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Novel GaAs Surface Phases via Direct Control of Chemical Potential


Using *in situ* surface electron microscopy, we show that the surface chemical potential of GaAs (001), and hence the surface phase, can be systematically controlled by varying temperature with liquid Ga droplets present as Ga reservoirs. With decreasing temperature, the surface approaches equilibrium with liquid Ga. This provides access to a previously unattained regime, where we find phases ultra-rich in Ga, extending the range of surface phases available in this technologically important system. The same behaviour is expected to occur for similar binary or multi-component semiconductors such as InGaAs.

GaAs surfaces are of great scientific and technological importance, and have been intensively studied over the years (see e.g., [1-13]). Much of this work has focused on the (001) surface which is used in most electronic applications. This surface exhibits a variety of structures having different surface composition, ranging from the As-rich c(4×4) and (2×4) through to Ga-rich c(8×2), (6×6) and (4×6). Particular surface phases of differing structure and composition are used in the growth of optoelectronic materials, InGaAs quantum devices and dilute magnetic semiconductors for spintronics by molecular beam epitaxy. In addition, surface composition is known to be critical for the incorporation of elements such as Bi to adjust the lattice constant and bandgap [14]. It is also important in the fabrication of low density GaAs quantum dots via droplet epitaxy for potential applications as quantum light sources [15]. This has led to significant efforts to understand and control the stability of surface phases as a function of experimental conditions, as well as to seek new ways of accessing different structures to influence growth mechanisms for potential device applications [1-15].

At fixed temperature, the stable structure (the one with the lowest Gibbs free surface energy) depends on the values of the Ga and As chemical potentials. The control of surface chemical potential is therefore paramount in order to stabilise surface phases. It is well appreciated that transitions between As-rich surface phases can be induced by varying the As flux and/or the substrate temperature [1-3]. The control of Ga-rich phases is more challenging, but careful work has shown how deposition of excess Ga can be used to stabilize very Ga-rich surfaces (see e.g., [1,11]). Ultimately, one would like a method to map the equilibrium phase diagram in this Ga-rich regime by incrementally adjusting the surface chemical potential.

Here we describe a new approach to controlling the chemical potential of surfaces by slowly varying the substrate temperature with liquid droplets present as Ga reservoirs. In the case of GaAs (001), this allows the surface phases to establish near-equilibrium with Ga liquid at low
temperature, enabling us to approach a previously unattained, extreme Ga-rich limit. This regime is explored by in situ surface electron microscopy. We find new surface phases which are stabilised by the high Ga chemical potential, thereby extending the experimentally accessible GaAs (001) phase diagram in this technologically important system.

Experiments were performed in an ultrahigh-vacuum (UHV) low energy electron microscope (LEEM) specially designed for III-V epitaxy [16]. Temperatures \( T \) were measured using an infrared pyrometer, including a correction due to the \( T \)-dependence of the surface emissivity [17] and calibrated to the congruent evaporation temperature \( T_c \) of 625 °C [18,19]. We degassed a (001)-oriented undoped GaAs sample at 300 °C for 24 hours. This was followed by high temperature flashing up to 600 °C and annealing at 580 °C for 2 hours to remove the surface oxide. Ga droplets of radius \( \sim 2 \mu m \) were prepared by annealing above \( T_c \) at 650 °C and the droplets were allowed to run across the surface [20,21], creating smooth planar (001) regions which we utilise for our imaging experiments [22]. A mirror electron microscope (MEM) image of a set of droplets and smooth trails is shown in Fig. 1(a). Droplets appear in MEM as a uniform dark disc somewhat larger than the actual droplet, surrounded by a concentric bright ring [23]. The droplet density on the sample was \( \sim 7x10^{-3} \mu m^{-2} \). The specific (001) region used to image surface phases using LEEM is displayed in Fig. 1(b) and is within 10 \( \mu m \) of the accompanying droplet.

The sample was then carefully annealed at a series of decreasing temperatures, from 580 °C down to 300 °C. At temperatures where phase transformations were observed, the relevant temperature range was scanned in reduced increments to identify the transition temperature. To ensure that the observed phase distributions had fully stabilised, each anneal temperature was held constant for 60 min. The phase transformations observed were all found to be fully reversible.

