## Thermochemcial Prediction of Seismic Discontinuity Topography from Mantle Circulation Models: Supplementary information

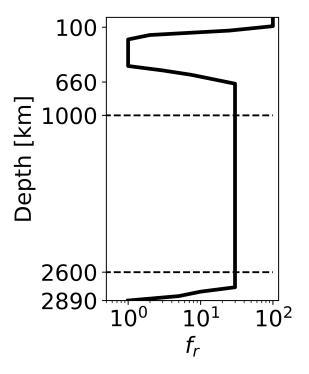


Figure S1. Variation of viscosity pre-factor with depth.

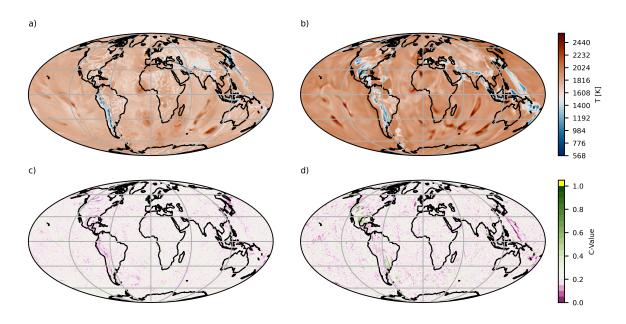


Figure S2. Thermochemical structure of simulation 'm\_cc\_066\_u'. a) Thermal structure at 410 km depth b) C-Value structure at 410 km depth c) Thermal structure at 660 km depth d) C-Value structure at 660 km depth

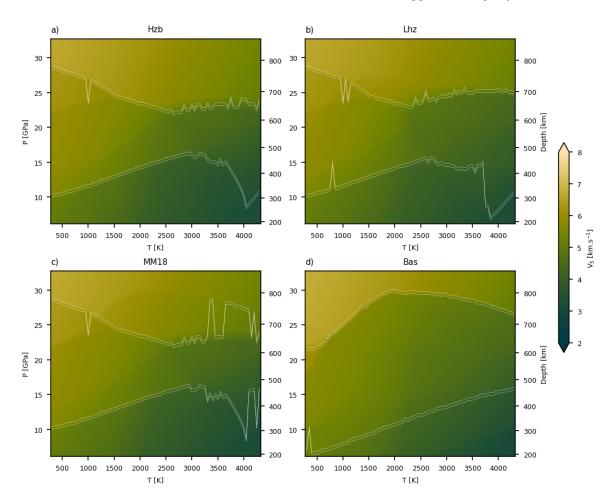
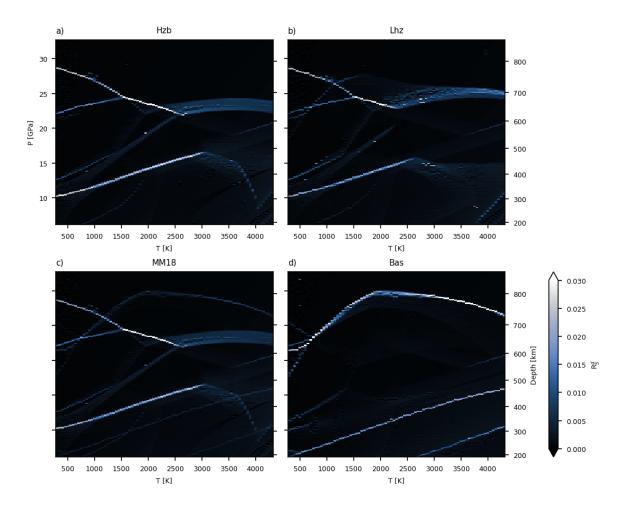


Figure S3.  $V_S$  structure of mineral physics tables for end-member compositions used in this study. a) Harzburgite, b) Lherzolite, c) MM18 a 'pyrolite' composition mechanical mixture of 18% Basalt and 82% Harzburgite, d) Basalt.  $V_S$  structure shown by color fill and the peak reflectivity pressures in the '660' and '410' regions are outlined by fine white lines 0.2 GPa above and below the picked pressure.



