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Mathematical Methodology for Defining a Frequent Attender within Emergency Departments

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2 ABSTRACT

3 **Objective:** Emergency department (ED) frequent attenders (FA) have been the subject of
4 discussion in many countries. This group of patients have contributed to the high expenses of
5 health services and strained capacity in the department. Studies related to ED FAs aim to describe
6 the characteristics of patients such as demographic and socioeconomic factors. The analysis
7 may explore the relationship between these factors and multiple patient visits. However, the
8 definition used for classifying patients varies across studies. While most studies used frequency
9 of attendance to define the FA, the derivation of the frequency is not clear.

10 **Methods:** We propose a mathematical methodology to define the time interval between ED
11 returns for classifying FAs. K-means clustering and the Elbow method were used to identify
12 suitable FA definitions. Recursive clustering on the smallest time interval cluster created a new,
13 smaller cluster and formal FA definition.

14 **Results:** Applied to a case study dataset of approximately 336,000 ED attendances, this
15 framework can consistently and effectively identify FAs across EDs. Based on our data, a
16 FA is defined as a patient with three or more attendances within sequential 21-day periods.

17 **Conclusion:** This study introduces a standardised framework for defining ED FAs, providing
18 a consistent and effective means of identification across different EDs. Furthermore, the
19 methodology can be used to identify patients who are at risk of becoming a FA. This allows for
20 the implementation of targeted interventions aimed at reducing the number of future attendances.

21 **Keywords:** Emergency Department, Frequent Attender, K-means Clustering, Health Services, Health Care Utilisation, Targeted
22 Interventions

1 INTRODUCTION

23 Emergency departments (EDs) are the first point of contact for patients who require urgent medical care.
24 The ED is a complex system influenced by many factors, including the patient, the staff, the hospital, and
25 the community. The ED is a dynamic system that is constantly changing. The number of patients attending
26 EDs has increased over the years, with attendances in England rising by 20% between 2008 and 2018
27 (Budhwani et al., 2022). This increase in attendances has resulted in EDs becoming overcrowded, with

28 patients experiencing long waiting times. The increase in attendance has also led to a rise in the number
29 frequent attenders (FAs). FAs, sometimes referred to as frequent flyers or frequent users, are patients
30 who attend EDs multiple times within a given period. Although this group of patients represents a small
31 minority, they contribute significantly to the volume of ED attendances, which continues to increase each
32 year (Hunt et al., 2006; Pek et al., 2022; Jacob et al., 2016).

33 It is important to recognise that the high utilisation of ED services by FAs is not simply a reflection of
34 these patients being a burden on the healthcare system. Rather, FAs are often dealing with complex, chronic
35 medical and social issues that are not being adequately addressed elsewhere in the care system. Conditions
36 such as asthma (Wakefield et al., 1997), cancer (Wong et al., 2018), neurological issues (Lago et al., 2019)
37 and mental health and alcoholism concerns (Jacob et al., 2016; Mak et al., 2022) contribute significantly to
38 individuals making multiple visits to the ED.

39 ED FAs are associated with an increased risk of admission, mortality (Greenfield et al., 2020), and
40 hospital length of stay (LOS) (Street et al., 2018). Ultimately, they contribute to the high utilisation of ED
41 personnel or other services such as ambulance services (Wooden et al., 2009; Shen et al., 2018), primary
42 care (Williams et al., 2001), community health centres (Savageau et al., 2006), and social services (Byrne
43 et al., 2003). The challenge is to identify these patients systematically and provide them with coordinated,
44 comprehensive care.