Figure 2(a) contains a LEEM image of a planar (001) region with accompanying micro-low energy electron diffraction (\( \mu \)LEED) pattern. The dashed circle indicates the position of the illumination aperture used to collect the \( \mu \)LEED diffraction data and is within 10 \( \mu m \) of the accompanying droplet. A schematic diffraction pattern is also shown where large circles indicate the positions of (1×1) spots. In Fig. 2(a) the \( \mu \)LEED pattern reveals a pure c(8×2) phase which was found to exist down to \( \sim 540 °C \), as indicated on the left side of Fig. 3.

On decreasing the anneal temperature further, c(8×2) is found to coexist over a small temperature range with a phase of (6×6) periodicity which we term (6×6)D (panel 2(b)). This phase is clearly disordered along [\( \overline{1}10 \)] as indicated by the \( \mu \)LEED pattern. On decreasing \( T \) below 540 °C, the dominant mixture is a combination of c(8×2) and (4×6). This is surprising since it is believed the ultra-rich Ga (4×6) phase can only be obtained following deposition of Ga [1,11,15]. Eventually, below 530 °C, a new unforeseen c(2×12) phase appears as shown in panel 2(c), coexisting with (4×6). To our best knowledge, this is the highest periodicity along a symmetry axis observed on GaAs (001) since no 12× LEED features have been reported previously [5]. Note that a small amount of residual c(8×2) phase is always stabilised at surface steps throughout the experiments. Extremely weak, disordered (n×6) \( \mu \)LEED streaks are also observed along [110] directions in the range 400-500 °C.

To establish that Ga droplets are responsible for the unexpected new phases we completely removed the droplets from the surface by annealing below \( T_c \) at 570 °C. Flat trail regions were again imaged by LEEM and the c(8×2) phase was observed at the sample anneal temperature
of \( T = 580 \, ^\circ \text{C} \). This is the most Ga-rich phase observed during annealing without droplets [1,7]. As \( T \) is decreased, a transition to the less Ga-rich (6×6) is observed at around 525 \, ^\circ \text{C} \) which is separated by a region of phase coexistence. This is in good agreement with the observations of others who observe these phases at high and low temperatures, respectively, during annealing [1,5,9,11]. We note that the relative intensities of the (6×6) LEED spots without droplets are very different from the (6×6)D phase observed with droplets present. We therefore expect that (6×6)D may have basically the same structure as (4×6), but with a different periodicity to accommodate slightly different amounts of excess Ga, while the normal (6×6) could be a very different structure [5,13].

We can explain the very different phase diagrams observed in the presence and absence of droplets by considering the competing pathways for Ga atoms. In the absence of droplets, Ga is lost by evaporation; but decomposition of GaAs provides a source of Ga that increases rapidly with temperature. The net result is that the surface becomes more Ga-rich at higher temperatures. When droplets are present, they provide an additional source of surface Ga. At high temperature, evaporation and decomposition may still dominate, because the whole surface contributes. But with decreasing temperature, the surface approaches equilibrium with the droplets because of the lower energy barriers associated with Ga adatom detachment from the droplets compared to evaporation or GaAs decomposition. As a result, while the bare surface becomes less Ga-rich with decreasing \( T \), the surface with droplets present becomes more Ga-rich.

To illustrate this behaviour concretely, we propose a simple model describing the Ga balance at a GaAs surface at temperature \( T \), with or without droplets present. The surface is assumed to be in equilibrium with the crystal so that \( \mu_{Ga} + \mu_{As} = \mu_{Ga,As} \) where \( \mu_{Ga} \) and \( \mu_{As} \) are the respective Ga and As surface chemical potentials and \( \mu_{Ga,As} \) is the chemical potential (per two-atom unit) of the bulk crystal. Let us first consider the case of a droplet-free surface. Assuming a standard transition rate model for Ga and As evaporation, the respective evaporation rates per unit area are

\[
F_{Ga} = r_{Ga} \exp\left(\frac{\mu_{Ga} - E_{Ga}}{kT}\right),
\]

and

\[
F_{As} = N_{r_{As}} \exp\left(\frac{N_{\mu_{Ga,As}} - N_{\mu_{Ga}} - E_{As,N}}{kT}\right).
\]

This assumes that As evaporates as an N-mer (most likely a dimer). \( E_{Ga} \) and \( E_{As,N} \) are the respective transition state energies for Ga adatom and As N-mer evaporation, with associated rate constants \( r_{Ga} \) and \( r_{As} \) including the transition state entropy or degeneracy, e.g. number of sites for evaporation per unit area. In Eq. (2), \( F_{As} \) is defined per atom independent of \( N \), while \( r_{As} \) refers to \( N \)-mer desorption events.

