf. Sec. 5.2 for analysis)



Figure 5. The SkipPLUS method can be applied in conjunction with any attribution technique to improve its performance. In contrast, the Rollout aggregation approach is not robust; its multiplicative properties frequently lead to suboptimal interactions with the ReLU operation in ALTI, resulting in attribution maps that are largely composed of zero values. Further qualitative examples are provided in the appendices. The model employed in this figure is ViT Base (Patch Size 8).



Figure 6. This figure presents a preliminary qualitative evaluation of the class discriminativity of various attribution methods applied to the EVA Large model. Theoretically class-insensitive methods such as ALTI and GlobEnc have been excluded from this analysis. The images selected for this evaluation are among the few suitable instances in the COCO 2017 training set [42] that contain both zebras and elephants within the same frame, with the animals mostly visible and not cropped out. We chose zebras and elephants because prior work, such as [34], has also used these animals in their evaluations. Additionally, ImageNet has a single class for zebras and three classes for elephants (we chose "African Elephant" as the target class here), which is in contrast to most other animals that can have tens of different fine-grained ImageNet classes.

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A. Further Experimental Details

A.1. Faithfulness Evaluation Metrics

Modern literature favors evaluations for input attribution methods that are collectively called faithfulness, which intuitively measures how well the attribution scores reflect the true contribution of each input feature to the target output. Although several metrics have been proposed to quantify faithfulness, we adopt the most comprehensive approach, which involves computing the area under the curve (AUC) for the deletion and insertion operations, considering the changes in accuracy and the target probability [14, 27, 47, 50].

The deletion accuracy curve is obtained by progressively removing input features in order of decreasing attribution scores and measuring the model's accuracy at each step. A faithful attribution method should result in a steep drop in performance as the most important features are removed first. The deletion accuracy scores are normalized using the formula 100 - x, where x is the original score, so that higher scores always indicate better performance.

Similarly, the deletion AOPC curve is generated by gradually removing input features in order of decreasing attribution scores and evaluating the change in the target output probability at each step. A faithful attribution method should lead to a rapid decrease in the target probability as the most important features are removed first.

Using the input images \mathbf{x}_i , the perturbed input $\tilde{\mathbf{x}}_i^k$ is created by deleting k% of the most significant patches from \mathbf{x}_i . Subsequently, Area Over the Perturbation Curve [19, AOPC] evaluates the mean alteration in the predicted class probability across the entire validation dataset using the following formula:

$$AOPC(k) = \frac{1}{N} \sum_{i=1}^{N} p\left(\hat{y}|\mathbf{x}_{i}\right) - p\left(\hat{y}|\tilde{\mathbf{x}}_{i}^{k}\right).$$

Here, N represents the total number of instances, \hat{y} stands for the predicted class, and $p(\hat{y}|\cdot)$ denotes the probability of the predicted class.

Conversely, the insertion accuracy curve is generated by gradually adding input features in order of decreasing attribution scores and evaluating the model's performance at each step. A faithful attribution method should lead to a rapid increase in performance as the most important features are added first.

Likewise, the insertion AOPC curve is obtained by progressively adding input features in order of decreasing attribution scores and measuring the change in the target output probability at each step. A faithful attribution method should result in a steep increase in the target probability as the most important features are added first. Similar to deletion accuracy, the insertion AOPC scores are also normalized using 100 - x, ensuring that higher scores consistently represent better performance.

A.2. True Token Masking

Instead of simply overlaying a color mask, we choose to completely exclude the masked patches from the model's input [16]. At the same time, we preserve accurate positional encodings for the unmasked patches. We term this strategy *True Token Masking*. The conventional method of using the color black (or simply zeroing the tokens in text-based Transformers) for patch masking encounters several issues:

- If a patch is predominantly black, painting it black does not effectively eliminate its informational content. For instance, a black drawing on a white background would remain mostly unchanged.
- Patches might serve computational functions, such as acting as a scratchpad for the model's internal processes. Masking these with black does not prevent the model from using them for such purposes.
- Introducing a black mask can create artifacts in the image, potentially leading to out-of-distribution data, which affects the model's performance.



B. Is SkipPLUS's Choice of Skipping the First Half of the Network Optimal?

Figure 7. Either PLUS (starting the attribution method from all layers and aggregating information) or SkipPLUS (starting the attribution method from layers in the latter half of the network and aggregating information) are always near the optimal selection of the cutoff layer.



C. Composing PLUS and SkipPLUS With Other Methods

Figure 8. Evaluating the composition of PLUS and SkipPLUS with the Vanilla Gradients of tokens and attention weights.