45 Studies related to FAs aim to investigate the factors that influence repeated visits, the broader impact of
46 FA attendances on health and social services and the efficacy of intervention programmes in mitigating
47 attendances. These influencing factors encompass a spectrum, ranging from the clinical challenges faced
48 by patients to their demographic profiles, environmental context and behavioural patterns. While exploring
49 factors associated with FAs is a prevalent focus in the literature, it is worthwhile noting that the definition
50 of an FA can vary. The most commonly employed criterion for identifying FAs involves their attendance
51 frequency. Typically, a FA is defined as a patient who attends the ED more than a determined threshold
52 within a given period. Table 1 demonstrates the different definitions used in the literature across different
53 countries. Within these papers, there was no justification for how they defined a FA. When different
54 definitions are employed within the same country, a significant challenge arises in determining the true
55 prevalence of FAs. Recognising and accurately identifying FAs is critical because they are known to
56 contribute to the high expenses of health services (Furia et al., 2023; Ruger et al., 2004; Williams, 2001). It
57 is important to recognise that these individuals have needs that require attention, even if those needs are
58 not clearly linked to a specific medical condition (Neal et al., 2000). This means they may face ongoing
59 challenges in their daily lives, such as social, emotional or psychological issues, that do not always show
60 up in traditional medical assessments but significantly impact their overall well-being (Birrenbach et al.,
61 2022).

62 The definition of FAs should be tailored to each ED, driven by data and reflective of the unique patient
63 characteristics and demographics of each ED. Acknowledging the variability across different EDs, a
64 data-driven approach ensures a more relevant understanding of FAs within each setting. Furthermore,
65 the definition should be dynamic enough to operate in real-time, allowing the prompt identification of
66 individuals who are at risk of becoming FAs. This real-time capability is crucial for swiftly implementing
67 targeted interventions aimed at reducing the number of future attendances by ensuring the needs of these
68 individuals are met.

69 By aligning the definition with the specific attributes of each ED's patient population and incorporating
70 a real-time capability, healthcare providers can enhance their ability to proactively address the complex

71 medical, social and environmental factors that put certain individuals at risk of becoming FAs (Al-Jaroodi
72 et al., 2020). Rather than simply viewing FAs as a challenge posed by the patients themselves, this approach
73 recognises it as a reflection of shortcomings in the broader system of care (Ablard et al., 2017). With this
74 understanding, providers can work to implement holistic, patient-centred interventions that connect FAs
75 with the appropriate resources and support they need.

76 This study aims to introduce a mathematical methodology for determining the time interval between
77 successive visits to EDs that qualifies a patient as a FA. This proposed methodology holds the potential
78 to establish a standardised framework applicable not only to the specific ED under investigation but
79 also transferable for defining FAs in other EDs. The distinctive advantage of employing a mathematical
80 approach lies in its precision and adaptability. Unlike alternative methods, a mathematical methodology
81 offers a systematic and data-driven way to objectively identify FAs based on time intervals between visits.
82 Furthermore, this method's versatility enhances its applicability to a wide range of EDs, accommodating the
83 variability in patient demographics and characteristics. By offering a standardised yet flexible approach, the
84 proposed mathematical methodology provides a valuable tool for healthcare providers seeking a consistent
85 and effective means of identifying FAs.

2 METHODS

86 2.1 Study Design and Setting

87 This study employed a retrospective cohort design, utilising data from a major ED department in Wales,
88 UK. Spanning a six-year period, from January 2017 to December 2022, the research sought to explore
89 patterns of ED visits and define FAs based on time intervals between return visits. The retrospective cohort
90 design allowed for the examination of historical data to discern trends and associations.

91 2.2 Participant Selection

92 The study population consisted of adult patients, defined as individuals aged 17 years or older, who
93 sought medical attention at the ED between January 2017 and December 2022, who were classified as a
94 'Major' patient. The ED defines a major patient as one who requires very urgent emergency care (NHS
95 England, 2024). The decision to focus exclusively on 'Major' patients in this study was guided by the need
96 to align the model with the clinical and operational priorities of EDs. Major patients are characterised by
97 high-acuity conditions that necessitate significant resources and urgent care. Their frequent attendances
98 impose a disproportionate burden on ED resources, making them a critical group for targeted intervention
99 strategies (Iacobucci, 2022). However, it is important to note that this classification is inherently subjective
100 and may vary across institutions. By tailoring the model to identify patterns specific to this cohort, the study
101 aims to address the most pressing challenges associated with ED overcrowding and resource allocation.

