

Exciton coherence propagation measured with non-local four-wave mixing micro-spectroscopy

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Received 5 November 2025; revised 7 January 2026; accepted 10 January 2026; published 20 February 2026

Coherence transfer is a multi-disciplinary topic of interest, including chemistry, biology, and physics. In quantum technologies, achieving non-local coherent coupling between solid-state qubits is of the utmost importance. Here, we demonstrate that excitons—i.e., electron-hole pairs bound by the Coulomb force within a quantum well—can act as a medium for mesoscopic optical coherence transfer in semiconductors. To this end, we use a femtosecond laser pulse to resonantly generate excitons within the light cone. These excitons can then either recombine radiatively or scatter out of the light cone, gaining an in-plane momentum in the process. In samples without disorder, such as the CdTe quantum wells used here, the resulting fast excitons can diffuse over mesoscopic distances before recombining radiatively. Using coherent nonlinear micro-spectroscopy, we carry out exciton time-of-flight measurements. Specifically, we monitor the spatio-temporal propagation of launched exciton wave packets, selectively observing their coherence or density on a scale of up to 10 μm . Our proof-of-principle experiment demonstrates that free excitons inherit a phase modulation from the optical pulsed excitation and can generate coherent links within excitonic circuits, offering a higher level of miniaturisation and compactness than photonic or polaritonic architectures.

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<https://doi.org/10.1364/OPTICA.582443>

Controlling the electron transport in semiconductor devices is part of the groundwork of CMOS micro-electronics and computing. Single electron manipulation and transfer along the on-demand circuits can nowadays be achieved [1], enabling quantum optics experiments with electrons [2,3]. To realize coherent control in

solids on ultrafast, i.e., sub-picosecond time scales, one needs to use optical excitation schemes, usually generating Coulomb-bound electron-hole pairs, called excitons, typically hosted by a low-dimensional heterostructure, like a quantum well (QW). Moving excitons across macroscopic distances is however challenging, because: (i) the excitons' charge neutrality renders them less steerable with external electric fields than electrons, (ii) the excitons' centre of mass (CoM) can be captured on a disorder in a QW [4–6], thus hindering the propagation, (iii) due to their short lifetime, excitons show an intrinsic non-equilibrium, driven-dissipative nature, requiring optical source.

In practice, low-momentum excitons thus mostly recombine radiatively on pico- to nanosecond time scales [7], instead of exhibiting the CoM movement. To overcome the disorder-induced localization of QW excitons, one could replace them with polaritons, the propagation of which has been investigated since early studies on bulk crystals [8,9]. Owing to the motional narrowing [10], polaritons are less sensitive to microscopic disorder, permitting them to travel across hundreds of microns [11–13], yet still displaying a lifetime in a picosecond scale owing to its photon part. For the same reason, the polariton coherence volume is more than two orders of magnitude larger than that of the excitons, which could be considered as a disadvantage when it comes to miniaturisation limits. Conversely, working with indirect excitons in double QW systems, the radiative lifetime could be prolonged to microseconds [14], enabling observation of their diffusion on a scale of one hundred microns [15–17]. In a more recent and analogous system, consisting of a hetero-layer of transition metal dichalcogenides (TMDs), the transport of dark excitons has recently been reported [18]. By reducing the disorder in van der Waals heterostructures and injecting free carriers into the layers, the carrier localization could be suppressed to a level that permits the diffusion of direct (but dark, i.e., out-of-the-light-cone) excitons [19,20] on a hundred microns scale [21,22]. The presence of the electron gas in a QW is known to efficiently screen

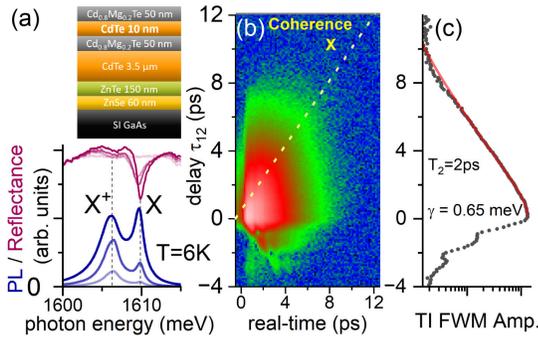


Fig. 1. Linear and nonlinear optical response of the investigated CdTe quantum wells. (a) Top: sample layout, bottom: micro-photoluminescence (blue) excited with a 532 nm CW diode, micro-reflectance (red) measured with a femtosecond pulse centered at 1610 meV, revealing the exciton-positive trion complex (X/X⁺). An increasing 532 nm excitation intensity encoded from the semi-transparent to solid lines. (b) Time-resolved FWM of the exciton versus delay τ_{12} , showing the free-induction decay. (c) Time-integrated (TI) FWM amplitude versus delay τ_{12} yielding $(T_2, \gamma) = (2 \text{ ps}, 0.65 \text{ meV})$.

out the residual disorder, further reducing the spectral inhomogeneous broadening [23–25], which typically reflects the amount of disorder present in the exciton environment.