In the absence of droplets, \( \mu_{Ga} \) is determined by congruent evaporation from the surface. We denote this as \( \mu_{Ga}^{b} \) where \( b \) refers to the bare, droplet-free surface. During congruent evaporation, \( \mu_{Ga}^{b} \) attains a steady-state value such that Ga and As evaporate at equal rates (
$F_{Ga} = F_{As}$). Evaporation of As has a larger activation barrier than Ga evaporation and so as $T$ increases, the increased As evaporation causes Ga to accumulate on the surface which in turn increases $\mu_{Ga}$ until $F_{Ga} = F_{As}$ is restored. However, if $\mu_{Ga}$ rises above the liquidus value $\mu_{Ga}^l(T_c)$ at temperature $T_c$, then droplets can form which defines the upper limit for congruent evaporation. As long as there are no droplets present, from Eqs. (1) and (2) we can obtain the surface chemical potential $\mu_{Ga}^b$ (see appendix 1),

$$\mu_{Ga}^b = \mu_{Ga}^l(T_c) + c_s(T - T_c),$$

where $c_s$ is a constant related to the kinetics of evaporation.

Now consider the surface in the presence of Ga droplets, as in Fig. 1. Our LEEM experiments show that the phase transformations occur uniformly over distances greater than the average droplet separation, so we assume attachment/detachment limited kinetics for Ga moving between surface and droplet. Then the Ga chemical potential on the surface with droplets present, $\mu_{Ga}^d$, is to a good approximation spatially uniform. The droplets act as a source (or sink) for surface Ga adatoms at a rate

$$F_d = r_d \exp\left(\frac{-E_d}{kT}\right)\left[\exp\left(\frac{\mu_{Ga}^l}{kT}\right) - \exp\left(\frac{\mu_{Ga}^d}{kT}\right)\right],$$

where $\mu_{Ga}^l$ is the chemical potential of the liquid droplet, and $r_d = s_d k_d$ where $s_d$ is the perimeter length of the droplets per unit area of the surface, and $k_d$ and $E_d$ are the respective rate constant and activation energy for attachment at the droplet perimeter. We assume that the droplet is nearly in equilibrium with the GaAs substrate at liquidus composition.

To obtain $\mu_{Ga}^d$ we assume that the surface is in quasi-steady state so that $F_{As} = F_d$, i.e. surface Ga resulting from As evaporation and net detachment from the droplet is equal to the Ga lost by evaporation; and we neglect the reduction in surface area by droplet coverage. Combining Eq’s (1), (2) and (4) for $N = 2$ with this steady state condition then yields

$$\exp\left(\frac{3\mu_{Ga}^d}{kT}\right) - \frac{r_d \exp\left(\frac{2\mu_{Ga}^d + \mu_{Ga}^l - E_d}{kT}\right)}{r_{Ga} \exp\left(\frac{-E_Ga}{kT}\right)} + \frac{r_d \exp\left(-E_d/kT\right)}{r_{Ga} \exp\left(-E_Ga/kT\right)} = 0.$$

This is a cubic equation in $\exp(\mu_{Ga}^d/kT)$, and $\mu_{Ga}^d$ is the real solution (see appendix 1). Our model, consisting of Eq. (5) for $\mu_{Ga}^d$ and Eq. (3) for $\mu_{Ga}^b$, describes the temperature dependence with and without droplets in terms of three material parameters $c_s$, $r_{Ga}/r_d$ and $(E_d - E_Ga)$ (see appendix 1).