102 Our initial dataset contained 336,898 patients. We applied data preprocessing to retain only patients with
103 complete demographic and clinical information relevant to our analysis. First, 66 patients were removed
104 due to missing National Health Service (NHS) numbers. Next, 233 patients lacked recorded admission or
105 discharge dates and times, leading to their exclusion. We also filtered out 512 patients based on implausible
106 age data, specifically those recorded as being over 120 years old. Finally, 46 patients were removed due to
107 incomplete information on gender.

108 This filtering, designed with the specific purpose of enabling the ability to track patients and time between
109 visits, resulted in a total of 184,051 patients, contributing to a total of 336,041 ED visits. Of these visits,
110 152,183 (45%) were identified as return visits, denoting subsequent visits made after the initial identified

111 visit. Notably, 34.6% of patients made more than one visit within the specified six-year timeframe. This
112 comprehensive dataset provided a robust foundation for the subsequent analyses.

113 2.3 Statistical Analysis

114 This research introduces an innovative approach to defining FAs by shifting from traditional frequency-
115 based definitions to a time interval-based definition. Our research investigated diverse statistical clustering
116 methodologies to establish an enhanced definition of frequent ED users that goes beyond simple visit
117 counts. While previous research typically relied on basic frequency measurements to classify FAs, we
118 sought to develop a more sophisticated approach by considering both the number of visits and the temporal
119 spacing between them. Although Monte Carlo methods, which are well-known in healthcare management
120 for their probabilistic sampling approach, might seem an appropriate choice given their familiarity in
121 ED settings, we opted for a deterministic clustering approach. Unlike Monte Carlo simulations, which
122 provide probabilistic approximations that vary between runs, our selected methodology needed to deliver
123 consistent, reproducible classifications of frequent attenders. This requirement for deterministic outcomes,
124 combined with our focus on identifying distinct patterns in visit frequency and timing, led us to explore
125 various clustering techniques.

126 We systematically evaluated multiple clustering algorithms to determine their effectiveness. Our approach
127 aligns with machine learning model selection principles, including data preparation, feature selection and
128 model optimisation, as detailed by Ramlakhan et al. (2022b), to ensure robust and reproducible outcomes.
129 Initially, we investigated hierarchical clustering through the agglomerative approach, which demonstrated
130 strengths in gradual cluster formation but proved impractical for our extensive ED dataset due to its
131 computational demands. We then explored Density-Based Spatial Clustering of Applications with Noise
132 (DBSCAN) and the Ordering Points to Identify the Clustering Structure (OPTICS) algorithms, which
133 excel at identifying irregularly shaped clusters and isolating outliers. However, these methods presented
134 challenges in our context due to their requirement for specific density parameters, which proved difficult to
135 optimise given the variable patterns of ED utilisation.

136 We also considered Gaussian Mixture Models (GMM) for their probabilistic approach to cluster
137 assignment. Yet, the underlying assumption of normally distributed data made this method suboptimal for
138 our ED visit patterns, which typically follow non-Gaussian distributions. The K-modes algorithm was also
139 evaluated, particularly for its strength in categorical data analysis, but it failed to adequately capture the
140 temporal aspects of visit patterns that were crucial to our study.

141 After comprehensive testing, K-means clustering initially emerged as the optimal methodology. However,
142 due to the wide range of time scales present in the data, we extended this to a two-stage K-means approach.
143 The initial K-means method was selected based on several factors: its computational efficiency when
144 handling large datasets, its ability to effectively process both visit frequency and inter-visit intervals and
145 its straightforward implementation approach. To determine the ideal number of clusters for each stage,
146 we employed the Elbow method, which helped us identify the point where additional clusters provided
147 minimal additional benefit, thus optimising the balance between model complexity and accuracy.