**Figure S4.**  $R_S$  structure of mineral physics tables for end-member compositions used in this study. a) Harzburgite, b) Lherzolite, c) MM18 a 'pyrolite' composition mechanical mixture of 18% Basalt and 82% Harzburgite, d) Basalt.

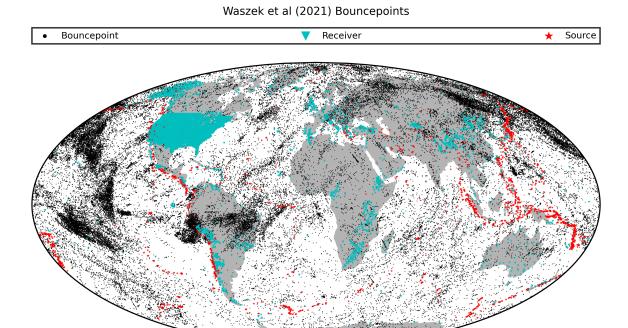
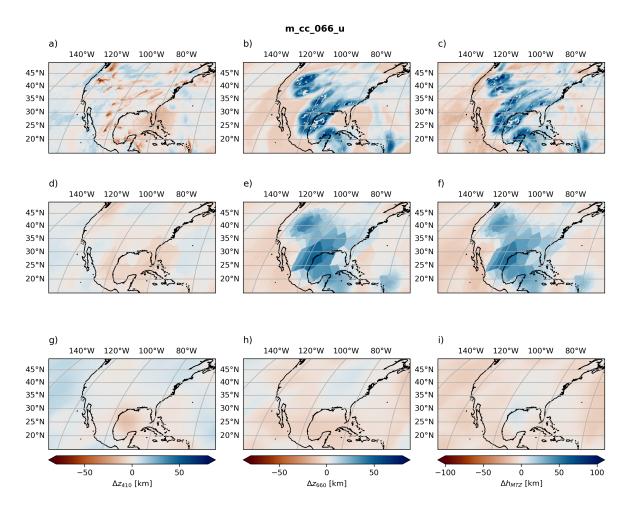


Figure S5. Distribution of seismic sources (red stars) and receivers (cyan triangles) used in Waszek et al. (2021). Bounce-points (Black dots) are then calculated as the mid-point along great circles between source-receiver pairs. Bounce-points are distributed unevenly, with clusters in the North Pacific, beneath NE Asia, Central & Eastern Europe, and Central South America.



**Figure S6.** d410 (a, d, g), d660 (b, e, h) and MTZ thickness (c, f, i) topographies predicted beneath the USA and neighbouring regions from m<sub>cc</sub>\_066<sub>u</sub> (a-c), predicted and filtered with a 500 km radius spherical cap (d-f) and the Waszek et al. (2021) model in the region (g-i).