Previous works have mostly explored propagative effects of excitons by measuring the spatio-temporal spread of their non-resonantly excited photoluminescence. In more involved experiments, the exciton [22], carrier [26,27], or magnon [28] diffusion has been probed by using incoherent spatially resolved pump-probe approaches. Newly, nonlinear spectroscopy was applied to demonstrate non-local coherent coupling between spatially separated polariton states [29]. In this paper, we employ coherent nonlinear spectroscopy to investigate the coherent spatial propagation of QW excitons. To this end, we perform non-four-wave mixing (FWM) spectroscopy. Heterodyne detection [30] previously permitted us to work in a microscopy configuration, enabling to perform hyperspectral FWM imaging [31]. Here, by spatially displacing and temporarily delaying respective beams driving the FWM, we perform time-of-flight measurement of either the exciton density or coherence.

The studied samples consist of a 10 nm wide CdTe quantum well sandwiched between Cd_{0.8}Mg_{0.2}Te barriers. Molecular beam epitaxy growth of QWs and the sample structure are described in Ref. [32], however, here QWs are undoped. We take advantage of the long-standing spectroscopic studies of this material system offering today samples of an excellent optical quality, as witnessed in the photoluminescence and reflectance presented in Fig. 1(a). The FWM characterization is presented in Supplement 1, Fig. S1. Moreover, CdTe QWs host excitons of higher binding energy than the GaAs platform, and thus are more robust, especially in the presence of free carriers. The positive doping is due to the acceptor levels located on the surface supplying holes, penetrating to the QW. The reflectance spectrum obtained at 6 K with a femtosecond laser pulse is dominated by the exciton-trion complex, similarly to previous works [33]. Thanks to the photo-doping, the absorption ratio between the exciton and the trion could be tuned through the intensity of an auxiliary non-resonant illumination [Fig. 1(a)]. We here use a 532 nm CW laser diode with an average power of only a few μW , homogeneously covering the sample area of around 50 μm diameter. As such, the density of free carriers of 10^{11} cm^{-2} is present, efficiently screening the electronic disorder, while

performing the FWM experiments. The resident holes in a QW further screen the residual disorder acting on the excitons, at the same time saturating the non-radiative recombination traps, both of which hinder the in-plane propagation of the excitons' CoM.

With FWM spectroscopy we can disentangle inhomogeneous and homogeneous broadenings (σ, γ) within the spectral line shape of an optical transition [30]. Under the so-called photon echo configuration, there is a phase conjugation between the first-order polarization and the FWM. If $\sigma \gg \gamma$, the signal is a Gaussian centered at $t = \tau_{12}$, marked with a yellow dashed line in Fig. 1(b), with a time-integrated amplitude decaying in τ_{12} according to $T_2 = 2\hbar/\gamma$. When decreasing σ , the temporal width of the echo increases. When $\sigma \ll \gamma$, the temporal rephasing effect becomes negligible and the FWM transient takes the form of an exponential decay, regardless of the delay τ_{12} : this is called the free-induction decay. To check the dominating broadening mechanism, we have spectrally shaped the excitation laser, to selectively excite the heavy-hole exciton, X. The resulting time-resolved FWM is presented in Fig. 1(b). The data show no traces of the photon echo formation, thus revealing a homogeneously broadened QW system, i.e., $\sigma \ll \gamma$. In fact, via raster scanning the FWM transients across the area of 20 $\mu\text{m} \times 10 \mu\text{m}$, no signs of the photon echo formation could be observed. Free-induction decay dominates, which is a smoking gun of a suppressed disorder on a mesoscopic scale. The time-integrated FWM, shown in Fig. 1(c), displays an exponential decay $\exp(-\tau_{12}/T_2)$, from which we obtain dephasing time of $T_2 = 2 \text{ ps}$ and $\gamma = 0.65 \text{ meV}$ (FWHM). Note the presence of the signal for $\tau_{12} < 0$ and the quantum beat, both stemming from the exciton-biexciton interaction [34], also indicating the disorder-free environment.