148 The final framework, combining two-stage K-means clustering with Elbow method optimization,
149 represents a significant advancement in identifying ED frequent attenders. This hierarchical approach
150 provides a more nuanced understanding compared to traditional counting methods by first grouping
151 patients based on their temporal visit patterns, followed by sub-clustering based on visit frequencies. Our
152 methodology offers a more comprehensive and accurate way to identify and understand patterns in ED

153 utilisation, particularly when dealing with varying time scales, which can better inform healthcare resource
154 allocation and intervention strategies.

155 2.3.1 K-means Clustering

156 In the broader literature, K-means clustering has been successfully used on ED data to predict patient
157 outcomes and ED utilisation. For example, Grant et al. (2020) applied K-means to identify patients with
158 complex profiles, predicting diverse healthcare utilisation and mortality outcomes. Additionally, Liu et al.
159 (2017) used K-means clustering to create a triage system within EDs, with Huang et al. (2008) clustering
160 patients against medical utilisation, discovering that their FA population, more often utilised other medical
161 services.

162 To provide insight into the mathematical model for the clustering algorithm, the K-means method clusters
163 together ED patient data points with similar returns to ED times. K-means clustering is an iterative machine
164 learning algorithm designed to partition a dataset into K clusters, where each data point is assigned to
165 the cluster with the nearest mean. The goal is to minimise the within-cluster sum of squares, which is
166 represented by the objective function:

$$J = \sum_{i=1}^K \sum_{j=1}^n \|x_j^i - c_i\|^2 \quad (1)$$

167 where n is the number of data points, x_j^i is the j^{th} data point in cluster i and c_i is the centroid of cluster i .
168 $\|x_j^i - c_i\|^2$ is the Euclidean distance between the data point and the centroid.

169 To provide a definition for FA, recursive clustering was applied to the cluster with the smallest LOS mean
170 (n_1). This means the K-means clustering algorithm was then performed again on the smallest cluster to
171 create m new clusters from cluster n_1 . The cluster with the smallest LOS mean (m_1) was then used to
172 define a FA. This method is known as two-stage K-means clustering (Salman et al., 2011). In two-stage
173 clustering, the initial clustering identifies broad groups in the data. Then, clustering is applied a second
174 time to divide the groups into more granular segments. Applying this technique to healthcare data has
175 provided useful insights in many cases (Ayanore et al., 2016; You-Shyang et al., 2012; Marshman et al.,
176 2016). For more detail about the K-means method, we have provided a step-by-step applied example in the
177 supplementary material.

178 2.3.2 Elbow Method

179 Determining the optimal number of clusters is an important step in the K-means clustering method. The
180 Elbow method is a heuristic method used to determine the optimal number of clusters (K) in a dataset. The
181 idea is to perform the K-means algorithm for a range of values K , calculate the sum of squared distances
182 from each point to its assigned centre (J), and plot the results. The ‘elbow’ point is often considered the
183 point where the rate of decrease of J slows down, suggesting that the addition of more clusters does not
184 significantly reduce the within-cluster sum of squares. The algorithm uses the same objective function
185 as the K-means clustering algorithm, Equation (1). The Elbow method offers an empirical approach to
186 determine the appropriate number of clusters based on the data itself. However, it is important to note that
187 identifying the exact location of the elbow involves a qualitative assessment and subjective judgement.

188 2.3.3 Scenario Impact

189 This study examines the impact of FAs on ED resources by quantifying ‘hours of patient ED time’,
190 representing the cumulative hours FAs spend in EDs. This metric serves as an indicator of the system
191 burden created by FAs. We calculated this based on the average duration each patient remained in the ED
192 per visit. Estimating ‘hours of patient ED time’ allows for a clearer assessment of how reducing specific
193 frequent attendance patterns could alleviate ED capacity strains, aligning with the NHS four-hour wait
194 target for patients.

3 RESULTS

195 This section will present the results of applying the K-means clustering and Elbow method to the ED
196 data. The results discussed will include the descriptive statistics of the data, the clustering results, and the
197 definition of a FA.