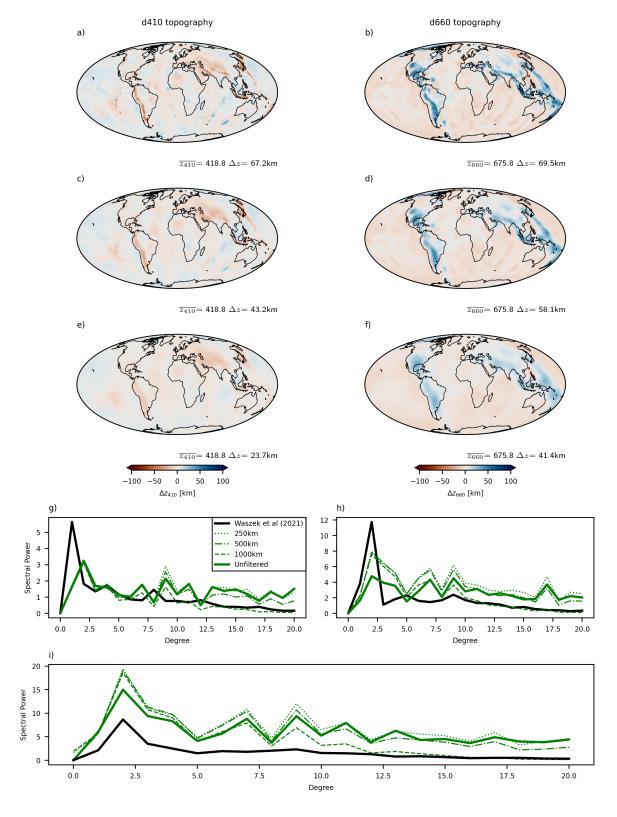
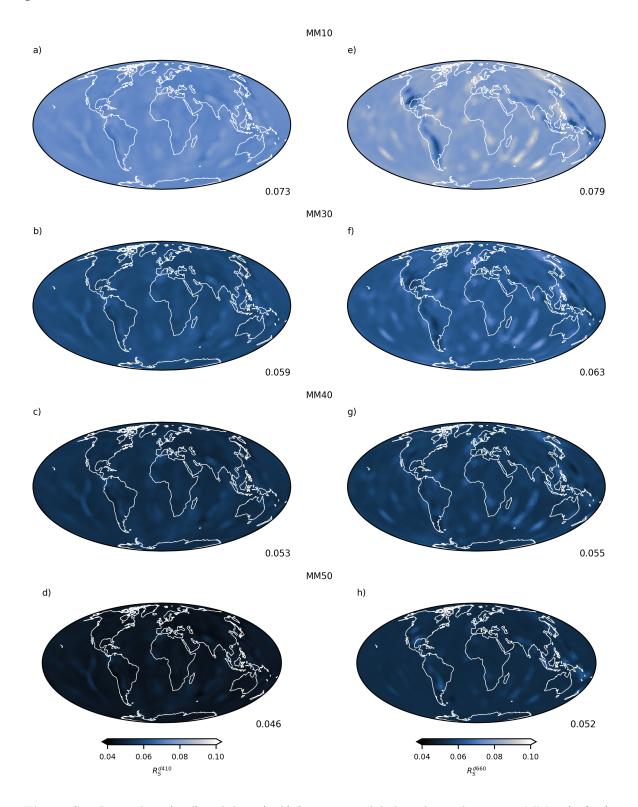
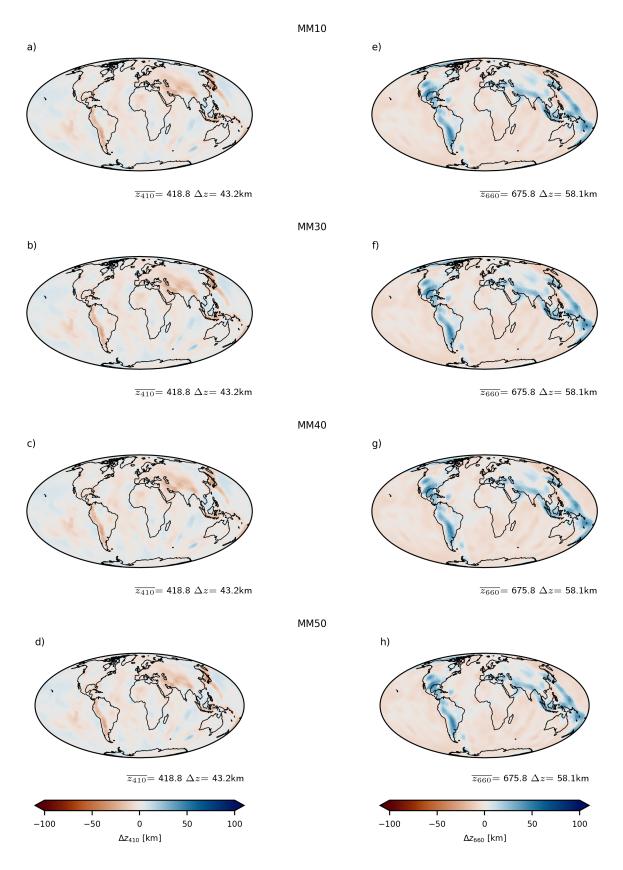