The chemical potentials $\mu_{Ga}^d$, $\mu_{Ga}^b$ and $\mu_{Ga}^l$ are plotted in Fig. 4 for illustrative values of the parameters, since the actual values are not known. Ideally we would like to use the chemical potential as a direct guide to how Ga-rich the surface will be. However, in fact the chemical
potentials all decrease with increasing temperature due to the vibrational contributions to the free energy. To make the plot a better indicator of Ga richness when comparing surfaces at different $T$, we subtract out a rough estimate $(-4kT)$ of the surface vibrational free energy, plotting $\mu + 4kT$ [24]. The curve for the bare surface chemical potential $\mu_{Ga}^b$ monotonically rises with increasing temperature reflecting a more Ga-rich surface. (This behaviour extends above $T_c$, since droplets do not nucleate at a detectable rate when $\mu_{Ga}^b$ is only slightly above $\mu_{Ga}^l$, due to a large barrier for Ga droplet nucleation.) This variation of $\mu_{Ga}^b$ produces the transition between c(8x2) and (6x6) via a transition zone involving phase coexistence (Fig. 3). Regions of coexistence separating distinct phases appear to be a regular feature of this system [1,2,5,9,25], resulting from long-range electrostatic and elastic interactions between surface domains [26,27].

When droplets are present on the surface, they act as reservoirs of Ga at liquidus composition $\mu_{Ga}^l$. For the temperature range of interest, the droplet contains less than 0.3 % As and so $\mu_{Ga}^l$ is well approximated by that of pure liquid Ga which can be evaluated from thermodynamic data [28]. $\mu_{Ga}^l$ is plotted in Fig. 4 and decreases quite rapidly with increasing $T$ due to the large liquid entropy compared with the crystal solid.

The surface chemical potential in the presence of droplets $\mu_{Ga}^d$, as evaluated from Eq. (5) for an illustrative set of parameters, is plotted in Fig. 4 and can be seen to lie in between the limits of the liquidus $\mu_{Ga}^l$ and the evaporation-dominated bare-surface $\mu_{Ga}^b$. At $T_c$, the surface chemical potential must be equal to the Ga liquidus value whether or not droplets are present. Insofar as the kinetics are dominated by evaporation at this temperature, the slopes of $\mu_{Ga}^d$ and $\mu_{Ga}^b$ start to approach each other close to $T_c$.

Below 575 °C, evaporation from the GaAs (001) surface is much reduced [29]. The attachment barrier at the droplet ($E_d$) is expected to be much smaller than the energy barriers controlling evaporation ($E_{Ga}, E_{As,N}$), so with decreasing $T$, $F_d$ plays an increasingly important role compared with $F_{Ga}$ and $F_{As}$ in determining $\mu_{Ga}^d$. At sufficiently low $T$, we expect that $F_d$ becomes so dominant that the condition for mass balance reduces to $F_d \approx 0$, i.e. the surface approaches equilibrium with the droplet and $\mu_{Ga}^d \approx \mu_{Ga}^l$.

For a given $T$, increasing the number or size of droplets increases the droplet perimeter length per unit area, and hence the parameter $r_d$. As can be seen from Fig. 4, this shifts the crossover to the droplet dominated regime to higher temperatures.

We can now explain the experimentally observed sequence of phases as a function of temperature as illustrated in Fig. 4. Without droplets, the surface is most Ga-rich at high $T$ with the chemical potential approximately equal to $\mu_{Ga}(T_c)$. But with droplets present, the surface is most Ga-rich at low $T$. Close to $T_c$, $\mu_{Ga}^d \approx \mu_{Ga}^b$, so the observed surface reconstruction c(8x2) is identical in both cases. However, as $T$ decreases further, the behaviour of the Ga surface chemical potential in the presence of droplets is very different. Since the activation energy for droplet attachment/detachment is lower than the activation
barrier for Ga evaporation, $\mu^d_{\text{Ga}}$ rises above $\mu_{\text{Ga}}(T_c)$, accessing a new regime of high Ga chemical potential. This leads to the appearance of new phase mixtures; first c(8×2) with (6×6)D and then c(8×2) with (4×6). The (4×6) phase has only been previously observed following deposition of Ga [1,11,15], but is stabilised here by the droplet modified surface chemical potential which significantly exceeds $\mu^d_{\text{Ga}}(T_c)$.