198 3.1 Descriptive Statistics

199 The K-means clustering and Elbow method as discussed previously was performed on the six years’
200 worth of data from 1st January 2017 to 31st December 2022. The total number of patients included in the
201 dataset was 184,051 who made a total of 336,041 visits. The proportion of male and female patients is 48%
202 and 52% respectively. The distribution of male and female patients’ ages is significantly different (Kruskal
203 Wallis test = 201.9, p -value < 0.001). The mean age for male patients is 49 years old (Q1 = 30, Q3 = 66)
204 compared to the mean age for female patients of 48.6 years old (Q1 = 27, Q3 = 69). The average total time
205 spent in the ED department was calculated to be 10.7 hours (sd = 16.8 hours) per patient. However, the
206 median total time spent was found to be 5.6 hours with 50% of patients staying in the ED between three
207 and 11 hours. At an aggregated level, there was no significant difference between male and female patients’
208 time spent in the ED (p -value = 0.25). Within 30 days of attending the ED, 25% of patients will present
209 again. Around 36.2% female patients have return visits compared to 33.1% male patients.

210 3.2 Clustering Results

211 The Elbow method was performed on the data, with the results showing the elbow occurs at $K = 3$.
212 Therefore, the K-means clustering algorithm was performed with $K = 3$. The results show three determined
213 clusters between 0 and 324 days, 325 and 913 days and, 914 and 2171 days (Table 2). The smallest cluster
214 is between 0 and 324 days, with 68.58% of patients falling into this cluster. The mean time between visits
215 for this cluster is approximately three months.

216 Since returning within 324 days provides too broad of a definition for a FA, the K-means clustering
217 algorithm was performed again on this cluster. Taking the smallest cluster of returning between 0 and 324
218 days, the Elbow method was performed again to determine the optimal number of clusters. The results
219 show an Elbow method of eight clusters. Therefore, performing the K-means algorithm with eight clusters
220 results in the smallest cluster being between 0 and 21 days. Overall, there are 31.4% of patients falling
221 into this cluster. The mean time between visits for this cluster is 7.08 days (Table 3). This cluster accounts
222 for 9.72% of all attendances. In practice, this represents 10.1% of patients. In our analysis, we found
223 that age did not significantly impact the clustering results, indicating that the observed patterns in patient
224 characteristics were consistent across both adult and elderly populations.

225 3.3 Definition of a Frequent Attender

226 The results from the two-stage K-means clustering algorithm show that the smallest cluster is between 0
227 and 21 days. In order to provide a formal definition, this cluster can be examined further.

228 Our provisional definition will specify a threshold number of visits within each 21 day period as qualifying
229 for FA status. As illustrated in Figure 1 the 21 day count is reset after each visit, so the frequency pattern is
230 evaluated over rolling 21 day windows. This approach quantifies FA based on the number of admissions
231 within sequential 21 day periods, rather than just looking at the initial admissions. By scrutinising the
232 admission patterns in this manner, we can precisely define FAs as exhibiting a high number of admissions
233 in 21 days, recurrently over time. This definition captures the essence of multiple frequent admissions over
234 successive short intervals, which is the key characteristic of FAs.