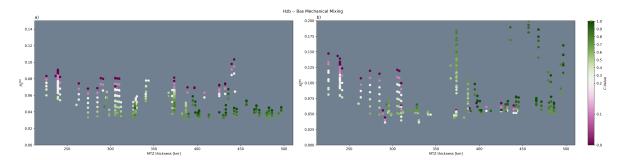
Figure S7. Variation in post-filtered topography with radius of cap used in bounce-point-spherical cap filter. a, c, e) topography on 410 discontinuity with spherical cap radius 250, 500, and 1000; km respectively; b), d), f) topography on 660 discontinuity with spherical cap radius 250, 500, and 1000; km respectively; g) power spectra of 410 discontinuity with varying spherical cap radius; h) same as for g, but for 660 discontinuity. i) same as for g and g but for MTZ thickness



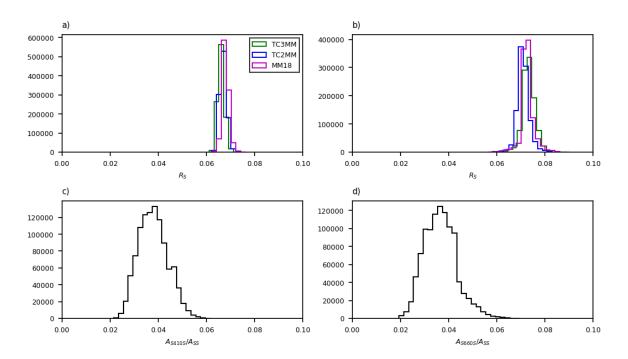
**Figure S8.**  $R_S$  on d410 (a-d) and d660 (e-h) for varying global mechanical mixtures MM10 (a & e), MM30 (b & f), and MM40 ((c & g) and MM50 (d and h).



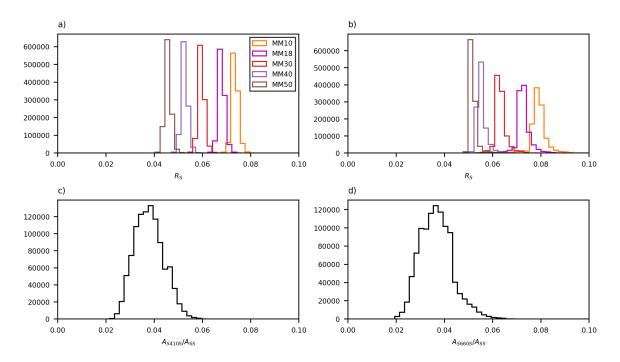
**Figure S9.** Filtered topography on d410 (a-c) and d660 (e-g) for varying global mechanical mixtures MM10 (a & e), MM30 (b & f), and MM40 ((c & g)) and MM50 (d & d)



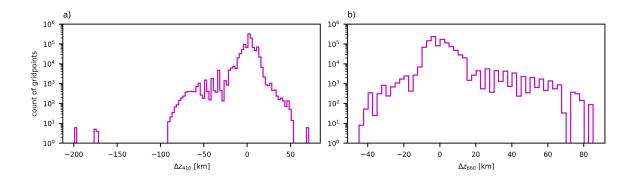
**Figure S10.** Relationship between  $R_S$  and MTZ thickness on a) d410 b) d660 as found from the tables used here.



**Figure S11.** Histograms of a)  $R_S^{410}$  and b)  $R_S^{660}$  for the topographies predicted from the geodynamic model considered here using the local mechanical mixing assumptions and normalised SS-precursor amplitude histograms on c) d410 and d) d660 from (Waszek et al. 2021).



**Figure S12.** Histograms of a)  $R_S^{410}$  and b)  $R_S^{660}$  for the topographies predicted from the geodynamic model considered here using the different global assumed mechanical mixture compositions and normalised SS-precursor amplitude histograms on c) d410 and d) d660 from Waszek et al. (2021).



**Figure S13.** Histograms of a) d410 and b) d660 topography predicted from the geodynamic model 'm\_cc\_066\_u', unfiltered using the MM18 compositional assumptions.

## REFERENCES

Waszek, L., Tauzin, B., Schmerr, N. C., Ballmer, M. D., & Afonso, J. C., 2021. A poorly mixed mantle transition zone and its thermal state inferred from seismic waves, *Nature Geoscience*, **14**(12), 949–955, doi: 10.1038/s41561-021-00850-w.