Figure 9. GenAtt, the previous state-of-the-art baseline, is not enhanced by our proposed PLUS or SkipPLUS methods, but it is also not harmed.



Figure 10. Evaluating the composition of PLUS and SkipPLUS with FullGrad.



Figure 11. Evaluating the composition of PLUS and SkipPLUS with InputxGradient (IxG) and an attention-enhanced variant, AttIxG. The PLUS compositions of these methods are also known as CAT and AttCAT, respectively.



Figure 12. Evaluating the composition of PLUS and SkipPLUS with CAM methods from CNNs. 18

D. Qualitative Results

D.1. ViT Base (Patch Size 8)



Figure 13. Additional qualitative examples demonstrating the application of SkipPLUS on ViT Base (Patch Size 8). The images presented were selected at random.



Figure 14. Additional qualitative examples demonstrating the application of SkipPLUS on ViT Base (Patch Size 8). The images presented were selected at random.



Figure 15. Additional qualitative examples demonstrating the application of SkipPLUS on ViT Base (Patch Size 8). The images presented were selected at random.



Figure 16. Additional qualitative examples demonstrating the application of SkipPLUS on ViT Base (Patch Size 8). The images presented were selected at random.



Figure 17. Additional qualitative examples demonstrating the application of SkipPLUS on ViT Base (Patch Size 8). The images presented were selected at random.

D.2. EVA Large (Patch Size 14)



Figure 18. Additional qualitative examples demonstrating the application of SkipPLUS on EVA Large (Patch Size 14). The images presented were selected at random.



Figure 19. Additional qualitative examples demonstrating the application of SkipPLUS on EVA Large (Patch Size 14). The images presented were selected at random.



Figure 20. Additional qualitative examples demonstrating the application of SkipPLUS on EVA Large (Patch Size 14). The images presented were selected at random.



Figure 21. Additional qualitative examples demonstrating the application of SkipPLUS on EVA Large (Patch Size 14). The images presented were selected at random.



Figure 22. Additional qualitative examples demonstrating the application of SkipPLUS on EVA Large (Patch Size 14). The images presented were selected at random.



Figure 23. Additional qualitative examples demonstrating the application of SkipPLUS on EVA Large (Patch Size 14). The images presented were selected at random.



Figure 24. Additional qualitative examples demonstrating the application of SkipPLUS on EVA Large (Patch Size 14). The images presented were selected at random.



Figure 25. Additional qualitative examples demonstrating the application of SkipPLUS on EVA Large (Patch Size 14). The images presented were selected at random.



Figure 26. Additional qualitative examples demonstrating the application of SkipPLUS on EVA Large (Patch Size 14). The images presented were selected at random.



Figure 27. Additional qualitative examples demonstrating the application of SkipPLUS on EVA Large (Patch Size 14). The images presented were selected at random.

E. Related Work

Input attribution methods are techniques designed to quantify the influence of individual input features, or groups of them, on a model's output [6, 38, 43, 44, 61, 68, 69, 80]. Input attribution methods can assist in understanding a model's decision locally for a single input considered in isolation. They also act as foundational elements for more advanced explanation techniques. For instance, in conceptbased explanation methods like CRAFT [25], attribution methods are employed for two main purposes: to quantify the impact of each activated concept and to identify the specific input features responsible for activating these concepts.

Attribution methods have a wide array of applications beyond merely explaining model outputs to humans [22, 63, 72, 74]. They are useful for enhancing the robustness of models against out-of-distribution data, spurious correlations, and adversarial inputs [3, 12, 51, 79]. Additionally, attribution methods have been employed to improve the performance of text-to-image models [13, 37, 54]. Furthermore, adapting forward-mode attribution methods has been explored for on-the-fly feature pruning [24, 46] and model quantization [5]. Attribution methods have been utilized to construct more effective adversarial attacks against models [33, 77, 81].

E.1. Gradient-Based Methods

Gradient-based methods compute the gradient of the model's output y_c w.r.t. the input features x_i which can be pixels, regions, or tokens of the whole input x. The general idea is that larger gradients indicate higher importance of the input features x_i on the prediction y_c .