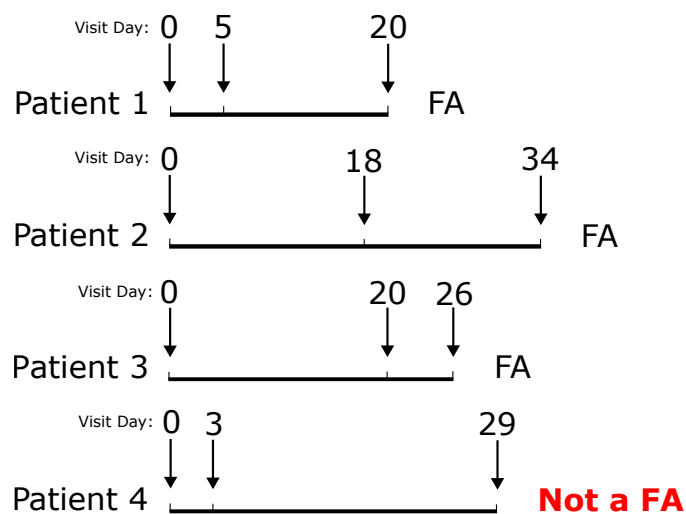


Figure 1. Visualisation of FA definition

235 Analysis of the 0 to 21 day cluster, reveals patients in this group exhibit a high rate of recurrent
236 readmissions over short time intervals. Specifically, on average, if a patient in this cluster attends within
237 21 days of discharge, they will have an additional 1.8 attendances in the subsequent 21 days. As depicted
238 within Figure 1, there is a pattern of multiple repeat admissions within 21 day subsequential periods.
239 Therefore, based on the ED data used, we propose a FA is defined as a patient who has three or more
240 attendances within sequential 21 day periods.

241 The selection of the 21-day period was guided by the results of K-means clustering, which identified
242 this as the smallest cluster with frequent and recurrent attendances. This interval aligns with acute care
243 utilisation patterns observed in FAs and represents a meaningful timeframe for intervention. The choice of
244 three attendances within the 21-day window reflects a balance between sensitivity and specificity. While
245 two attendances in this period may signify episodic or transient patterns, three or more visits indicate
246 sustained and potentially preventable reliance on ED services. This threshold ensures the definition targets
247 a group whose frequent usage imposes significant demands on resources.

248 It is acknowledged that patients attending less frequently, such as once per month, may not meet the
249 FA definition if they only accumulate two attendances in any successive 21-day clusters. However, this
250 reflects an intentional focus on patients with more intense usage patterns, who are most likely to benefit

251 from targeted care interventions. Those with less frequent but consistent visits are typically better served by
252 outpatient or primary care pathways rather than interventions aimed at reducing high-frequency ED usage.

4 DISCUSSION

253 This study introduced a novel application of K-means clustering and the Elbow method to define frequent
254 ED attenders based on time intervals, instead of visit frequency. Applied to six years of data from one
255 major ED, the technique found a pattern of repeat visits within 21 day periods. This identified a data
256 driven definition of a FA as a patient who has three or more attendances within sequential 21 day periods,
257 capturing recurrent high utilisation of ED services over short intervals. When compared to the literature,
258 as shown in Table 1, the 9% FA rate is comparable with other studies, demonstrating the validity of the
259 approach. The proposed methodology offers a standardised framework to quantify FAs in an adaptive way
260 which can be tailored to each ED's unique patient population.

261 Using the suggested framework, the definition for a FA is three attendances within sequential 21-day
262 periods. This definition is data-driven and tailored to the specific ED dataset analysed. However, applying
263 the framework to different ED data would likely result in a different definition, reflecting the variability in
264 patient demographics and attendance patterns across settings. While it is challenging to directly compare
265 frequency-based methods with time-interval approaches, our methodology offers greater precision by
266 identifying FAs more quickly. By focusing on shorter intervals, it can detect changes in attendance patterns,
267 including seasonal variations, more quickly. This allows for earlier identification of FAs and enables the
268 timely implementation of targeted interventions, which is crucial for managing the high resource demands
269 associated with frequent attendance.

270 4.1 Generalisability

271 While this study introduced a methodology using data from a single ED, the overall mathematical
272 approach has the potential for broader generalisability. The technique provides a standardised framework
273 that could be applied to other EDs to adaptively define FAs based on their specific patients and utilisation
274 patterns. However, the generalisability may be influenced by factors such as patient demographics,
275 healthcare system differences and access to primary care.

276 The optimal clustering patterns and FA definitions may differ across EDs, with substantially different
277 contexts and patient mixes. Therefore, while the method itself is generalisable, with a structured framework
278 provided, the specific resulting FA definition would likely need to be tailored and validated for each
279 ED environment based on its unique characteristics. This includes testing the model on unseen datasets
280 and validating against domain-expert-defined FA populations to ensure its applicability across settings
281 (Graham et al., 2018; Ramlakhan et al., 2022a; Yao et al., 2021). This flexible mathematical approach
282 means an adaptive solution can be implemented, rather than imposing a universal standard definition that
283 fails to capture local variability. Additional research across diverse settings is needed to further test the
284 methodology and refine definitions suited to different ED contexts.