There has been considerable interest in seeking the most extreme Ga-rich phase of GaAs (001) [1,4,5,11]. (4×6) is presently regarded as the most Ga-rich phase [1,11]. However, our capability to control chemical potential via $T$ in the presence of a droplet reservoir and establish equilibrium within an ultra-rich Ga phase space has produced an unexpected c(2×12) phase which is seen to coexist with (4×6) below 530 °C. The $12\times$ LEED features represent the highest reconstruction periodicity observed along a symmetry axis to date [5]. Since c(2×12) occurs under extreme Ga rich surface conditions induced by Ga droplets, it is also clearly a strong candidate for the most Ga-rich phase found to date.

Most analyses of GaAs surface phases have been based on density functional theory (DFT) calculations of the enthalpy at $T = 0$. In that case, the Ga-rich limit is defined by equilibrium with solid Ga (see, for example [11]). However, at the much higher $T$ of experiments, the Ga-rich limit is defined by equilibrium with liquid Ga. This corresponds to a much less Ga-rich surface than in T=0 calculations, because the liquid has substantial extra entropy, making it a stronger sink for Ga (lower chemical potential relative to GaAs). While the surface chemical potential is close to that of liquid Ga at high temperature, near $T_c$, the most Ga-rich surfaces can only be reached via equilibrium with liquid Ga at far lower temperatures, where the contribution from the excess entropy of the liquid is reduced.

In summary, we have developed a method of controlling the chemical potential of GaAs surfaces, under UHV conditions, using liquid droplets as a reservoir for Ga. By varying the temperature, it is possible to carefully control and extend the range of chemical potential so that the surface approaches equilibrium with the droplet. This stabilises a new, high periodicity c(2×12) phase in an ultra-rich Ga regime. Such phases may have applications in quantum structure fabrication [3,15] and enhanced elemental incorporation [14]. We also anticipate the use of droplets to access previously unobtainable phase space and create new surface structures will see wide applicability in other technologically important systems such as GaN and InGaAs.

References

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Appendix 1

Approximating Free Energies in terms of Enthalpy and Entropy at a fixed Temperature

We can write the Gibbs free energy at temperature $T$ in terms of the enthalpy $H$ and entropy $S$ as

$$G(T) = H(T) - TS(T). \quad (A1)$$

If we expand around some temperature $T_0$ in our experimental range of interest we obtain

$$G(T) \approx G(T_0) + (T - T_0)G'(T_0), \quad (A2)$$

which, from (A1) can be written,

$$G(T) \approx G(T_0) + (T - T_0)[H'(T_0) - S(T_0) - T_0S'(T_0)]$$

$$= G(T_0) + (T - T_0)[H'(T_0) - T_0S'(T_0)] - (T - T_0)S(T_0). \quad (A3)$$

However at constant pressure the heat capacity, $C_p = \frac{dH}{dT} = TdS/dT$ and we can write

$$G(T) \approx G(T_0) - (T - T_0)S(T_0), \quad (A4)$$

which from (A1) gives,

$$G(T) \approx H(T_0) - TS(T_0). \quad (A5)$$

We subsequently assume that the temperature dependence of all free energies and chemical potentials can be approximated in this form.

Derivation of bare surface chemical potential $\mu_{Ga}^b$ in the absence of droplets

All symbols are defined in the main text. Assuming a standard transition rate model for Ga and As evaporation, the respective evaporation rates per unit area are

$$F_{Ga} = r_{Ga} \exp \left( \frac{\mu_{Ga} - E_{Ga}}{kT} \right), \quad (A6)$$

and

$$F_{As} = N r_{As} \exp \left( \frac{N\mu_{GaAs} - N\mu_{Ga} - E_{As,N}}{kT} \right). \quad (A7)$$

with $\mu_{Ga} + \mu_{As} = \mu_{GaAs}$. Congruent evaporation implies $F_{As} = F_{Ga}$. 
\[ r_{Ga} \exp\left( \frac{\mu_{Ga} - E_{Ga}}{kT} \right) = N r_{As} \exp\left( \frac{N \mu_{GaAs} - N \mu_{As} - E_{As}}{kT} \right) \]  \hspace{1cm} (A8)

hence,

\[ (N + 1) \mu_{Ga} = kT \ln \left( \frac{N r_{As}}{r_{Ga}} \right) + N \mu_{GaAs} + E_{Ga} - E_{As,N}. \]  \hspace{1cm} (A9)