Vanilla Gradients. The most straightforward approach to these methods is to use the gradient as the exact importance score [68].

$$\begin{aligned} \text{VanillaGrad}_{i} &= \sum_{j} \frac{\partial y_{c}}{\partial x_{i,j}}.\\ \text{VanillaGrad:Norm2}_{i} &= \left\| \frac{\partial y_{c}}{\partial x_{i}} \right\|_{2}. \end{aligned}$$

Input×**Gradient (IxG).** IxG [2, 66, 67] multiplies the input values by their corresponding gradients. Let x_i be a spatial feature of the input, where $x_{i,j}$ represents the *j*-th channel of x_i . The Input×Gradient attribution for the spatial feature x_i with respect to the target class *c* is computed as follows, where y_c is the output of the model for the target class *c*:

$$\text{Input} \times \text{Gradient}_{i} = \sum_{j} \frac{\partial y_{c}}{\partial x_{i,j}} \cdot x_{i,j}, \quad (7)$$

E.1.1 CAM Methods

CAM methods, popularized by GradCAM [62], usually start from the very last layer of the network. In this, their intuition has certain similarities with SkipPLUS; they both recognize the noisy nature of the first layers of the network.

GradCAM.

- A^k : the k-th channel of the feature map in the final layer
- c: the class w.r.t. which the attribution map is computed
- y^c : the class score (logit)
- Gradients are averaged over the width and height dimensions (indexed by i and j respectively) to obtain the neuron (channel) importance weights α^c_k:

$$\alpha_k^c = \underbrace{\frac{1}{Z}\sum_{i}\sum_{j}}_{\text{gradients via backprop}} \underbrace{\frac{\partial y^c}{\partial A_{ij}^k}}_{\text{gradients via backprop}}$$

AttCAM. Chefer et al. [11] introduce a Transformerspecific adaptation of GradCAM [62], and reuse the name GradCAM for it. We term this modified method AttCAM.

XGradCAM. It weights the gradients by their corresponding activation value when computing the spatial average [29]. XGradCAM was proposed on ReLU CNNs where the activations were always positive, hence they did not specify using the absolute value of the activations in the above computation, as is more intuitive. We name the variant with absolute activations XGradCAM+, and test both of them.

Other CAM methods include GradCAM++ [9], HiResCAM [21], and GradCAMElementWise [31].

E.1.2 Gradient-Based Rollout Methods

TransAtt. TransAtt [11] employs the Deep Taylor Decomposition technique [49] to attribute local relevance and subsequently propagates these relevance scores through the entire architecture of a Transformer model. This process effectively enables the backward propagation of information across all layers, starting from the output and extending back to the input. Additionally, this method incorporates gradients of attention weights. The method's functioning can be summarized as follows:

$$Rollout\left(\mathbb{E}_{H:= ext{Heads}}\left[\left(\mathtt{R}\odot \mathtt{Attn}\mathtt{Grad}
ight)^{+}
ight]
ight)$$

where R stands for the relevancy scores of attention weights. The Rollout technique is a method to aggregate the layerwise attribution maps. We refer the reader to [1] for a detailed overview. **GenAtt.** The dependence of TransAtt on specific rules for the propagation of relevance scores imposes limitations on its capacity to furnish explanations for various types of Transformer architectures. To cope with this issue, GenAtt [10] attempts to explain predictions for any Transformer-based architecture by using the attention weights in each block to update the relevancy maps, as demonstrated by the following expression:

$$Rollout\left(\mathbb{E}_{H:=\text{Heads}}\left[\left(\texttt{Attn}\odot\texttt{AttnGrad}\right)^{+}
ight]
ight).$$

The notation $()^+$ denotes a filtering through the ReLU function. [10] show that GenAtt is at least as effective as TransAtt, if not better.

E.1.3 Special Cases of PLUS

The methods described below can be viewed as special cases of PLUS, where PLUS is composed with a previously existing method.

GradSAM. GradSAM [4] is equivalent to composing GenAtt [10] with PLUS, instead of using Rollout. (cf. Fig. 9 in the appendices)

CAT. Class Activation Tokens [56] is equivalent to IxGoPLUS. (cf. Fig. 11 in the appendices)

AttCAT. We can define an attention-enhanced variant of IxG, AttIxG, by multiplying IxG with AttnFrom:

$$\texttt{AttnFrom}_j = \frac{1}{H \times N} \sum_{h=1}^{H := \texttt{Heads}} \sum_{i=1}^{N := \texttt{Tokens}} \texttt{RawAttn}_{h,i,j}$$

Note that attention weights have three dimensions: heads, to, from.