285 4.2 Scenario Impact

286 The impact of FAs on EDs is substantial, with high utilisation leading to increased waiting times, costs
287 and reduced quality of care (Hoot and Aronsky, 2008; Moskop et al., 2009; Pines et al., 2011). However,
288 it is crucial that this is done in a compassionate, patient-centred manner that recognises the complex
289 needs of this population, rather than simply viewing them as a burden on the system. While the 21-day

290 period is used to identify recurrent patterns of ED use and forecast immediate resource savings, it is
291 important to emphasise that interventions targeting FAs are not expected to yield results within such a short
292 timeframe. The true value of identifying FAs early lies in the ability to implement long-term, coordinated
293 care strategies, such as chronic disease management and mental health support, that can help reduce
294 persistent ED use over time. The 21-day window serves as a tool for early identification, enabling proactive
295 and sustained care that addresses the root causes of frequent ED visits.

296 If the fourth visit within 21 days is prevented, this would result in 43,075.20 hours of patient ED time
297 saved per year, with an average of 6.3 hours per patient in an ED. If this was able to be increased to prevent
298 third visits onwards within 21 days, this would result in 62,937 hours of patient ED time saved per year.

299 Calculating the average time patients spend with an ED doctor within our dataset equates to 42 minutes
300 per patient. This is comparable to other ED studies (Walker et al., 2019; Wrede et al., 2020). This value
301 can be used to estimate the impact of FAs on ED resources. For example, if we prevent visits from the
302 fourth attendance within 22 days, this would result in 3,418.67 minutes of doctor time saved per year. This
303 equates to 142.44 hours per year. Similarly, if we were to reduce this to the third visit, this would increase
304 to 208.13 hours of doctor time saved per year. By saving doctor hours, this could be used to treat other
305 patients, reducing waiting times, improving the quality of care and reduce the pressures faced on current
306 staff.

307 It is important to note that the goal of this work is not to simply reduce or restrict FA attendance, as that
308 could further exacerbate the challenges they face in accessing appropriate care. Rather, the aim is to use the
309 identification of FAs as an opportunity to proactively content them with the coordinated, patient-centred
310 services they require to address the root cause driving their high utilisation. This compassionate, system-
311 level approach has the potential to improve outcomes for this vulnerable population by supporting them to
312 access care and support from providers suitable for their needs, whilst also alleviating pressures on the
313 emergency care system.

314 4.3 Limitations

315 This study has some limitations to consider. Firstly, the data was used from a single ED from a single
316 country, which might not be fully representative of other EDs or healthcare systems. Secondly, even though
317 six years' worth of data was used, this may not have been sufficient to capture the full range of utilisation
318 patterns. Our data included the period of Covid19 when traditionally there were fewer attendances to ED
319 (Lateef, 2020). This could have resulted in patients not being classified as a FA when they would have
320 been in a non-Covid period. Thirdly, the use of the 'Major' patient classification in the ED is inherently
321 subjective and can vary across different institutions. The categorisation of patients as 'Major' or 'Minor'
322 typically relies on clinical judgment, which introduces variability that could impact the generalisability of
323 the model. Another limitation is that the data was limited to the ED and did not include other healthcare
324 services. This means that patients who were classified as a FA may have been using other healthcare
325 services, which could have resulted in a different FA definition. Finally, the study only focused on temporal
326 patterns in defining FAs, whereas with additional clinical and demographic factors, further insight could
327 have been provided into high utilisers of ED services.