As our QW is virtually free from disorder, the excitons experience no spatial localization due to the microscopic potential fluctuations. Under these conditions, the scattering toward the momentum dark states, illustrated in Fig. 2(a), occurs via acoustic phonons [35,36] and exciton collisions [37]. The resulting fast excitons can diffuse over mesoscopic distances before relaxing back into the light-cone and recombining radiatively. The excitons with a large in-plane momentum of their CoM (outside the light cone) can propagate in-plane of the quantum well reaching a mesoscopic distance of around 10 μm , as shown in Figs. 2(c), 2(d).

We here take advantage of the microscopic configuration of the FWM to probe the diffusion of the exciton density. In contrast to previous FWM studies of exciton diffusion [38], we use diffraction-limited excitation spots of 0.7 μm diameter, permitting us to carry out a time-of-flight experiment directly. To this end, FWM is measured for different spatial separations between the overlapping pumps $\mathcal{E}_{1,2}$, and the probe \mathcal{E}_3 , as depicted in Fig. 2(b). The two pumps $\mathcal{E}_{1,2}$ —which are 100 fs laser pulses radio-frequency upshifted by Ω_1 and Ω_2 using an acousto-optic deflection—impinge the sample, resonantly driving the exciton transition. Subsequent exciton wave packets, traveling outwards from $\mathcal{E}_{1,2}$, generate the temporal density grating modulated at the $\Omega_2 - \Omega_1$ frequency. If this grating is sustained during the in-plane propagation, it is converted by the probe beam \mathcal{E}_3 , modulated at Ω_3 , into the FWM at the frequency $\Omega_3 + \Omega_2 - \Omega_1$. The signal is then heterodyne detected, with the sensitivity enhanced by spectrally interfering with the reference beam \mathcal{E}_R , focused 12 μm above \mathcal{E}_3 .

The central result is shown in Figs. 2(c) and 2(d), where the exciton density dynamics, i.e., FWM amplitude versus τ_{23} , is

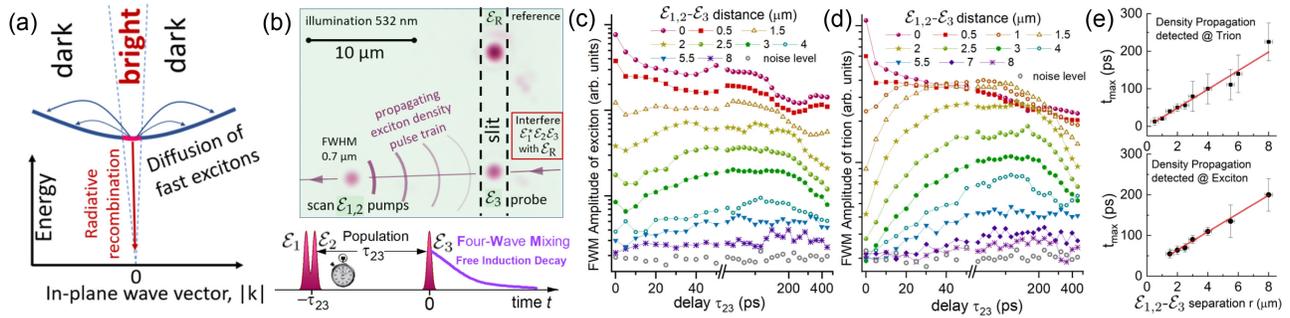


Fig. 2. Density diffusion of QW excitons measured with non-local four-wave mixing microscopy. (a) Schematics of the QW excitons' dynamics, depicting an interplay of the direct radiative recombination of bright excitons and scattering toward the dark states, supplying large in-plane momenta and thus enabling a long-range spatial diffusion. (b) Experimental configuration: pumps $\mathcal{E}_{1,2}$ induce propagation of the exciton's density. The spatio-temporal dynamics of the diffusion process is inferred by measuring FWM amplitude as a function of $\mathcal{E}_{1,2} - \mathcal{E}_3$ distance and delay τ_{23} , as illustrated in the pulse sequence. (c) and (d) Signatures of the exciton diffusion observed in the FWM (τ_{23} , r)-dependence, detected at the exciton X and trion X+, respectively. Note that the propagation signature appears to be more pronounced when monitoring X+. This is because X+ absorption, and thus FWM, is highly sensitive to the incoming exciton population. (e) Time-of-flight analysis yielding the density propagation velocity of $v_d = 40$ km/s.