Attentive Class Activation Tokens [56, AttCAT] would then be equivalent to AttIxGoPLUS. (cf. Fig. 11 in the appendices)

LayerCAM. LayerCAM [36] was introduced for ReLU CNN networks, where it is equivalent to applying a normalization process on the layer-wise attribution maps obtained from GradCAMElementWise [31], followed by the PLUS aggregation method. The normalization step is proposed because earlier layers tend to have smaller attribution maps compared to later layers. By normalizing the maps, LayerCAM ensures that each layer contributes more equally to the final attribution map. However, this approach is not suitable for ViTs, as we explicitly want to avoid giving earlier layers the same impact on the final attribution map as later layers (cf. Fig. 2, also supported by our preliminary quantitative evaluations).

E.2. Forward Attention-Based Token Attribution Methods

Although we have mathematically detailed most of the previous methods, the complexity of the subsequent approaches surpasses the scope of this paper. Therefore, we will provide a succinct overview of their core concepts. For a more thorough understanding, we recommend readers refer to the original papers.

Attention×Input_Norm (AttIN). Kobayashi et al. [39] multiply the attention weights by the norms of the vectors corresponding to each attention weight. Kobayashi et al. [40] extends AttIN to also incorporate the residual connections.

GlobEnc & ALTI. AttIN assumes that tokens retain their original identity. As each self-attention module mixes all the tokens, this assumption might not necessarily hold. Using gradient-based techniques, Brunner et al. [7] studies contextual information aggregation across the model. Following Brunner et al. [7] work, the global token attribution analysis method [45, GlobEnc] further extends AttIN by including the Transformer block's second normalization layer in its analysis. In parallel with GlobEnc, the Aggregation of Layer-Wise Token-to-Token Interactions method [27, ALTI] was introduced. ALTI shares core concepts with GlobEnc, but the two differ in certain mathematical specifics.

DecompX. DecompX [47] enhances GlobEnc by integrating the one element previously overlooked by GlobEnc: the MLP module in the Encoder Transformer layer. This inclusion enables DecompX to generate a set of decomposed vectors that collectively sum up to the actual output vector. Unlike GlobEnc and ALTI, which require computing and aggregating layer-wise attribution maps using techniques like Rollout, DecompX facilitates the direct propagation of these decomposed vectors across layers. This capability allows for the direct computation of attribution maps from any layer to any other layer.

In this paper, unless specified otherwise, we utilize the DecompX variation that omits biases, referred to as DecompX W/O Bias in [47]. Our decision stems from our preliminary tests where no significant differences were observed across various methods of handling biases. To sidestep the complexities and hyperparameters introduced by distributing bias attributions among tokens, we opted for the simplest approach. A detailed evaluation of different methods for bias attribution distribution is reserved for future research.

E.3. Black-Box Methods

Black-box attribution methods treat the model as an opaque entity, (partially) disregarding its internal structure and gradients. These methods typically involve perturbing the input and observing the corresponding changes in the model's output to infer the importance of each input feature. However, this approach often comes with significant computational costs due to the need for multiple model evaluations. In contrast, white-box methods leverage the internal structure and gradients of the model, providing a more efficient and fine-grained understanding of the model's behavior.

In this paper, we focus on white-box methods for several reasons. Firstly, they offer a more computationally efficient approach compared to black-box methods. Secondly, and more importantly, black-box methods can be seen as directly optimizing the faithfulness metrics on which we evaluate the attribution methods. This raises concerns related to Goodhart's law, which states that when a measure becomes a target, it ceases to be a good measure. In other words, the faithfulness metrics we use are merely proxies for the ultimate desirable properties we seek in attribution methods. By directly optimizing these metrics, black-box methods may inadvertently introduce biases or artifacts that undermine the true faithfulness of the attributions. Therefore, to avoid this potential pitfall and maintain a more objective evaluation, we refrain from including comparisons with black-box methods in this study, acknowledging that they have different trade-offs and use cases.

LIME [59] explains the predictions of any classifier by learning a local interpretable model around the prediction.

RISE [55] is a black-box approach that generates an importance map indicating the saliency of each pixel for the model's prediction by probing the model with randomly masked versions of the input image and obtaining the corresponding outputs.

PAMI [65] masks the majority of the input and uses the corresponding model output as the relative contribution of the preserved input part to the original model prediction.

ScoreCAM [73] is a post-hoc visual explanation method based on class activation mapping that eliminates the dependence on gradients by obtaining the weight of each activation map through its forward passing score on the target class.

ViT-CX [78] adapts ScoreCAM for ViTs.

AtMan [17] is a perturbation method that manipulates the attention mechanisms of transformers to produce relevance maps for the input with respect to the output prediction.

HSIC [52] is a black-box attribution method based on the Hilbert-Schmidt Independence Criterion, measuring the dependence between regions of an input image and the model's output using kernel embeddings of distributions.