5 CONCLUSION

328 In conclusion, this study presents an innovative methodology for defining FAs based on time intervals
329 between ED visits. The approach offers a standardised framework that can be applied to different EDs

330 to define FAs based on their specific patients and utilisation patterns. This methodology provides a data
331 driven approach to precisely identify FAs, enabling targeted interventions to reduce future attendances.
332 By shifting from traditional frequency based definitions to a time interval based definition, a FA can be
333 identified more efficiently. This mathematical approach provides a valuable tool for healthcare providers
334 seeking a consistent and effective means of identifying FAs. Future research should focus on utilising the
335 method with clinical and demographic factors to further refine FA definitions and explore the impact in
336 practice of interventions on FAs.

6 ETHICS STATEMENT

337 Ethical review and approval was not required for the study on human participants in accordance with the
338 local legislation and institutional requirements. Written informed consent for participation was not required
339 for this study in accordance with the national legislation and the institutional requirements

7 CONFLICT OF INTEREST STATEMENT

340 The authors declare that the research was conducted in the absence of any commercial or financial
341 relationships that could be construed as a potential conflict of interest.

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Table 1. Published definitions of frequent attenders of EDs.

Authors	Country	Definition	Proportion of FA attendance
Wooden et al. (2009)	Australia	≥ 1 in 1 month	4.5%
Wakefield et al. (1997)	Australia	≥ 2 in 12 months	40-60%
Butler et al. (2020); Cordell et al. (2022); Halcomb et al. (2017); Street et al. (2018)	Australia	≥ 4 in 12 months	3.7%-64.7%
Jelinek et al. (2008)	Australia	≥ 5 in 12 months	2.4%
Quilty et al. (2016)	Australia	≥ 6 in 12 months	13%
Lago et al. (2019)	Australia	≥ 7 in 12 months	2.6%
Zhou et al. (2022)	Australia & Canada	≥ 4 in 12 months	4.7%-5.6%
Palmer et al. (2014)	Canada	≥ 4 in 12 months	11.3%
Greenfield et al. (2020)	England	≥ 3 in 12 months	27.1%
Greenfield et al. (2021); Locker et al. (2007); Moore et al. (2009)	England	≥ 4 in 12 months	9.1%-13.9%
Hotham et al. (2022); Jacob et al. (2016)	England	≥ 5 in 12 months	4.4%-11.5%
Williams et al. (2001)	England	≥ 7 in 12 months	N/A
Scheiner et al. (2019); Sousa et al. (2019)	England	≥ 15 in 12 months	N/A
Uí Bhroin et al. (2019)	Ireland	≥ 3 in 12 months	29%
Byrne et al. (2003)	Ireland	≥ 4 in 12 months	N/A
Skinner et al. (2009)	Scotland	≥ 10 in 6 months	N/A
Shen et al. (2021, 2018)	Singapore	≥ 3 in 12 months	8%-22.1%
Pek et al. (2022); Wong et al. (2018)	Singapore	≥ 4 in 12 months	19.6%-35.4%
Chan et al. (2018); Paul et al. (2010)	Singapore	≥ 5 in 12 months	8%-14.6%
Hansagi et al. (2001)	Sweden	≥ 4 in 12 months,	4%
Michelen et al. (2006)	US	≥ 3 in 6 months	N/A
Sandoval et al. (2010)	US	≥ 3 in 12 months	7%
Hunt et al. (2006); Sun et al. (2003)	US	≥ 4 in 12 months	8%-28%

Cluster	Patient Count	% of Total Patients	Mean	Minimum	Maximum
0	104359	68.58%	92.32	0	324
1	34227	22.49%	166.04	325	913
2	13597	8.93%	1271.89	914	2171

Table 2. Results from the K-means clustering algorithm.

Cluster	Patient Count	% of Total Patients	Mean	Minimum	Maximum
0	32748	31.4%	7.08	0	21
1	16500	15.8%	35.75	22	52
2	12709	12.2%	69.62	53	88
3	11038	10.6%	108.13	89	129
4	9529	9.1%	150.96	130	174
5	8395	8.0%	197.53	175	222
6	7157	6.9%	246.82	223	272
7	6283	6.0%	297.79	273	324

Table 3. Results from the two-stage K-means clustering algorithm.