Now \( \mu_{GaAs} \) is equivalent to the crystal free energy per atom pair given by \( G_{GaAs} = H_{GaAs} - TS_{GaAs} \) where \( H_{GaAs} \) and \( S_{GaAs} \) are the respective enthalpy and entropy, so we can write (A9) as

\[ (N + 1) \mu_{Ga} = kT \left[ \ln \left( \frac{N r_{As}}{r_{Ga}} \right) - N \frac{S_{GaAs}}{k} \right] + N H_{GaAs} + E_{Ga} - E_{As,N}. \]  \hspace{1cm} (A10)

At \( T = T_c \) we have \( \mu_{Ga} = \mu_{Ga}^l(T_c) \) which from (A10) gives

\[ (N + 1) \mu_{Ga} = (N + 1) \mu_{Ga}^l(T_c) + k(T - T_c) \left[ \ln \left( \frac{N r_{As}}{r_{Ga}} \right) - N \frac{S_{GaAs}}{k} \right]. \]  \hspace{1cm} (A11)

Therefore,

\[ \mu_{Ga} = \mu_{Ga}^b = \mu_{Ga}^l(T_c) + c_k(T - T_c), \]  \hspace{1cm} (A12)

where

\[ c_k = \frac{k}{(N + 1)} \left[ \ln \left( \frac{N r_{As}}{r_{Ga}} \right) - N \frac{S_{GaAs}}{k} \right]. \]  \hspace{1cm} (A13)

**Independent parameters governing \( \mu_{Ga}^b \)**

We assume that \( S_{GaAs} \) and the transition state entropies contained in \( r_{Ga} \) and \( r_{As} \) are defined at \( T_0 = 525 \) °C. \( S_{GaAs} = 55.9 \) J mol\(^{-1}\) K\(^{-1}\) is obtained from fitting \( G_{GaAs} = H_{GaAs} - TS_{GaAs} \) to thermodynamic data [28] which leaves \( r_{As} / r_{Ga} \), or equivalently the slope \( c_k \), as the only free parameter.

**Derivation of surface chemical potential \( \mu_{Ga}^d \) in the presence of droplets**

The droplets act as a source (or sink) for surface Ga adatoms at a rate,

\[ F_d = r_g \exp\left( \frac{-E_d}{kT} \right) \exp\left( \frac{\mu_{Ga}^b}{kT} \right) - \exp\left( \frac{\mu_{Ga}^d}{kT} \right). \]  \hspace{1cm} (A14)

The condition for quasi-steady state is \( F_{As} + F_d = F_{Ga} \) so that from (A6), (A7) and (A14) we have,
0 = \left[r_{Ga} \exp\left(-\frac{E_{Ga}}{kT}\right) + r_d \exp\left(-\frac{E_d}{kT}\right)\right] \exp\left(-(N+1)\mu_{Ga}^d\right) - r_d \exp\left(-\frac{E_d}{kT}\right) \exp\left(-N\mu_{Ga}^d\right) - N r_{As} \exp\left(-N\mu_{AsGaAs}^d\right)

(A15)

Substituting \( \mu_{GaAs}^d = H_{GaAs} - TS_{GaAs} \), \( \mu_{Ga}^d = H_{Ga} - TS_{Ga} \), where \( H_{Ga} \) and \( S_{Ga} \) are the respective Ga liquid enthalpy and entropy then with \( N = 2 \) we can rewrite (A15) as

\[ x^3 - b(T)x^2 - c(T) = 0 \]  

(A16)

The chemical potential is obtained from the real solution \( x = \exp(\mu_{Ga}^d/kT) \) with,

\[
\begin{align*}
\frac{b(T)}{c(T)} &= \frac{2r_{As} r_{Ga} \exp\left(-\frac{E_d}{kT}\right)}{r_d r_{Ga} \exp\left(-\frac{E_{Ga}}{kT}\right)} + 1, \\
&= \frac{2r_{As} r_{Ga} \exp\left(-\frac{2H_{GaAs} - E_{As,2} + E_d}{kT}\right)}{r_d r_{Ga} \exp\left(-\frac{E_{Ga}}{kT}\right)} + 1.
\end{align*}
\]

(A17)