plotted for increasing spatial separation r between $\mathcal{E}_{1,2}$ and \mathcal{E}_3 , and read out at X and X+, respectively. At the spatial overlap of all three beams (the top-most traces), we observe a decrease of the FWM signal on a scale of a few ps, due to a direct radiative decay, followed by secondary recombination of longer-lived dark excitons on a nanosecond timescale [39], also see Fig. S2. With increasing r , two main features are observed: first, the signal at $\tau_{23} = 0$ is gradually suppressed by more than two orders of magnitude down to the noise level. This indicates a negligible influence of scattered light and Airy fringes originating from the pumps $\mathcal{E}_{1,2}$ at the position of the probe beam \mathcal{E}_3 , as characterized in Fig. S3. Second, the maximum of the FWM distribution shifts to increasingly longer delays, which is a decisive signature of the diffusive excitons. This experiment is thus an analog of the time-of-flight measurement [8,40]: a progressively longer lag of the FWM maximum is observed with increasing r . Namely, for $r = 4$ μm the lag-time is around 100 ps, yielding the exciton group velocity of $v_d = 40$ km/s. Which physical processes permit the excitons to reach such v_d ? First, the energy of the excitons within the radiative cone, generated at a focus of 0.7 μm , corresponds to 2.2 μeV , which results in a group velocity of barely 1.5 km/s. Second, at 6 K, cold excitons generated at the bottom of their dispersion curve get thermally distributed within 0.5 meV, enabling velocities of up to 12 km/s to be reached. Thus, to attain v_d efficient exciton-acoustic-phonon and exciton-exciton scatterings are required, as discussed further. In Fig. S4, the same data are presented as a function of r for different delays τ_{23} , intuitively illustrating the spatial diffusion of excitons. In Fig. S5, we further verified that the redistribution of the FWM amplitude versus τ_{23} when varying r originates from the exciton diffusion, and not from the scattered light from $\mathcal{E}_{1,2}$ reaching \mathcal{E}_3 .

To interpret the above results, we consider the equation for isotropic diffusion, which in two dimensions and in radial coordinates takes the following form:

$$\frac{\partial n(r, t)}{\partial t} = D \frac{\partial^2 n(r, t)}{\partial r^2} + \frac{D}{r} \frac{\partial n(r, t)}{\partial r} - \frac{n(r, t)}{\tau}. \quad (1)$$

Here, D is a diffusion coefficient, and τ is the population radiative and non-radiative decay, see Fig. S2 for details. The well-known solution reads

$$n(r, t) = \frac{n(r=0, t=0)}{4\pi Dt} \exp\left(\frac{-r^2}{4Dt} - \frac{t}{\tau}\right). \quad (2)$$

The measured FWM amplitude reflects the spatio-temporal dynamics of exciton population, i.e., $n(r, t)$. Due to spatially varying carrier concentration and partial beam overlap for small separations between the beams, the resulting FWM could be quite complex. Nevertheless, the above expression predicts that the exciton distribution will reach a maximum at $t_{\max}(r) = \frac{\tau}{2} \left(\sqrt{1 + \frac{r^2}{D\tau}} - 1 \right)$. For $r^2 \gg D\tau$ this can be approximated with a linear function $t_{\max}(r) \approx \frac{\tau}{2} \left(\frac{r}{\sqrt{D\tau}} - 1 \right)$. To corroborate this prediction with our experimental results, we assign the local maxima from the FWM distributions presented in Figs. 2(c), 2(d) and plot them in Fig. 2(e). The maxima indeed follow a linear dependence with respect to the separation r , when monitoring both X and X+. These considerations permit us to estimate the diffusion coefficient: $D \simeq (r/t_{\max})^2 \tau / 4 = v_d^2 \tau / 4 = 16$ cm^2/s , which is well consistent with the previous work on a CdTe QW [38].

The propagation of density measured via FWM microscopy presented above is equivalent to the more common incoherent diffusion of excitons, as measured using pump-probe or time-resolved photoluminescence spatial imaging techniques. In the following, we demonstrate the propagation of exciton coherence. FWM spectroscopy is perfectly suited to this task, which, however, remains challenging owing to dephasing in a picosecond range. The geometry of the experiment is similar to Fig. 2(b), while the pulse sequence is depicted in Fig. 3(a). Here, \mathcal{E}_1 generates exciton coherence traveling in the plane of a QW. Upon reaching the overlapping $\mathcal{E}_{2,3}$, the coherence is converted into FWM, interfered with \mathcal{E}_R and heterodyne detected. The result of such an experiment for an increasing distance between \mathcal{E}_1 and $\mathcal{E}_{2,3}$ is shown in Fig. 3(a). As the separation between $\mathcal{E}_1 - \mathcal{E}_{2,3}$ increases, coherence dynamics diverts from a single exponential decay and develops local maximum which shifts toward positive τ_{12} , to finally form a separate lagged peak. For example, for 5 μm separation the measured time-of-flight of exciton coherence is about 4 ps, from which we deduce coherence propagation velocity of $v_c = 1250$ km/s. Such a surprisingly high v_c , two orders of magnitude higher than v_d , calls for different mechanisms involved in the exciton density and coherence propagation. The random walk of the exciton density evolving on a nanosecond time scale can be modeled by diffusive transport [Eq. (1)]. Conversely, coherence