**Independent parameters governing \( \mu_{Ga}^d \)**

\( H_{d}^j = 18.9 \text{ kJ mol}^{-1}, \quad S_{d}^j = 85.8 \text{ J mol}^{-1} \text{ K}^{-1} \) and \( S_{GaAs} = 55.9 \text{ J mol}^{-1} \text{ K}^{-1} \) are known from fitting thermodynamic data [28]. This leaves \( r_{As} / r_d \) and \( (E_d - E_{Ga}) \) as independent parameters. In addition, we need to know \( (2H_{GaAs} - E_{As,2} + E_d) \) which can be expressed in terms of the other unknown parameters by noting that at \( T = T_c \) we have \( \mu_{Ga}^d(T_c) = \mu_{Ga}^d(T_c) \) so that from (A16) and (A17) we obtain

\[
2H_{GaAs} - E_{As,2} + E_d = kT_c \ln \left[ \frac{1}{2} \frac{r_{As} r_{Ga}}{r_d r_{As}} \exp\left(\frac{E_d - E_{Ga}}{kT_c}\right) + 1 \right] \exp\left(\frac{2S_{GaAs}}{kT_c}\right) - b(T_c) \exp\left(\frac{2\mu_{Ga}^d(T_c)}{kT_c}\right)
\]

(A18)

Since \( c_k \) is a function of \( r_{As} / r_{Ga} \) [(A13)], the three independent parameters for \( \mu_{Ga}^d \) are \( c_k \), \( r_{Ga} / r_d \) and \( (E_d - E_{Ga}) \).
FIG. 1 (a) MEM image of a set of planar (001) trail regions produced by the motion of Ga droplets. The primary electron energy was 20 keV and this was offset with respect to surface potential by -0.3 eV. (b) LEEM image of the planar (001) region used for the phase transformation studies. The dashed circle indicates the position of the illumination aperture used to collect the μLEED diffraction data in Fig. 2. The electron energy is 2.4 eV. The scale markers in (a) and (b) are 5 μm and 2 μm, respectively.
FIG.2 LEEM images and accompanying $\mu$ LEED diffraction patterns obtained from a GaAs (001) planar region with liquid Ga droplets present on the surface. The dashed circle in panel (a) indicates the position of the illumination aperture used to collect the $\mu$LEED diffraction data. The scale marker in (c) is 2 $\mu$m across. Schematic diffraction patterns are also shown where large circles indicate the positions of (1×1) spots. In (a) the pattern indicates a pure c(8×2) phase. (b) c(8×2) coexists with (6×6)D (superimposed red spots and lines). (6×6)D is disordered along $[\bar{T}10]$ and differs from the (6×6) phase observed without droplets (see text). (c) Phase coexistence between (4×6) (black) and a high periodicity c(2×12) phase (green). Each phase distribution was carefully stabilised by annealing for 60 min. The electron energy for LEEM imaging was 2.4 eV and 10.3 eV for $\mu$ LEED diffraction.
FIG. 3 Phase diagram with and without droplets deduced from LEEM imaging and μLEED as a function of temperature (see Fig. 2). Phase transformations with and without droplets occur at boundaries $\Gamma_1$, $\Gamma_2$, $\Gamma_3$ and $\Delta_1$, $\Delta_2$ respectively.
FIG.4 Model for variation of Ga chemical potential with temperature. $\mu_{Ga}^d$ and $\mu_{Ga}^b$ are the respective Ga surface chemical potentials with and without droplets present. The droplet chemical potential $\mu_{Ga}^d$ is well approximated by that of liquid Ga, evaluated from the thermodynamic data contained in [28]. $\mu_{Ga}^b$ and $\mu_{Ga}^d$ (solid line) are calculated from Eqs. (3) and (5) respectively using illustrative values $c_s = -37$ eV K$^{-1}$, $r_{sa}/r_d = 30$ and $(E_d - E_{Ga}) = -0.35$ eV. The temperatures of the actual phase transformations in Fig. 3 are indicated on the $\mu_{Ga}^b$ and $\mu_{Ga}^d$ curves. The dashed curve represents $\mu_{Ga}^d$ for a factor of four decrease in droplet perimeter per unit area. A value of $4kT$ has been added to the vertical chemical potential axis to make the plots more readable.