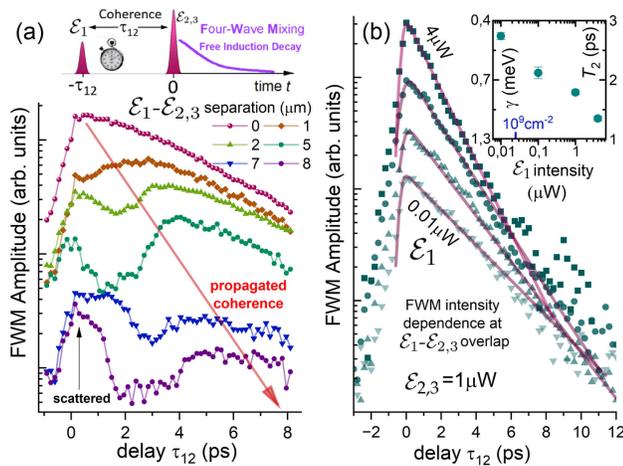


Fig. 3. Coherence propagation of QW excitons (X) measured with non-local four-wave mixing. (a) Top: pulse sequence employed to measure coherence dynamics. Bottom: FWM amplitude of X as a function of τ_{12} . For increasing spatial separation of \mathcal{E}_1 and $\mathcal{E}_{2,3}$ a cross-over from an exponential decay toward delayed maximum of the FWM occurs due to coherence propagating from \mathcal{E}_1 to $\mathcal{E}_{2,3}$. The leftover FWM signal around $\tau_{12} = 0$ is due to direct scattering of \mathcal{E}_1 onto $\mathcal{E}_{2,3}$. (b) \mathcal{E}_1 intensity dependence of the coherence dynamics at the beam overlap.

is only assigned to bright excitons, meaning it vanishes within the dephasing time of a few picoseconds, indicating that coherence propagation is ballistic, and therefore $v_c \gg v_d$. To assess the impact of the scattered light from \mathcal{E}_1 onto coherence propagation result, in Fig. 3(b) we present intensity dependence of the coherence dynamics. With increasing \mathcal{E}_1 intensity, the coherence decay remains exponential, showing that the FWM redistribution in Fig. 3(a) is indeed due to the coherence propagation. However, the data reveal a considerable excitation-induced dephasing [39] (see inset). This confirms the presence of exciton–exciton scattering, which, alongside exciton-phonon scattering, supplies excitons with high in-plane momenta.

To conclude, we took advantage of the strong, coherent nonlinear optical response of a homogeneously broadened CdTe QW to carry out non-local FWM experiments. We demonstrated spatial diffusion of excitons' coherence and density on a length scale of 10 μm . Our results demonstrate that FWM micro-spectroscopy can be used to infer the propagative effects of excitons in semiconductor nanostructures. This is particularly impactful in the context of emerging non-local coherent control experiments of individual quantum systems embedded in photonic circuits [41]. Our approach could be employed to prove a remote coherent interaction via propagating photons [29,31]. Another fascinating perspective is to investigate the propagation of coherence and density of valley-excitons in emerging 2D heterostructures with a variable confinement [42]. Beyond the condensed matter physics, coherent propagation of carriers at the micro- and meso-scale is crucial in biology [43], photovoltaics [44], and chemistry [45], highlighting the interdisciplinary nature of our work.

Funding. Narodowe Centrum Nauki (2023/51/B/ST3/01710, 2021/41/B/ST3/04183); National Research Foundation of Korea (RS-2023-0023679).

Acknowledgment. We thank Daniel Wigger and Kwangseuk Kyhm for their constructive comments on the paper.

Disclosures. The authors declare no conflicts of interest.

Data availability. Data underlying the results presented in this paper are not publicly available at this time but may be obtained from the authors upon reasonable request.

Supplemental document. See Supplement 1 for supporting content.

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